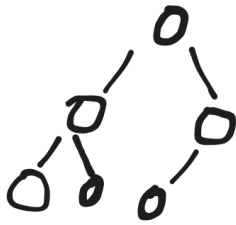


What is a binary Tree?



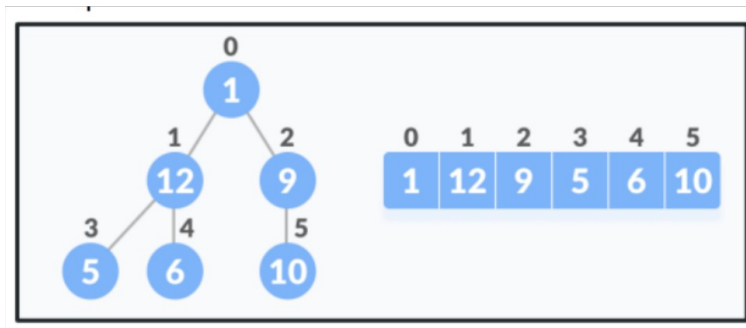
What is a Heap?

What is a max heap?

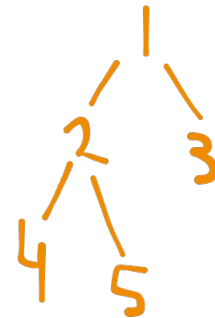
the parent nodes, are bigger than the children

What is a min heap?

the parent nodes, are smaller than the children



[1, 2, 3, 4, 5]

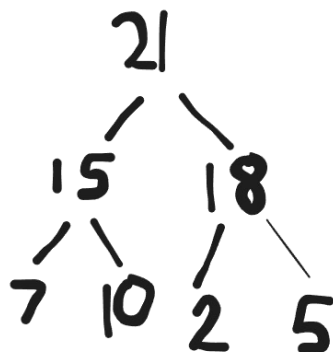


Build a Max Heap!

[15, 7, 2, 10, 18, 5, 21]



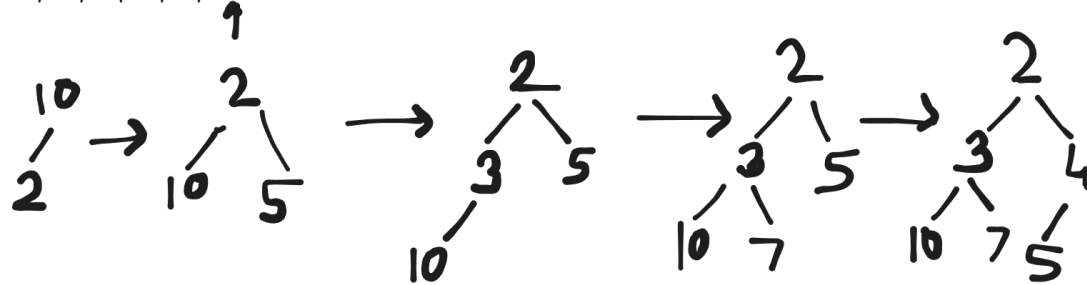
Heapify!



[21, 15, 18, 7, 10, 2, 5]

Build a Min-Heap!

[10, 2, 5, 3, 7, 4]

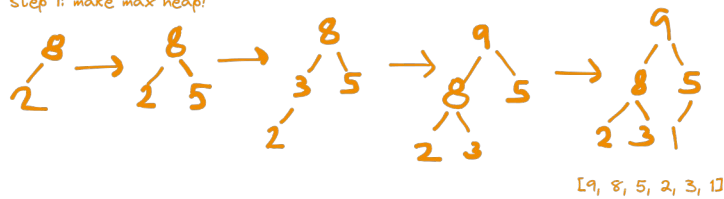


[2, 3, 4, 10, 7, 5]

Heap Sort!

[2, 8, 5, 3, 9, 1] smallest to largest (ascending)

step 1: make max heap!



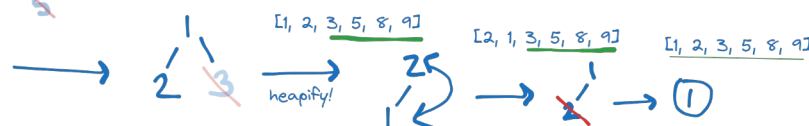
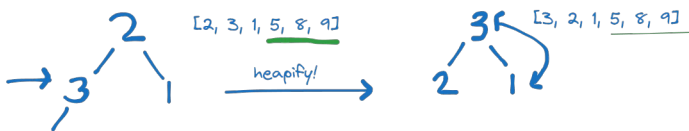
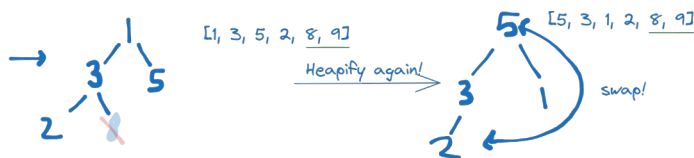
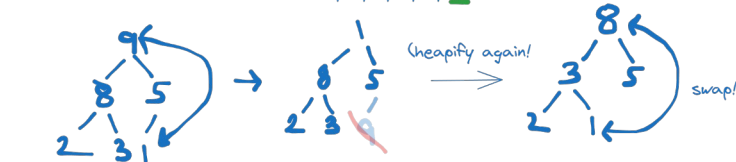
step 2: (repeat until sorted)

take the top, swap it with the end, and consider it sorted

[9, 8, 5, 2, 3, 1]

[1, 8, 5, 2, 3, 9]

[8, 3, 5, 2, 1, 9]



1) Build the right heap
Max heap if smallest to biggest
Min heap if biggest to smallest

2) swap the top with the last
number in the array

3) remove the last value
from the heap, and re-heapify!

4) repeat until there is only
one value left in the heap!

Big O: $O(n \log n)$

Given an array, how can you tell if its a max heap?

loop through the array, check if left is smaller than the parent,
check if the right is **smaller** than the parent, otherwise return false.

left: $2i + 1$

right: $2i + 2$

biggest = i

