Data Structures and Algorithms for competitive programming

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November 25, 2018

C	Contents		5	Algorithms NlogN LIS	10
1	Graphs	2		RectInHist	
	Traversal BFS Dijkstras Trees MST LCA Centroid Decomposition SCC Tarjans AP & Bridges Network Flow Edmond Karp Max Flow Ford Fulkerson Max Flow	2 2 2 3 3 3 3	6	Maths Miller Rabin Binomial Coefficients Gaussian Elimination Ternary Search Matrix Exponential	11 11 12
2	Data Structures Fenwick Tree UFDS . Sparse Table Segment Tree Convex Hull Trick	5 5			
3	Geometry Convex Hull				
4	Strings Suffix Array	8 8 8			

1 Graphs

Traversal

```
\mathbf{BFS}
```

```
int dist[MXN];
   vector < int > adjList [MX.N];
3
   int main(){
 5
        for(int i = 0; i < MX_N; i++)
 6
            dist[i]=INF;
        queue<int> q;
 8
        q.push(0);
9
        dist[0] = 0;
10
        while (!q.empty()) {
            int u = q.front(); q.pop();
11
12
            int d = dist[u];
            for(int i : adjList[u]){
13
                 if (dist [i]==INF) {
14
                     dist[i]=d+1;
15
16
                     q.push(i);
17
18
19
20
        return 0;
   Dijkstras
   struct path {
2
        int u,d;
3
        bool operator < (const path& p) const {
 4
            return d > p.d;
 5
 6
    };
    for (int i =0; i < N; ++i)
        dist[i] = INF;
    dist[S] = 0;
   priority_queue < path > q;
   q.push(path(S,0));
12
   while (!q.empty()) {
13
        path p = q.top(); q.pop();
14
        u = p.u, d = p.d;
15
        if(dist[u] < d)
16
            continue;
17
        for (auto v : adjList[u]) {
            nd = d + v.second;
18
19
            if(nd < dist[v.first]){</pre>
20
                 dist[v.first] = nd;
21
                q.push(path{v.first,nd});
22
23
24
```

Trees

MST

```
struct edge {
2
        int x, y, w;
3
        bool operator < (edge e) const {
4
            return w < e.w;
5
6
    };
8
   int main(){
9
        vector<edge> eList; //Input
10
        for (int i = 0; i < N; i++)// Set up UFDS
11
            p[i]=i;
12
        vector<ii> treeList;
13
        sort (eList.begin(), eList.end());
14
        int cost = 0;
15
        int sz=N;
16
        int u, v, w;
17
        for (const auto &i : eList) {
18
            v=i.x; u=i.y; w=i.w;
19
            if (!connected(u,v)){
20
                join (u,v);
21
                treeList.push\_back(\{min(u,v),max(u,v)\});
22
                sz --;
23
                 cost+=w;
24
25
26
        if (sz!=1)
27
            puts("Impossible");
28
   LCA
    *H/u is first visit of u
    *E[x] is vertex at time x
4
    *L[x] is depth at time x
5
    */
    void vis(int u, int d){
6
        H[u] = vind;
8
        E[vind] = u;
9
        L[vind++] = d;
10
        for (auto i : adjList[u]) {
11
            if(H[i]!=-1)
12
                continue;
13
            vis(i,d+1);
14
            E[vind] = u;
15
            L[vind++] = d;
16
17
18
19
    int LCA(int u, int v){
20
        if(H[u] > H[v])
```

```
21
            int t = u:
22
            u = v;
23
            v = t;
24
25
        //run some range min query on L
26
        //between H/u/ and H/v/
27
        int ind = rmq(H[u], H[v]);
28
        return E[ind];
29
30
31
   int dist(int u, int v){
32
        int a = H[u];
33
        int b = H[v];
34
        int ind = LCA(u, v);
35
        return abs(L[H[ind]]-L[a])
36
            + abs(L[H[ind]]-L[b]);
37
   Centroid Decomposition
   void fill_sz(int u, int p){
2
        sz[u] = 1;
3
        for(int v : adjList[u]) {
            if (v==p || mkd[v])
4
                continue;
            fill_sz(v,u);
            sz[u]+=sz[v];
8
9
10
   int get_centroid(int u, int n, int p){
11
        for(int v : adjList[u]){
12
13
            if (v==p || mkd[v])
14
                continue;
15
            if(sz[v] > n/2)
                return get_centroid(v, n, u);
16
17
18
        return u;
19
20
21
   int decomp(int u){
22
        fill_sz(u, -1);
23
        int cent = get_centroid(u, sz[u], -1);
24
        mkd[cent] = true;
25
        for(int v : adjList[cent]){
26
            if (mkd [v])
27
                continue:
28
            int r = decomp(v);
29
            centP[r] = cent;
30
31
        return cent;
32
```

SCC Tarjans

```
stack<int> scc;
   int dfsCounter=1;
    int sccIdx=1;
    map<int, int> sccMap;
6
    void tarjans(int u){
        scc.push(u);
8
        vis [u]=true;
9
10
        dfs_low[u] = dfs_num[u] = dfsCounter++;
11
12
        for (int i = 0; i < adjList[u].size(); i++)
13
             int v = adjList[u][i];
             if(dfs_num[v]==0)
14
15
                 tarjans(v);
16
                 dfs_low[u] = min(dfs_low[u], dfs_low[v]);
17
             } else if (vis [v]) {
                 dfs_low[u] = min(dfs_low[u], dfs_num[v]);
18
19
20
21
        if(dfs_low[u]==dfs_num[u])
             while (1) {
22
23
                 int v = scc.top(); scc.pop();
24
                 \operatorname{sccMap}[v] = \operatorname{sccId}x;
25
                 vis[v] = false;
26
                 if (v==u)
27
                     break;
28
29
             sccIdx++;
30
31
    AP & Bridges
1
    int dfs(int u,int p){
2
        dfs_num[u] = dfs_low[u] = ++dfs_counter;
3
        for(auto v : adjList[u]){
4
             if(dfs_num[v]==0)
5
                 dfs(v,u);
6
                 if(dfs_low[v] >= dfs_num[u])
                     articulation [u]=true;
8
9
                 if(dfs_low[v] > dfs_num[u])
10
                     bridge = true;
11
                 dfs_low[u] = min(dfs_low[u], dfs_low[v]);
12
             } else if(v!=p)
                 dfs_low[u] = min(dfs_low[u], dfs_num[v]);
13
14
15
```

Network Flow

Edmond Karp Max Flow

```
1 void aug(int u, int minE){
2
        if(u==S){ f=minE; return; }
3
        if(p[u]!=u){
             aug(p[u], min(minE, res[p[u]][u]));
4
 5
             res[p[u]][u]-=f;
6
             res[u][p[u]]+=f;
 8
9
10 int main(){
11
        int mf=0;
12
        for (;;) {
13
             f=0;//Global
             for (int i = 0; i < N; i++)
14
15
                 dist[i]=INF, p[i]==i;
16
             dist[S]=0;
17
             queue < int > q; q.push(S);
18
             while (!q.empty()) {
                 int u = q. front(); q.pop();
19
20
                 if(u==T) break;
21
                 for (int i = 0; i < N; i++)
22
                      if (res [u] [i] > 0 && dist [i]==INF)
23
                          \operatorname{dist}[i] = \operatorname{dist}[u] + 1, p[i] = u, q.\operatorname{push}(i);
24
25
             aug(T, INF);
26
             if(f==0) break;
27
             mf+=f;
28
29
        vector<ii> used;
30
        for(int i = 0; i < N; i++)
31
             for (int j = 0; j < N; j++)
                 if (graph [i][j] > 0 && res[i][j] < graph [i][j])
32
33
                     used.push_back(make_pair(i,j));
34 }
   Ford Fulkerson Max Flow
1 int ff(int u, int minE){
2
        i f ( u==T)
3
             return minE;
4
        vis [u]=true;
5
        for(auto i : adjList[u]){
6
             if (! vis [i] && res [u] [i] > 0) {
                 if(int f = ff(i, min(minE, res[u][i])))
7
                     res[u][i] -= f;
9
                     res[i][u] += f;
10
                     return f;
11
12
13
14
        return 0;
15 }
16
17 int main(){
        int mf = 0;
18
```

```
19
        while (1) {
20
            memset(vis,0,sizeof(vis));
21
            int f = ff(S, INF);
22
            if(f==0)
23
                break;
24
            mf+=f;
25
26
        printf("%d\n",mf);
27 }
```

2 Data Structures

13 for (int j = 1; (1 << j) <= N; j++)

Fenwick Tree

```
1 int tree [MX.N];
 2 int N;
    int lsOne(int i) \{ return i \& (-i); \}
    void update(int k,int v){
          for (; k<MX_N; k+=lsOne(k))
 6
                tree[k]+=v;
 7
    int query(int k){
 8
          int cnt=0;
10
          for (; k; k-=lsOne(k)) {
11
                cnt+=tree [k];
12
13
          return cnt;
14 }
    UFDS
   int find(int u) { return p[u] = (p[u] = u ? u : find(p[u])); }
 3
    inline void join (int a, int b) {
          pa = find(a);
          pb = find(b);
 6
          if (pa!=pb) {
                if(rank[pa] < rank[pb])
                     ni = pb;
                     pb = pa;
10
                     pa = ni;
11
12
                p[pb] = pa;
                if (rank [pa]==rank [pb])
13
14
                     rank[pa]++;
15
16
    Sparse Table
    inline int rmq(int u, int v){
 2
          if(u > v)
 3
                return -20000000000;
 4
          int k=(int) floor(log2((double)(v-u+1)));
 5
          if (r [mtable [u] [k]] >
 6
                     r [ mtable [ v-(1 << k) + 1 ] [k] ] )
                return mtable[u][k];
 8
          \textbf{return} \hspace{0.2cm} \text{mtable} \left[ \hspace{0.1cm} v \hspace{-0.1cm} - \hspace{-0.1cm} (1 \hspace{-0.1cm} < \hspace{-0.1cm} k \hspace{0.1cm} \right] \hspace{0.1cm} \left[ \hspace{0.1cm} k \hspace{0.1cm} \right] \hspace{0.1cm} ; \hspace{0.1cm}
9
10
    for (int i = 0; i < N; i++)
11
          mtable[i][0] = i;
```

```
14
        for (int i = 0; i + (1 << j) - 1 < N; ++i)
15
             if (r [mtable [i] [j−1]]
16
                     >r [ mtable [ i+(1<<(j-1)) ] [ j-1] ])
17
                 mtable[i][j] = mtable[i][j-1];
18
             else
19
                 mtable[i][j]=mtable[i+(1<<(j-1))][j-1];
    Segment Tree
   int tree [MX_N*4 + 2];
   int a [MX_N];
   int N;
    void construct (int p, int L, int R) {
6
        if (L=R) {
             tree[p] = a[L];
             return:
9
10
        if (R<L)
11
             return;
12
        int md = (L+R)/2;
13
        construct (2*p,L,md);
14
        construct(2*p+1,md+1,R);
15
        tree[p] = min(tree[2*p], tree[2*p+1]);
16
17
18
    void update(int p, int L, int R, int ind, int v) {
19
        if (L=R) {
20
             a[ind] = v;
21
             tree[p] = v;
22
             return;
23
24
        int md = (L+R)/2;
25
        if (ind \le md)
26
             update(2*p,L,md,ind,v);
27
        else
28
             update(2*p+1,md+1,R,ind,v);
29
        tree[p] = min(tree[2*p], tree[2*p+1]);
30
31
    int rmq(int p, int L, int R, int l, int r){
32
33
        if(r < L \mid \mid l > R)
34
             return INF:
35
        if(l>=L && r<=R)
36
             return tree[p];
37
        int md = (l+r)/2;
38
        return \min(\operatorname{rmg}(2*p, L, R, l, md), \operatorname{rmg}(2*p+1, L, R, md+1, r));
39
    Convex Hull Trick
1 // Convex hull trick, simpler if can sort insertions and queries
    struct CvxHullTrickSimple {
        vector < ll > A;
```

```
vector < ll > B;
                                                                                      55
5
                                                                                      56
                                                                                               bool bad(set < line > :: iterator y) {
6
        int ptr;
                                                                                      57
                                                                                                   auto z = next(y);
                                                                                      58
                                                                                                   if (y=hull.begin()) {
        cvxH():ptr(0)\{\}
                                                                                      59
                                                                                                       if (z==hull.end())
9
                                                                                      60
                                                                                                            return false;
10
        // insert a descending
                                                                                      61
                                                                                                       return y\rightarrow a == z\rightarrow a \&\& y\rightarrow b >= z\rightarrow b;
11
        void addLine(11 a, 11 b) \{ // intersection of (A[len-2],B[len-2]) with 62 \}
             (A/len-1), B/len-1) must lie to the left of intersection of (A/len63)
                                                                                                   auto x = prev(y);
             -1/,B/len-1/) with (a,b)
                                                                                                   if (z=hull.end())
12
             while (sz(A) >= 2 \&\& (B[sz(B) - 2] - B[sz(B) - 1]) * (a - A[sz(A)65])
                                                                                                       return x->a == y->a && x->b <= y->b;
                 [-1] >= [B[sz(B) - 1] - b] * (A[sz(A) - 1] - A[sz(A) - 2])) 66
                                                                                                   return xcomp(*x, *y, *z) < 0;
13
                 A. pop_back();
                                                                                      67
                 B. pop_back();
                                                                                      68
14
                                                                                      69
                                                                                               void addLine(ll a, ll b) { // add line a*x + b
15
             A. pb(a);
                                                                                      70
                                                                                                   CvxHullOpt::line l{a,b};
16
             B.pb(b);
                                                                                      71
                                                                                                   auto v = hull.insert(1);
17
                                                                                                   if(bad(y)) { hull.erase(y); return;}
18
                                                                                      72
19
                                                                                      73
                                                                                                   while (\text{next}(y) != \text{hull.end}() \&\& \text{bad}(\text{next}(y)))
20
        // query x ascending
                                                                                      74
                                                                                                       hull.erase(next(y));
21
        ll minValue(ll x) {
                                                                                                   while (y!=hull.begin() && bad(prev(y)))
                                                                                      75
           ptr = min(ptr, sz(A) - 1);
22
                                                                                      76
                                                                                                       hull.erase(prev(v));
23
           while (ptr + 1 < sz(A) \&\& A[ptr + 1] * x + B[ptr + 1] <= A[ptr] * x77
                                                                                                   if(next(y)=hull.end())
               + B[ptr]) {
                                                                                                       y->xLeft = -INF;
24
                                                                                      79
                                                                                                   else
             ++ptr;
25
                                                                                      80
                                                                                                       y \rightarrow x Left = xin(*y, *next(y));
          return A[ptr] * x + B[ptr];
26
                                                                                                   if(v != hull.begin())
                                                                                      81
27
                                                                                      82
                                                                                                       prev(y) \rightarrow xLeft = xin(*prev(y), *y);
28
    };
                                                                                      83
29
                                                                                      84
   struct CvxHullOpt {
                                                                                      85
                                                                                               ll eval(ll x)
31
        // Fully dynamic variant for use if can't quarantee
                                                                                      86
                                                                                                   auto l = hull.lower_bound(\{qV, 0, x\});
        // insertion or query order
32
                                                                                      87
                                                                                                   return l \rightarrow a*x + l \rightarrow b;
        // stores lower envelope, negate lines and function to get upper
                                                                                      88
33
34
                                                                                      89
                                                                                         };
        static const 11 qV = -(1LL << 50); //hacky special value
35
        struct line {
36
             11 a.b:
37
             mutable double xLeft;
38
             bool operator < (const line& l) const {
39
                 if(l.a!= qV)
40
                      return a < l.a;
41
                 return xLeft > l.xLeft;
42
43
        };
44
        multiset < line > hull:
45
46
        ll xcomp(const line& a, const line& b, const line& c){
             // < 0 \Rightarrow AxB < AxC
47
48
             // > 0 \Rightarrow AxB > AxC
             return (a.a-c.a)*(b.b-a.b) - (c.b-a.b)*(a.a-b.a);
49
50
51
52
        double xin(const line& a, const line& b){
53
             return (b.b - a.b)/(1.0*(a.a-b.a));
54
```

3 Geometry

Convex Hull

```
int main() {
2
        for (int i = 0; i < N; i++){
3
            perm[i]=i;
4
 5
        sort (perm, perm+N,
                 [](int a, int b){
                     const point &pa = V[a];
                     const point &pb = V[b];
9
                     if (real (pa)!=real (pb))
10
                         return real(pa) < real(pb);
11
                     return imag(pa) < imag(pb);
12
13
        vector<int> L; vector<int> U;
14
        for (int i = 0; i < N;) {
15
            int t = L. size();
16
            if(t \ge 2 \&\& ! ccw(V[L[t-2]],V[L[t-1]],V[perm[i]]))
17
                 L. pop_back();
18
19
                 L. push_back(perm[i++]);
20
21
        for (int i = N-1; i >=0;) {
22
            int t = U. size();
23
            if(t \ge 2 \&\& ! ccw(V[U[t-2]],V[U[t-1]],V[perm[i]]))
24
                 U.pop_back();
25
            else
26
                 U. push_back (perm [i --]);
27
28
        vector<int> hull;
29
        for (int i = 0; i < L. size() -1; ++i)
30
             hull.push_back(L[i]);
31
        for (int i = 0; i < U. size() -1; ++i)
32
             hull.push_back(U[i]);
33
        return 0;
34
```

Geometry Axioms

```
1 typedef complex < double > pt;
2 typedef complex < double > vec;
3 typedef vector < pt > pgon;
4 typedef struct { pt p,q; } lseg;
5 struct circ { pt c; double r; };
6 struct rect { pt p,q;}; // X(p) <= X(q) and Y(p) <= Y(q)
7
8 double cross (const vec& a, const vec &b) {
9 return x(a)*y(b)-y(a)*x(b);
10 }
11 // cross product of (b-a) and (c-b), 0 is collinear
12 int orientation (const pt& a,
13 const pt& b, const pt& c) {</pre>
```

```
14
        double v = cross(b-a, c-b);
15
        if(abs(v-0.0) < EPS)
16
            return 0;
17
        return v > 0 ? 1 : 2;
18
19
    //Line segment intersection
    bool intersects (const lseg& a, const lseg& b) {
21
        if(a.q = b.p \mid\mid b.q = a.p)
22
            return false;
23
        if (orientation (a.p,a.q,b.p)
24
                 != orientation (a.p,a.q,b.q)
25
                 && orientation (b.p,b.q,a.p)
26
                 != orientation(b.p,b.q,a.q))
27
            return true;
28
        return false;
29
30
   //Area of polygon
31
    double area (const pgon& p) {
32
        double area = 0.0;
33
        for(int i = 1; i < p.size(); ++i)
34
            area += cross(p[i-1],p[i]);
35
        return abs(area)/2.0;
36
37
    //If a \rightarrow b \rightarrow c is a counterclockwise turn
38
    double ccw(const point& a, const point& b,
39
            const point& c){
40
        if (a==b | b==c | a==c)
41
            return false:
42
        point relA = b-a;
43
        point relC = b-c;
44
        return cross (relA, relC) >= 0.0;
45
    //Returns if point p is in the polygon poly
47
    bool in Poly (const pgon& poly, const pt& p) {
48
        for (int i = 0; i < poly.size()-1; i++){
49
             if (! ccw ( poly [ i ] , p , poly [ i +1] ) )
50
                 return false;
51
52
        return true:
53
    //Distance from p to line (a,b)
    double distToLine(const pt& p, const pt& a,
56
            const pt &b){
57
        vec ap = p-a;
        vec ab = b-a:
58
59
        double u = dot(ap, ab)/dot(ab, ab);
60
        //Ignore for non-line segment
        if(u < 0.0) //Closer to a
61
62
            return abs(a-p);
63
        if (u > 1.0) //Closer to b
64
            return abs(b-p);
65
        pt c = a+ab*u; // This is the point
66
        return abs(c-p);
67
    //intersection pts of two circles
```

```
vector<pt> insct(const circ& a, const circ& b){
70
         vector <pt> o;
71
         double dist = abs(a.c - b.c);
72
         if(dist > a.r + b.r)
73
             return o; //none, don't touch
         if(abs(a.r-b.r) > dist)
74
75
             return o; //none, inside
76
         if(abs(dist - (a.r + b.r)) < EPS) \{ // one intersect \}
77
             pt p = a.c + (a.r/dist)*(b.c-a.c);
78
             o.pb(p);
79
             return o;
80
         double delta = (sq(dist) + (a.r-b.r)*(a.r+b.r))/(2.0*dist);
81
82
         pt cent = a.c + (delta/dist)*(b.c-a.c);
83
84
         double h = sqrt(sq(a.r) - sq(delta));
85
86
         pt dVec = (b.c - a.c)/dist;
87
         o.pb(cent + h*pt(0,1)*dVec);
88
         o.pb(cent + h*pt(0,-1)*dVec);
89
         return o:
90
91
    // intersection of two rectangles, sets none to true if no overlap
    rect overlap (const rect& a, const rect& b, bool& none) {
94
         rect r:
95
         if(X(a.p) > X(b.q) | | Y(a.p) > Y(b.q)
96
             | | X(b.p) > X(a.q) | | Y(b.p) > Y(a.q) ) |
97
             none=true;
98
             return r;
99
100
        r.p = \{\max(X(a.p), X(b.p)), \max(Y(a.p), Y(b.p))\};
101
         r.q = \{ \min(X(a.q), X(b.q)), \min(Y(a.q), Y(b.q)) \};
102
         return r;
103
```

4 Strings

Suffix Array

```
void countingSort(int k){
        int i, sum, maxi=\max(300,N);
3
        memset(c, 0, sizeof(c));
4
        for (i = 0; i < N; i++)
            c[i+k < N ? RA[i+k] : 0]++;
        for (i=sum=0; i < maxi; i++)
            int t = c[i];
8
            c[i]=sum;
9
            sum+=t;
10
11
        for (i = 0; i < N; i++)
12
            tempSA [c [SA [i]+k < N
                 ? RA[SA[i]+k]: 0]++] = SA[i];
13
14
        for (i=0; i < N; i++)
15
            SA[i] = tempSA[i];
16
17
18
    int main(){
19
        for (int i = 0; i < N; i++)
20
            SA[i]=i, RA[i]=input[i];
21
22
        for (int k = 1; k < N; k <<= 1) {
23
            countingSort(k);
24
            countingSort(0);
25
            tempRA[SA[0]] = r = 0;
26
            for (int i = 1; i < N; i++){
27
                 tempRA [SA [ i ] ]
                     =(RA[SA[i]])==RA[SA[i-1]]
28
29
                     && RA[SA[i]+k] = RA[SA[i-1]+k]
30
                     ? r:++r);
31
32
            for (int i = 0; i < N; i++)
33
                 RA[i] = tempRA[i];
34
35
        return 0;
36
    Trie
    struct node {
2
        node * children [26];
3
        int count;
4
        node(){
5
            memset(children, 0, sizeof(children));
            count = 0;
8
    };
10
   void insert(node* nd, char *s){
11
        if(*s){
```

```
12
             if (!nd->children[*s-'a'])
                 nd \rightarrow children [*s-'a'] = new node();
13
14
            insert(nd->children[*s-'a'],s+1);
15
16
        nd \rightarrow count ++;
17
18
19
   int count(node* nd, char *s){
20
        if(*s){
21
            if (!nd->children[*s-'a'])
22
                 return 0;
23
            return count (nd->children [*s-'a'], s+1);
24
        } else {
25
            return nd->count;
26
27 }
   KMP
1 vector < int > buildFailure(string s){
2
        vector < int > T(n+1,0);
3
        T[0] = -1;
        int j = 0;
4
 5
        for (int i = 1; i < s. size(); ++i){
6
            if (s[i]==s[j]) {
                 T[i]=T[j];
8
                 j++;
9
            } else{
10
                 T[i] = j;
11
                 j = T[j];
12
                 while (j >= 0 \&\& s[i]! = s[j])
13
                     j = T[j];
14
                 j++;
15
16
       T[s.size()] = j;
17
18
        return T;
19
20
   vector < int > search (string W, string S) {
21
        auto T=buildFailure(W);
22
        vector <int> p;
23
        int k = 0;
24
        int j = 0;
25
        \mathbf{while}(j < S.size())
26
            if(W[k]==S[j])
27
                 k++; j++;
28
                 if (k=₩. size ()) {
29
                     p.push_back(j-k);
30
                     k = T[k];
31
32
            }else{
33
                 k = T[k];
34
                 if(k < 0)
35
                     j+=1, k+=1;
36
```

37 38 return p; 39 }

5 Algorithms

NlogN LIS

```
1 int ls [MX_N];
   int L[MX_N];
   int I[MX.N];
 5
   void nlogn(){
        for (int i = 1; i < N+1; ++i)
            I[i]=INF;
 8
        I[0] = -INF;
9
        int mx = 1;
        for (int i = 0; i < N; ++i){
10
            int ind = lower_bound(I, I+N+1, ls[i]) - I;
11
            I[ind] = ls[i];
12
13
            L[i] = ind;
14
            mx = max(mx, ind);
15
16
        int prv = INF;
17
        vector < int > out;
18
        for (int i = N-1; i >= 0; —i){
            if(ls[i] < prv && L[i]==mx){
19
20
                out.push_back(ls[i]);
21
                prv = ls[i];
22
                mx--;
23
24
25
```

RectInHist

```
1 int R,C;
   char board [MX_RC] [MX_RC];
   int h[MX_RC][MX_RC];
5
   int perim(int 1, int w){
        if ( l==0 | | w==0)
6
            return 0:
8
        return 2*1 + 2*w;
9
10
11 int main(){
12
        for (int i = 0; i < R; i++){
13
            int run=0;
14
            for (int j = 0; j < C; j++){
15
                run = (board[i][j] == '. '?run + 1:0);
16
                h[i][j] = run;
17
18
19
        int mx = 0;
20
        for (int j = 0; j < C; j++){
21
            stack<int> s;
22
            for (int i = 0; i < R; i++){
```

```
23
                 if (s.empty()
24
                          | | h [ i ] [ j ] > h [ s.top() ] [ j ])
25
                      s.push(i);
26
                 else if(h[i][j]<h[s.top()][j]){
27
                      while (!s.empty()
28
                     &&h[i][j]<h[s.top()][j]){
                          int l = h[s.top()][j];
29
30
                          s.pop();
31
                          int pm = perim(1,
32
                               (s.empty()?
33
                               i:i-s.top()-1));
34
                          mx = max(mx,pm);
35
36
                      s.push(i);
37
                 \} else if (h[i][j]==h[s.top()][j])
38
                      s.pop();
39
                      s.push(i);
40
41
42
             while (! s . empty()) {
43
                 int l = h[s.top()][j]; s.pop();
44
                 int pm = perim(1, s.empty() ? R : R - s.top()-1);
45
                 mx = max(mx, pm);
46
47
48
        printf("%d\n",mx-1);
49
```

6 Maths

Miller Rabin

```
void factor(ll x, ll& e, ll& k){
2
        while (x\%2LL==0LL)
3
            x/=2LL;
 4
            ++e;
 5
 6
        k = x;
 7
    //increase x for higher certainty, 5 works well
    bool is_prime(ll n, int x){
11
        if (n&2LL==0 | n==1LL)
12
            return false;
13
        if (n==2 | | n==3 | | n==5 | | n==7)
14
            return true;
15
        ll e, k;
16
        factor (n-1,e,k);
17
        while (x-->0){
18
            11 a = (rand())\%(n-5LL) + 2LL;
19
            ll p = mod_exp(a,k,n);
20
            if (p==1LL || p==n-1LL)
21
                 continue;
22
            bool all_fail = true;
23
            for (int i = 0; i < e-1; ++i) {
24
                p = mod_exp(p, 2, n);
25
                 if(p=n-1LL)
26
                     all_fail = false;
27
                     break;
28
29
30
            if (all_fail)
31
                return false;
32
33
        return true;
34
```

Binomial Coefficients

```
void factor(ll x, ll& e, ll& k){
2
        while (x\%2LL==0LL)
3
             x/=2LL;
4
            ++e;
6
        k = x;
7
    //increase x for higher certainty, 5 works well
    bool is_prime(ll n, int x){
        if (n&2LL==0 | | n==1LL)
11
12
             return false;
        if (n==2 || n==3 || n==5 || n==7)
13
14
             return true;
15
        ll e, k;
16
        factor(n-1,e,k);
17
        while (x-->0){
             11 \ a = (rand())\%(n-5LL) + 2LL;
18
19
             ll p = mod_exp(a,k,n);
20
             if (p==1LL | | p==n−1LL)
21
                 continue:
22
             bool all_fail = true;
23
             for (int i = 0; i < e-1; ++i){
24
                 p = mod_exp(p, 2, n);
25
                 \mathbf{i} \mathbf{f} (p=n-1LL) 
26
                      all_fail = false;
27
                     break;
28
29
30
             if (all_fail)
31
                 return false;
32
33
        return true;
34
    Gaussian Elimination
    * mat is augmented matrix
     * e.q 3x + 4y = 2 is [3,4,2]
     */
    void gauss (double mat [MX_N] [MX_N+1], double ans [MX_N], int n) {
6
        int i, j, k, l; double t;
7
8
        for (j = 0; j < n-1; ++j)
9
            l = i;
10
             for (i = j+1; i < n; ++i)
11
                 if (fabs (mat[i][j]) > fabs (mat[l][j]))
12
                     l=i:
13
14
             \mathbf{for}(k = j; k \le n; ++k)
15
                 t=mat[j][k], mat[j][k]=mat[l][k], mat[l][k]=t;
16
             for (i = j+1; i < n; ++i)
17
                 for(k = n; k >= j; ---k)
                     mat[i][k] = mat[j][k] * mat[i][j] / mat[j][j];
18
```

```
19
20
21
        for (j = n-1; j >= 0; ---j)
22
            for (t=0.0, k=j+1; k< n; ++k)
23
                t += mat[j][k] * ans[k];
24
            ans[j] = (mat[j][n] - t) / mat[j][j];
25
26
   Ternary Search
   double ternary_search (double 1, double r) { //maximises
2
        while (r - l > EPS) {
3
            double m1 = 1 + (r - 1) / 3;
4
            double m2 = r - (r - 1) / 3;
            double f1 = f(m1);
            double f2 = f(m2);
            if (f1 < f2)
                l = m1;
9
            else
10
                r = m2;
11
12
        return f(l);
13
   Matrix Exponential
   /* c = a * b * /
   void mu(11 a[][NMAT], 11 b[][NMAT], 11 c[][NMAT], int _n) {
            for (int i=0; i<_n; i++)
                    for(int j=0; j<_n; j++) {
4
5
                             c[i][j]=0;
                             for (int h=0;h<_n;h++) {
                                      c[i][j] += (a[i][h]*b[h][j])%mod;
                                      c [ i ] [ j]%=mod;
9
10
11
12
    /* returns ans=mat^b*/
   void power(ll ans[][NMAT], ll mat[][NMAT], ll b, int _n) {
14
15
            11 tmp [NMAT] [NMAT];
16
            for (int i=0; i<_n; i++)
17
                    for (int j = 0; j < n; j++)
18
                             ans[i][j]=i==j;
19
            while(b) {
20
                     if (b&1) {
21
                             mu(ans, mat, tmp, _n);
22
                             for (int i = 0; i < n; i++)
23
                                      for (int j=0; j<_n; j++)
^{24}
                                              ans[i][j]=tmp[i][j];
25
26
                    mu(mat, mat, tmp, _n);
27
                    for (int i=0; i<_n; i++)
```

```
for (int j=0; j<_n; j++)
                                       mat[i][j]=tmp[i][j];
                     b >> = 1;
32 }
```

28

29

30

31