Data Structures and Algorithms for competitive programming

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1 Graphs

Traversal

```
\mathbf{BFS}
```

```
int dist[MXN];
   vector < int > adjList [MX.N];
3
   int main(){
 5
        for(int i = 0; i < MX_N; i++)
 6
            dist[i]=INF;
        queue<int> q;
 8
        q.push(0);
9
        dist[0] = 0;
10
        while (!q.empty()) {
            int u = q.front(); q.pop();
11
12
            int d = dist[u];
            for(int i : adjList[u]){
13
                 if (dist [i]==INF) {
14
                     dist[i]=d+1;
15
16
                     q.push(i);
17
18
19
20
        return 0;
   Dijkstras
   struct path {
2
        int u,d;
3
        bool operator < (const path& p) const {
 4
            return d > p.d;
 5
 6
    };
    for (int i =0; i < N; ++i)
        dist[i] = INF;
    dist[S] = 0;
   priority_queue < path > q;
   q.push(path(S,0));
12
   while (!q.empty()) {
13
        path p = q.top(); q.pop();
14
        u = p.u, d = p.d;
15
        if(dist[u] < d)
16
            continue;
17
        for (auto v : adjList[u]) {
            nd = d + v.second;
18
19
            if(nd < dist[v.first]){</pre>
20
                 dist[v.first] = nd;
21
                q.push(path{v.first,nd});
22
23
24
```

Trees

MST

```
struct edge {
2
        int x, y, w;
3
        bool operator < (edge e) const {
4
            return w < e.w;
5
6
    };
8
   int main(){
9
        vector<edge> eList; //Input
10
        for (int i = 0; i < N; i++)// Set up UFDS
11
            p[i]=i;
12
        vector<ii> treeList;
13
        sort (eList.begin(), eList.end());
14
        int cost = 0;
15
        int sz=N;
16
        int u, v, w;
17
        for (const auto &i : eList) {
18
            v=i.x; u=i.y; w=i.w;
19
            if (!connected(u,v)){
20
                join (u,v);
21
                treeList.push\_back(\{min(u,v),max(u,v)\});
22
                sz --;
23
                 cost+=w;
24
25
26
        if (sz!=1)
27
            puts("Impossible");
28
   LCA
    *H/u is first visit of u
    *E[x] is vertex at time x
4
    *L[x] is depth at time x
5
    */
    void vis(int u, int d){
6
        H[u] = vind;
8
        E[vind] = u;
9
        L[vind++] = d;
10
        for (auto i : adjList[u]) {
11
            if(H[i]!=-1)
12
                continue;
13
            vis(i,d+1);
14
            E[vind] = u;
15
            L[vind++] = d;
16
17
18
19
    int LCA(int u, int v){
20
        if(H[u] > H[v])
```

```
21
            int t = u:
22
            u = v;
23
            v = t;
24
25
        //run some range min query on L
26
        //between H/u/ and H/v/
27
        int ind = rmq(H[u], H[v]);
28
        return E[ind];
29
30
31
   int dist(int u, int v){
32
        int a = H[u];
33
        int b = H[v];
34
        int ind = LCA(u, v);
35
        return abs(L[H[ind]]-L[a])
36
            + abs(L[H[ind]]-L[b]);
37
   Centroid Decomposition
   void fill_sz(int u, int p){
2
        sz[u] = 1;
3
        for(int v : adjList[u]) {
            if (v==p || mkd[v])
4
                continue;
            fill_sz(v,u);
            sz[u]+=sz[v];
8
9
10
   int get_centroid(int u, int n, int p){
11
        for(int v : adjList[u]){
12
13
            if (v==p || mkd[v])
14
                continue;
15
            if(sz[v] > n/2)
                return get_centroid(v, n, u);
16
17
18
        return u;
19
20
21
   int decomp(int u){
22
        fill_sz(u, -1);
23
        int cent = get_centroid(u, sz[u], -1);
24
        mkd[cent] = true;
25
        for(int v : adjList[cent]){
26
            if (mkd [v])
27
                continue:
28
            int r = decomp(v);
29
            centP[r] = cent;
30
31
        return cent;
32
```

SCC Tarjans

```
stack<int> scc;
   int dfsCounter=1;
    int sccIdx=1;
    map<int, int> sccMap;
6
    void tarjans(int u){
        scc.push(u);
8
        vis [u]=true;
9
10
        dfs_low[u] = dfs_num[u] = dfsCounter++;
11
12
        for (int i = 0; i < adjList[u].size(); i++)
13
             int v = adjList[u][i];
             if(dfs_num[v]==0)
14
15
                 tarjans(v);
16
                 dfs_low[u] = min(dfs_low[u], dfs_low[v]);
17
             } else if (vis [v]) {
                 dfs_low[u] = min(dfs_low[u], dfs_num[v]);
18
19
20
21
        if(dfs_low[u]==dfs_num[u])
             while (1) {
22
23
                 int v = scc.top(); scc.pop();
24
                 \operatorname{sccMap}[v] = \operatorname{sccId}x;
25
                 vis[v] = false;
26
                 if (v==u)
27
                     break;
28
29
             sccIdx++;
30
31
    AP & Bridges
1
    int dfs(int u,int p){
2
        dfs_num[u] = dfs_low[u] = ++dfs_counter;
3
        for(auto v : adjList[u]){
4
             if(dfs_num[v]==0)
5
                 dfs(v,u);
6
                 if(dfs_low[v] >= dfs_num[u])
                     articulation [u]=true;
8
9
                 if(dfs_low[v] > dfs_num[u])
10
                     bridge = true;
11
                 dfs_low[u] = min(dfs_low[u], dfs_low[v]);
12
             } else if(v!=p)
                 dfs_low[u] = min(dfs_low[u], dfs_num[v]);
13
14
15
```

Network Flow

Edmond Karp Max Flow

```
1 void aug(int u, int minE){
2
        if(u==S){ f=minE; return; }
3
        if(p[u]!=u){
             aug(p[u], min(minE, res[p[u]][u]));
4
 5
             res[p[u]][u]-=f;
6
             res[u][p[u]]+=f;
 8
9
10 int main(){
11
        int mf=0;
12
        for (;;) {
13
             f=0;//Global
             for (int i = 0; i < N; i++)
14
15
                 dist[i]=INF, p[i]==i;
16
             dist[S]=0;
17
             queue < int > q; q.push(S);
18
             while (!q.empty()) {
                 int u = q. front(); q.pop();
19
20
                 if(u==T) break;
21
                 for (int i = 0; i < N; i++)
22
                      if (res [u] [i] > 0 && dist [i]==INF)
23
                          \operatorname{dist}[i] = \operatorname{dist}[u] + 1, p[i] = u, q.\operatorname{push}(i);
24
25
             aug(T, INF);
26
             if(f==0) break;
27
             mf+=f;
28
29
        vector<ii> used;
30
        for(int i = 0; i < N; i++)
31
             for (int j = 0; j < N; j++)
                 if (graph [i][j] > 0 && res[i][j] < graph [i][j])
32
33
                     used.push_back(make_pair(i,j));
34 }
   Ford Fulkerson Max Flow
1 int ff(int u, int minE){
2
        i f ( u==T)
3
             return minE;
4
        vis [u]=true;
5
        for(auto i : adjList[u]){
6
             if (! vis [i] && res [u] [i] > 0) {
                 if(int f = ff(i, min(minE, res[u][i])))
7
                     res[u][i] -= f;
9
                     res[i][u] += f;
10
                     return f;
11
12
13
14
        return 0;
15
16
17 int main(){
        int mf = 0;
18
```

```
19
        while (1) {
20
            memset(vis,0,sizeof(vis));
21
            int f = ff(S, INF);
22
            if(f==0)
23
                break;
24
            mf+=f;
25
26
        printf("%d\n",mf);
27 }
```

2 Data Structures

13 for (int j = 1; (1 << j) <= N; j++)

Fenwick Tree

```
1 int tree [MX_N];
2 int N;
  int lsOne(int i) \{ return i \& (-i); \}
   void update(int k,int v){
        for (; k<MX_N; k+=lsOne(k))
6
            tree[k]+=v;
7
   int query(int k){
8
        int cnt=0;
10
        for (; k; k-=lsOne(k)) {
11
            cnt+=tree[k];
12
13
        return cnt;
14 }
   UFDS
1 int find(int u) { return p[u] = (p[u] = u ? u : find(p[u])); }
3
   inline void join (int a, int b) {
        pa = find(a);
        pb = find(b);
6
        if (pa!=pb) {
            if(rank[pa] < rank[pb])
8
                ni = pb;
9
                pb = pa;
10
                pa = ni;
11
12
            p[pb] = pa;
            if (rank [pa]==rank [pb])
13
14
                rank[pa]++;
15
16
   Sparse Table
   inline int rmq(int u, int v){
2
        if(u > v)
3
            return -20000000000;
4
        int k=(int) floor(log2((double)(v-u+1)));
5
        if (r [mtable [u] [k]] >
6
                r [ mtable [ v-(1 << k) + 1 ] [k] ] )
            return mtable[u][k];
8
        return mtable [v-(1 << k) + 1][k];
9
10
   for (int i = 0; i < N; i++)
11
        mtable[i][0] = i;
```

```
14
        for (int i = 0; i + (1 << j) - 1 < N; ++i)
15
             if (r [mtable [i] [j−1]]
16
                     >r [ mtable [ i+(1<<(j-1)) ] [ j-1] ])
17
                 mtable[i][j] = mtable[i][j-1];
18
             else
19
                 mtable[i][j]=mtable[i+(1<<(j-1))][j-1];
    Segment Tree
1 int tree [MX_N*4 + 2];
   int a [MX_N];
3
   int N;
    void construct (int p, int L, int R) {
6
        if (L=R) {
7
             tree[p] = a[L];
8
             return:
9
        if (R<L)
10
11
             return;
12
        int md = (L+R)/2;
13
        construct (2*p,L,md);
14
        construct(2*p+1,md+1,R);
15
        tree[p] = min(tree[2*p], tree[2*p+1]);
16
17
18
    void update(int p, int L, int R, int ind, int v){
19
        if (L=R) {
20
             a[ind] = v;
21
             tree[p] = v;
22
             return:
23
24
        int md = (L+R)/2;
25
        if (ind \ll md)
26
             update(2*p,L,md,ind,v);
27
28
             update(2*p+1,md+1,R,ind,v);
29
        tree[p] = min(tree[2*p], tree[2*p+1]);
30
31
32
    int rmq(int p, int L, int R, int l, int r){
        if(r < L \mid \mid l > R)
33
34
             return INF;
35
        if(l>=L && r<=R)
36
             return tree[p];
37
        int md = (l+r)/2;
38
        return \min(\text{rmq}(2*p, L, R, l, md), \text{rmq}(2*p+1, L, R, md+1, r));
39 }
```

3 Geometry

Convex Hull

```
int main() {
2
        for (int i = 0; i < N; i++){
3
            perm[i]=i;
4
 5
        sort (perm, perm+N,
                 [](int a, int b){
                     const point &pa = V[a];
                     const point &pb = V[b];
9
                     if (real (pa)!=real (pb))
10
                         return real(pa) < real(pb);
11
                     return imag(pa) < imag(pb);
12
13
        vector<int> L; vector<int> U;
14
        for (int i = 0; i < N;) {
15
            int t = L. size();
16
            if(t \ge 2 \&\& ! ccw(V[L[t-2]],V[L[t-1]],V[perm[i]]))
17
                 L. pop_back();
18
            else
19
                 L. push_back(perm[i++]);
20
21
        for (int i = N-1; i >=0;) {
22
            int t = U. size();
23
            if(t \ge 2 \&\& ! ccw(V[U[t-2]],V[U[t-1]],V[perm[i]]))
24
                 U.pop_back();
25
            else
26
                 U. push_back (perm [i --]);
27
28
        vector<int> hull;
29
        for (int i = 0; i < L. size() -1; ++i)
30
             hull.push_back(L[i]);
31
        for (int i = 0; i < U. size() -1; ++i)
32
             hull.push_back(U[i]);
33
        return 0;
34
```

Geometry Axioms

```
typedef complex<double> pt;
   typedef complex<double> vec;
   typedef vector <pt> pgon;
   typedef struct { pt p,q; } lseg;
   struct circ { pt c; double r; };
   double cross (const vec& a, const vec &b) {
        return x(a)*y(b)-y(a)*x(b);
8
    //cross\ product\ of\ (b-a)\ and\ (c-b), 0 is collinear
10 int orientation (const pt& a,
11
            const pt& b, const pt& c){
12
        double v = cross(b-a, c-b);
        if(abs(v-0.0) < EPS)
13
```

```
14
            return 0:
15
        return v > 0 ? 1 : 2;
16
17
    //Line segment intersection
    bool intersects (const lseg& a, const lseg& b) {
        if(a.q = b.p \mid\mid b.q = a.p)
19
20
            return false;
        if(orientation(a.p,a.q,b.p)
21
22
                != orientation (a.p, a.q, b.q)
23
                && orientation (b.p,b.q,a.p)
24
                != orientation(b.p,b.q,a.q))
25
            return true;
26
        return false:
27
28
   //Area of polygon
29
    double area (const pgon& p) {
30
        double area = 0.0;
31
        for (int i = 1; i < p. size(); ++i)
32
            area + = cross(p[i-1], p[i]);
33
        return abs(area)/2.0;
34
35
    //If a \rightarrow b \rightarrow c is a counterclockwise turn
36
    double ccw(const point& a, const point& b,
37
            const point& c){
38
        if (a==b | b==c | a==c)
39
            return false:
40
        point relA = b-a;
41
        point relC = b-c;
42
        return cross(relA, relC) >= 0.0;
43
    //Returns if point p is in the polygon poly
    bool in Poly (const pgon& poly, const pt& p) {
45
46
        for (int i = 0; i < poly.size()-1; i++){
47
            if (! ccw(poly[i],p,poly[i+1]))
48
                return false;
49
50
        return true;
51
    //Distance from p to line (a,b)
    double distToLine(const pt& p, const pt& a,
53
54
            const pt &b){
55
        vec ap = p-a;
56
        vec ab = b-a;
57
        double u = dot(ap, ab)/dot(ab, ab);
58
        //Ignore for non-line segment
59
        if(u < 0.0) //Closer to a
60
            return abs(a-p);
        if(u > 1.0) //Closer to b
61
62
            return abs(b-p);
63
        pt c = a+ab*u; // This is the point
64
        return abs(c-p);
65
    //intersection pts of two circles
    vector<pt> insct(const circ& a, const circ& b){
68
        vector<pt> o;
```

```
69
        double dist = abs(a.c - b.c);
70
        if(dist > a.r + b.r)
71
            return o; //none, don't touch
        if(abs(a.r-b.r) > dist)
72
73
            return o; //none, inside
74
        if(abs(dist - (a.r + b.r)) < EPS) \{ // one intersect \}
75
            pt p = a.c + (a.r/dist)*(b.c-a.c);
76
            o.pb(p);
77
            return o;
78
79
        double delta = (sq(dist) + (a.r-b.r)*(a.r+b.r))/(2.0*dist);
80
        pt cent = a.c + (delta/dist)*(b.c-a.c);
81
        double h = sqrt(sq(a.r) - sq(delta));
82
83
84
        pt dVec = (b.c - a.c)/dist;
85
        o.pb(cent + h*pt(0,1)*dVec);
86
        o.pb(cent + h*pt(0,-1)*dVec);
87
        return o;
88
```

4 Strings

Suffix Array

```
void countingSort(int k){
2
        int i, sum, maxi=max(300, N);
3
        memset(c, 0, sizeof(c));
4
        for (i = 0; i < N; i++)
5
            c[i+k < N ? RA[i+k] : 0]++;
6
        for (i=sum=0; i < maxi; i++)
            int t = c[i];
8
            c[i]=sum;
9
            sum+=t;
10
11
        for (i = 0; i < N; i++)
12
            tempSA [c [SA [i]+k < N
                 ? RA[SA[i]+k]: 0]++] = SA[i];
13
14
        for (i=0; i < N; i++)
            SA[i] = tempSA[i];
15
16
17
18
    int main(){
        for (int i = 0; i < N; i++)
19
20
            SA[i]=i, RA[i]=input[i];
21
22
        for (int k = 1; k < N; k <<= 1) {
23
            countingSort(k);
24
            countingSort(0);
25
            tempRA[SA[0]] = r = 0;
            for (int i = 1; i < N; i++){
26
27
                 tempRA [SA [ i ] ]
                     =(RA[SA[i]])==RA[SA[i-1]]
28
29
                     && RA[SA[i]+k] = RA[SA[i-1]+k]
30
                     ? r:++r);
31
32
            for (int i = 0; i < N; i++)
33
                RA[i] = tempRA[i];
34
35
        return 0;
36
    Trie
    struct node {
2
        node * children [26];
3
        int count;
4
        node(){
5
            memset(children, 0, sizeof(children));
            count = 0;
7
8
    };
10
   void insert(node* nd, char *s){
11
        if(*s){
```

```
12
             if (!nd->children[*s-'a'])
                 nd \rightarrow children [*s-'a'] = new node();
13
14
            insert(nd->children[*s-'a'],s+1);
15
16
        nd \rightarrow count ++;
17
18
19
   int count(node* nd, char *s){
20
        if(*s){
21
            if (!nd->children[*s-'a'])
22
                 return 0;
23
            return count (nd->children [*s-'a'], s+1);
24
        } else {
25
            return nd->count;
26
27 }
   KMP
1 vector < int > buildFailure(string s){
2
        vector < int > T(n+1,0);
3
        T[0] = -1;
        int j = 0;
4
 5
        for (int i = 1; i < s.size();++i){
6
            if (s[i]==s[j]) {
                 T[i]=T[j];
8
                 j++;
9
            } else{
10
                 T[i] = j;
11
                 j = T[j];
12
                 while (j >= 0 \&\& s[i]! = s[j])
13
                     j = T[j];
14
                 j++;
15
16
       T[s.size()] = j;
17
18
        return T;
19
20
   vector < int > search (string W, string S) {
21
        auto T=buildFailure(W);
22
        vector <int> p;
23
        int k = 0;
24
        int j = 0;
25
        \mathbf{while}(j < S.size())
26
            if(W[k]==S[j])
27
                 k++; j++;
28
                 if (k=₩. size ()) {
29
                     p.push_back(j-k);
30
                     k = T[k];
31
32
            }else{
33
                 k = T[k];
34
                 if(k < 0)
35
                     j+=1, k+=1;
36
```

37 38 return p; 39 }

5 Algorithms

NlogN LIS

```
1 int ls [MX_N];
   int L[MX_N];
   int I[MX.N];
 5
   void nlogn(){
        for (int i = 1; i < N+1; ++i)
            I[i]=INF;
 8
        I[0] = -INF;
9
        int mx = 1;
        for (int i = 0; i < N; ++i){
10
            int ind = lower_bound(I, I+N+1, ls[i]) - I;
11
            I[ind] = ls[i];
12
13
            L[i] = ind;
14
            mx = max(mx, ind);
15
16
        int prv = INF;
17
        vector < int > out;
18
        for (int i = N-1; i >= 0; —i){
            if(ls[i] < prv && L[i]==mx){
19
20
                out.push_back(ls[i]);
21
                prv = ls[i];
22
                mx--;
23
24
25
```

RectInHist

```
1 int R,C;
   char board [MX_RC] [MX_RC];
   int h[MX_RC][MX_RC];
5
   int perim(int 1, int w){
        if ( l==0 | | w==0)
6
            return 0:
8
        return 2*1 + 2*w;
9
10
11 int main(){
12
        for (int i = 0; i < R; i++){
13
            int run=0;
14
            for (int j = 0; j < C; j++){
15
                run = (board[i][j] == '. '?run + 1:0);
16
                h[i][j] = run;
17
18
19
        int mx = 0;
20
        for (int j = 0; j < C; j++){
21
            stack<int> s;
22
            for (int i = 0; i < R; i++){
```

```
23
                 if (s.empty()
24
                          | | h [ i ] [ j ] > h [ s.top() ] [ j ])
25
                     s.push(i);
26
                 else if(h[i][j]<h[s.top()][j]){
27
                     while (!s.empty()
                     &&h[i][j]<h[s.top()][j]){
28
                          int l = h[s.top()][j];
29
30
                          s.pop();
31
                          int pm = perim(1,
32
                               (s.empty()?
33
                               i:i-s.top()-1));
34
                          mx = max(mx,pm);
35
36
                     s.push(i);
37
                 \} else if (h[i][j]==h[s.top()][j])
38
                     s.pop();
39
                     s.push(i);
40
41
42
             while (! s . empty()) {
43
                 int l = h[s.top()][j]; s.pop();
44
                 int pm = perim(1, s.empty() ? R : R - s.top()-1);
45
                 mx = max(mx, pm);
46
47
48
        printf("%d\n",mx-1);
49
```

6 Maths

Miller Rabin

```
void factor(ll x, ll& e, ll& k){
2
        while (x\%2LL==0LL)
3
            x/=2LL;
 4
            ++e;
 5
 6
        k = x;
 7
    //increase x for higher certainty, 5 works well
    bool is_prime(ll n, int x){
11
        if (n&2LL==0 | n==1LL)
12
            return false;
13
        if (n==2 | | n==3 | | n==5 | | n==7)
14
            return true;
15
        ll e, k;
16
        factor (n-1,e,k);
17
        while (x-->0){
18
            11 a = (rand())\%(n-5LL) + 2LL;
19
            ll p = mod_exp(a,k,n);
20
            if (p==1LL || p==n-1LL)
21
                 continue;
22
            bool all_fail = true;
23
            for (int i = 0; i < e-1; ++i) {
24
                p = mod_exp(p, 2, n);
25
                 if(p=n-1LL)
26
                     all_fail = false;
27
                     break;
28
29
30
            if (all_fail)
31
                return false;
32
33
        return true;
34
```

Binomial Coefficients

```
void factor(ll x, ll& e, ll& k){
2
        while (x\%2LL==0LL)
3
             x/=2LL;
4
            ++e;
6
        k = x;
7
    //increase x for higher certainty, 5 works well
    bool is_prime(ll n, int x){
        if (n&2LL==0 | | n==1LL)
11
12
             return false;
        if (n==2 || n==3 || n==5 || n==7)
13
14
             return true;
15
        ll e, k;
16
        factor(n-1,e,k);
17
        while (x-->0){
             11 \ a = (rand())\%(n-5LL) + 2LL;
18
19
             ll p = mod_exp(a,k,n);
20
             if (p==1LL | | p==n−1LL)
21
                 continue:
22
             bool all_fail = true;
23
             for (int i = 0; i < e-1; ++i){
24
                 p = mod_exp(p, 2, n);
25
                 \mathbf{i} \mathbf{f} (p=n-1LL) 
26
                      all_fail = false;
27
                     break;
28
29
30
             if (all_fail)
31
                 return false;
32
33
        return true;
34
    Gaussian Elimination
    * mat is augmented matrix
     * e.q 3x + 4y = 2 is [3,4,2]
     */
    void gauss (double mat [MX_N] [MX_N+1], double ans [MX_N], int n) {
6
        int i, j, k, l; double t;
7
8
        for (j = 0; j < n-1; ++j)
9
            l = i;
10
             for (i = j+1; i < n; ++i)
11
                 if (fabs (mat[i][j]) > fabs (mat[l][j]))
12
                     l=i:
13
14
             \mathbf{for}(k = j; k \le n; ++k)
15
                 t=mat[j][k], mat[j][k]=mat[l][k], mat[l][k]=t;
16
             for (i = j+1; i < n; ++i)
17
                 for(k = n; k >= j; ---k)
                     mat[i][k] = mat[j][k] * mat[i][j] / mat[j][j];
18
```

```
19
20
21
        for (j = n-1; j >= 0; ---j)
22
            for (t=0.0, k=j+1; k< n; ++k)
23
                t += mat[j][k] * ans[k];
24
            ans[j] = (mat[j][n] - t) / mat[j][j];
25
26
   Ternary Search
   double ternary_search (double 1, double r) { //maximises
2
        while (r - l > EPS) {
3
            double m1 = 1 + (r - 1) / 3;
4
            double m2 = r - (r - 1) / 3;
            double f1 = f(m1);
            double f2 = f(m2);
            if (f1 < f2)
                l = m1;
9
            else
10
                r = m2;
11
12
        return f(l);
13
   Matrix Exponential
   /* c = a * b * /
   void mu(11 a[][NMAT], 11 b[][NMAT], 11 c[][NMAT], int _n) {
            for (int i=0; i<_n; i++)
                    for(int j=0; j<_n; j++) {
4
5
                             c[i][j]=0;
                             for (int h=0;h<_n;h++) {
                                      c[i][j] += (a[i][h]*b[h][j])%mod;
                                      c [ i ] [ j]%=mod;
10
11
12
    /* returns ans=mat^b*/
   void power(ll ans[][NMAT], ll mat[][NMAT], ll b, int _n) {
14
15
            11 tmp [NMAT] [NMAT];
16
            for (int i=0; i<_n; i++)
17
                    for (int j = 0; j < n; j++)
18
                             ans[i][j]=i==j;
19
            while(b) {
20
                     if (b&1) {
21
                             mu(ans, mat, tmp, _n);
22
                             for (int i = 0; i < n; i++)
23
                                      for (int j=0; j<_n; j++)
^{24}
                                              ans[i][j]=tmp[i][j];
25
26
                    mu(mat, mat, tmp, _n);
27
                    for (int i = 0; i < n; i++)
```