

(g)

$$\begin{cases} 4x - 3y = -18 \\ 2y + 5z = -8 \\ x - 2y - 3z = 0 \end{cases} \quad (7)$$

$$\Rightarrow \begin{cases} 4x - 3y + 0 = -18 \\ 0x + 2y + 5z = -8 \\ x - 2y - 3z = 0 \end{cases} \Rightarrow \begin{cases} 4x - 3y + 0 = -18 \\ 0x + 6y + z = -4 \\ 6x + 5y + 12z = -18 \end{cases}$$

1°

$$-4 \cdot w_3 = -4x + 8y + 12z = 0$$

$$w_1 = 4x - 3y + 0 = -18$$

$$5y + 12z = -18$$

2°

$$2 \cdot w_3 = -10y - 24z = 36$$

$$5 \cdot w_2 = 10y + 25z = -40$$

$$z = -4$$

$$y = 6$$

$$x = 0$$

(b)

$$\begin{cases} 4x - y - 3z = 15 \\ 3x - 2y + 5z = -7 \\ 2x + 3y + 4z = 7 \end{cases}$$

$$\Rightarrow \begin{cases} 2x + 3y + 4z = 7 \\ 3x - 2y + 5z = -7 \\ 4x - y - 3z = 15 \end{cases} \Rightarrow \begin{cases} 2x + 3y + 4z = 7 \\ -7y - 11z = 1 \\ 13y + 2z = 35 \end{cases}$$

$$\begin{aligned} -4x - 6y - 8z &= -14 \\ 4x - y - 3z &= 15 \\ \hline -7y - 11z &= 1 \end{aligned}$$

$$\begin{aligned} 3 \cdot w_1 &= 6x + 9y + 12z = 21 \\ -2 \cdot w_2 &= -6x + 4y - 10z = 14 \\ \hline 13y + 2z &= 35 \end{aligned}$$

$$\begin{aligned} 13 \cdot w_2 &= -91y - 143z = 13 \\ 7 \cdot w_3 &= 91y + 14z = 245 \\ \hline -129z &= 258 \end{aligned}$$

$$\begin{cases} 2x + 3y + 4z = 7 \\ -7y - 11z = 1 \\ 13y + 2z = 35 \end{cases}$$

$$\Rightarrow \begin{cases} 2x + 3y + 4z = 7 \\ -7y - 11z = 1 \\ -129z = 258 \end{cases}$$

$$\begin{aligned} z &= -2 \\ y &= \frac{-21}{-7} \\ y &= 3 \end{aligned}$$

$$2x + 9 - 8 = 7$$

$$x = 3$$

(c)

$$\begin{cases} 2x + 3y - 2z = 2 \\ 3x - 5y + 4z = 5 \\ x - 2y - 7z = -24 \end{cases}$$

$$\Rightarrow \begin{cases} x - 2y - 7z = -24 \\ 3x - 5y + 4z = 5 \\ 2x + 3y - 2z = 2 \end{cases}$$

$$\Rightarrow \begin{cases} x - 2y - 7z = -24 \\ y + 25z = 77 \\ 7y + 12z = 50 \end{cases}$$

$$\begin{aligned} -2 \cdot w_1 &= -2x + 4y + 14z = 48 \\ 2x + 3y - 2z &= 2 \\ \hline 7y + 12z &= 50 \end{aligned}$$

$$7y + 12z = 50$$

$$\begin{aligned} -3w_2 &= -3x + 6y + 21z = 72 \\ -3x + 6y + 21z &= 72 \\ 3x - 5y + 4z &= 5 \\ \hline y + 25z &= 77 \end{aligned}$$

$$y + 25z = 77$$

$$\begin{aligned} -7 \cdot w_3 &= -7x - 175z = -539 \\ 7x + 12z &= 50 \\ \hline -163z &= -489 \end{aligned}$$

$$-163z = -489$$

$$\begin{cases} x - 2y - 7z = -24 \\ y + 25z = 77 \\ 7y + 12z = 50 \end{cases} \Rightarrow \begin{cases} x - 2y - 7z = -24 \\ y + 25z = 77 \\ -163z = -489 \end{cases}$$

$$z = 3$$

$$x = 1$$

$$y = 2$$

(d)

$$\begin{cases} x + 2y + 3z = 10 \\ 3x + 4y + 6z = 23 \\ 3x + 2y + 3z = 10 \end{cases}$$

$$\Rightarrow \begin{cases} x + 2y + 3z = 10 \\ -2y - 3z = -7 \\ -4y - 6z = -20 \end{cases} \Rightarrow \begin{cases} x + 2y + 3z = 10 \\ -2y - 3z = -7 \end{cases}$$

$$\begin{array}{l|l|l} -3 \cdot h_1 = -3x - 6y - 9z = 30 & -3 \cdot h_1 = -3x - 6y - 9z = 30 & -2 \cdot h_2 = -4y - 6z = 14 \\ h_2 = 3x + 4y + 6z = 23 & h_3 = 3x + 2y + 3z = 10 & -4y - 6z = -20 \\ \boxed{-2y - 3z = -7} & \boxed{-4y - 6z = -20} & \boxed{0 = 6} \\ & & \downarrow \\ & & ??? \end{array}$$

Sistema sem  
solução

$$e) \begin{cases} 5x - 3y - 7z = -5 \\ 4x - y - z = 2 \\ -2x + 4y + 8z = 10 \end{cases} \Rightarrow$$

$$\begin{cases} 5x - 3y - 7z = -5 \\ -7y - 23z = -30 \\ 14y + 26z = 40 \end{cases}$$

$$2. L_1 = 10x - 6y - 14z = -10$$

$$5. L_3 = -10x + 20y + 40z = 50$$

$$\boxed{14y + 26z = 40}$$

$$4. L_1 = 20x - 12y - 28z = -20$$

$$-5. L_2 = -20x + 5y + 5z = -10$$

$$\boxed{-7y - 23z = -30}$$

$$\boxed{z=1}$$

$$\boxed{y=1}$$

$$\boxed{x=1}$$

$$\begin{cases} 5x - 3y - 7z = -5 \\ -7y - 23z = -30 \\ 140z = 140 \end{cases}$$

$$1. L_2 = -98y - 322z = -420$$

$$L_3 = 98y + 182z = 280$$

$$1) \begin{cases} 3x - 8y - 9z = 14 \\ 7x + 3y + 2z = -12 \\ -8x - 9y + 6z = 11 \end{cases} \Rightarrow \begin{cases} 3x - 8y - 9z = 14 \\ -65y - 69z = 134 \\ -91y - 54z = 145 \end{cases}$$

$$8. L_1 \Rightarrow 21x - 64y - 72z = 112 \quad | \quad 7. L_1 = 21x - 56y - 63z = 98$$

$$3. L_3 = -24x - 27y + 18z = 33 \quad // \quad -3. L_2 = -21x - 9y - 6z = 36$$

$$\text{nova } L_3 \Rightarrow \boxed{-91y - 54z = 145} \quad | \quad \text{nova } L_2 \Rightarrow \boxed{-65y - 69z = 134}$$

$$\Rightarrow \begin{cases} 3x - 8y - 9z = 14 \\ -65y - 69z = 134 \\ 2769z = -2769 \end{cases}$$

$$\boxed{z = -1}$$

$$\boxed{y = -1}$$

$$-91. L_2 = 5915y + 6279z = -12.194$$

$$65. L_3 = -5915y - 3510z = 9.425$$

$$\text{nova } L_3 \Rightarrow \boxed{2.769z = -2769}$$

$$3x + 8 + 9 = 14$$

$$3x = -3$$

$$\boxed{x = -1}$$



$$h) \begin{cases} 2x - 5y - z = -8 \\ 3x - 2y - 4z = -11 \\ -5x + y + z = -9 \end{cases}$$

$$\begin{cases} 2x - 5y - z = -8 \\ -11y + 5z = -2 \\ -23y - 3z = -58 \end{cases}$$

$$5L_1 = 10x - 25y - 5z = -40$$

$$2L_3 = -10x + 2y + 2z = -18$$

$$\text{nova } L_3 \rightarrow \boxed{-23y - 3z = -58}$$

$$3 \cdot L_1 = 6x - 15y - 3z = -24$$

$$-2 \cdot L_2 = -6x + 4y + 8z = 22$$

$$\text{nova } L_2 \rightarrow \boxed{-11y + 5z = -2}$$

$$-23L_2 = 253y - 115z = 46$$

$$11L_3 = -253y - 33z = -638$$

$$-148z = -592$$

$$\boxed{y = 2}$$

$$\boxed{z = 4}$$

$$\boxed{x = 3}$$