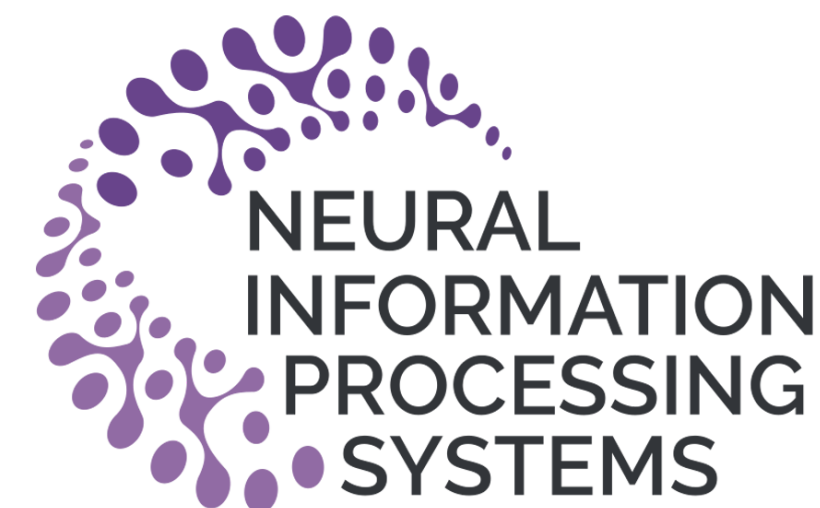


# Model-based Safe Deep Reinforcement Learning via a Constrained Proximal Policy Optimisation Algorithm

Ashish Kumar Jayant, Shalabh Bhatnagar

Dept. of Computer Science Automation

Indian Institute of Science, Bangalore



# Safety in Reinforcement Learning (RL)

- RL agents do lot of unsafe exploration during initial iterations.
- Limits the potential application of RL in financial and robotics sequential decision making problems.
- Safety in RL is formally studied under Constrained Markov Decision Processes (CMDP) Framework

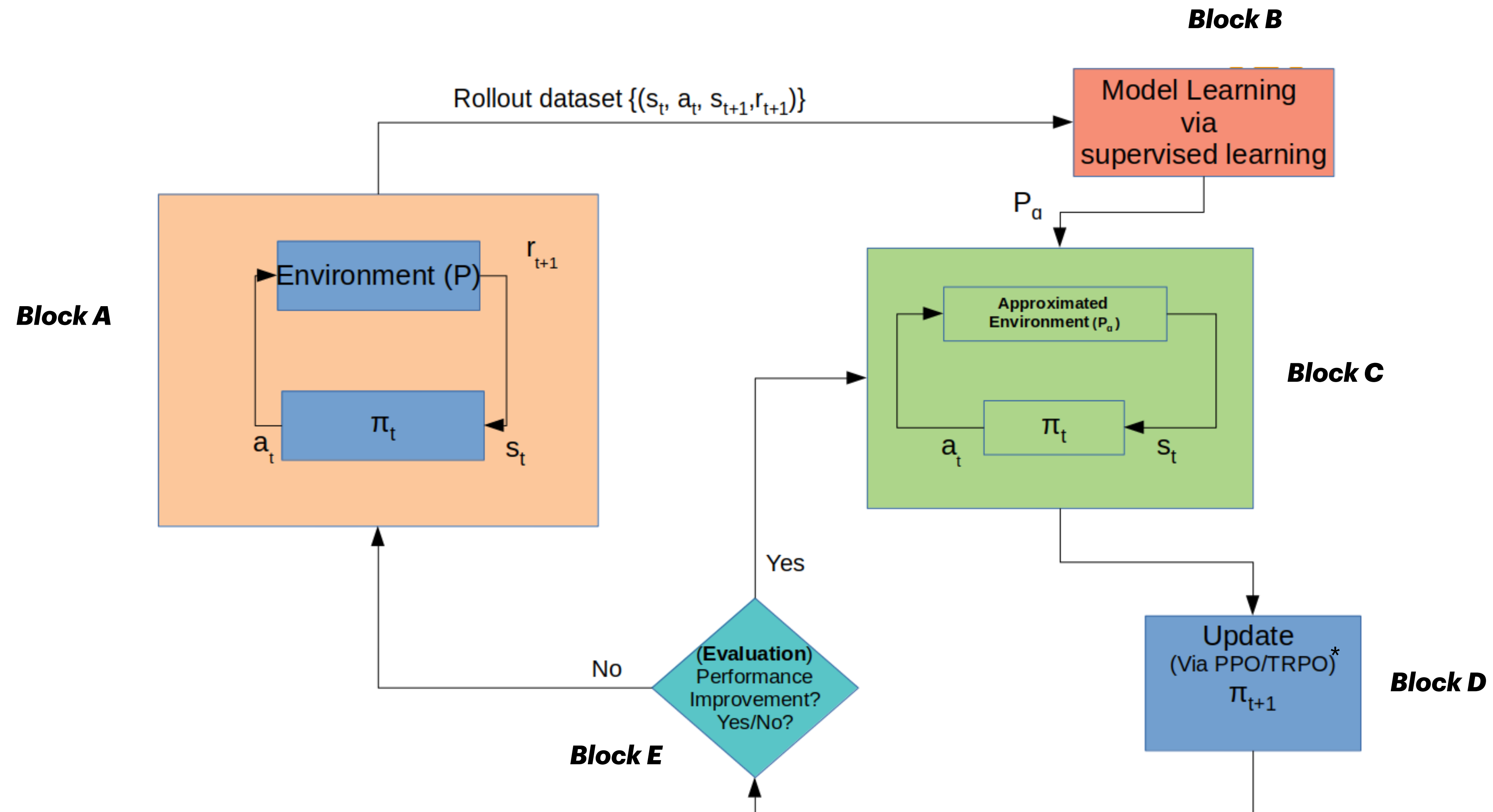
# Constrained Markov Decision Processes (CMDP)

- $(S, A, R, C_i, \mu, P)$  tuple where -
  - $S$  denotes state space
  - $A$  denotes action space
  - $\mu : S \rightarrow [0,1]$  denotes initial state distribution
  - $R : S \times A \times S \rightarrow \mathbb{R}$  denotes single-stage reward function
  - $C_i : S \times A \times S \rightarrow \mathbb{R}^+$  denotes single-stage i-th non-negative cost function
  - We use policy optimisation route, where policy parameterized by  $\theta$  denoted by  $\pi_\theta$

# Constrained RL Problem Formulation

- $\max_{\pi_{\theta}} J^R(\pi_{\theta})$  such that  $J^{C_i}(\pi_{\theta}) \leq d_i$  where,
  - $J^R(\pi_{\theta}) = \mathbb{E} \left[ \sum_{t=0}^{\infty} \gamma^t R(s_t, a_t, s_{t+1}) \mid s_0 \sim \mu, a_t \sim \pi_{\theta}, \forall t \right]$
  - $J^{C_i}(\pi_{\theta}) = \mathbb{E} \left[ \sum_{t=0}^{\infty} \gamma^t C_i(s_t, a_t, s_{t+1}) \mid s_0 \sim \mu, a_t \sim \pi_{\theta}, \forall t \right]$
  - $d_i$  is prescribed cost-threshold for  $i$ -th constraint function
- Lagrangian relaxation methods are one of the well-known and easy-to-implement methods to solve these. e.g - *PPO-Lagrangian*[1]

# Model-based RL

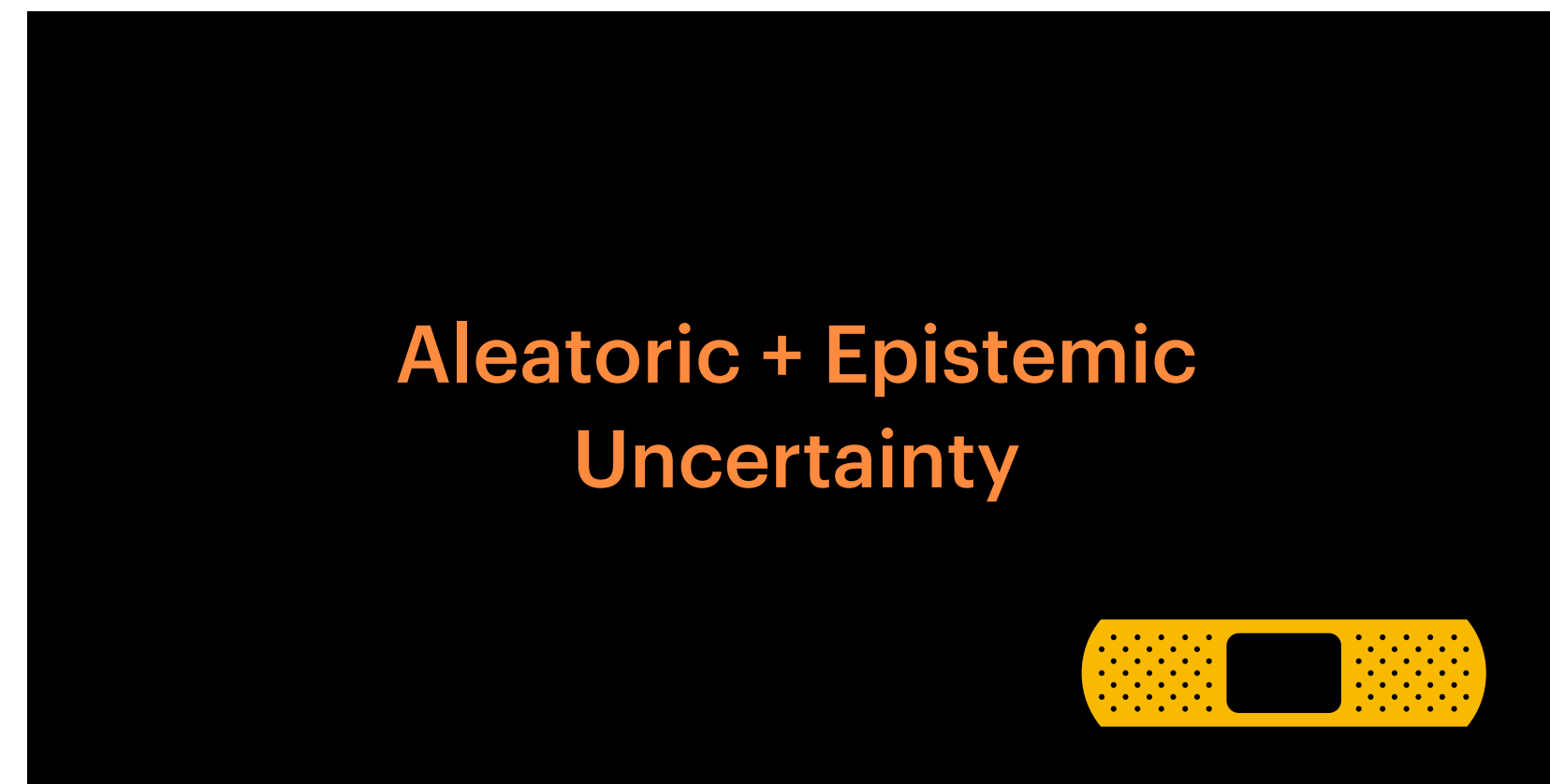


\*(we consider on-policy setting)

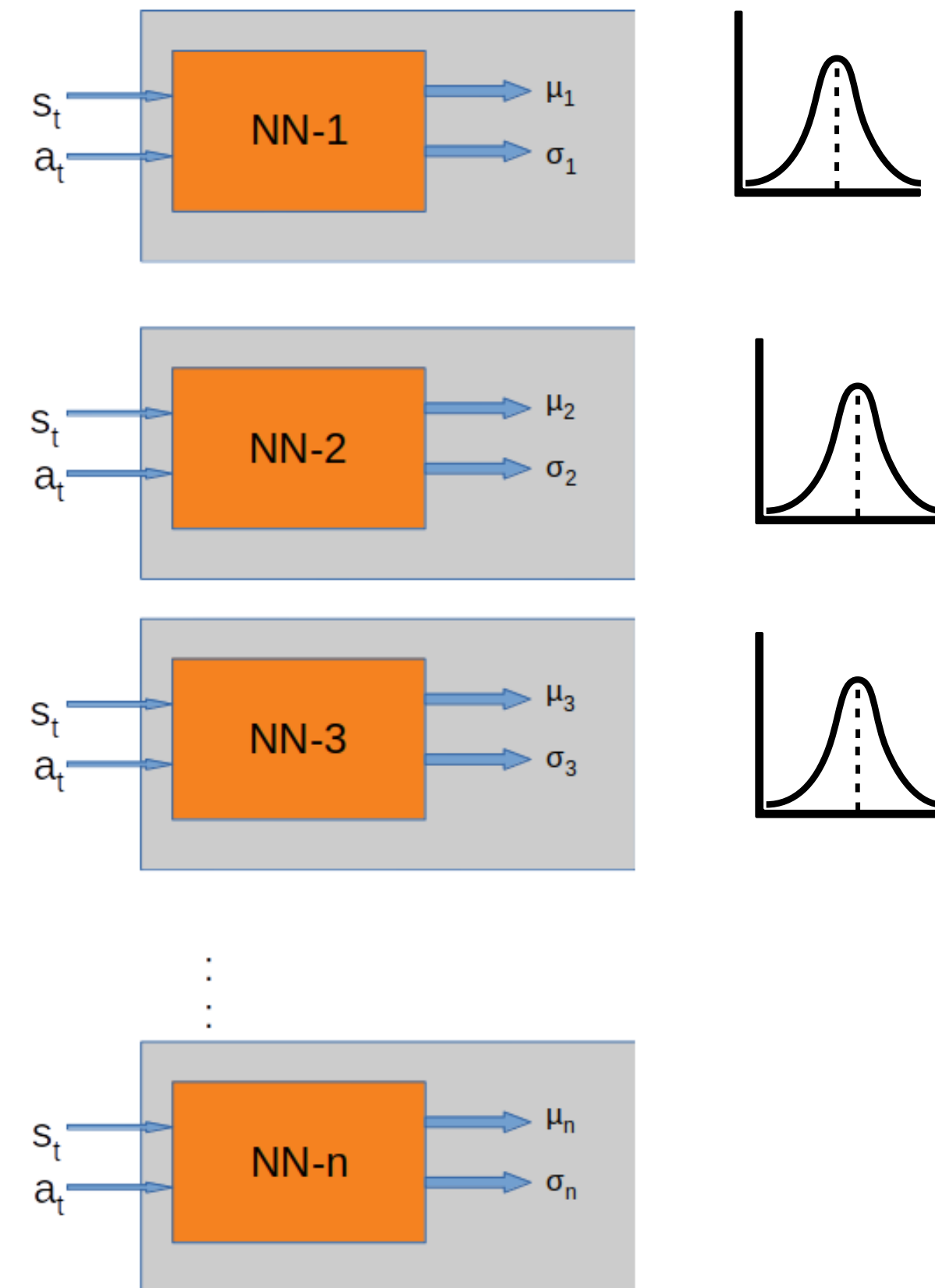
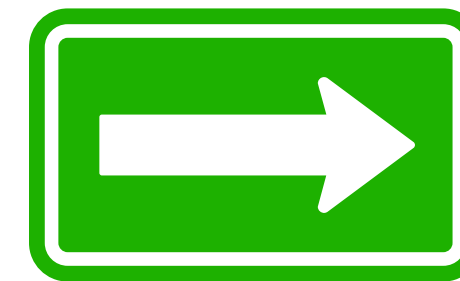
# Idea : Combine Lagrangian relaxation + Model-based RL



# Tackling challenges of model-based RL



Solution



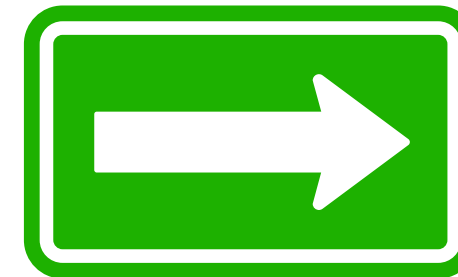
**Ensemble of randomly  
initialised uncertainty-aware  
neural nets [2]**

# Tackling challenges of model-based RL

Aggregation of error over horizon  
(Model-bias)



Solution



Use  
truncated horizon  
for planning ( $H < T$ )



Issue

Specific to constrained RL  $\left\{ \begin{array}{l} J^{C_i}(\pi_\theta) = \mathbb{E} \left[ \sum_{t=0}^H \gamma^t C_i(s_t, a_t, s_{t+1}) \mid s_0 \sim \mu, s_{t+1} \sim P_\alpha(\cdot \mid s_t, a_t), a_t \sim \pi_\theta, \forall t \right] \end{array} \right.$

Underestimation of cost returns



# Stricter cost threshold

- $\max_{\pi_\theta \in \Pi_\theta} J^R(\pi_\theta)$  such that  $J^C(\pi_\theta) \leq d'$  where, (Assuming 1 constraint)
  - $J^R(\pi_\theta) = \mathbb{E} \left[ \sum_{t=0}^H \gamma^t R(s_t, a_t, s_{t+1}) \mid s_0 \sim \mu, s_{t+1} \sim P_\alpha, a_t \sim \pi_\theta \forall t \right]$
  - $J^C(\pi_\theta) = \mathbb{E} \left[ \sum_{t=0}^H \gamma^t C(s_t, a_t, s_{t+1}) \mid s_0 \sim \mu, s_{t+1} \sim P_\alpha, a_t \sim \pi_\theta, \forall t \right]$
  - is  $d'$  modified prescribed cost-threshold for l-th constraint function
- We change  $d' = d * \beta$  where  $\beta \in [0,1)$
- We tune  $\beta$  empirically.

# Effect of $\beta$

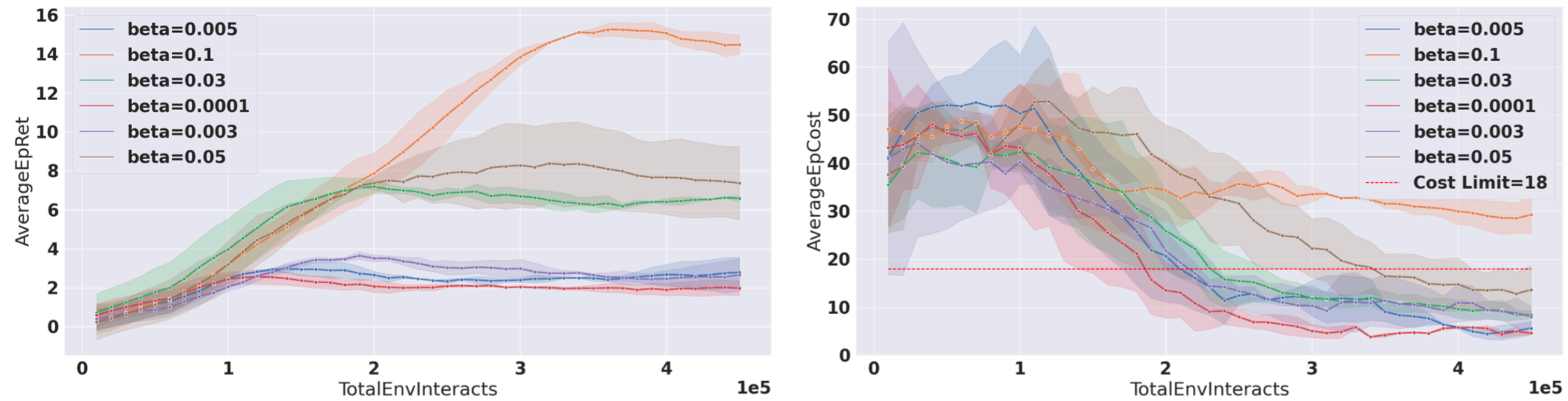
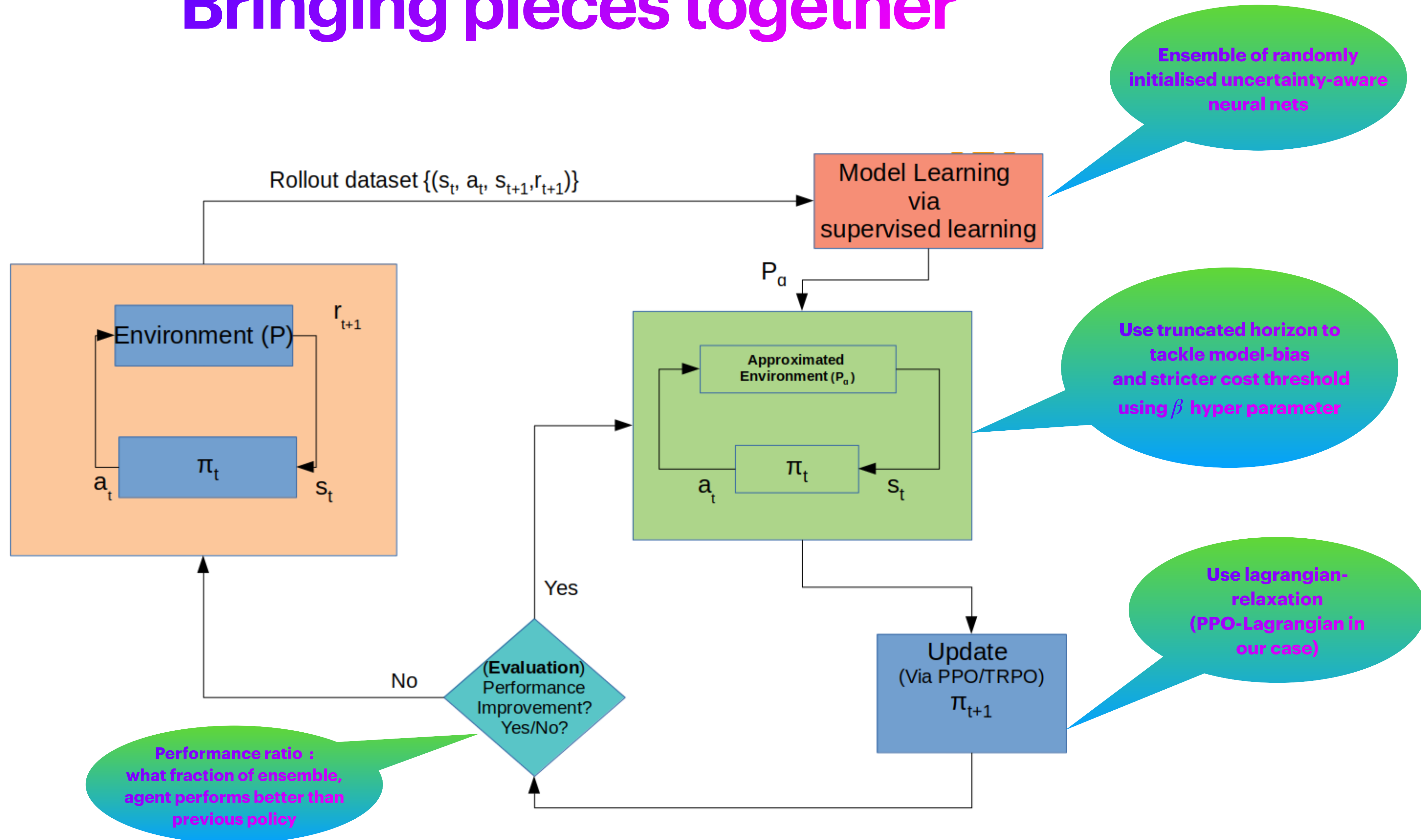


Figure 1: Effect of beta parameter ( $\beta$ ) on expected cost returns (left) and expected reward returns (right) in PointGoal environment. (Here  $\beta = 0.1$  corresponds to  $\frac{H}{T}$ )

**As we increase  $\beta$ , cost threshold becomes more lenient, reward returns increase but cost return also increase!**

# Bringing pieces together



# Results on Safety Gym : PointGoal

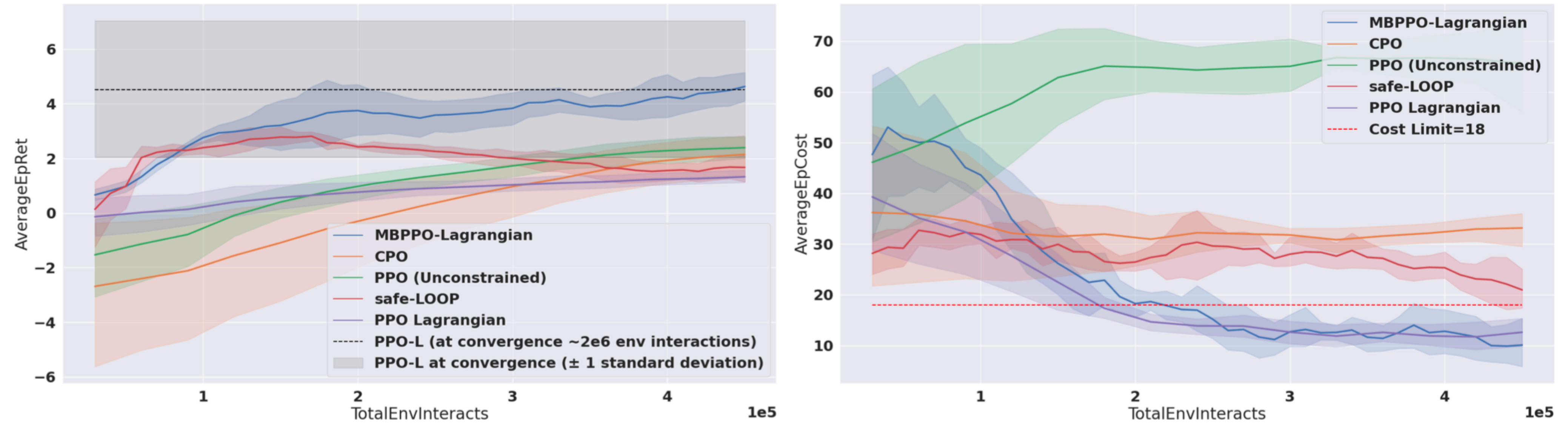


Figure 2: Reward Performance (Left) and Cost Performance (Right) in PointGoal Environment, where y-axis denotes Average Episode Reward Returns (left) / Cost Returns (right) and x-axis denotes total environment interacts

**\*Our approach : MBPPO-Lagrangian**



# Results on Safety Gym : CarGoal

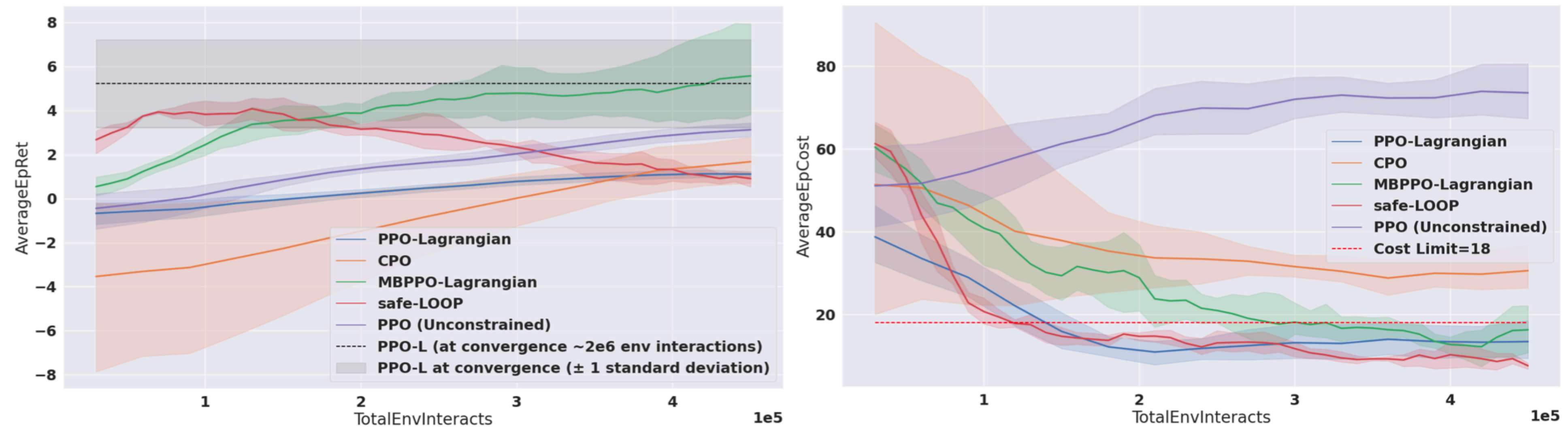


Figure 3: Reward Performance (Left) and Cost Performance (Right) in CarGoal Environment, where y-axis denotes Average Episode Reward Returns (left) / Cost Returns (right) and x-axis denotes total environment interacts

**\*Our approach : MBPPO-Lagrangian**

# Results on Safety Gym

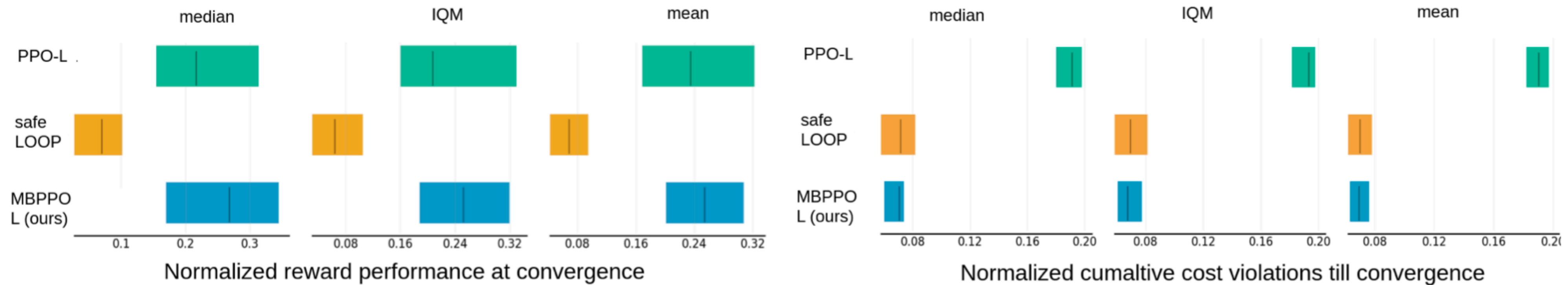


Figure 4: Normalized Reward Returns at Convergence (left) with median, inter-quartile mean (IQM), mean estimates and Normalized Cumulative Violations (right) with median, inter-quartile mean (IQM), mean estimates. Top rows (in green) represent PPO-Lagrangian, middle rows (in orange) represent safe-LOOP and bottom rows (in blue) represent our approach.

**Thank you!**