

# Abstract

We study various two-point functions in certain defect versions of  $\mathcal{N} = 4$  super Yang Mills theory. These defect theories are obtained by insertion of a D7 probe-brane, with either  $AdS_4 \times S^2 \times S^2$  or  $AdS_4 \times S^4$  geometry, into the standard D3 brane configuration of AdS / CFT. The  $\mathcal{N} = 4$  SYM theories, arising from the decoupling limit of these brane configurations, have non-zero vacuum expectation values (vevs) for the scalar fields  $\phi_i$ . These non-zero vevs breaks super symmetry completely and conformal symmetry partially, thus presenting us with an interesting opportunity to make non-trivial tests of the AdS / CFT duality.

We focus first on two-point functions with  $SO(3) \times SO(3)$  symmetric vevs, between chiral primary operators of the forms  $\text{tr } Z^L$ ,  $\text{tr } \bar{Z}^L$ ,  $\text{tr } X^L$ , where  $X = \phi_1 + i\phi_4$ ,  $Y = \phi_2 + i\phi_5$  and  $Z = \phi_3 + i\phi_6$ . By use of perturbative methods, we were able to reduce the connected tree-level contributions to these two-point functions, down to expressions involving complicated infinite sums. These infinite sums unfortunately seem unevaluable in general. However, for specific values of  $L$  and parameters associated to the stabilization of the brane configurations, we were able to evaluate the sums explicitly.

We also study two-point functions, first with  $SO(3) \times SO(3)$  symmetric vevs, between short scalar operators  $\mathcal{O}_{W_1 W_2} = \text{tr}[W_1 W_2]$  with scalars  $W_1, W_2 = X, Y, Z, \bar{X}, \bar{Y}, \bar{Z}$ , and Bethe state operators  $\mathcal{O}_L = \Psi_M^{i_1 \dots i_L} \text{tr}[V_{i_1} \dots V_{i_L}]$ , with  $V_i = X, Z$  and  $\Psi_M$  being a Bethe wavefunction with  $M$  excitations. By use of integrability techniques, we find that certain choices of  $W_1, W_2$  allows for the tree-level contribution to these two-point functions to be expressed in terms of the tree-level value of  $\langle \mathcal{O}_L \rangle$ . The computations of these various types of two-point functions provide the first step towards a very non-trivial check of the AdS / CFT duality. We hope that future work will enable us to complete this endeavor, by studying the corresponding objects on the gravity side of the duality.

# Acknowledgements

I would like to thank my supervisor *Charlotte Kristjansen*, first for presenting me with the opportunity to write this thesis, and subsequently for taking time to answer my seemingly endless stream of questions. I would also like to thank *Matthias Wilhelm* and *Matthias Volk* for engaging in many helpful discussions, as well as sharing thier valuable knowledge on the topic of this thesis. A big thank you also goes out to *Marius de Leeuw*, who generously shared with me some very helpful Mathematica notebooks, concerning the computation of certain results from [10] relevant to this thesis.