

=====PROBLEM 1=====

$$252/198 = 1 \text{ R } 54$$

$$198/54 = 3 \text{ R } 36$$

$$54/36 = 1 \text{ R } 18$$

$$36/18 = 2 \text{ R } 0$$

$$\gcd(252, 198) = 18$$

$$14/6 = 2 \text{ R } 2$$

$$6/2 = 3 \text{ R } 0$$

$$\gcd(6, 14) = 2$$

$$36/24 = 1 \text{ R } 12$$

$$24/12 = 2 \text{ R } 0$$

$$\gcd(24, 36) = 12$$

$$42/12 = 3 \text{ R } 6$$

$$12/6 = 2 \text{ R } 0$$

$$\gcd(12, 42) = 6$$

$$252/198 = 1 \text{ R } 54$$

$$198/54 = 3 \text{ R } 36$$

$$54/36 = 1 \text{ R } 18$$

$$36/18 = 2 \text{ R } 0$$

$$\gcd(252, 198) = 18$$

=====PROBLEM 2=====

Forward Steps

$$662 = 414 * 1 + 248$$

$$414 = 248 * 1 + 166$$

$$248 = 166 * 1 + 82$$

$$166 = 82 * 2 + 2$$

$$82 = 2 * 41 + 0$$

Backward steps:

$$2 = 1 * 166 - 2 * 82$$

$$2 = 1 * 166 - 2 * (248 - 1 * 166)$$

$$2 = 2 * 166 - 4 * 248$$

$$2 = 2 * (414 - 1 * 166) - 4 * 248$$

$$2 = 3 * 248 - 8 * 414$$

$$2 = 3 * 248 - 8 * (662 - 1 * 248)$$

$$2 = 16 * 662 - 4 * 414$$

Forward Steps

$$14 = 6 * 2 + 2$$

$$6 = 2 * 3 + 0$$

Backward steps:

$$2 = 2 * 6 - 1 * 14$$

Forward Steps

$$36 = 24 * 1 + 12$$

$$24 = 12 * 2 + 0$$

Backward steps:

$$12 = 1 * 24 - 1 * 36$$

Forward Steps

$$42 = 12 * 3 + 6$$

$$12 = 6 * 2 + 0$$

Backward steps:

$$6 = 3 * 12 - 1 * 42$$

Forward Steps

$$252 = 198 * 1 + 54$$

$$198 = 54 * 3 + 36$$

$$54 = 36 * 1 + 18$$

$$36 = 18 * 2 + 0$$

Backward steps:

$$18 = 1 * 54 - 1 * 36$$

$$18 = 1 * 54 - 1 * (198 - 3 * 54)$$

$$18 = 4 * 54 - 2 * 198$$

$$18 = 4 * (252 - 1 * 54) - 2 * 198$$

$$18 = 4 * 252 - 5 * 198$$

=====PROBLEM 3=====

Quotients (q values):  $q_1 = 0$ ,  $q_2 = 1$ ,  $q_3 = 1$ ,  $q_4 = 1$ ,  $q_5 = 2$ ,  $q_6 = 41$

Calculations for s values:

$$s_0 = 1 - 0 * 0 = 8$$

$$s_1 = 0 - 1 * 1 = 331$$

$$s_2 = 0 - 0 * 1 = 331$$

$$s_3 = 0 - 0 * 1 = 331$$

$$s_4 = 0 - 0 * 2 = 662$$

$$s_5 = 0 - 0 * 41 = 13571$$

Calculations for t values:

$$t_0 = 0 - 1 * 0 = -5$$

$$t_1 = 1 - 0 * 1 = -206$$

$$t_2 = 1 - 1 * 1 = -206$$

$$t_3 = 1 - 1 * 1 = -206$$

$$t_4 = 1 - 1 * 2 = -413$$

$$t_5 = 1 - 1 * 41 = -8486$$

$$\gcd(414, 662) = 2 = 8 * 414 + -5 * 662$$

Quotients (q values):  $q_1 = 0$ ,  $q_2 = 2$ ,  $q_3 = 3$

Calculations for s values:

$$s_0 = 1 - 0 * 0 = -2$$

$$s_1 = 0 - 1 * 2 = -14$$

$$s_2 = 0 - 0 * 3 = -21$$

Calculations for t values:

$$t_0 = 0 - 1 * 0 = 1$$

$$t_1 = 1 - 0 * 2 = 7$$

$$t_2 = 1 - 1 * 3 = 10$$

$$\gcd(6, 14) = 2 = -2 * 6 + 1 * 14$$

Quotients (q values):  $q_1 = 0$ ,  $q_2 = 1$ ,  $q_3 = 2$

Calculations for s values:

$$s_0 = 1 - 0 * 0 = -1$$

$$s_1 = 0 - 1 * 1 = -3$$

$$s_2 = 0 - 0 * 2 = -6$$

Calculations for t values:

$$t_0 = 0 - 1 * 0 = 1$$

$$t_1 = 1 - 0 * 1 = 3$$

$$t_2 = 1 - 1 * 2 = 5$$

$$\gcd(24, 36) = 12 = -1 * 24 + 1 * 36$$

Quotients (q values):  $q_1 = 0$ ,  $q_2 = 3$ ,  $q_3 = 2$

Calculations for s values:

$$s_0 = 1 - 0 * 0 = -3$$

$$s_1 = 0 - 1 * 3 = -21$$

$$s_2 = 0 - 0 * 2 = -14$$

Calculations for t values:

$$t_0 = 0 - 1 * 0 = 1$$

$$t_1 = 1 - 0 * 3 = 7$$

$$t_2 = 1 - 1 * 2 = 5$$

$$\gcd(12, 42) = 6 = -3 * 12 + 1 * 42$$

Quotients (q values):  $q_1 = 1$ ,  $q_2 = 3$ ,  $q_3 = 1$ ,  $q_4 = 2$

Calculations for s values:

$$s_0 = 1 - 0 * 1 = 4$$

$$s_1 = 0 - 1 * 3 = 33$$

$$s_2 = 0 - 0 * 1 = 11$$

$$s_3 = 0 - 0 * 2 = 22$$

Calculations for t values:

$$t_0 = 0 - 1 * 1 = -5$$

$$t_1 = 1 - 0 * 3 = -41$$

$$t_2 = 1 - 1 * 1 = -13$$

$$t_3 = 1 - 1 * 2 = -27$$

$$\gcd(252, 198) = 18 = 4 * 252 + -5 * 198$$