

# Comparison Table of Epidemic Models for Spatial Heterogeneity

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2021-03-08

Tasks	Variables	Spatial structure parameters	Spatial effect modeling mechanism	Additional model features	Model analysis and investigation
Modeling approach					
Multi-site extension by graph (Antonov, [AA1])	Discrete in space, continuous in time	<ul style="list-style-type: none"><li>Population sizes for each site.</li><li>Contingency table of traveling patterns between graph nodes.</li><li>Different at each site:<ul style="list-style-type: none"><li>Death rates</li><li>Incubation periods</li><li>Infectious periods</li></ul></li><li>Model specific choice of population types that travel. (Can travel or are allowed to.)</li></ul>	<ul style="list-style-type: none"><li>The migrant populations produce new “birth-like” equation terms.</li><li>The new-comers at a given site become part of site’s population.</li></ul>	<ul style="list-style-type: none"><li>Uses System Dynamics perspective.</li><li>It is assumed that sites can be become empty.</li><li>Persons are interchangeable — person’s site origin does not matter.</li><li>Chain-able model-transformations. E.g.<ol style="list-style-type: none"><li>Modify SEIR with air-travel patterns only of Susceptible and Recovered populations.</li><li>Modify the obtained model with land-travel patterns for all populations.</li></ol></li><li><b>Works adequately if the time step is small.</b> (E.g. a day for COVID-19 simulations.)</li></ul>	<ul style="list-style-type: none"><li>Demonstrating the algorithm using a:<ul style="list-style-type: none"><li>Trivial graph</li><li>Grid graph</li><li>Random graph</li></ul></li></ul>
Multi-patch SEIR (Lloyd & May, [LM1])	Discrete in space, continuous in time	<ul style="list-style-type: none"><li>Population sizes at each patch.</li><li>Contact rates between patches.</li><li>Universal death rate, average latent disease period, and average infectious period.</li></ul>	<ul style="list-style-type: none"><li>Region-to-region mingling terms are used.</li><li>The mingling parameters are given as a matrix of contact rates.</li></ul>	<ul style="list-style-type: none"><li>Simple, yet general approach.</li></ul>	<ul style="list-style-type: none"><li>SEIR model based analysis.</li><li>Stability and bifurcation analysis.<ul style="list-style-type: none"><li>Forced seasonalities.</li></ul></li></ul>
Multi-region mobility incorporation into SIR (Sattenspieal & Dietz, [SD1])	Discrete in space, continuous in time	<ul style="list-style-type: none"><li>Population sizes for each region.</li><li>Fractions of travelers for each patch.</li><li>Probability to go from patch <i>i</i> to patch <i>j</i>.</li><li>Per capita return rate for travelers from patch <i>i</i> at patch <i>j</i>.</li><li>A list of matrices for the proportion of contacts in region <i>k</i> between a susceptible from region <i>i</i> and an infective from region <i>j</i>.</li><li>Average number of contacts per person for each patch.</li></ul>	<ul style="list-style-type: none"><li>Region-to-region mingling terms are used.</li><li>Multiple mingling parameters. (See left cell.)</li></ul>	<ul style="list-style-type: none"><li>Markov chain perspective on traveling.</li><li>Travelers do not “forget their home.”</li><li>No death rate, average latent disease period, and average infectious period are included in the model.</li></ul>	<ul style="list-style-type: none"><li>Taking the model to different extreme cases in order to do mathematical analysis.</li><li>SIR model based analysis.</li><li>Application to real-life Measles modeling.</li></ul>
By Partial Differential Equations (PDEs), (Kot [MK1], Wu [JW1])	Continuous in space, continuous in time.	<ul style="list-style-type: none"><li>The continuous distribution of the population in space and its growth in time.</li><li>Diffusion coefficients population motion.</li><li>Relevant death rates, contact rates, incubation period, etc.</li></ul>	<ul style="list-style-type: none"><li>PDEs of reaction-diffusion type.</li></ul>	<ul style="list-style-type: none"><li>Assumes populations migrate according to Fick’s laws of diffusion.</li></ul>	<ul style="list-style-type: none"><li>Derivation of the model</li><li>Application to real-life Rabies and West Nile virus modeling.</li></ul>

## References

[AA1] Anton Antonov, "Scaling of Epidemiology Models with Multi-site Compartments", (2020), SystemModeling at [GitHub/antononcube](#).

[MK1] Kot, M.: Elements of Mathematical Ecology. Cambridge University Press, Cambridge (2001).

[LM1] Lloyd,A., and May, R.M.: Spatial heterogeneity in epidemic models. J.Theor. Biol. 179, 1–11 (1996).

[SD1] Sattenspiel, L. and Dietz, K.:A structured epidemic model incorporating geographic mobility among regions. Math. Bios. 128, 71–91 (1995).

[JW1] Jianhong Wu,“Spatial Structure: Partial Differential Equations Models”, in Mathematical Epidemiology, Springer, 2008.