LECTURE-2

WAVE MECHANICAL CONCEPT OF THE ATOM

TEXT

"Essentials of Physical Chemistry"

B. S. Bahl, G. D. Tuli and Arun Bahl,

Dual Nature of Matter

In Bohr atomic model, we see the electron as particle.

But in modern wave mechanical concept described by Louis de Broglie in 1924, electron has both wave and particle nature which is known as dual nature of matter.

Dual Nature of Matter (contd.)

Louis de Broglie (1892-1987) who was working on his Ph.D. degree at the time, made a daring hypothesis:

"if radiant energy could, under appropriate circumstances behave as though it were a stream of particles, then could matter, under appropriate circumstances, exhibit wave-like properties?"

Dual Nature of Matter (contd.)

The dual character- wave and particle may not be confined to radiation alone but extended to matter as well which is called 'Wave mechanical Theory'.

Hence Bohr concept has been superseded completely by the modern wave mechanical concept.

Heisenberg's Uncertainty Principle

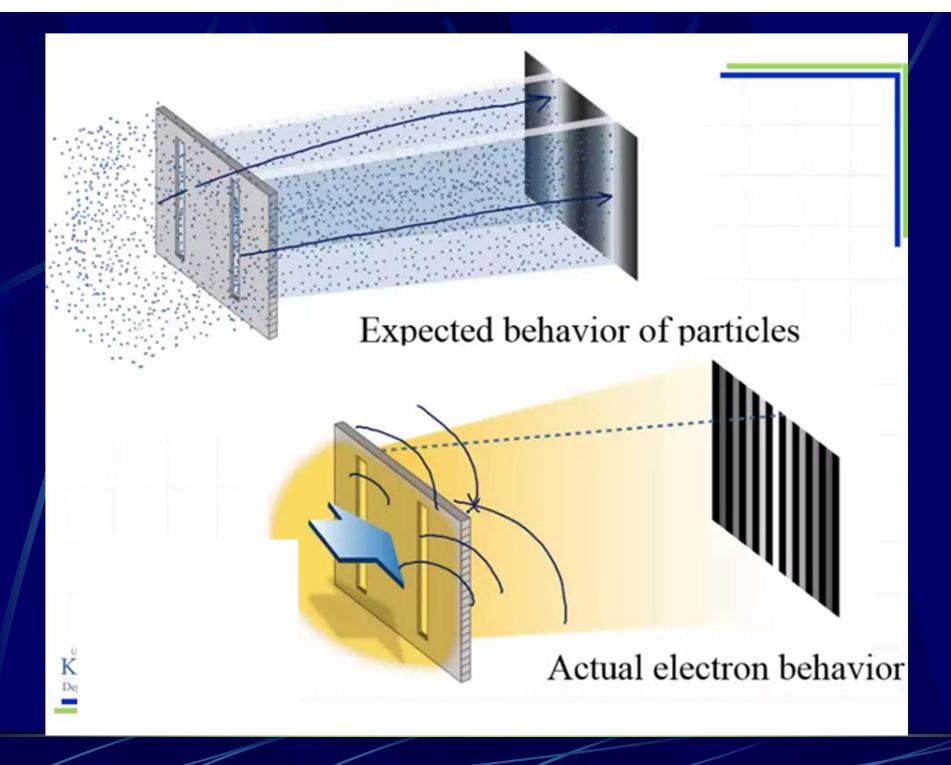
For a relatively large solid object, like a bowling ball, we can determine its position and velocity at any given moment with a high degree of accuracy.

However, if an object (like an electron) has wave-like properties then how can we accurately define its' position?

Werner Heisenberg (1901-1976) concluded (in 1927) that due to the dual nature of matter (both particle and wavelike properties) it is impossible to simultaneously know both the position and momentum (mass-velocity) of an object as small as an electron.

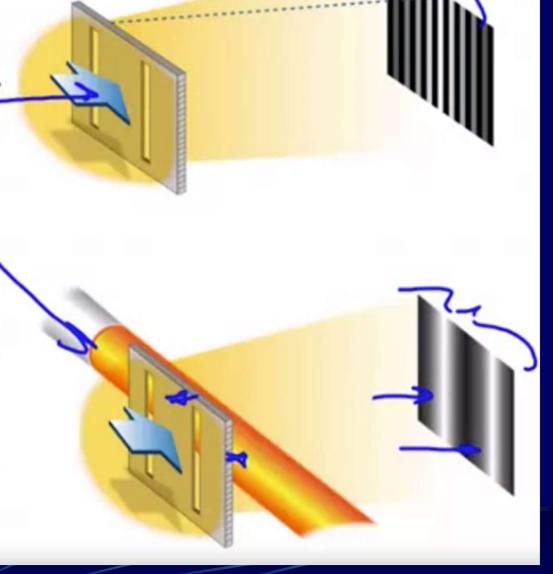
Heisenberg's Uncertainty Principle (contd.)

- Thus, it is not appropriate to imagine the electrons as moving in well-defined circular orbits about the nucleus.
- The position and momentum of a moving particle are interdependent and cannot be measured with absolute exactness.
- If momentum is measured accurately, the position becomes less precise; if the position is determined accurately, the momentum becomes uncertain or less accurate.



The Uncertainty Principle

- We know electrons have a wave nature.
- We know electrons have a particle nature.
- If we try to observe both aspects simultaneously, we ALWAYS fail.



Heisenberg's Uncertainty Principle (contd.)

Heisenberg's relationship can be shown as

 $\Delta x \times \Delta p \ge \frac{h}{4\pi}$

or, $\Delta x \times m \Delta v \ge \frac{h}{4\pi}$

where, $\Delta x =$ position of a moving particle and $\Delta x = m\Delta v =$ momentum.

De Broglie's Equation

- According to Planck quantum theory, we know
- \bullet E = hv --- (1)
- Where E = photon energy, h = Planck constant and v
 = frequency of radiation.
- From Einstein theory of relativity (mass-energy relationship) we know,
- \bullet E= mc² --- --- (2)
- Where m= mass of photon and c = velocity of radiation.

De Broglie's Equation (contd.)

From equation (1) and (2), we get

or, mc =
$$\frac{hc}{\lambda}$$
 [$v = \frac{c}{\lambda}$]

or, mc = $\frac{h}{\lambda}$ --- --- (3)

or, mass × velocity = $\frac{h}{wavelength}$

- or, momentum $\propto \frac{1}{wavelength}$
- i.e. the momentum of a particle in motion is inversely proportional to wavelength.
- This equation is known as de Broglie's equation.

De Broglie's Equation (contd.)

The de Broglie's equation is true for all particles, but it is only with very small particles, such as electrons, that the wave-like aspect is of any significance. Large particles in motion though possess wavelength, but it is not measurable or observable. Let us consider de Broglie's wavelengths associated with two bodies and compare their values.

- (a) For a large mass: A stone of 100g with a velocity of 1000 cm/sec.
 - $\therefore \lambda = h/mc = 6.6256 \times 10^{-32} \text{ cm (h} = 6.6256 \times 10^{-27} \text{ cm)}$
- (b) For a small mass like atom: Hydrogen atom of 9.109 $\times 10^{-28}$ g moves with a velocity of 2.188×10^{8} cm/sec.
 - $\therefore \lambda = h/mc = 3.32 \times 10^{-8} \text{ cm}$

Examples:

- Calculate the wavelength of an particle having mass 6.6×10^{-27} kg moving with a speed of 10^5 cm sec⁻¹. Given that h = 6.6×10^{-34} kg m² sec⁻¹. (Ans: 1×10^{-10} m)
- Calculate the uncertainty in position of an electron if the uncertainty in velocity is 5.7×10^5 msec⁻¹. (Ans: 1×10^{-10} m)

Problems:

Problem-10. What is the wavelength associated with a particle of mass 0.1g moving with a speed of 1×10^5 cm sec⁻¹. (h =6.6×10⁻²⁷ erg sec).

Problem-11. The uncertainty in the position of a moving bullet of mass 0.01 kg is 1.0×10^{-5} m; calculate the uncertainty in its velocity. (*Answer*. 5×10^{-28} msec⁻¹)

Problem-12. What is the mass of a photon of sodium light with a wavelength of 5890 Å? (Hints: λ =h/mc; h =6.6×10⁻²⁷ erg sec, λ =5890×10⁻⁸cm, v=3×10¹⁰cm/sec; *Ans*. 3.76 ×10⁻³³ g)

<u>Problem-13</u>. The uncertainty in the position and velocity of a particle are 10^{-10} m and 5.27×10^{-24} m sec⁻¹ respectively. Calculate the mass of the particle. (Given Planck's constant, h = 6.6×10^{-34} kg m² sec⁻¹).

<u>Problem-14</u>. The velocity of a ball being bowled by Mohammad Rafiq is 25 m sec⁻¹. Calculate the wavelength of the matter-wave associated with the ball. (Weight of the ball = $158.5 \, \text{g}$; h = $6.625 \times 10^{-27} \, \text{erg sec}$).

Schrödinger's Wave Equation:

To calculate the probability of finding the electron at various points in an atom, Schrödinger in 1926 derived an equation. This is called the Schrödinger's wave equation.

$$d^2\psi/dx^2 + d^2\psi/dy^2 + d^2\psi/dz^2 + 8\pi^2m/h^2$$
 (E-P.E.) $\psi=0$

where, ψ = wave motion, x, y & z = distance from nucleus considering three axis, λ = wavelength and A = constant (maximum value of ψ).

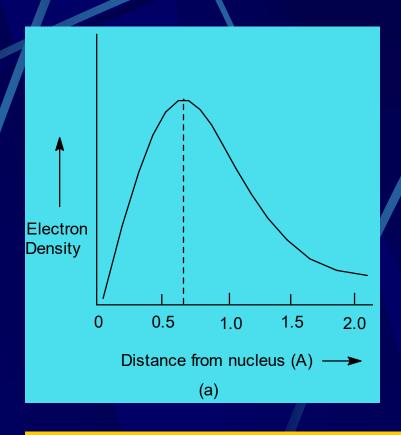
Probability Distribution Curves:

The **Schrödinger's** wave equation gives a three-dimensional arrangement of points to find a electron. There are region where the chances of finding electron are relatively greater. Such regions are called 'cloud of negative charge'.

The three-dimensional region within which there is higher probability that an electron having certain energy will be found, is called an 'orbital'.

An orbital is the most probable space in which the electron spends most of its time while in constant motion. In other words, it is the spatial description of the motion of an electron corresponding to a particular energy level. The energy of electron in an atomic orbital is always the same.

Probability Distribution Curves:



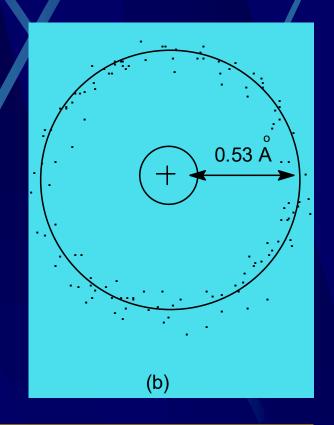


Figure: Shows the probability distribution of electron Cloud;

- (a) gives the graphical representation while,
- (b) depicts cross-section of the cloud.

Quantum Numbers (Q.N.)

Principal \Quantum \Number, \n:

The main shell (or level) to which the electron belongs (size). This number has a dependence only on the distance between the electron and the nucleus. The average distance increases with n, and hence quantum states with different principal quantum numbers are said to belong to different shells.

Principal quantum number (<i>n</i> =)	1	2	3	4
Letter designation	K	L	M	Ν
Maximum number of electrons $(2n^2=)$	2	8	18	32

Quantum Numbers (contd.)

Subsidiary Quantum Number, / I:

The sub-shell which governs the angular momentum of the electron. In chemistry, this quantum number is very important, since it defines the **shape** of an **atomic orbital** occupied by the electron and strongly influences **chemical bonds** and **bond angles**. For any given value of the principal quantum number 'n', the azimuthal quantum number 'l' may have all integral values from 0 to n-1.

n=1	n=2	n=3	n=4
<i>l</i> =0 (1s)	<i>I</i> =0 (2s)	<i>I</i> =0 (3s)	<i>l</i> =0 (4s)
	<i>I</i> =1 (2p)	<i>l</i> =1 (3p)	<i>l</i> =1 (4p)
		<i>l</i> =2 (3d)	<i>l</i> =2 (4d)
			/=3 (4f)

Quantum Numbers (contd.)

Magnetic Quantum Number, m: This governs the energies of electrons in an external magnetic field and gives orientation. This is the projection of the orbital angular momentum along a specified axis. For any given value of the azimuthal quantum number 'l', the magnetic quantum number 'm' may assume all the integral values from +l to -lthrough zero i.e. +l, (+l-1), ...0, ...(-l+1), -l. Therefore for each value of 'l' there will be (2l+1) values of 'm'.

Quantum Numbers (contd.)

- Spin Quantum Number, s: This quantum number has been introduced to account for the *spin* of electrons about their axis. Since an electron can spin clockwise or anticlockwise, there are two possible values of 's' that are equal and opposite, $+\frac{1}{2}$ and $-\frac{1}{2}$ along the specified axis for each value of 'm'.
- Since a spinning charge is associated with a magnetic field, an electron must have a magnetic moment associated with it.

	Principal Azimuthal Q-number, n I (0 to n-1)		mber,	Magnetic Q-number, m (-/ to +/)	Spin Q-number, s (+½ to -½) (for each value of 'm')	Number of electrons accommo dated	
1	K	0	S	0	(+½, -½) ,,	2	2
2 L	0	S	0	(+½, -½) ,,	2	0	
	L	1	р	+1, 0, -1	(+½, -½) ,,	6	8
3 M	0	S	0	(+½, -½) ,,	2	18	
	1	р	+1, 0, -1	(+½, -½) ,,	6		
	2	d	+2, +1, 0, -1, -2	(+½, -½) ,,	10		
4 N		0	S	0	(+½, -½) ,,	2	
		1	р	+1, 0, -1	(+½, -½) ,,	6	
	N	2	d	+2, +1, 0, -1, -2	(+½, -½) ,,	10	32
		3	f	+3, +2, +1, 0, -1, -2, -3	(+½, -½) ,,	14	

Orbitals

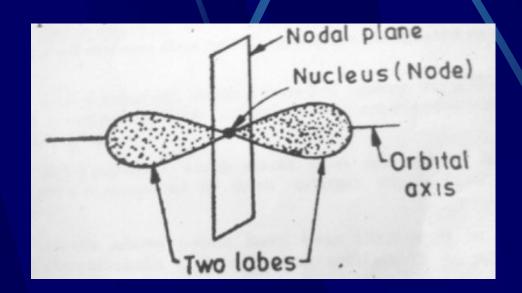
- An atomic orbital is a mathematical function that describes the wave-like behavior of either one electron or a pair of electrons in an atom. This function can be used to calculate the probability of finding any electron of an atom in any specific region or shell around the atom's nucleus.
- Each shell is subdivided into subshells, which are made up of orbitals, each of which has electrons with different angular momentum. Each orbital in a shell has a characteristic shape, and is named by a letter. They are: s, p, d, and f.

Orbitals...

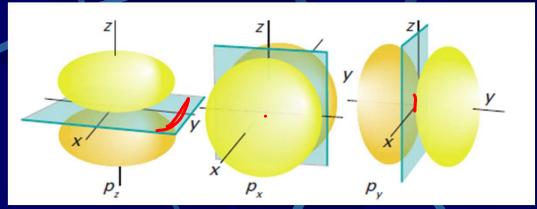
- In a one-electron atom (e.g. H, He⁺, Li⁺, etc.) the energy of each orbital within a particular shell is identical. However, when there are multiple electrons, they interact and split the orbitals into slightly different energies. Within any particular shell, the energy of the orbitals depend on the angular momentum of orbitals s, p, d, and f in order of lowest to highest energy. No two orbitals have the same energy level.
- Orbitals having same energy are known as degenerate orbitals. Since the number of p-orbitals having the same energy is three, these orbitals are said to be three-fold degenerate orbitals etc.

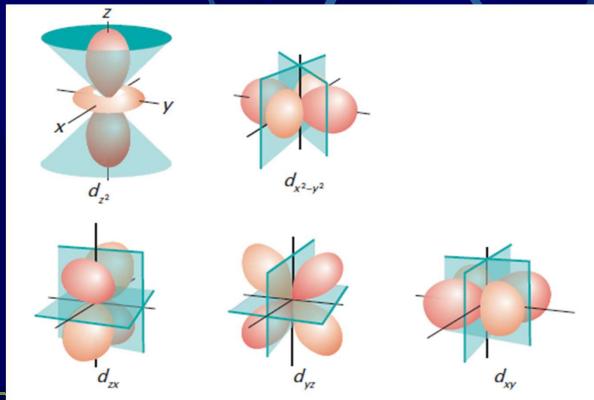
Node & Nodal Plane

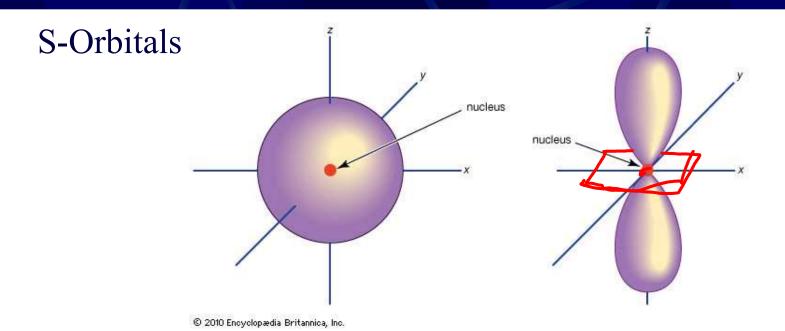
The nucleus at which the electron density is zero is called *node* and the plane passing through the orbital-axis is called *nodal plane*. At this plane the electron density is also zero.



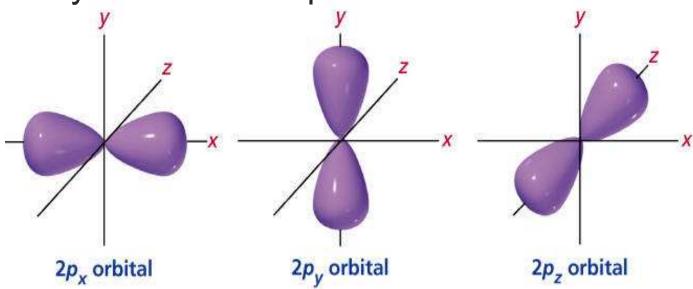
Node & nodal plane of p & d- orbitals

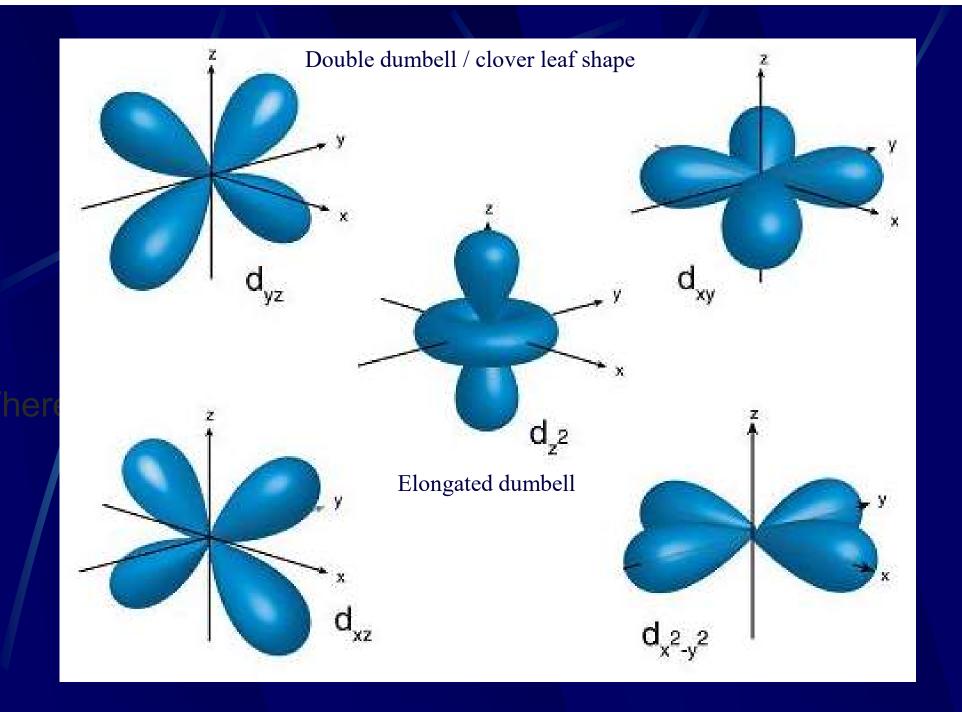




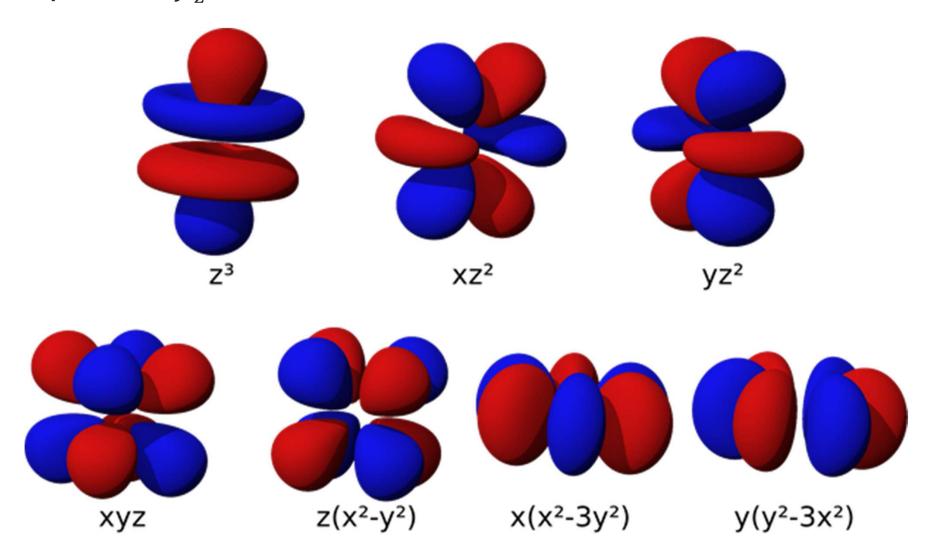


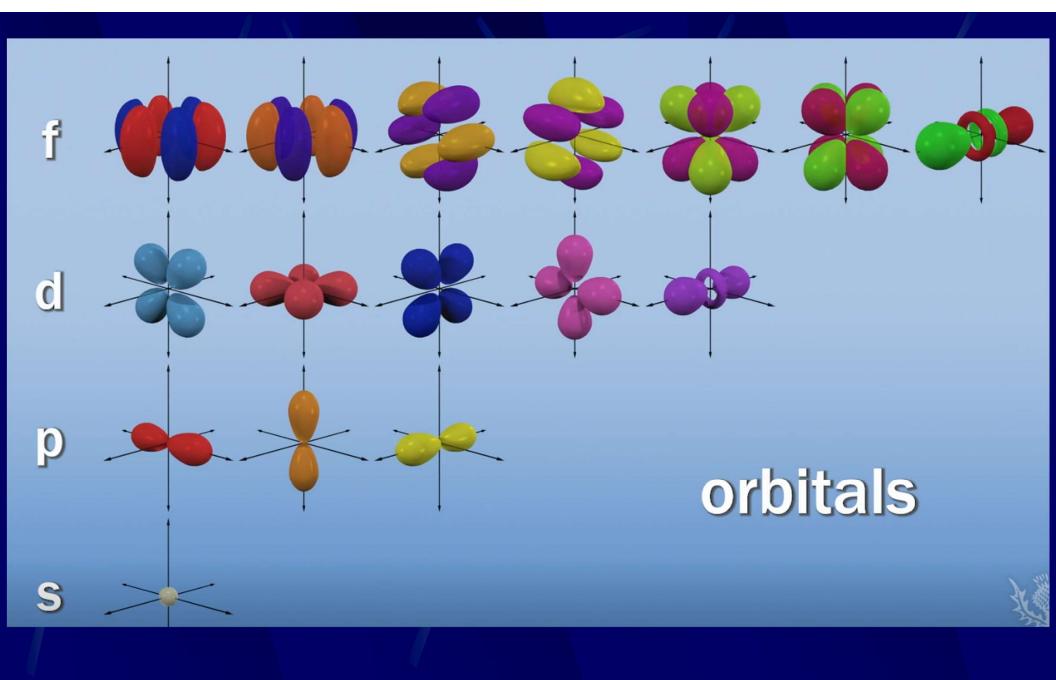
There are typically two lobes for p orbitals



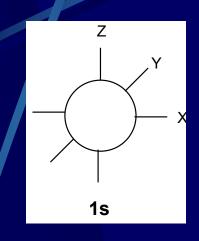


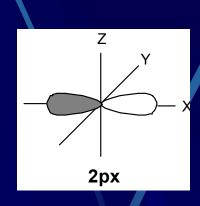
There are typically six lobes for f-orbitals with the exception of f_{z^3} .

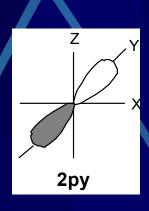


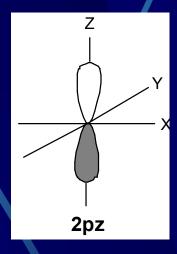


Shapes and orientations of s, p & donor orbitals









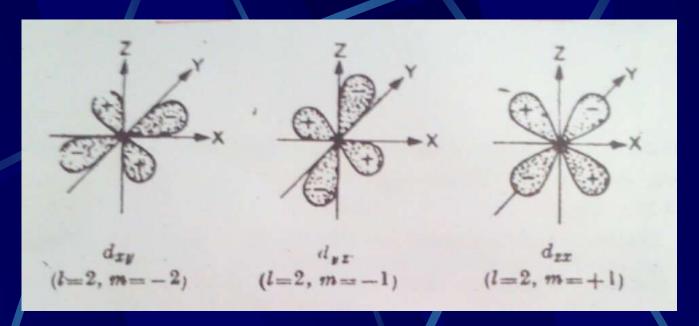
s- orbitals: spherical shaped

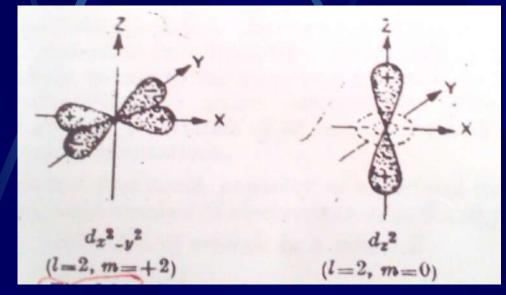
p- orbitals: p-orbitals are dumb-bell shaped consisting of two lobes along axis.

d- orbitals: d-orbitals are complex geometrical shapes as compared to p-orbitals, lobes lie in the plane, along axis.

Shapes & orientation of d-orbitals...

- There are **five different d-orbitals** on the basis of the orientation of their lobes of maximum electron density with respect to x, y and z axes. They are designated as dxy (I = 2, m = -2), dyz (I = 2, m = -1), dzx (I = 2, m = +1), dx²-y² (I = 2, m = +2) and dz² (I = 2, m = 0).
- All these five d-orbitals are not identical in shape. Four out of five d-orbitals namely dxy, dyz, dzx (lobes lie in the plane) and dx²-y² (lobes lie along axis) for a given energy level contain four lobes (double dumbbell shaped) and the fifth orbital, dz² consists of only two lobes lie along z-axis (dumb-bell shaped).



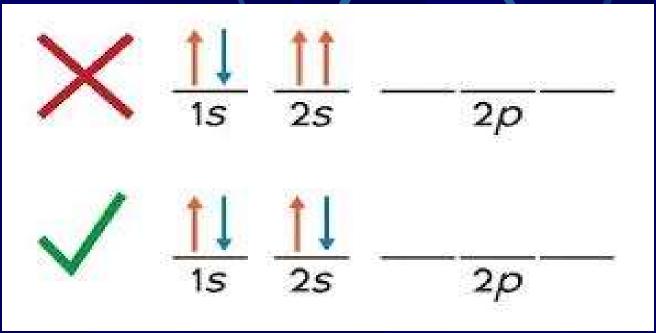


Principles of Electronic Configuration of Atoms

- Pauli's Exclusion Principle
- Aufbau Principle
- Hund's Rule

The Pauli Exclusion Principle

The Pauli Exclusion Principle: An atomic orbital may describe at most two electrons, at least one for that orbital to exist. To occupy the same orbital, two electrons must have opposite spins. If two electrons occupy the same orbital they are said to be paired. Orbitals with one electron are unpaired.



Exercise

Give the electronic configuration of Fe, Fe 2+, Cr, Cu , Sc3+ Cl-, Cr+, O2- ,S2

Pauli's Exclusion Principle

The four quantum numbers of two electrons of an atom will never be same. e.g. He (2)

$$(e_1)$$
 n = 1, I = 0, m = 0, s = $+\frac{1}{2}$

$$(e_2)$$
 n = 1, l = 0, m = 0, s = $-\frac{1}{2}$

i. e. spin is different.

Mt l=

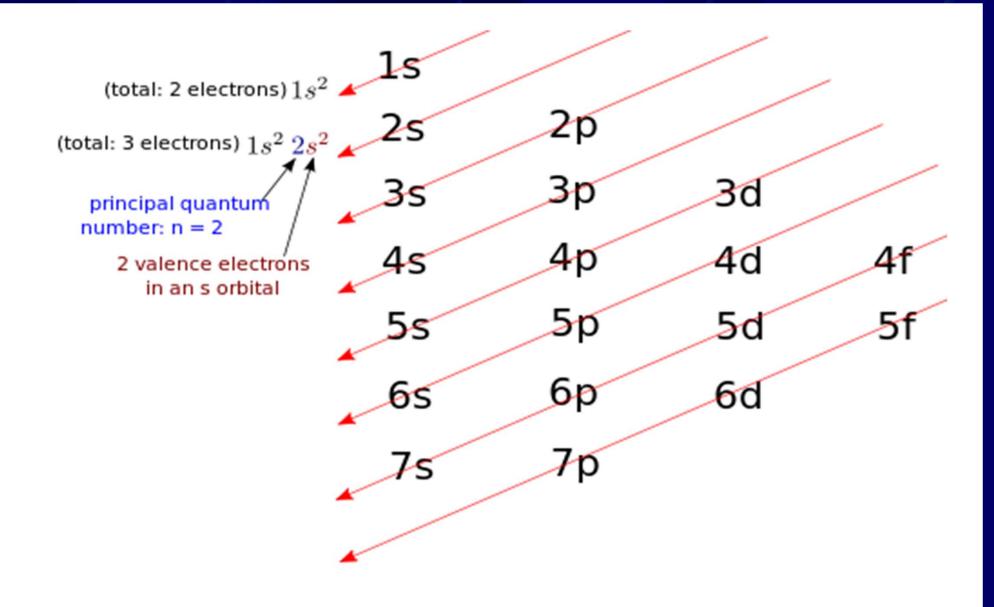
Aufbau principle

The Aufbau principle (from the German Aufbau, "building up, construction") was an important part of Bohr's original concept of electron configuration. It may be stated as:

a maximum of two electrons are put into orbitals in the order of increasing orbital energy: the lowest-energy orbitals are filled before electrons are placed in higher-energy orbitals.

Energy determination rule of Orbitals:

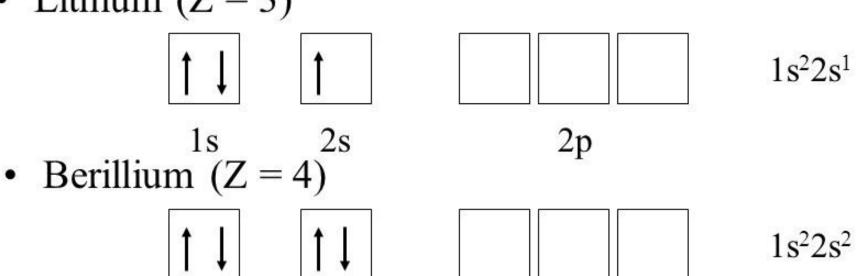
- Orbitals are filled in the order of increasing n+l;
- Where two orbitals have the same value of n+l, they are filled in order of increasing n.



Calculate maximum number of electrons in 4th & 5th energy level.

The Aufbau Principal (cont.)

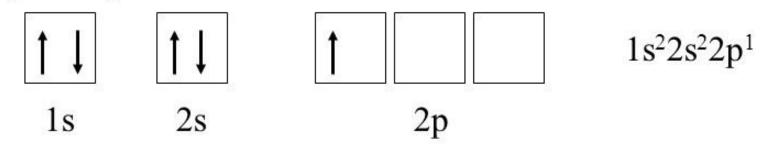
• Lithium (Z = 3)



• Boron (Z = 5)

1s

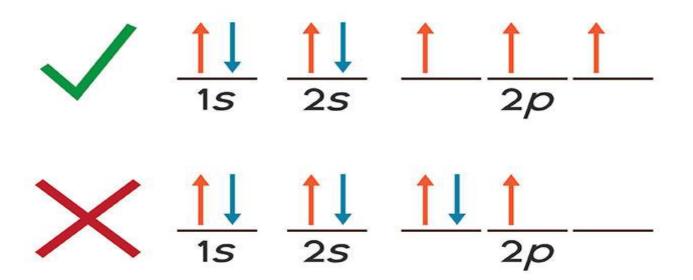
2s



2p

Hund's Rule

• Hund's Rule: When electrons occupy orbitals of equal energy, one electron enters each orbital until all the orbitals contain one electron, with spins parallel, before they are paired. Second electrons then add to each orbital so that their spins are paired.



Exercise

Explain Hund's, Afbau and pauli's exclusion principle. How many electrons the M (n=3) shell may have.

Using Hund's rule draw the valence electron orbital of Al (13) and Fe³⁺(26).

Some exceptions

- Cu $(29) 1s^2 2s^2 2p^6 3s^2 3p^6 3d^9 4s^2$ will be $3d^{10}4s^1$
- Cr (24) 1s² 2s² 2p⁶ 3s² 3p⁶ 3d⁴ 4s²
 will be 3d⁵ 4s¹

Because for a more stable configuration half-filled and full-filled orbitals are preferred.

Problems:

Problem-15. (a) An electron is in 4f orbital. What possible values for the quantum numbers n, l, m and s can it have? (b) What designation is given to an orbital having (i) n=2, l=1 and (ii) n=4, l=0?

<u>Problem-16</u>. A neutral atom has 2K, 8L, 5M electrons. Find out the following from the data (a) atomic number, (b) total number of s electrons, (c) total number of p electrons, (d) number of protons in the nucleus, and (e) valency of elements.

<u>Problem-17</u>. State which of the following sets of quantum numbers would be possible and which would be impossible for an electron in an atom.

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(a) n=0, l=0, m=0, s=+\frac{1}{2} [Impossible]; (b) n=1, l=1, m=0, s=+\frac{1}{2} [Impossible] (c) n=1, l=0, m=0, s=-\frac{1}{2} [Possible]; (d) n=2, l=1, m=-2, s=+\frac{1}{2} [Impossible]
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(e) n=2, l=1, m= -1, s= + $\frac{1}{2}$ [Possible]

Problem 18. (a) How many electrons are there in hydrogen and chlorine atom (atomic number 17)? How they are arranged? What is the valency of hydrogen and chlorine in HCl? (b) The atomic number of Na and Cl are 11 and 17 respectively. Determine the number of electrons in Na⁺ and Cl⁻.

Possible Questions???

- * Explain Hund's, Afbau and pauli's exclusion principle. How many electrons the M (n=3) shell may have.
- *Explain Higenberg uncertainty principle. Solving related mathematical problem
- * What is dual nature of matter?
- *Using Hund's rule draw the valence electron orbital of Al (13) and Fe³⁺(26).
- *Draw the electronic configuration for N(7) & O(8) and explain with pauli's exclusion principle
- *Explain n+l rule/ afbau rule.
- * Write down the physical significance of four quantum numbers



Next Class
Quiz-2 &
Modern Periodic Table

Thank you