▶ JUAN P. AGUILERA, The  $\Pi_2^1$ -spectrum conjecture. Ghent University, Belgium.

 $E ext{-}mail:$  aguilera@logic.at.

The  $\Pi_2^1$ -soundness ordinal of a theory T, denoted  $o_2^1(T)$ , is a measure of how close T is to being  $\Pi_2^1$ -correct. The  $\Pi_2^1$ -spectrum conjecture asserts that the possible values of  $o_2^1(T)$  for recursively enumerable extensions of  $\mathsf{ACA}_0$  are precisely the  $\Sigma_1^1$ -definable epsilon numbers. In this talk, we present a proof of the following theorem, which is formalizable in weak set theories: If the  $\Pi_2^1$ -Spectrum Conjecture fails, then Second-Order Arithmetic is consistent. This is joint work with Fedor Pakhomov.