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To test aerodynamics of a new prototype automobile, scale model is tested in wind tunnel

Dynamic similarity: $Re_{\text{proto}} = Re_{\text{model}}$ Scale of prototype - model: 1:10.

Both prototype and model exposed to standard air pressure, what's better for wind tunnel air to be cooler or hotter than standard sea-level air temperature of 15°C ?

Reynold's number are similar between prototype and model

$$\Rightarrow \frac{V_m l_m}{\nu_m} = \frac{V l}{\nu} \quad (\nu_m, \nu: \text{kinematic viscosity})$$

$$\Rightarrow V_m = \frac{\nu_m}{\nu} \cdot \frac{l}{l_m} V = \frac{\nu_m}{\nu} 10V \quad (\text{Scale is 1:10})$$

V is prototype automobile's velocity. We know that cars are fast and 10 times the velocity of cars is hard to replicate in the model. To be realistic, V_m should be $< 10V$

\Rightarrow To reduce $10V$ magnitude, $\frac{\nu_m}{\nu}$ should be smaller than 1

$\Rightarrow \nu_m < \nu \Rightarrow \nu_m < 1.57 \times 10^{-5}$ according to table B.4

Since temperature is proportional to kinematic viscosity $\Rightarrow T_m < T$

\Rightarrow It's better for wind tunnel air to be colder than standard air temperature of 15°C (Ans)