

Task Description:

Task-1: Count the number of primitive operations executed below and determine the best & the worst cases: (1 points)

Algorithm: *arrayMin(A, n)*
currentMin \leftarrow *A*[0]
i \leftarrow 1
while *i* \leq *n* - 1 **do**
 if *currentMin* \geq *A*[*i*] **then**
 currentMin \leftarrow *A*[*i*]
 i \leftarrow *i* + 1
return *currentMin*

Best Case: $O(4)$ if $i > n-1$ and it doesn't go into the loop
Worst case: $O(3n+3)$ if it goes into the loop

Task-2: Determine the Big-O notation for: (3 points)

a) $2 + n(2 + 3n)$

$O(n)$

b) $n + 2(n + 3n)n + \frac{n}{2}$

$O(n^2)$

c) $n^3 \log n + 2n + 1 + 3n^2 + n(\log n)^2$

$O(n^3 \log n)$

Task-3: Determine the Complexity Of The Following Small Functions: (6 points)

a) **for** (*i* = *sum* = 0; *i* < *n*; *i*++)
 sum += *a*[*i*];

$O(n)$

b) **for** (*i* = 0; *i* < *n*; *i*++)
 for (*j* = 0; *j* < *n*; *j*++)
 a[*i*][*j*] = *i***j*;

$O(n^2)$

c) **for** (*i* = *n*; *i* >= 1; *i*--)
 for (*j* = *i*; *j* <= *n*; *j*++) /* Note that the value of the inner loop variable (*j*) */
 ... /* depends on the value of the outer loop variable (*i*) */

$O(n^2)$

d) `for (i = 1; i <= n; i++)`
 `for (j = i; j <= i; j++)` /* Note that the value of the inner loop variable (j) */
 ... /* depends on the value of the outer loop variable (i) */
 $O(n)$

e) `for (i = 0; i < n; i++)`
 `for (j = n; j > 1; j/=2)`
 ...
 $O(n \log n)$

f) `int factorial (int n)`
 {
 if (n <= 1)
 return 1;
 else
 return n * factorial(n-1);
 }
 $O(n)$