

Algorithm analysis, Selection Sort

| Instruction | Cost | # Repeat |
|--|----------|----------------------------|
| ArrayList<Game> list = c.getWishList(); | c_1 | 1 |
| for (int i = 0; i < list.size(); i++) | c_2 | $n + 1$ |
| Game minor = list.get(i); | c_3 | n |
| int cual = i; | c_4 | n |
| for (int j = i + 1; j < list.size(); j++) | c_5 | $\frac{n(n+1)}{2} - (n-1)$ |
| Shelve s1 = searchShelve(list.get(i).getShelveName()); | c_6 | $\frac{n(n+1)}{2} - n$ |
| Shelve s2 = searchShelve(list.get(j).getShelveName()); | c_7 | $\frac{n(n+1)}{2} - n$ |
| if (s1.getNameShelve().compareTo(s2.getNameShelve()) == 0) | c_8 | $\frac{n(n+1)}{2} - n$ |
| if (s2.getGameShelve().getIndexInTable(list.get(j).getCode()) < s1.getGameShelve().getIndexInTable(list.get(i).getCode())) | c_9 | $\frac{n(n+1)}{2} - n$ |
| minor = list.get(j); | c_{10} | $\frac{n(n+1)}{2} - n$ |
| cual = j; | c_{11} | $\frac{n(n+1)}{2} - n$ |
| else if (s1.getNameShelve().compareTo(s2.getNameShelve()) > 0) | c_{12} | $\frac{n(n+1)}{2} - n$ |
| Game temp1 = list.get(i); | c_{13} | $\frac{n(n+1)}{2} - n$ |
| list.set(i, list.get(j)); | c_{14} | $\frac{n(n+1)}{2} - n$ |
| list.set(j, temp1); | c_{15} | $\frac{n(n+1)}{2} - n$ |
| Game temp2 = list.get(i); | c_{16} | n |
| list.set(i, minor); | c_{17} | n |
| list.set(cual, temp2); | c_{18} | n |
| c.setWishList(list); | c_{19} | 1 |

Note: We assume that $n = \text{list.size}$

Analysis of time complexity

$$\begin{aligned}
T(n) = & c_1 + c_2(n+1) + c_3n + c_4n + c_5 \left(\frac{n(n+1)}{2} - (n-1) \right) + c_6 \left(\frac{n(n+1)}{2} - n \right) + c_7 \left(\frac{n(n+1)}{2} - n \right) + c_8 \left(\frac{n(n+1)}{2} - n \right) \\
& + c_9 \left(\frac{n(n+1)}{2} - n \right) + c_{10} \left(\frac{n(n+1)}{2} - n \right) + c_{11} \left(\frac{n(n+1)}{2} - n \right) + c_{12} \left(\frac{n(n+1)}{2} - n \right) + c_{13} \left(\frac{n(n+1)}{2} - n \right) \\
& + c_{14} \left(\frac{n(n+1)}{2} - n \right) + c_{15} \left(\frac{n(n+1)}{2} - n \right) + c_{16}n + c_{17}n + c_{18}n + c_{19}
\end{aligned}$$

$$\begin{aligned}
T(n) = & c_1 + c_2 + c_2n + c_3n + c_4n + c_5 + \frac{c_5n^2 - c_5n + c_6n^2 - c_6n + c_7n^2 - c_7n + c_8n^2 - c_8n + c_9n^2 - c_9n + c_{10}n^2 - c_{10}n + c_{11}n^2 - c_{11}n}{2} \\
& + \frac{c_{12}n^2 - c_{12}n + c_{13}n^2 - c_{13}n + c_{14}n^2 - c_{14}n + c_{15}n^2 - c_{15}n}{2} + c_{16}n + c_{17}n + c_{18}n + c_{19}
\end{aligned}$$

$$\begin{aligned}
T(n) = & n^2 \left(\frac{c_5}{2} + \frac{c_6}{2} + \frac{c_7}{2} + \frac{c_8}{2} + \frac{c_9}{2} + \frac{c_{10}}{2} + \frac{c_{11}}{2} + \frac{c_{12}}{2} + \frac{c_{13}}{2} + \frac{c_{14}}{2} + \frac{c_{15}}{2} \right) \\
& + n \left(c_2 + c_3 + c_4 - \frac{c_5}{2} - \frac{c_6}{2} - \frac{c_7}{2} - \frac{c_8}{2} - \frac{c_9}{2} - \frac{c_{10}}{2} - \frac{c_{11}}{2} - \frac{c_{12}}{2} - \frac{c_{13}}{2} - \frac{c_{14}}{2} - \frac{c_{15}}{2} + c_{16} + c_{17} + c_{18} \right) + (c_1 + c_2 + c_5 + c_{19})
\end{aligned}$$

Assuming that

$$k = \frac{c_5}{2} + \frac{c_6}{2} + \frac{c_7}{2} + \frac{c_8}{2} + \frac{c_9}{2} + \frac{c_{10}}{2} + \frac{c_{11}}{2} + \frac{c_{12}}{2} + \frac{c_{13}}{2} + \frac{c_{14}}{2} + \frac{c_{15}}{2}$$

$$y = c_2 + c_3 + c_4 - \frac{c_5}{2} - \frac{c_6}{2} - \frac{c_7}{2} - \frac{c_8}{2} - \frac{c_9}{2} - \frac{c_{10}}{2} - \frac{c_{11}}{2} - \frac{c_{12}}{2} - \frac{c_{13}}{2} - \frac{c_{14}}{2} - \frac{c_{15}}{2} + c_{16} + c_{17} + c_{18}$$

$$z = c_1 + c_2 + c_5 + c_{19}$$

We have that

$$T(n) = n^2(k) + n(y) + z \rightarrow \theta(n^2)$$

Spatial complexity analysis

| Type | Variable | Size of 1 atomic value | Amount values |
|-------------|-----------------|-------------------------------|----------------------|
| Input | List | 32 bits | 1 |
| Auxiliar | Minor | 32 bits | 1 |
| Auxiliar | Cual | 32 bits | 1 |
| Auxiliar | S1 | 32 bits | 1 |
| Auxiliar | S2 | 32 bits | 1 |
| Auxiliar | Temp1 | 32 bits | 1 |
| Auxiliar | Temp2 | 32 bits | 1 |

- Total Spatial Complexity = $Input + Auxiliary + Output = 7 = \theta(7)$
- Auxiliary Spatial Complexity = $6 = \theta(6)$
- Auxiliary Spatial Complexity Output = $Auxiliary + Output = 6 = \theta(6)$