

**Homework 3**  
**Problem 1**  
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*I certify that I have personally done the coding, generated the figures and written the report without aid from anybody else, and that I have not plagiarized, self-plagiarized, or used AI-generated text. I certify that I have acknowledged any sources I used to complete this assignment. ARM.*

### 1 Part 1: K-Means Clustering of Soccer Image

Figure 1 shows the soccer image reconstructed using K-means from values of  $k=2 \dots 10$ . We can see when  $k=2$  only the most dominant colors are shown in the image, green and white. At  $k=2$  the shapes are not well defined, and we cannot really see the picture clearly. As we increase the value of  $k$  more and more color is added to the image. A trend we can see with increasing values of  $k$  is that more detail is preserved because more colors are used for the k-means in turn allowing us to perceive the entire image in full detail.

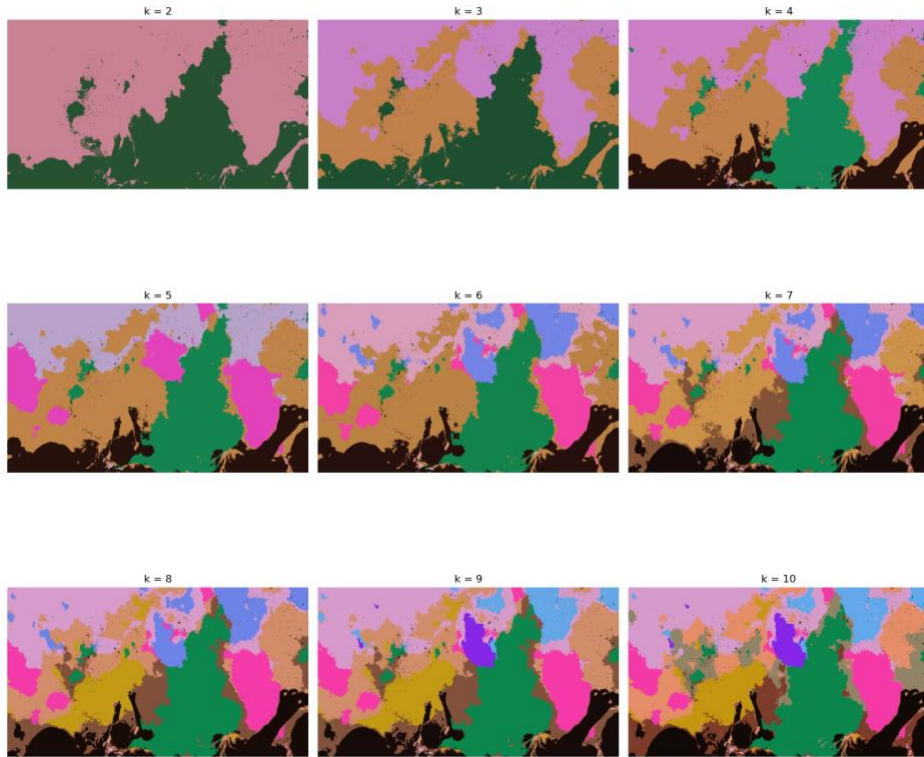
Image Reconstruction using K-means Color Quantization



**Figure 1.** Image reconstruction of soccer image using K-means and vector quantization.

### 2 Part 2: K-Means Clustering of Holi Image

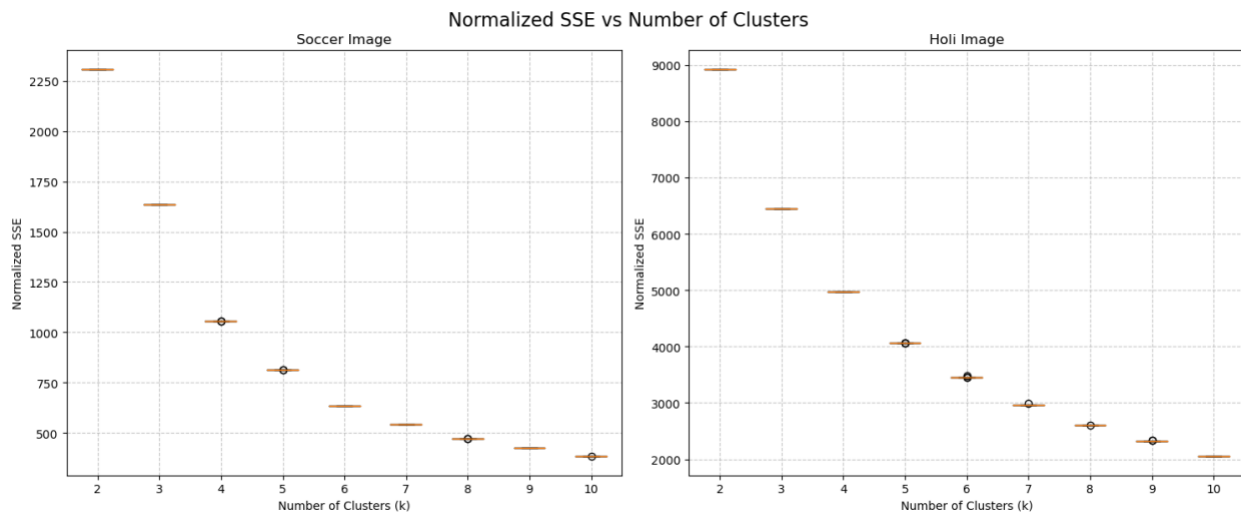
Figure 2 shows the Holi image reconstructed using K-means from values of  $k=2 \dots 10$ . We see a similar trend to part 1 with the soccer image. At  $k=2$  we only see the 2 most dominant colors that are present in the image. At  $k=2$  we cannot really see any details of the image. As we increase the value of  $k$  we get more and more color. This adds details to the image and lets us see the complete image in focus unlike at lower values of  $k$  where the number of colors is too small to preserve detail in the image.



**Figure 2.** Image reconstruction of Holi image using K-means and vector quantization.

### 3 Part 3: SSE between Original and Reconstructed Image

Figure 3 plots the SSE between the original image and the reconstructed image for both the soccer image and Holi image.



**Figure 3.** Plot between the SSE of the original image and the reconstructed image for both the soccer and Holi images. A trend we see in both graphs is that the normalized SSE decreases as k increases. This is because with more clusters and higher values of k, we can represent the original image more completely.

These graphs don't have a clear elbow point or a point where we can clearly tell that is the optimal value of  $k$ . On these graphs we have a much larger range to pick from for the most optimal value of  $k$ . The variation in SSE on different runs decreases as we run the algorithm over and over. This shows that the algorithm is more stable at higher levels of  $k$ .

#### **4 Resources used to achieve this goal**

**Canvas:** Homework template

**Python Libraries:** NumPy, pandas, matplotlib, sci-kit learn

#### **5 References**

scikit-learn. "Sklearn.cluster.KMeans — Scikit-Learn 0.21.3 Documentation." *Scikit-Learn.org*, 2019, [scikit-learn.org/stable/modules/generated/sklearn.cluster.KMeans.html](https://scikit-learn.org/stable/modules/generated/sklearn.cluster.KMeans.html).