

BITCOIN MECHANICS & OPTIMIZATIONS:

A TECHNICAL OVERVIEW

SISHIR GIRI & HAENA LEE

LECTURE OVERVIEW

Ol Cryptographic Hash Functions

O2 A Tamper-Evident Database

O3 SIGS, ECDSA, AND ADDRESSES

04 BITCOIN SCRIPT



INTRODUCING YOUR LECTURERS



Haena Lee
Education



Sishir Giri Consulting







How do we ensure trust in communication in a trustless environment?

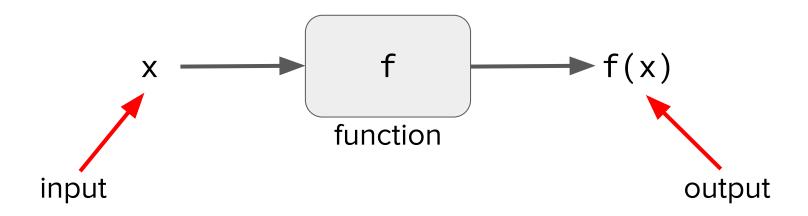
⇒ With cryptographic hash functions

USED HIGHLY IN DIGITAL SIGNATURES

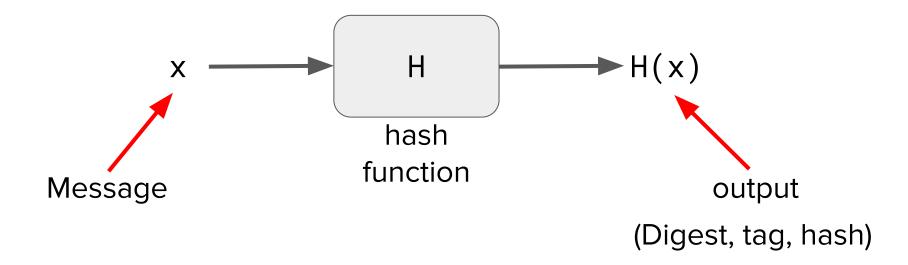


Image source: https://spiritegq.com/wp-content/uploads/2016/03/63180952 fingerprint types624.jpg

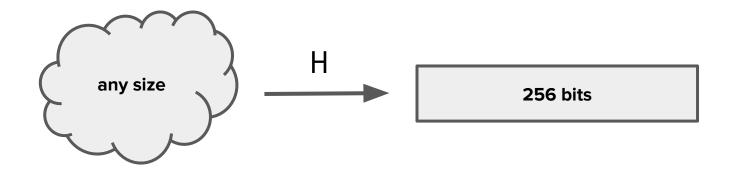














Cryptographic hash function:

A hash function with three special properties:

- Computationally Efficient
- Collision resistance
- Hide information

The equivalent of mathematical fingerprints/identifiers

Image source

http://chimera.labs.oreilly.com/books/12340000 01802/ch08.html# proof of work algorithm

```
I am Satoshi Nakamoto0 => a80a81401765c8eddee25df36728d732...
  am Satoshi Nakamoto1 => f7bc9a6304a4647bb41241a677b5345f...
 am Satoshi Nakamoto2 => ea758a8134b115298a1583ffb80ae629...
 am Satoshi Nakamoto3 => bfa9779618ff072c903d773de30c99bd...
  am Satoshi Nakamoto4 => bce8564de9a83c18c31944a66bde992f...
 am Satoshi Nakamoto5 => eb362c3cf3479be0a97a20163589038e...
 am Satoshi Nakamoto6 => 4a2fd48e3be420d0d28e202360cfbaba...
  am Satoshi Nakamoto7 => 790b5a1349a5f2b909bf74d0d166b17a...
 am Satoshi Nakamoto8 => 702c45e5b15aa54b625d68dd947f1597...
 am Satoshi Nakamoto9 => 7007cf7dd40f5e933cd89fff5b791ff0...
 am Satoshi Nakamoto10 => c2f38c81992f4614206a21537bd634a...
 am Satoshi Nakamoto11 => 7045da6ed8a914690f087690e1e8d66...
  am Satoshi Nakamoto12 => 60f01db30c1a0d4cbce2b4b22e88b9b...
  am Satoshi Nakamoto13 => 0ebc56d59a34f5082aaef3d66b37a66...
 am Satoshi Nakamoto14 => 27ead1ca85da66981fd9da01a8c6816...
 am Satoshi Nakamoto15 => 394809fb809c5f83ce97ab554a2812c...
 am Satoshi Nakamoto16 => 8fa4992219df33f50834465d3047429...
  am Satoshi Nakamoto17 => dca9b8b4f8d8e1521fa4eaa46f4f0cd...
 am Satoshi Nakamoto18 => 9989a401b2a3a318b01e9ca9a22b0f3...
 am Satoshi Nakamoto19 => cda56022ecb5b67b2bc93a2d764e75f...
```



Computationally efficient:

Set of computation to get a digest/hash should not take a long time

<u>Fingerprint analogy:</u>
Whose fingerprint is this?





Collision Resistance:

It should be hard to find two inputs that maps the same output/hash/Digest. **Output** should look random

Fingerprint analogy:

Can you find two random people with the same fingerprint?





Hide information:

Given the output, it should be hard to find anything interesting about the input. Ex: even or odd Number

Fingerprint analogy:

Can you find someone with the same fingerprint as you?





Avalanche effect: a small change in the input produces a pseudorandom change in the output

- Often a significant difference from the first output
- Prevents "hot or cold" game with inputs to produce or predict outputs

```
I am Satoshi Nakamoto0 => a80a81401765c8eddee25df36728d732...
  am Satoshi Nakamoto1 => f7bc9a6304a4647bb41241a677b5345f...
  am Satoshi Nakamoto2 => ea758a8134b115298a1583ffb80ae629...
 am Satoshi Nakamoto3 => bfa9779618ff072c903d773de30c99bd...
  am Satoshi Nakamoto4 => bce8564de9a83c18c31944a66bde992f...
  am Satoshi Nakamoto5 => eb362c3cf3479be0a97a20163589038e...
  am Satoshi Nakamoto6 => 4a2fd48e3be420d0d28e202360cfbaba...
  am Satoshi Nakamoto7 => 790b5a1349a5f2b909bf74d0d166b17a...
I am Satoshi Nakamoto8 => 702c45e5b15aa54b625d68dd947f1597...
  am Satoshi Nakamoto9 => 7007cf7dd40f5e933cd89fff5b791ff0...
  am Satoshi Nakamoto10 => c2f38c81992f4614206a21537bd634a...
  am Satoshi Nakamoto11 => 7045da6ed8a914690f087690e1e8d66...
  am Satoshi Nakamoto12 => 60f01db30c1a0d4cbce2b4b22e88b9b...
  am Satoshi Nakamoto13 => 0ebc56d59a34f5082aaef3d66b37a66...
 am Satoshi Nakamoto14 => 27ead1ca85da66981fd9da01a8c6816...
  am Satoshi Nakamoto15 => 394809fb809c5f83ce97ab554a2812c...
  am Satoshi Nakamoto16 => 8fa4992219df33f50834465d3047429...
    Satoshi Nakamoto17 => dca9b8b4f8d8e1521fa4eaa46f4f0cd...
  am Satoshi Nakamoto18 => 9989a401b2a3a318b01e9ca9a22b0f3...
 am Satoshi Nakamoto19 => cda56022ecb5b67b2bc93a2d764e75f...
```



SHA-256: A cryptographic hash function designed by the NSA

Bitcoin uses SHA-256^2 ("SHA-256 squared"), meaning that H(x) actually means SHA256(SHA256(x))

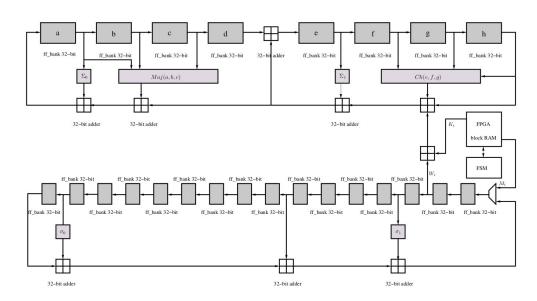


Image source:

https://opencores.org/usercontent,img,137598584

3



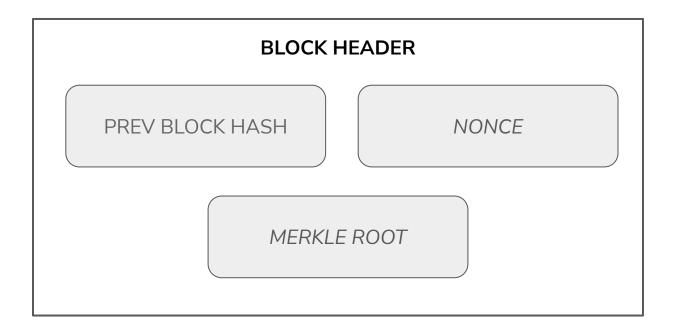




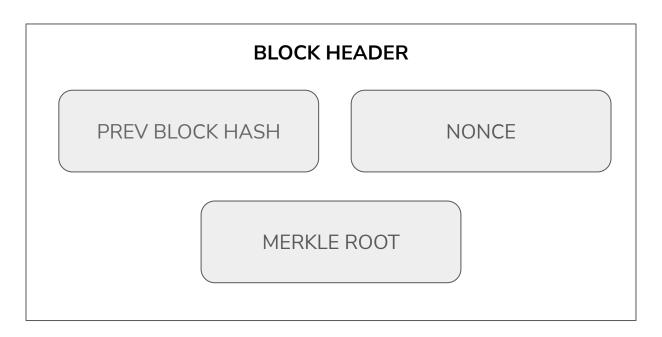






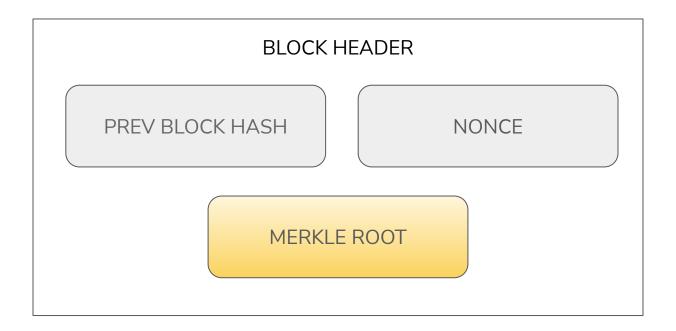






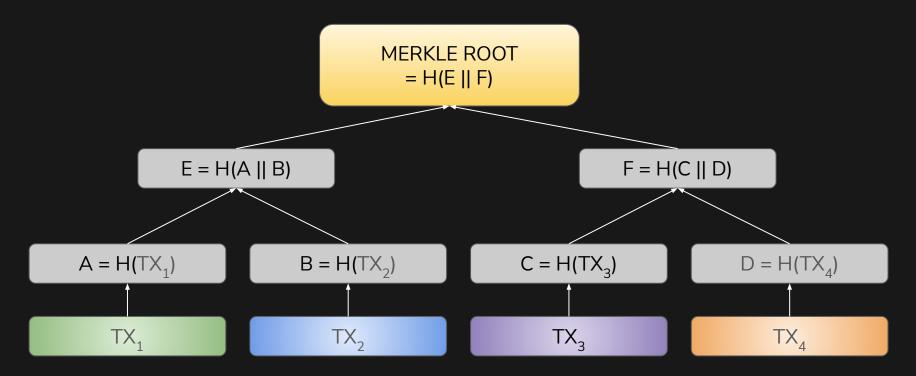
blockID = H(blockHeader) = H(prevBlockHash || merkleRoot || nonce)





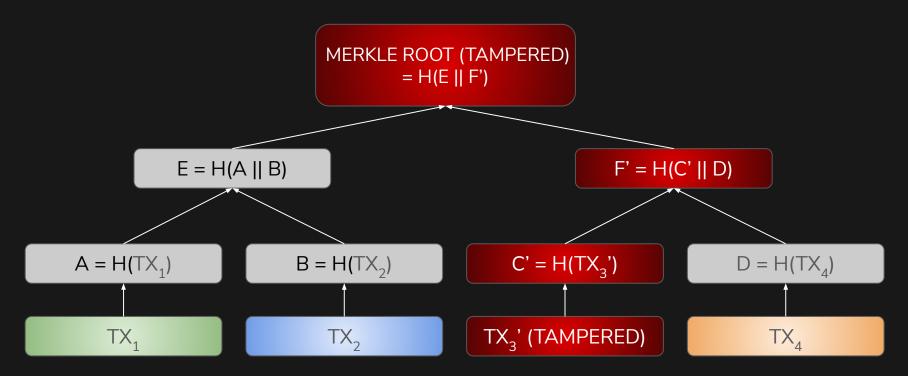


MERKLE ROOT

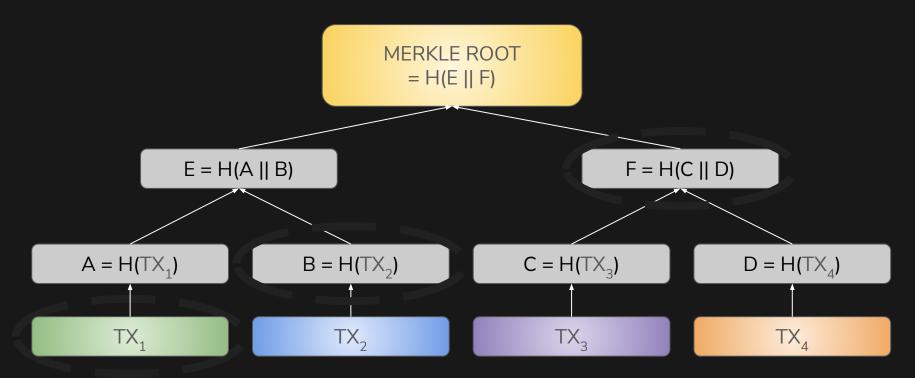




MERKLE ROOT





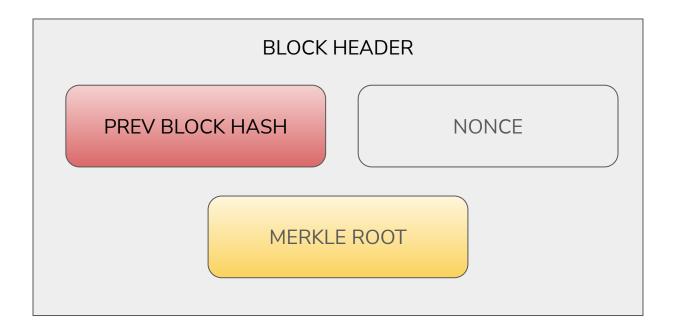








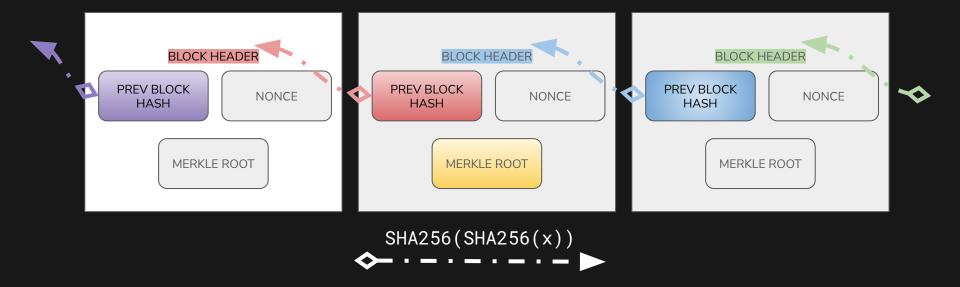






PROTECTING THE CHAIN

A TAMPER-EVIDENT DATABASE

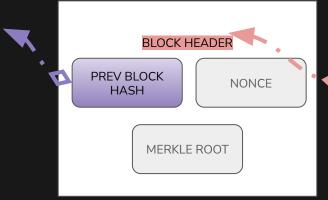


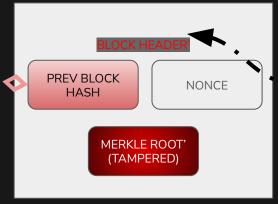
prevBlockHash = H(prevBlockHash || merkleRoot || nonce)

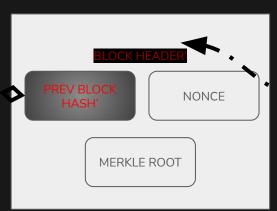


PROTECTING THE CHAIN

A TAMPER-EVIDENT DATABASE







SHA256(SHA256(x))

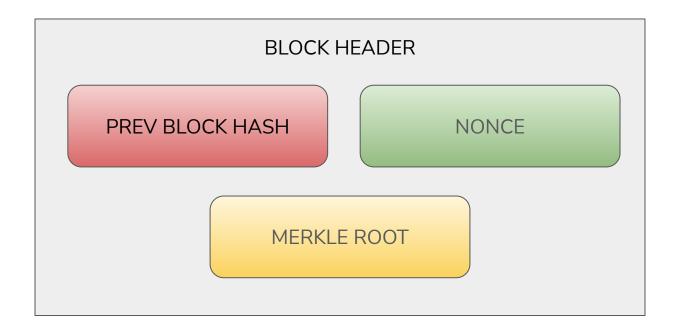
prevBlockHash = H(prevBlockHash || merkleRoot || nonce)













HASH PUZZLE

A TAMPER-EVIDENT DATABASE

 Bitcoin's Proof of Work consensus requires miners to solve a computationally difficult puzzle

Hash puzzles need to be:

- 1. Computationally difficult.
- 2. Adjustable
- Easily verifiable.



Bitcoin's partial preimage hash puzzle: A problem with a requirement to find a nonce that satisfies the following inequality:

H(prevBlockHash || merkleRoot || nonce) < target



HASH PUZZLE

A TAMPER-EVIDENT DATABASE

Bitcoin's partial preimage hash puzzle:



```
H(prevBlockHash || merkleRoot || nonce)

H("Hello, world!0")
```

0x1312af178c253f84028d480a6adc1e25e81caa44c749ec81976192e2ec934c64





```
H(prevBlockHash || merkleRoot || nonce)

H("Hello, world!1")
```

0xe9afc424b79e4f6ab42d99c81156d3a17228d6e1eef4139be78e948a9332a7d8





```
H(prevBlockHash || merkleRoot || nonce)

H("Hello, world!4250")
```

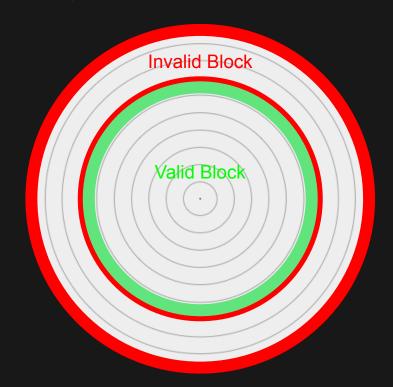
0x0000c3af42fc31103f1fdc0151fa747ff87349a4714df7cc52ea464e12dcd4e9

<

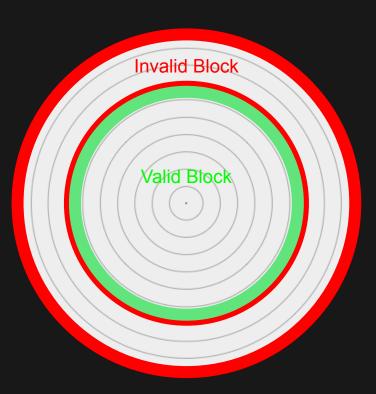
Solved!



- Mining is like throwing darts at a target while blindfolded:
 - Equal likelihood of hitting any part of the target
 - Faster throwers ⇒ more hits / second
- Miners look for a hash below an algorithmically decided target







Difficulty: A representation of the expected number of computations required to find a block

- Implemented as requirement of leading number of 0s
- Adjusts with global hashrate
- Adjusts every 2016 blocks (~2 weeks)

A TAMPER-EVIDENT DATABASE

H(prevBlockHash || merkleRoot || nonce) <</pre>



A TAMPER-EVIDENT DATABASE

Source: (from Princeton Textbook, 5.2)



EXAMPLE BLOCK

A TAMPER-EVIDENT DATABASE

REAL BITCOIN BLOCK EXAMPLE

https://www.blockchain.com/explorer

Source:

https://blockchain.info/block/00000000000000000013942c4215cd92306bbce769cfcb349d0b42f031c994eb















SIGS, ECDSA, AND ADDRESSES

INTRO TO DIGITAL SIGNATURE ALGORITHMS

Dilemma:

When sending transactions to other users, we want 2 seemingly contradictory things to happen:

- 1. Tie user identity to a transaction
- 2. Have no sensitive identifiable characteristics associated with a particular transaction



INTRO TO DIGITAL SIGNATURE ALGORITHMS

<u>Public Key Cryptography:</u> a cryptographic system that allows for secure dissemination of identity and authentication of valid messages.



INTRO TO DIGITAL SIGNATURE ALGORITHMS

- 1. <u>Public Key:</u> information about a user that can be distributed widely
- 2. **Private Key:** sensitive information about a user that should be only known by the user



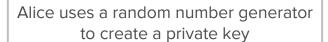
ECDSA (ELLIPTIC CURVE DSA)

- Elliptic Curve Digital Signature Algorithm (ECDSA):
 - the algorithm the Bitcoin network uses to generate public keys and verify transactions.
 - a variant of standard DSA but with elliptic curves



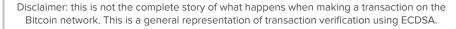








BOB







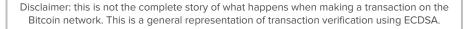
ALICE

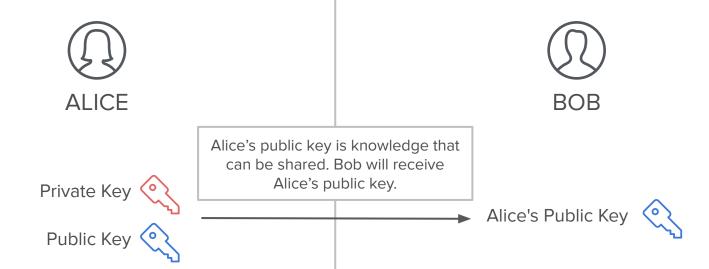


Alice uses ECDSA to calculate public key



BOB











ALICE



BOB





Public Key 🣀



Transaction



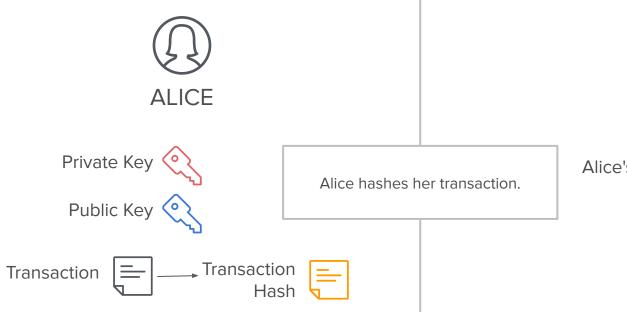
Alice has some transaction to send to Bob.

Alice's Public Key



UPDATED: HAENA LEE







BOB

Alice's Public Key



AUTHOR: PHILIP HAYES UPDATED: HAENA LEE





ALICE





Public Key 🧿



Transaction



Transaction Hash



Signature



=



+





BOB

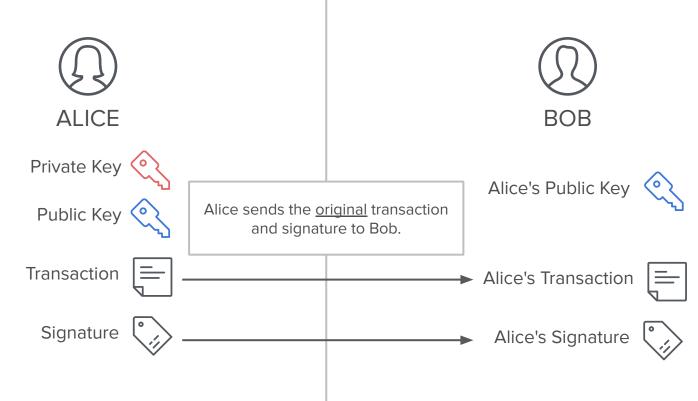
Alice's Public Key



Alice produces a signature using the hash, private key, and elliptic curve.

AUTHOR: PHILIP HAYES UPDATED: HAENA LEE











ALICE

Private Key

Public Key



Alice sends the <u>original</u> transaction and signature to Bob.



BOB

Alice's Public Key



Transaction



Signature



Alice's Transaction



Alice's Signature









ALICE





Transaction





Bob will be able to verify if Alice created the signature.



BOB

Alice's Public Key



Alice's Transaction



Alice's Signature





AUTHOR: PHILIP HAYES UPDATED: HAENA LEE





ALICE





Transaction



However, Bob cannot easily recover Alice's private key.

Signature





BOB

Alice's Public Key



Alice's Transaction



Alice's Signature

















ALICE

Private Key 🤄

Public Key

Transaction



Signature





EVE

Eve's Private Key



Eve's Public Key 🣀





BOB

Alice's Public Key



AUTHOR: GILLIAN CHU UPDATED: HAENA LEE





ALICE

Private Key 🤄



Transaction



Signature





EVE

Eve's Private Key



Eve's Public Key 🣀



private key + message = signature





BOB

Alice's Public Key



AUTHOR: GILLIAN CHU UPDATED: HAENA LEE





ALICE

Private Key 🣀



Transaction



Signature





EVE

Eve's Private Key



Eve's Public Key 🣀



Alice's Transaction



Eve's Signature





Alice's Public Key

BOB



Eve's Signature









Private Key 🤇

Public Key 🧿

Transaction

Signature



EVE

Eve's Private Key



Eve's Public Key 🣀



Alice's Transaction



Eve's Signature





BOB

Alice's Public Key



Alice's Transaction



Eve's Signature





AUTHOR: GILLIAN CHU

GUARANTEED PROPERTIES

ECDSA SUMMARY

Recipients given the (message, signature) pair should be able to verify:

- Message Origin: original sender (owner of private key) has authorized this message/transaction
- Non-repudiation: original sender (owner of private key) cannot backtrack
- Message Integrity: transaction cannot have been modified since sending

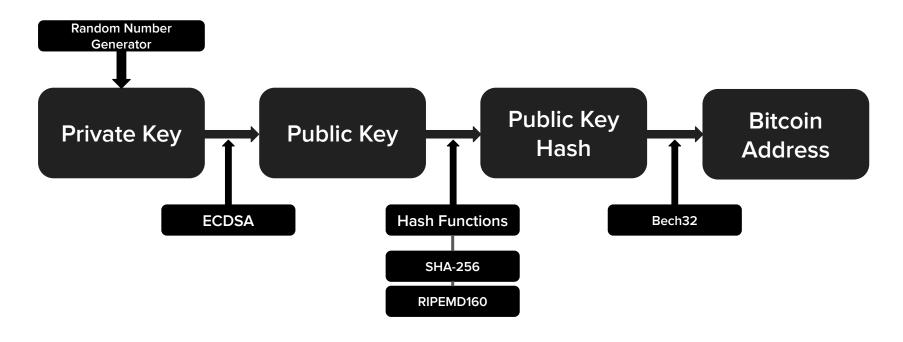






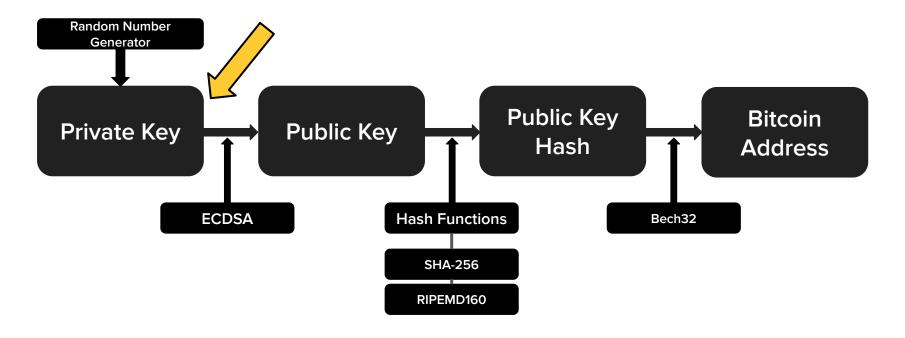


CONVERSION SUMMARY





CONVERSION SUMMARY



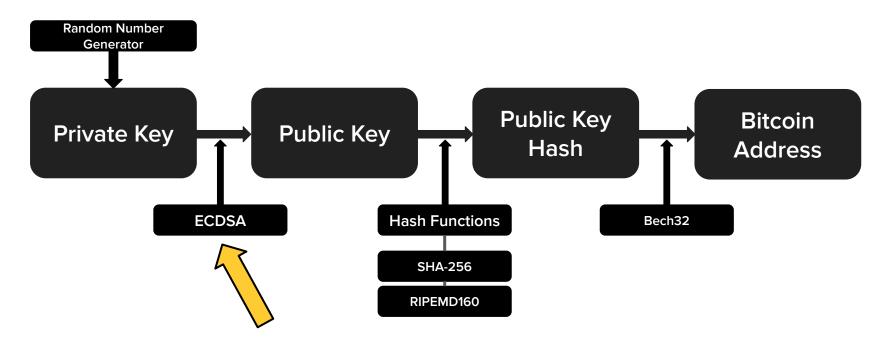


PRIVATE KEY GENERATION

- Private Keys on Bitcoin: 256-bit unsigned integers
- Private keys on Bitcoin are **not** generated using regular random number generators.
- Chances of two different individuals generating the same private key (collision) is extremely low.
 - ~2²⁵⁶ unique private keys
 - \circ Chances of collision: (1/2²⁵⁶) * (1/2²⁵⁶) = really, really low



CONVERSION SUMMARY



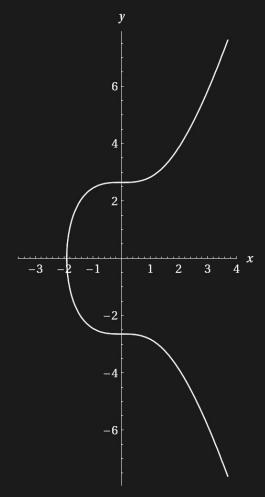


ELLIPTIC CURVES (SECP256K1)

PUBLIC KEY GENERATION

- Bitcoin uses **ECDSA** (Elliptic Curve Digital Signature Algorithm) to produce public keys
- The Elliptic Curve is defined by some mathematical function
 - Bitcoin's Elliptic Curve:

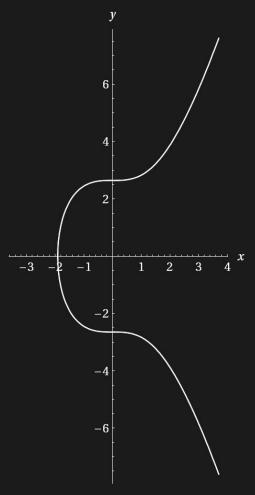
secp256k1:
$$Y^2 = (X^3 + 7)$$
 over (F_p)



ELLIPTIC CURVE SCALAR MULTIPLICATION

PUBLIC KEY GENERATION

- Using a private key as an input, we can generate a public key by performing point multiplication/elliptic curve scalar multiplication.
 - Key thing to note here: point multiplication is a trapdoor function.
 - This means calculating the public key is a one-way function.



TIME COMPLEXITY

PUBLIC KEY GENERATION

Input: public key

Output: corresponding private key

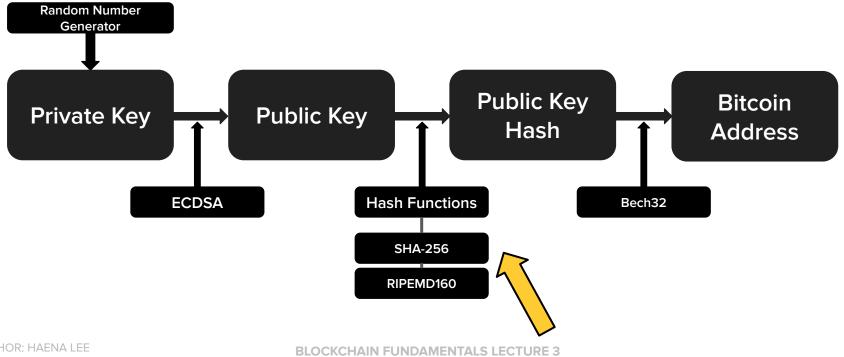
256 bit private key, takes O(sqrt(n)) operations to crack
15 * pow(2,40) hashes per second on the ENTIRE Bitcoin network

pow(2,128) / (15 * pow(2,40)) / 3600 / 24 / 365.25 = 0.6537992112229596e18

650 million billion years



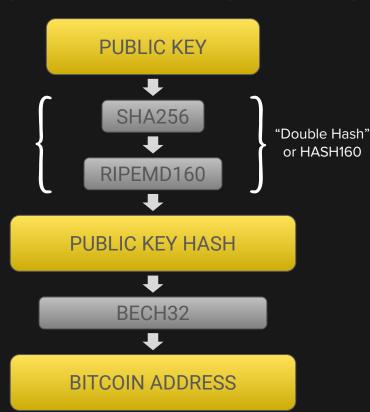
CONVERSION SUMMARY





PUBKEY TO PUBKEY HASH

PUBLIC KEY TO BITCOIN ADDRESS



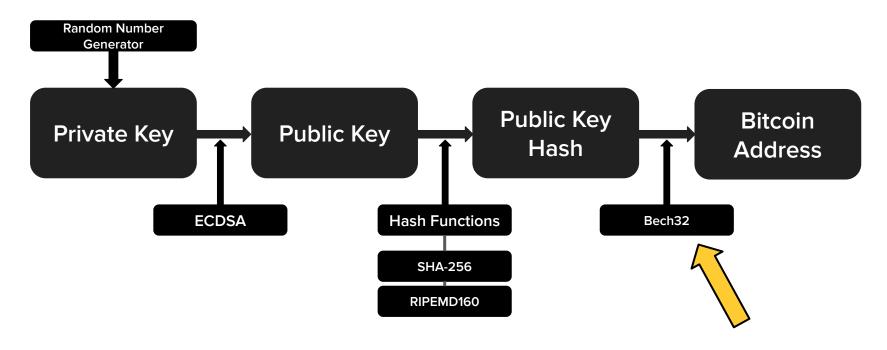
PUBKEYHASH = RIPEMD160(SHA256(K))

- SHA-256 (Secure Hashing Algorithm)
 - Used extensively in bitcoin scripts and mining
- RIPEMD (RACE Integrity Primitives Evaluation Message Digest)
 - o Produces 160-bit (20-byte) number



AUTHOR: GLORIA ZHAO UPDATED: GILLIAN CHU

CONVERSION SUMMARY















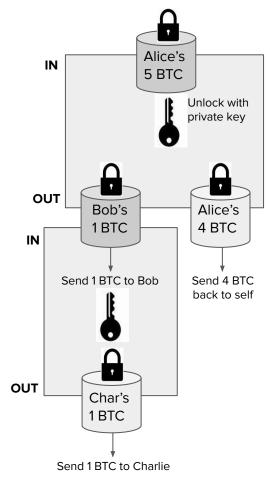
BITCOIN SCRIPT

REMEMBER THE UTXO MODEL?

BITCOIN SCRIPT

Reminders:

- Bitcoin uses a UTXO model
- Transactions map inputs to outputs,
- Transactions contain signature of owner of funds
- Spending Bitcoin is redeeming previous transaction outputs





CONTENTS OF A TRANSACTION



CONTENTS OF A TRANSACTION - METADATA

"hash": "5a42590fbe0a90ee8e8747244d6c84f0db1a3a24e8f1b95b10c9e050990b8b6b",

```
"ver": 1.
"vin sz": 2,
"vout sz": 1,
"lock time": 0,
"size": 404,
             "prev out": {
                     "hash": "3be4ac9728a0823cf5e2deb2e86fc0bd2aa503a91d307b42ba76117d79280260".
                     "n": 0
                     "scriptSig": "30440..."
             "prev out": {
                      "hash": "7508e6ab259b4df0fd5147bab0c949d81473db4518f8afc5c3f52f91ff6b34e".
                     "n"· 0
             "scriptSig": "3f3a4ce81...."
             "value": 10.12287097".
             "scriptPubKey": "OP DUP OP HASH160 69e02e18b5705a05dd6b28ed517716c894b3d42e OP EQUALVERIFY OP CHECKSIG"
```



hash or "ID"

of this transaction

Source: Princeton Textbook

CONTENTS OF A TRANSACTION - METADATA

'hash": "5a42590fbe0a90ee8e8747244d6c84f0db1a3a24e8f1b95b10c9e050990b8b6b",

```
"ver": 1.
                      size (number) of inputs
                      size (number) of outputs
"lock time": 0,
"size": 404,
            "prev_out": {
                    "hash": "3be4ac9728a0823cf5e2deb2e86fc0bd2aa503a91d307b42ba76117d79280260".
                    "n": 0
                    "scriptSig": "30440..."
             "prev_out": {
                    "hash": "7508e6ab259b4df0fd5147bab0c949d81473db4518f8afc5c3f52f91ff6b34e".
                    "n": 0
             "scriptSig": "3f3a4ce81...."
            "value": 10.12287097",
             "scriptPubKey": "OP DUP OP HASH160 69e02e18b5705a05dd6b28ed517716c894b3d42e OP EQUALVERIFY
OP_CHECKSIG'
```

hash or "ID" of this transaction



CONTENTS OF A TRANSACTION - METADATA

"hash": "5a42590fbe0a90ee8e8747244d6c84f0db1a3a24e8f1b95b10c9e050990b8b6b",

```
version
                                     size (number) of inputs
                                  size (number) of outputs
"lock time": 0,
                                                  lock time (useful for scripting)
"size": 404,
                                               size of transaction
"in": [
            "prev out": {
                    "hash": "3be4ac9728a0823cf5e2deb2e86fc0bd2aa503a91d307b42ba76117d79280260".
                    "n": 0
                    "scriptSia": "30440..."
            "prev out": {
                    "hash": "7508e6ab259b4df0fd5147bab0c949d81473db4518f8afc5c3f52f91ff6b34e".
            "scriptSig": "3f3a4ce81...."
            "value": 10.12287097".
            "scriptPubKey": "OP DUP OP HASH160 69e02e18b5705a05dd6b28ed517716c894b3d42e OP EQUALVERIFY OP CHECKSIG"
                                                                               Source: Princeton Textbook
```

hash or "ID" of this transaction

4

```
"ver" 1
       remember these?
"vout sz": 1,
"in": [
         "prev out": {
               "hash": "3be4ac9728a0823cf5e2deb2e86fc0bd2aa503a91d307b42ba76117d79280260",
               "n": 0
               "scriptSig": "30440..."
         "prev_out": {
               "hash": "7508e6ab259b4df0fd5147bab0c949d81473db4518f8afc5c3f52f91ff6b34e",
               "n": 0
         "scriptSig": "3f3a4ce81...."
```



```
2590fbe0a90ee8e8747244d6c84f0db1a3a24e8f1b95b10c9e050990b8b6b
"ver" 1
        remember these?
"vout sz": 1,
"in": [
          "prev out": {
  input 1:
                 "scriptSig": "30440..."
                                                                 ID of previous transactions being referenced
          "prev out": {
 input 2:
                 "hash": "7508e6ab259b4df0fd5147bab0c949d81473db4518f8afc5c3f52f91ff6b34e".
                 "n": 0
          "scriptSig": "3f3a4ce81...."
```



```
"ver" 1
       remember these?
"vout sz": 1,
"in": [
         "prev out":{
               "hash": "3be4ac9728a0823cf5e2deb2e86fc0bd2aa503a9
  input 1:
                        — index of input in previous transaction
               "scriptSig": "30440..."
                                                            ID of previous transactions being referenced
         "prev out": {
  input 2:
               "hash": "7508e6ab259b4df0fd5147bab0c949d81473db4518f8afc5c3f52f91ff6b34e".
                       index of input in previous transaction
         "scriptSig": "3f3a4ce81...."
```



```
"in": [
        "prev out": {
              "hash": "3be4ac9728a0823cf5e2deb2e86fc0bd2aa503a91d307b42ba76117d79280260",
              "n": 0
        },
                                          signature used to redeem previous transaction output
        "prev out": {
              "hash": "7508e6ab259b4df0fd5147bab0c949d81473db4518f8afc5c3f52f91ff6b34e",
              "n": 0
                                            signature used to redeem previous transaction output
```



```
"hash": "5a42590fbe0a90ee8e8747244d6c84f0db1a3a24e8f1b95b10c9e050990b8b6b",
"ver": 1,
"vin_sz": 2,
"vout sz": 1,
"lock_time": 0,
"size": 404.
"in": [
             "prev_out": {
                     "hash": "3be4ac9728a0823cf5e2deb2e86fc0bd2aa503a91d307b42ba76117d79280260",
                    "n": 0
                     "scriptSig": "30440..."
             "prev out": {
                     "hash": "7508e6ab259b4df0fd5147bab0c949d81473db4518f8afc5c3f52f91ff6b34e",
                    "n": 0
             "scriptSig": "3f3a4ce81...."
                     output amount (how much BTC is being sent)
             "value": 10.12287097",
             "scriptPubKey": "OP DUP OP HASH160 69e02e18b5705a05dd6b28ed517716c894b3d42e OP EQUALVERIFY OP CHECKSIG"
          type of script
                                                    output script
                                                                                 Source: Princeton Textbook
```

SOME NOTES

BITCOIN SCRIPT

Output "addresses" are actually scripts.

"scriptPubKey": "OP_DUP OP_HASH160 69e02e18b5705a05dd6b28ed517716c894b3d42e OP_EQUALVERIFY OP_CHECKSIG"

- → This particular Output Script: "This amount can be redeemed by the **public key** that hashes to address X, plus a **signature** from the owner of that public key"
- Inputs and outputs through scripting allows for future extensibility of Bitcoin.
- Script or "Bitcoin Scripting Language": Language built specifically for Bitcoin
 - Stack based
 - Simple, <u>not turing complete</u> (no loops)



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Source: Princeton textbook





