

osmar: OpenStreetMap and R

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Abstract OpenStreetMap provides freely accessible and editable geographic data. The **osmar** package smoothly integrates the OpenStreetMap project into the R ecosystem. The **osmar** package provides infrastructure to access OpenStreetMap data from different sources, to enable working with the OSM data in the familiar R idiom, and to convert the data into objects based on classes provided by existing R packages. This paper explains the package's concept and shows how to use it. As an application we present a simple navigation device.

Introduction

"OpenStreetMap creates and provides free geographic data such as street maps to anyone who wants them" announces the OpenStreetMap wiki main page (OSM Foundation, 2011) – and we think R users want free geographic data. Therefore, the add-on package **osmar** (Schlesinger and Eugster, 2012) provides extensible infrastructure for integrating the OpenStreetMap project (OSM) into the R project.

The aim of the OpenStreetMap project is to create a free editable map of the world. The project maintains a database of geographic elements (nodes, ways and relations) and features (such as streets, buildings and landmarks). These data are collected and provided by volunteers using GPS devices, aerial imagery, and local knowledge. The most prominent application is the rendering of the geographic data and features into raster images (for example, for the OSM map on the website). However, the project also provides an application programming interface (API) for fetching raw data from and saving to the OSM database.

The OpenStreetMap project provides data in the OSM XML format, which consists of three basic elements:

Node: The basic element. It consists of the attributes latitude and longitude.

Way: An ordered interconnection of nodes to describe a linear feature (e.g., a street). Areas (e.g., buildings) are represented as closed ways.

Relation: A grouping of elements (nodes, ways, and relations), which are somehow geographically related (e.g., bus and cycle routes).

Each element has further *attributes* like the element ID (unique within the corresponding element group) and timestamp. Furthermore, each element may have an arbitrary number of *tags* (key-value pairs) which describe the element. Ways and relations, in addition, have *references* to their members' IDs.

In order to access the data, OSM provides an application programming interface (API) over the hypertext transfer protocol (HTTP) for getting raw data from and putting it to the OSM database. The *main API* (currently in version 0.6) has calls to get elements (and all other elements referenced by it) by, among other things, their ID and a bounding box. However, the requests are limited (e.g., currently only an area of 0.25 square degrees can be queried). An (unlimited) alternative is provided by *planet files*. These are compressed OSM XML files containing different OSM database extracts (e.g., the entire world or an individual country or area). Planet files can be downloaded from the OSM wiki and processed using the command-line Java tool Osmosis (Henderson, 2011).

For a complete introduction into the OSM project, the OSM API, and the OSM XML file format we refer to the project's wiki available at <http://wiki.openstreetmap.org/>.

The aim of the package **osmar** is to provide extensible infrastructure to get and to represent the above described OSM data within R, to enable working with the OSM data in the familiar R idiom, and to convert the OSM data to objects based on classes provided by other packages. Figure 1 visualizes the package's concept. This is a different idea than existing packages like **OpenStreetMap** (Fellows, 2012), **RgoogleMaps** (Loecher, 2012), and **ggmap** (Kahle and Wickham, 2012) follow. Whereas these packages provide access to the already rendered data (i.e., raster images), **osmar** enables the usage of the raw OSM data.

In the following section we present the package's implementation and usage. Note that we try to increase readability by only showing the relevant arguments of plot statements. We refer to the "navigator" demo in the **osmar** package for the actual plot statements.

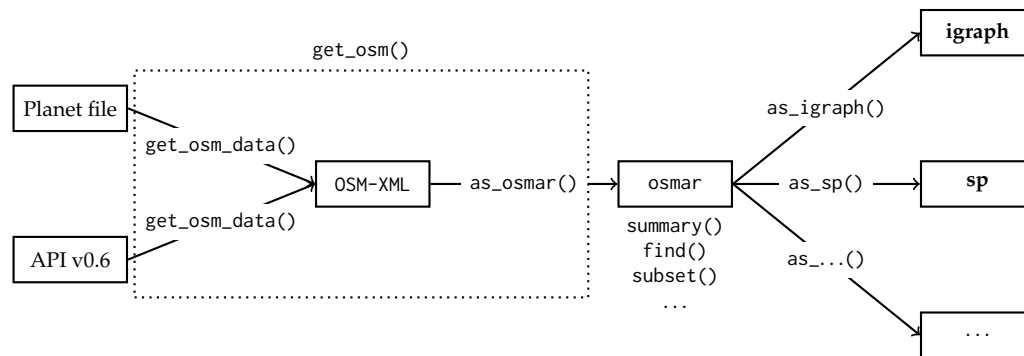


Figure 1: Schematic description of the **osmar** concept.

Getting the data

We begin with defining the data source. Currently two sources, HTTP-API and planet files, are supported. In this section we use the API of the OSM project with the default URL `url = http://api.openstreetmap.org/api/0.6/`:

```
> library("osmar")

Loading required package: XML
Loading required package: Rcurl
Loading required package: bitops
Loading required package: gtools
Loading required package: geosphere
Loading required package: sp
```

Attaching package: 'osmar'

The following object(s) are masked
from 'package:utils':

```
find
```

```
> src <- osmsource_api()
```

We can retrieve elements by using the IDs of the elements. The IDs in these examples have been extracted by hand from the OpenStreetMap website (via its export functionality). For example, one node:

```
> get_osm(node(18961430), source = src)
```

```
osmar object
1 nodes, 0 ways, 0 relations
```

Or, one way with the way-related data only or with the data for all referenced elements (nodes and relations):

```
> get_osm(way(3810479), source = src)
```

```
osmar object
0 nodes, 1 ways, 0 relations
```

```
> get_osm(way(3810479), source = src, full = TRUE)
```

```
osmar object
11 nodes, 1 ways, 0 relations
```

The first statement retrieves the way only (because the default value of the `full` argument is `FALSE`). The second statement additionally retrieves all nodes that are members of the way (i.e., all nodes that define the way).

The second possibility to retrieve elements is to specify a bounding box by defining the left, bottom, right, and top coordinates (`corner_bbox()`), or the center point and width and height in meters (`center_bbox()`):

```
> bb <- center_bbox(174.76778, -36.85056, 700, 700)
> ua <- get_osm(bb, source = src)
> ua
```

```
osmar object
2427 nodes, 428 ways, 70 relations
```

The use of planet files via Osmosis as source works analogously. The source is specified by the function `osmsource_osmosis()`. The function's two arguments are the path to the planet file (`file`) and the path to the 'osmosis' tool (`osmosis = "osmosis"`). Note that per default it is assumed that the Osmosis executable is in your 'PATH' environment variable. The navigator example demonstrates the usage of planet files.

Working with the data

The retrieved `osmar` object is a list with the three elements `nodes`, `ways`, and `relations`. Each element again is a list containing `data.frames` for the attributes (the `attrs` list element) and meta-data (the `tags` list element) of the OSM elements. Ways and relations additionally have a `data.frame` containing their members (the `refs` list element).

Summarize. For each element `nodes`, `ways`, and `relations` of an `osmar` object an individual summary method is available. The overall summary method for an `osmar` object shows the three individual summaries all at once.

```
> summary(ua$nodes)

osmar$nodes object
2427 nodes, 771 tags

..$attrs data.frame:
   id, lat, lon, user, uid, visible, version,
   changeset, timestamp
..$tags data.frame:
   id, k, v

Bounding box:
      lat      lon
min -36.85661 174.7627
max -36.84472 174.7753
```

Key-Value contingency table:

	Key	Value	Freq
1	addr:city	Auckland	101
2	addr:street	Queen Street	61
3	addr:country	NZ	40
4	addr:postcode	1010	39
5	comment	Determined via KeyPa...	29
6	addr:street	Symonds Street	27
7	highway	traffic_signals	23
8	addr:street	Lorne Street	19
9	highway	bus_stop	15
10	amenity	cafe	11

In the case of the summary for `nodes`, the number of elements and tags, as well as the available variables for each corresponding `data.frame` are shown. The bounding box of the coordinates and a contingency table of the top ten most frequently available key-value pairs are printed.

The summaries for the other two elements `ways` and `relations` are similar. Note that these methods in fact return the contingency table of all available key-value pairs and, in addition, further information which is not printed but may be useful for a descriptive analysis. We refer to the help pages (e.g., `?summary.nodes`) for a detailed description of the return values.

Find. In order to find specific elements within the `osmar` object, the `find()` function allows the object to be queried with a given condition. As the basis of `osmar` objects are `data.frames`, the condition

principally is a logical expression indicating the rows to keep. In addition, one has to specify to which element (nodes, `node()`; ways, `way()`; or relations, `relation()`) and to which data (attributes, `attrs()`; meta-data, `tags()`; or members, `refs()`) the condition applies.

If, for example, we want to find all traffic signal nodes, we know from the object's summary that the corresponding value in the `attrs` data.frame is "traffic_signals". We can express this condition as follows:

```
> ts_ids <- find(ua, node(tags(v == "traffic_signals")))
> ts_ids

[1] 25769635 25769637 25769641 ...
```

The result is a vector with node IDs (in this case 25 traffic signal nodes) or NA. If the correct spelling is unknown, the defined binary operators `%agrep%` for approximate matches (see `?agrep`) and `%grep%` for pattern matches (see `?grep1`) can be used:

```
> bs_ids <- find(ua, node(tags(v %agrep% "busstop")))
> bs_ids

[1] 678301119 737159091 1318401034 ...
```

This returns 15 bus stops available in the `ua osmar` object.

We use the functions `find_down()` and `find_up()` to find all related elements for given element IDs. The OSM basic elements define a hierarchy,

$$\text{node} \leftarrow \text{way} \leftarrow \text{relation},$$

and these two functions enable us to find the related elements up and down the hierarchy. For example, `find_up()` on a node returns all related nodes, ways, and relations; `find_down()` on a node returns only the node itself. On the other hand, `find_up()` on a relation returns only the relation itself; `find_down()` on a relation returns the relation and all related ways and nodes.

```
> hw_ids <- find(ua, way(tags(k == "highway")))
> hw_ids <- find_down(ua, way(hw_ids))
```

In this example we find all ways that have a tag with the `k` attribute set to "highway". These contain hardened and recognised land routes between two places used by motorised vehicles, pedestrians, cyclists, etc. The return value of `find_down()` and `find_up()` is a list containing the element IDs:

```
> str(hw_ids)

List of 3
 $ node_ids      : num [1:1321] 25769641 ...
 $ way_ids       : num [1:253] 4309608 ...
 $ relation_ids: NULL
```

Subset. The return value of the find functions then can be used to create subsets of `osmar` objects. The `subset()` method for `osmar` objects takes element IDs and returns the corresponding data as `osmar` objects. For example, the two subsets based on the traffic signal and bus stop element IDs are:

```
> ts <- subset(ua, node_ids = ts_ids)
> ts
```

```
osmar object
25 nodes, 0 ways, 0 relations
```

```
> bs <- subset(ua, node_ids = bs_ids)
> bs
```

```
osmar object
15 nodes, 0 ways, 0 relations
```

The subset based on the highway element IDs is:

```
> hw <- subset(ua, ids = hw_ids)
> hw
```

```
osmar object
1321 nodes, 253 ways, 0 relations
```

Note that the subsetting of osmar objects is divided into the two steps “finding” and “subsetting” to have more flexibility in handling the related elements (here with using `find_down()` and `find_up()`, but more sophisticated routines can be imagined).

Plot. The visualization of osmar objects is possible if nodes are available in the object (as only these OSM elements contain latitude and longitude information). The functions `plot_nodes()` and `plot_ways()` plot the available nodes as dots and ways as lines, respectively. The `plot()` method combines these two function calls. Note that this is a plot of the raw data and no projection is done (see the following section for a projected visualization).

```
> plot(ua)
> plot_ways(hw, add = TRUE, col = "green")
> plot_nodes(ts, add = TRUE, col = "red")
> plot_nodes(bs, add = TRUE, col = "blue")
```

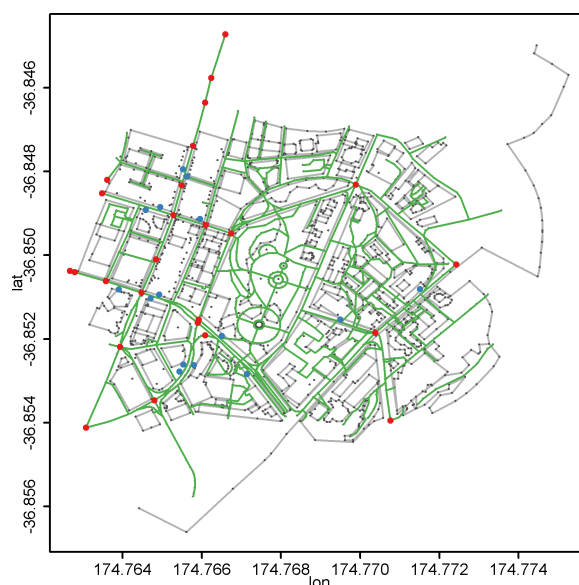


Figure 2: University of Auckland; roads are green lines; bus stops are blue and traffic signals are red points.

Converting the data

In order to use the complete power of R on OpenStreetMap data, it is essential to be able to convert osmar objects into commonly used objects based on classes provided by other packages. Currently, **osmar** provides two converters – into the **sp** (Bivand et al., 2008) and the **igraph** (Csardi, 2011) packages. In this section we show the conversion to **sp** objects, the navigation device example shows the conversion to **igraph** objects.

The **sp** package provides special data structures and utility functions for spatial data. Spatial data classes are available for points, lines, and polygons and others (see Bivand et al., 2008). The **osmar** package provides the `as_sp()` function,

```
> args(as_sp)

function(obj, what = c("points", "lines", "polygons"),
         crs = osm_crs(), simplify = TRUE)
NULL
```

to convert an osmar object into the corresponding classes for points, lines, and polygons in the **sp** package (given the required data are available). Note that the appropriate WGS84 coordinate reference system (CRS) for OpenStreetMap data is used (cf. `osm_crs()`).

Polygons. Polygons are used to represent areas, which OpenStreetMap represents as closed ways. Buildings, for example, are closed ways and can be converted to an **sp** polygon object:

```
> bg_ids <- find(ua, way(tags(k == "building")))
> bg_ids <- find_down(ua, way(bg_ids))
> bg <- subset(ua, ids = bg_ids)
> bg
```

```
osmar object
991 nodes, 110 ways, 0 relations
```

```
> bg_poly <- as_sp(bg, "polygons")
```

The result is a `SpatialPolygonsDataFrame` with the osmar object's attributes (the `attrs` element) as its data. Functionality provided by the `sp` package can now be used to analyze the OSM data; e.g., the `summary()` method or the `spplot()` method—the latter one, for example, to see how often each building was modified:

```
> spplot(bg_poly, c("version"))
```

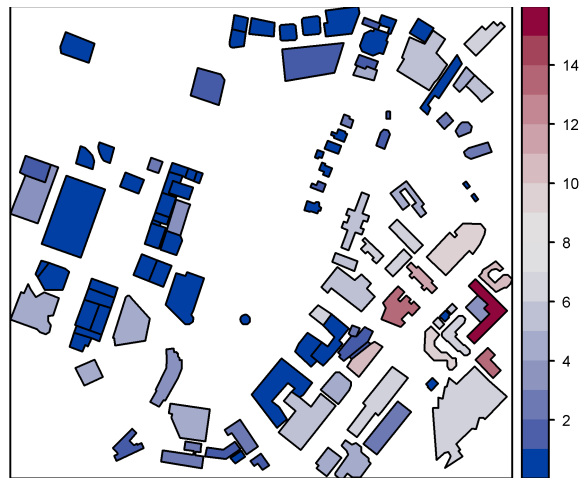


Figure 3: Number of modifications per building.

Meta-data (the `tags` element) and members (the `refs` element) are not automatically converted to a `SpatialPolygonsDataFrame`'s data.

Lines and points. The conversion of lines and points works similarly:

```
> hw_line <- as_sp(hw, "lines")
> bs_points <- as_sp(bs, "points")
```

The results are `SpatialLinesDataFrame` and `SpatialPointsDataFrame` objects, respectively.

In order to finalize the University of Auckland example we create a bus route map and visualize the available bus routes belonging to the bus stops. Therefore, we find all bus relations available in the object, retrieve the corresponding data from the OSM API, and convert the data into lines (note that this computation takes some time):

```
> bus_ids <- find(ua, relation(tags(v == "bus")))
> bus <- lapply(bus_ids,
+   function(i) {
+     raw <- get_osm(relation(i), full = TRUE)
+     as_sp(raw, "lines")
+   })
```

We use the argument `full = TRUE` to retrieve the relation itself and all related members. In detail, this means we retrieve all nodes, ways, and relations that are members of the specified relation; and, recursively, all nodes that are members of the retrieved ways.

We then use the `sp` plot methods to create the final bus route map:

```
> plot(bg_poly, col = "gray")
> plot(hw_line, add = TRUE, col = "green")
```

```
> plot(bs_points, add = TRUE, col = "blue")
> for ( i in seq(along = bus) ) {
+   plot(bus[[i]], add = TRUE, col = "blue")
+ }
```



Figure 4: Bus route map of the University of Auckland; roads are green lines; bus stops and bus routes are blue points and lines

R as navigator

We always wanted to know how a navigation device works. Now with **osmar**, R provides the necessary components and this serves as nice example on how to use **osmar**. The general idea is to (1) get the data, (2) extract all highways, (3) create a graph of all highway nodes with the distance between the highway nodes as edge weights, (4) compute the shortest path on the graph, and (5) trace the path on the highways.

Get the data. We use a planet file from Munich as the data source and use Osmosis ([Henderson, 2011](#)) to process the data. Note that ‘osmosis’ has to be in your ‘PATH’ environment variable.

```
> library("osmar")
> url <- "http://osmar.r-forge.r-project.org/"
> file <- "muenchen.osm.gz"
> download.file(sprintf("%s%s", url, file), file)
> system("gzip -d muenchen.osm.gz")
```

Get the center of Munich with a 3km × 3km bounding box:

```
> src <- osmsource_osmosis(file = "muenchen.osm")
> muc_bbox <- center_bbox(11.575278, 48.137222, 3000, 3000)
> muc <- get_osm(muc_bbox, src)
> muc
```

```
osmar object
13713 nodes, 3156 ways, 76 relations
```

For the navigation device we only need streets. This means, we have to find all ways that are tagged as highways and have a name tag, then find the associated nodes, and finally subset the full osmar object:

```
> hways_muc <- subset(muc, way_ids = find(muc, way(tags(k == "highway"))))
> hways <- find(hways_muc, way(tags(k == "name")))
> hways <- find_down(muc, way(hways))
> hways_muc <- subset(muc, ids = hways)
> hways_muc
```

```
osmar object
3889 nodes, 995 ways, 0 relations
```

Suppose we want to start our route at the “Sendlinger Tor”. This means we first have to find a node that is tagged with the name “Sendlinger Tor” and then the nearest highway node:

```
> hway_start_node <- local({
+   id <- find(muc, node(tags(v == "Sendlinger Tor")))[1]
+   find_nearest_node(muc, id, way(tags(k == "highway")))
+ })
> hway_start <- subset(muc, node(hway_start_node))
```

For a given node (by its ID), the function `find_nearest_node()` finds the nearest node with the specified conditions (the package [geosphere](#), [Hijmans et al., 2011](#) is used to compute the distances). The end of the route should be in the northeast part of Munich; so we find nodes that are in the northeast and take one highway node:

```
> hway_end_node <- local({
+   id <- find(muc, node(attrs(lon > 11.59 & lat > 48.150)))[1]
+   find_nearest_node(muc, id, way(tags(k == "highway")))
+ })
> hway_end <- subset(muc, node(hway_end_node))
```

Finally, we visualize the initial situation:

```
> plot_nodes(muc, col = "gray")
> plot_ways(hways_muc, add = TRUE)
> plot_nodes(hways_muc, add = TRUE, col = "black")
> plot_nodes(hway_start, add = TRUE, col = "red")
> plot_nodes(hway_end, add = TRUE, col = "blue")
```

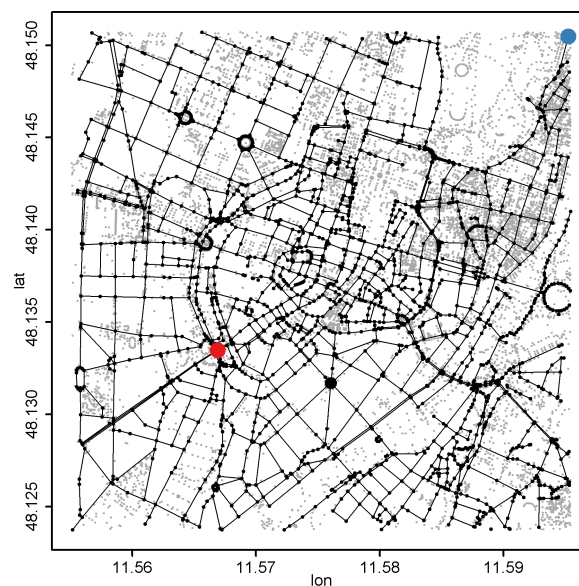


Figure 5: Highway map of Munich center.

The gray nodes are all nodes available in the full osmar object, the black nodes and lines are the road networks available in the highway-osmar object, the red and blue dots denote the starting and ending nodes of the searched route.

Compute the route. In order to compute the shortest route between the defined starting and ending nodes, we convert the highway-osmar object into a graph. R provides a set of packages to work with graphs, we decided to use **igraph**:

```
> library("igraph")
> gr_muc <- as_igraph(hways_muc)
> summary(gr_muc)
```



```

Vertices: 2381
Edges: 2888
Directed: TRUE
No graph attributes.
Vertex attributes: name.
Edge attributes: weight, name.

```

The `osmar` object nodes define the nodes of the graph (node IDs are used as graph node names). The `osmar` object ways define the edges (way IDs are used as edge names), and the weights of the edges are the geographical distance between the nodes.

The **igraph** package provides different shortest path algorithms (e.g., Dijkstra and Bellman-Ford) via the function `get.shortest.paths()`. The shortest route (not necessarily unique) is:

```

> route <- get.shortest.paths(gr_muc,
+   from = as.character(hway_start_node),
+   to = as.character(hway_end_node))[[1]]
> route_nodes <- as.numeric(V(gr_muc)[route]$name)

```

We construct a new `osmar` object containing only elements related to the nodes defining the route:

```

> route_ids <- find_up(hways_muc, node(route_nodes))
> route_muc <- subset(hways_muc, ids = route_ids)
> route_muc

```

```

osmar object
101 nodes, 83 ways, 0 relations

```

And add the route to the highway map of Munich center in Figure 5:

```

> plot_nodes(route_muc, add = TRUE, col = "green")
> plot_ways(route_muc, add = TRUE, col = "green")

```

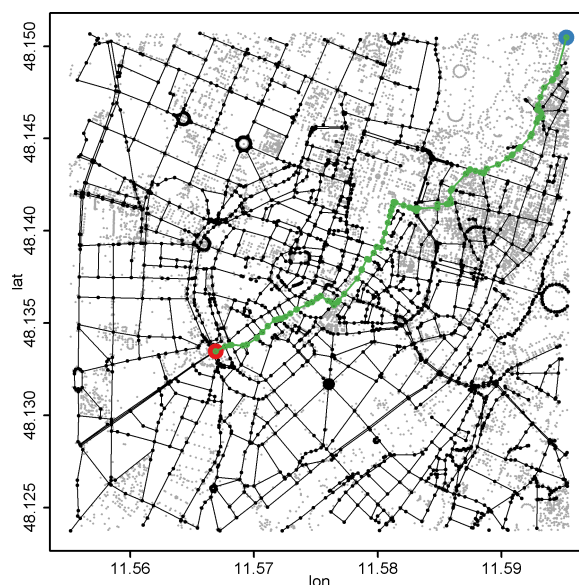


Figure 6: Shortest route on highway map of Munich center.

Route details. In order to present route details like street names, distances, and directions we have to work directly on the internals of the `osmar` objects.

We start by extracting the route's node IDs (which are in the correct order) and the way IDs (which we have to order) where the nodes are members:

```

> node_ids <- route_muc$nodes$attrs$id
> way_ids <- local({
+   w <- match(node_ids, route_muc$ways$refs$ref)
+   route_muc$ways$refs$id[w]
+ })

```

Then we extract the names of the ways in the correct order:

```
> way_names <- local({
+   n <- subset(route_muc$ways$tags, k == "name")
+   n[match(way_ids, n$id), "v"]
+ })
```

The next step is to extract the nodes' coordinates,

```
> node_coords <- route_muc$nodes$attrs[, c("lon", "lat")]
```

and to compute the distances (meters) and the bearings (degrees) between successive nodes (using the package **geosphere**):

```
> node_dirs <- local({
+   n <- nrow(node_coords)
+   from <- 1:(n-1)
+   to <- 2:n
+   cbind(dist = c(0,
+     distHaversine(node_coords[from, ], node_coords[to, ])),
+     bear = c(0,
+     bearing(node_coords[from, ],
+       node_coords[to, ])))
+ })
```

Finally, we pack together all the information, and additionally compute the cumulative distance and a 16-point compass rose direction (the `compass()` function is available in the "navigator" demo from the **osmar** package):

```
> route_details <- data.frame(way_names, node_dirs)
> route_details$cdist <- cumsum(route_details$dist)
> route_details$dir <- compass(route_details$bear)
```

The result is a `data.frame` with a row for each node of the route. The row shows the name of the associated way, the distance (meters) and bearing (degrees and compass rose) to the successive node of the route, and the cumulative distance:

```
> head(route_details)

      way_names dist bear cdist dir
1 Sendlinger-Tor-Platz    0    0    0  N
2      WallstraÃe    65   62   65 ENE
3 Herzog-Wilhelm-StraÃe   29   75   94 ENE
4      Oberanger    10   78  104 ENE
5      Oberanger    69   94  173  E
6 Nikolaus-Gradl-Weg    25   76  198 ENE
```

Needless to say that this navigation device can be made much more sophisticated. The **osmar** package contains the complete source code of the basic navigation device as a demo and we invite everybody to improve R as a navigator.

Summary

The **osmar** package extends the R ecosystem with infrastructure to work together with the OpenStreetMap project. So far, functionality is available to get data from different sources (e.g., planet file and API v0.6), to consolidate the data as an R **osmar** object, to work with the **osmar** object (e.g., subsetting and plotting), and to convert it to objects based on classes provided by other packages (e.g., to **igraph** and **sp** objects).

Future work includes the implementation of further converters; e.g., a converter from **osmar** objects to raster image objects via the **OpenStreetMap** package. We are also interested in implementing converters from objects provided by other R packages to **osmar** objects and in saving these objects in different OpenStreetMap sources via a `put_osm()` function. This would be, in fact, the completion of the **osmar** concept illustrated in Figure 1 with arrows from the right to the left blocks.

Furthermore, we would like to incorporate tools originated in the OpenStreetMap ecosystem. One idea is the implementation of a rule-based rendering tool for generating SVG images of OSM data along the lines of **Osmarender** (Topf, 2011). Another interesting project is **Osmium**, a fast and flexible

C++ and Javascript toolkit and framework for working with OSM data (Topf, 2012). An R interface (potentially via **Rcpp** modules; Eddelbuettel and François, 2011) would provide a very fast and flexible way to work with large OSM data sets.

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