

A GUIDed tour of Bayesian regression

by *Andrés Ramírez-Hassan and Mateo Graciano-Londoño*

Abstract This paper presents a graphical user interface (GUI) to carry out a Bayesian regression analysis in a very friendly environment without any programming skills (drag and drop). This paper is designed for teaching and applied purposes at an introductory level. Our GUI is based on an interactive web application using shiny, and libraries from R. We carry out some applications to highlight the potential of our GUI for applied researchers and practitioners. In addition, the Help option in the main tap panel has an extended version of this paper, where we present the basic theory underlying all regression models that we developed in our GUI, and more applications associated with each model.

Introduction

The main objective of this paper is to present an open source teaching graphical user interface (GUI) to implement Bayesian regression analysis using cross sectional and longitudinal data.¹ We present a tutorial for implementing these models in our GUI, and some applications. The Help option in the main tap panel exhibits an extended version of this paper where users can find more applications and the basic theory foundations of each model in our GUI. Therefore, practitioners and applied researchers can apply Bayesian regression analysis understanding its theoretical foundation without requiring programming skills. The latter seems to be a significant impediment to increasing the use of the Bayesian framework (Woodward, 2005; Karabatsos, 2016).

Table 1 shows the available graphical user interfaces for carrying out Bayesian regression analysis. ShinyStan (Stan Development Team, 2017) is a very flexible open source program, but users are required to have some programming skills. BugsXLA (Woodward, 2005) is open source, but less flexible. However, users do not need to have programming skills. Bayesian regression: Nonparametric and parametric models (Karabatsos, 2016) is a very flexible and friendly GUI that is based on MATLAB Compiler for a 64-bit Windows computer. Its focus is on Bayesian nonparametric regressions, and it can be thought of for users who have mastered basic parametric models, such as the ones that we show in our GUI. On the other hand, MATLAB toolkit, Stata and BayES are not open source.

We developed our GUI based on an interactive web application using shiny (Chang, 2018), and some libraries in R (R Core Team, 2018). The specific libraries and commands that are used in our GUI can be seen in Table 2. It has nine univariate models, four multivariate, three hierarchical longitudinal, Bayesian bootstrap, and six Bayesian model averaging frameworks. In addition, it gives basic summaries and diagnostics of the posterior chains, as well as the posterior chains themselves, and different plots, such as trace, autocorrelation and densities. In terms of its flexibility and possibilities, our GUI lies between ShinyStan and BugsXLA: users are not required to have any programming skills, but it is not as advanced as Karabatsos (2016)'s software. However, our GUI can be run in any operating system. Our GUI, which we call BESmarter,² is freely available at <https://github.com/besmarter/BSTApp>; so users have access to all our code and datasets.

After this brief introduction, we present in Section **Using BESmarter** our GUI, and how to use it. Section **Applications** presents some empirical examples to illustrate the potential use of our GUI. Lastly, Section **Concluding remarks** presents some conclusions and future developments.

Using BESmarter

Simulated and applied datasets are in the folders *DataSim* (see Table 3 for details), and *DataApp* (see Table 4 for details), respectively. The former folder also includes the files that were used to simulate different processes, so, the population parameters are available, and as a consequence these files can be used as a pedagogical tool to show some statistical properties of the inferential frameworks available in our GUI. The latter folder contains the datasets used in our applications in Section **Applications**.

¹We used instrumental variables to identify causal effects when there are endogeneity issues in linear regression. This is a very common approach among econometricians in this situation. Otherwise, all regression approaches presented here are well known by statisticians.

²Bayesian econometrics: Simulations, models and applications to research, teaching and encoding with responsibility.

Users should use these datasets as templates as a guide to the structure of their own datasets. Simply type `shiny::runGitHub("besmarter/BSTApp", launch.browser=T)` in the R package console or any R code editor to run our GUI.³

After this, users can see a new window where a presentation of our research team is displayed. In addition, the top panel in Figure 1 shows the class of models that can be estimated in our GUI.

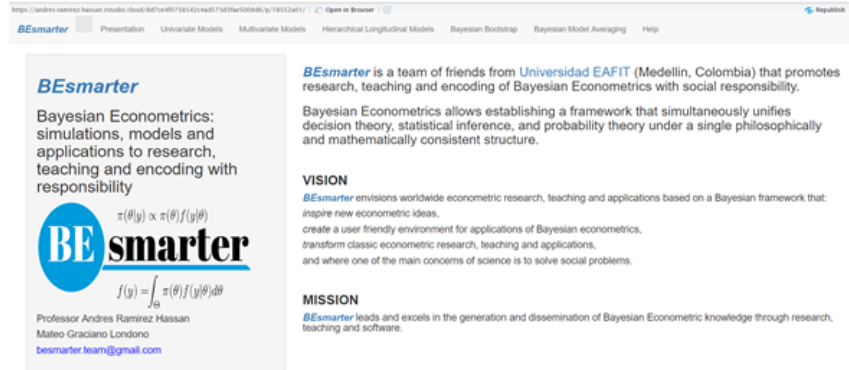


Figure 1: BESmarter GUI

The selection indicates univariate models in that the radio button on the left hand side shows the specific models inside this generic class. In particular, users can see that the normal model is selected from inside the class of univariate models. See Figure 2.

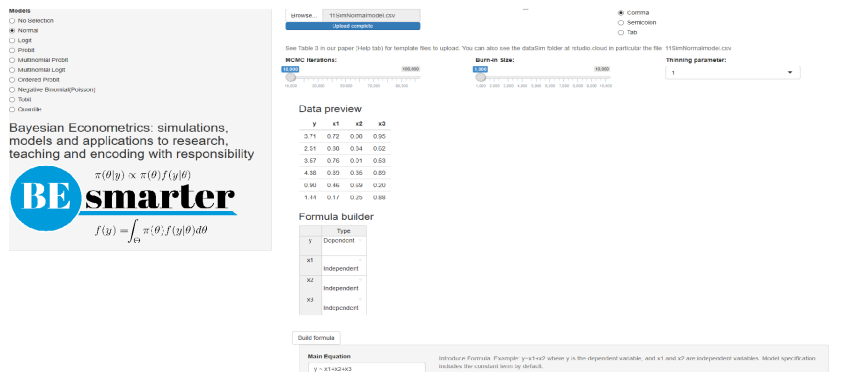


Figure 2: Univariate models: Specification

Then, the right hand side panel displays a widget to upload the input dataset, which should be a csv file with headers in the first row. Users also should select the kind of separator used in the input file: comma, semicolon, or tab (use the folders *DataSim* and *DataApp* for the input file templates). Once users upload the dataset, they can see a *Data preview*. Range sliders help to set the number of iterations of the MCMC and the amount of burn-in, and the thinning parameter can be selected as well (see online paper in Help tab for technical details). After this, users should specify the equation. This can be done with the formula builder, where users can select the dependent variable, and the independent variables, and then click on the "Build formula" tab. Users can see in the "Main Equation" space the formula expressed in the format used by R (see Main equation box in Figure 2, $y \sim x1 + x2 + x3$). Users can modify this if necessary, for instance, including higher order or interaction terms, other transformation are also allowed. This is done directly in the "Main Equation" space taking into account that this extra terms should follow formula command structure (see <https://www.rdocumentation.org/packages/stats/versions/3.6.2/topics/formula>). Note that the class of univariate models includes the intercept by default, except ordered probit, where the specification has to do this explicitly, that is, ordered probit models do not admit an intercept, for identification issues. Hence, users should write down specifically this fact ($y \sim x1 + x2 + x3 - 1$). Finally, users should define the hyperparameters of the prior; for instance, in the normal-inverse

³We strongly recommend to type this directly, rather than copy and paste. This is due to an issue with the quotation mark.

gamma model, these are the mean, covariance, shape, and scale (see Figure 3). However, users should take into account that our GUI has "non-informative" hyperparameters by default in all our modelling frameworks, so the last part is not a requirement.

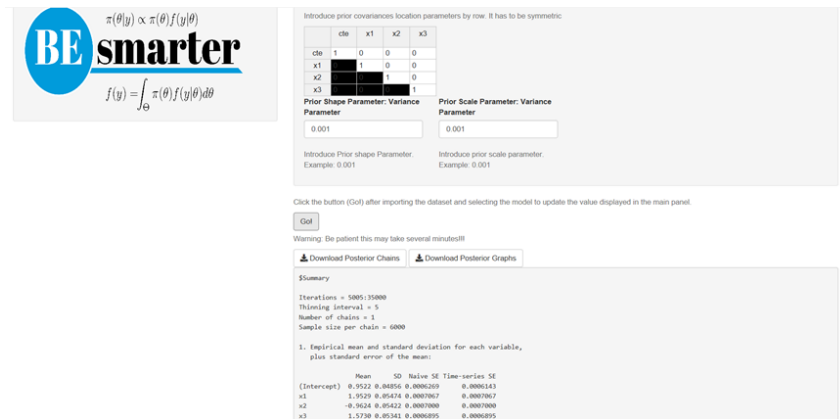


Figure 3: Univariate models: Results

After this specification process, users should click the Go! button to initiate the estimation. Our GUI displays the summary statistics and convergence diagnostics after this process is finished (see Figure 3). There are also widgets to download posterior chains (csv file) and graphs (pdf and eps files). Note that the order of the coefficients in the results (summary, posterior chains, and graphs) is first for the location parameters, and then for the scale parameters.

Multinomial models (probit and logit) require a dataset file to have in the first column the dependent variable, then alternative specific regressors (for instance alternatives' prices), and finally, non-alternative regressors (for instance, income). The formula builder specifies the dependent variable, and independent variables that are alternative specific and non-alternative specific. Specification also requires defining the base category, number of alternatives (this is also required in ordered probit), number of alternative specific regressors, and number of non-alternative regressors (see Figure 4). Multinomial logit also allows defining a tuning parameter, the number of degrees of freedom in this case, for the Metropolis–Hastings algorithm (see online paper in Help tab for technical details). This is a feature in our GUI when the estimation of the models is based on the Metropolis–Hastings algorithm. The order of the coefficients in the results of these models is first the intercepts (cte_l appearing in the summary display, l -th alternative), and then the non-alternative specific regressors (NAS_{jl} appearing in the summary display, l -th alternative and j -th non-alternative regressor), and lastly, the coefficients for the alternative specific regressors (AS_j appearing in the summary display, j -th alternative specific regressor). Note that the non-alternative specific regressors associated with the base category are equal to zero (they do not appear in the results). In addition, some coefficients of the main diagonal of the covariance matrix are constant due to identification issues in multinomial and multivariate probit models.

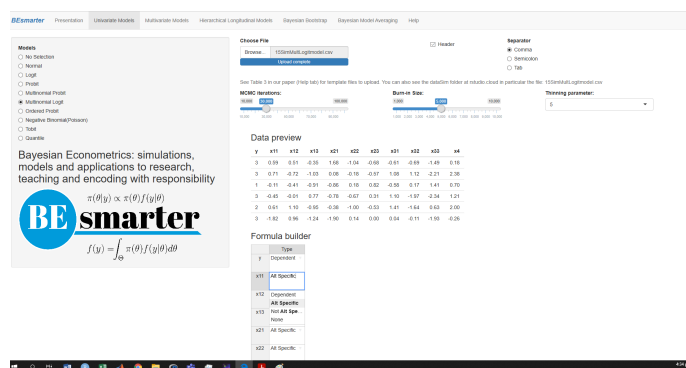


Figure 4: Univariate models: Multinomial

In the case of the negative binomial model, users should set a dispersion parameter (α , see the negative binomial model). User should also set the censorship points and quantiles in the Tobit and

quantile models, respectively.

Figure 5 displays the multivariate regression setting. In this case, the input file should have first the dependent variables, and then the regressors. If there are intercepts in each equation, there should be a column of 1's after the dependent variables in the input file. The user also has to set the number of dependent variables, the number of regressors, if necessary include the intercept, and the values of the hyperparameters (see Figure 5).

BEsmarter
Bayesian Econometrics:
simulations, models and
applications to research,
teaching and encoding with
responsibility

$$\pi(\theta|y) \propto \pi(\theta)f(y|\theta)$$

$$f(y) = \int_{\theta} \pi(\theta)f(y|\theta)d\theta$$

Choose File
Browse... 21SimMultivariate.csv
Upload console

☒ Header
Separator
Comma
Semicolon
Tab

MCMC Iterations: 100,000
Burn-in Size: 5,000
Thinning parameter: 10

Data set should have first endogenous variables by columns starting at first column, then exogenous variables. If it is required, you should include explicitly an intercept, that is, a column with 1's in your data set.

Number Endogenous Variables: m: 2
Integer indicating number of endogenous variables. Example: 2

Number Exogenous Variables: k: 3
Integer indicating number of exogenous variables. Example: 3

Prior mean matrix (k x m): Introduce prior mean location parameters. Each equation per column.

y1	y2
0.000	0.000
0.000	0.000
0.000	0.000

Prior covariance matrix (k x k): Introduce prior covariance matrix. It should be symmetric positive semidefinite.

Beta1	Beta2	Beta3
100	0	0

Figure 5: Multivariate models: Simple multivariate

The input file in seemingly unrelated regressions should have first the dependent variables, and then the regressors by equation, including the intercept in each equation if necessary (column of 1's). Users should define the number of dependent variables (equations), the number of total regressors, that is, the sum of all regressors associated with the equation (if necessary include intercepts, each intercept is an additional regressor), and the number of regressors by equation (if necessary include the intercept). Users can also set the values of the hyperparameters if there is prior information.

The results of the simple multivariate and seemingly unrelated regressions show first the posterior location parameters by equation, and then the posterior covariance matrix.

In the instrumental variable setting, users should specify the main equation and the instrumental equation. This setting includes intercepts by default. The first variable on the right hand side in the main equation has to be the variable with endogeneity issues. In the instrumental equation box, the dependent variable is the variable with endogeneity issues as a function of the instruments. Users can also specify the values of the hyperparameters if they have prior information. The input file should have the dependent variable, the endogenous regressor, the instruments, and the exogenous regressors. The results first list the posterior estimates of the endogenous regressor, then the location parameters of the auxiliary regression (instrumental equation), and the location parameters of the exogenous regressors. Last is the posterior covariance matrix.

BEsmarter
Bayesian Econometrics:
simulations, models and
applications to research,
teaching and encoding with
responsibility

$$\pi(\theta|y) \propto \pi(\theta)f(y|\theta)$$

$$f(y) = \int_{\theta} \pi(\theta)f(y|\theta)d\theta$$

Choose File
Browse... 24SimMultProbit.csv
Upload console

☒ Header
Separator
Comma
Semicolon
Tab

MCMC Iterations: 100,000
Burn-in Size: 5,000
Thinning parameter: 10

Data set has to be organized by individual. First column should be individual identifier, then endogenous variable, and then exogenous variables. If it is required, you should include explicitly an intercept, that is, a column with 1's in your data set.

Number of Individuals: n: 5000
Integer indicating number of individuals. Example: 500

Number of Exogenous Variables: k: 4
Integer indicating number of exogenous variables. Example: 3

Number of choices: L: 2
Integer indicating number of choices. Example: 2

Introduce prior mean vector location parameters

y1	y2
0.000	0.000
0.000	0.000
0.000	0.000
0.000	0.000

Introduce prior covariances location parameters. It has to be symmetric

Beta11	Beta12	Beta13	Beta14	Beta21	Beta22	Beta23	Beta24
100	0	0	0	0	0	0	0

Working on it. Running MCMC sampling

Figure 6: Multivariate models: Multivariate probit

The multivariate probit model requires an input dataset ordered by unit, for instance three choices implies repeat each unit three times. The first column has to be the identification of each unit; users should use ordered integers, then the dependent variable, just one vector, composed of 0's and 1's, then the regressors, which should include a column of 1's for the intercepts. Users should set the number of units, number of regressors, and number of choices (see Figure 6). The results first display the posterior location parameters by equation, and then the posterior covariance matrix.

The input files for hierarchical longitudinal models should have first the dependent variable, then the regressors and a cross sectional identifier ($i = 1, 2, \dots, m$). It is not a requirement to have a balanced dataset: n_i can be different for each i . Users should specify the fixed part equation and the random part equation, both in R format. In case of only requiring random intercepts, do not introduce anything in the latter part (see Figure 7). Users should also type the name of the cross sectional identifier variable. The results displayed and the posterior graphs are associated with the fixed effects and covariance matrix. However, users can download the posterior chains of all posterior estimates: fixed and random effects, and covariance matrix.

The screenshot shows the 'Hierarchical Longitudinal Models' tab in the BEsmarter application. On the left is a sidebar with the BEsmarter logo and a description: 'Bayesian Econometrics: simulations, models and applications to research, teaching and encoding with responsibility'. The main area contains several input fields:

- Choose File:** A file browser showing '31SimLongitudinalNormal.csv'.
- MCMC Iterations:** A slider set to 10,000.
- Burn-in Size:** A slider set to 5,000.
- Thinning parameter:** A dropdown menu set to 5.
- Main Equation: Fixed Effects:** A text input with 'y~x1+x2'.
- Main Equation: Random Effects:** A text input with 'x3+x4'.
- Name of grouping variable:** A text input with 'species'.
- Prior mean:** A table with columns 'cte', 'x1', 'x2' and rows 'cte', 'x1', 'x2'.
- Prior covariance matrix:** A table with columns 'cte', 'x1', 'x2' and rows 'cte', 'x1', 'x2'.

Figure 7: Hierarchical longitudinal models: Specification

Bayesian bootstrap only requires uploading a dataset, specifying the number of iterations of the MCMC, the resampling size, and the equation (see Figure 8). The input file has the same structure as the file used in the univariate normal model.

The screenshot shows the 'Bayesian Bootstrap' tab in the BEsmarter application. The layout is similar to Figure 7, but with additional features:

- Choose File:** A file browser showing '41SimBootstrapmodel.csv'.
- MCMC Iterations:** A slider set to 10,000.
- Resampling Size:** A slider set to 5,000.
- Data preview:** A table showing a sample of the data with columns 'y', 'x1', 'x2', 'x3'.
- Formula builder:** A table with columns 'Type' and 'Variable'.

Figure 8: Bayesian bootstrap: Specification

Bayesian model averaging based on a Gaussian distribution can be carried out using the Bayesian information criterion (BIC) approximation, Markov chain Monte Carlo model composition (MC3), or instrumental variables (see Figure 9). The former two approaches require an input dataset where the first column is the dependent variable, and then, the potentially important regressors. Users should set the band width model selection parameter (O_R) and number of iterations for BIC and MC3, respectively. The results include the posterior inclusion probability ($p! = 0$), expected value (EV), and standard deviation (SD) of the coefficients associated with each regressor. The BIC framework also displays the most relevant models, including the number of regressors, the coefficient of determination (R^2), the BIC, and the posterior model probability. Users can download two csv files: *Best models* and *Descriptive statistics coefficients*. The former is a 0-1 matrix such that the columns are the regressors

and the rows are the models; a 1 indicates the presence of a specific regressor in a specific model, 0 otherwise. Note that the last column of this file is the posterior model probability for each model (row). The latter file shows the posterior inclusion probabilities, expected values, and standard deviations associated with each regressor, taking into account the BMA procedure based on the best models.

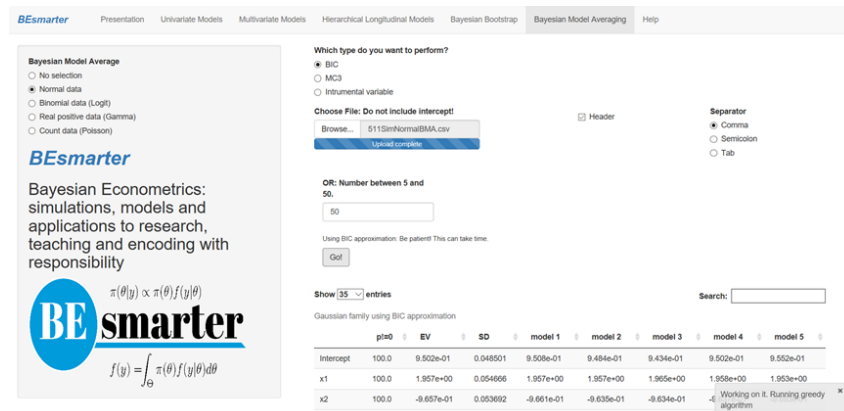


Figure 9: Bayesian model averaging: Specification and results

Bayesian model averaging with endogeneity issues requires two input files. The first one has the dependent variable in the first column, the next columns are the regressors with endogeneity issues, and then the exogenous regressors. The user should include a column of 1's if an intercept is required. The second input file has all the instruments. Users should also introduce the number of regressors with endogeneity issues (see Figure 10).

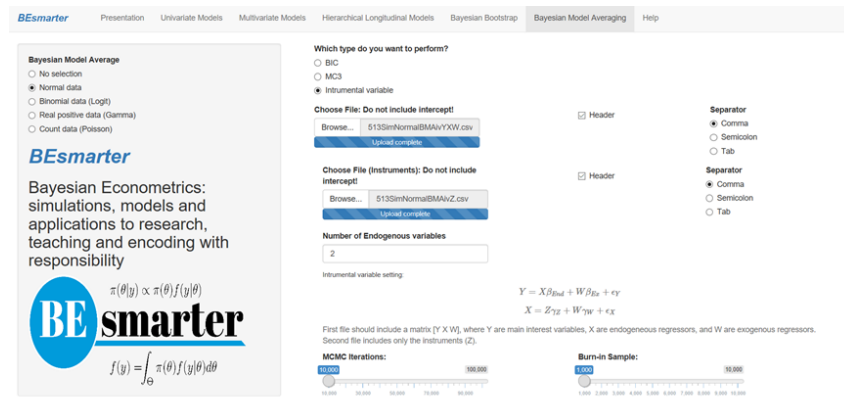


Figure 10: Bayesian model averaging: Instrumental variable specification

The results include the posterior inclusion probabilities and expected values for each regressor. The user can find the results of the main equation, and then of the auxiliary equations. Users can download csv files of BMA results for both the second stage (main equation) and the first stage (auxiliary equations). In addition, users can download the posterior chains of the location parameters of the main equation, β_l , $l = 1, 2, \dots, \dim\{\beta\}$, the location parameters of the auxiliary equations, $\gamma_{j,i}$, $j = 1, 2, \dots, \dim\{\beta_s\}$ where $\dim\{\beta_s\}$ is the number of regressors with endogeneity issues, $i = 1, 2, \dots, \dim\{\gamma\}$, where $\dim\{\gamma\}$ is the number of regressors in the auxiliary regressors (exogenous regressors + instruments), and the elements of the covariance matrix $\sigma_{j,k}$ (see online paper in Help tab for technical details).

Bayesian model averaging based on BIC approximation for non-linear models, logit, gamma, and Poisson, requires an input dataset where the first column is the dependent variable, and the other columns are the potentially relevant regressors. Users should specify the band width model selection parameters, which are also referred to as Occam's window parameters (O_R and O_L). Our GUI displays the PIP ($p! = 0$), the expected value of the posterior coefficients (EV), and the standard deviation (SD). In addition, users can see the results associated with the models with the highest posterior model probabilities, and download csv files with the results of specifications of the best models, and

descriptive statistics of the posterior coefficients from the BMA procedure. These files are similar to the results of the BIC approximation of the Gaussian model.

User should also note that sometimes our GUI shuts down. In our experience, this is due to computational issues using the implicit commands that we call when estimating some models, for instance, computationally singular systems, missing values where TRUE/FALSE needed, L-BFGS-B needs finite values of "fn", NA/NaN/Inf values, or Error in backsolve. Sometimes these issues can be solved by adjusting the dataset, for instance, avoiding high levels of multicollinearity. In addition, users can identify these problems by checking the console of their rstudio cloud sections, where the specific folder/file where the issue happened is specified. In any case, we would appreciate your feedback to improve and enhance our GUI.

Applications

The main purpose of this section is to illustrate the potential of our GUI to carry out some applications. We encourage users to replicate these applications, as we do not display in figures most of the results, due to space limitations.⁴ In addition, there are technical aspects that are covered in the online paper in Help tab of our GUI.

Univariate models

Continuous response: The market value of soccer players in Europe

We use the dataset *1ValueFootballPlayers.csv*, which was provided by [Serna Rodríguez et al. \(2018\)](#), to find the determinants of high performance soccer players in the five most important national leagues in Europe.

The specification to enter in the main equation box is

$$\log(\text{Value}) \sim \text{Perf} + \text{Perf}^2 + \text{Age} + \text{Age}^2 + \text{NatTeam} + \text{Goals} + \text{Goals}^2 + \text{Exp} + \text{Exp}^2 + \text{Assists},$$

where Value is the market value in Euros (2017), Perf is a measure of performance, Age is the players' age in years, NatTeam is an indicator variable that takes the value of 1 if the player has been on the national team, Goals is the number of goals scored by the player during his career, Exp is his experience in years, and Assists is the number of assist made by the player in the 2015–2016 season. All variables followed by a 2 are squared variables.

We initially assume that there are no censorship problems, the effect of the regressors are the same through the support of the dependent variable, and the dependent variable obeys a normal distribution. So, we ran a normal-inverse gamma model using 30,000 MCMC iterations plus a burn-in equal to 5,000, and a thinning parameter equal to 1 using the default hyperparameters.

The results suggest that age, squared age, national team, goals, experience, and squared experience are relevant regressors. For instance, we found that the 2.5% and 97.5% percentiles of the posterior estimate associated with the variable Goals are 4.57e-03 and 1.82e-02. These values can be used to find the 95% symmetric credible interval. This means that there is a 0.95 probability that the population parameter lies in (4.57e-03, 1.82e-02), which would suggest that this variable is relevant to explain the market value of a soccer player.⁵ We also found that the effect of having been on the national team has a 95% credible interval equal to (0.58, 1.04) with a median equal to 0.81, that is, an increase of the market value of the player of 124.8% ($\exp(0.81) - 1$) compared with a player that has not ever been on a national team. The posterior distribution of this variable can be seen in Figure 11. This graph is automatically generated by our GUI, and can be downloaded in the zip file named *Posterior Graphs.csv*; but we should take into account that the national team is the sixth variable, remember that by default the intercept is the first variable.

A good advantage of the Bayesian framework is that we can easily calculate the posterior distribution of functions of the parameter estimates, for instance, the age that maximizes the market value

⁴Take into account that as inference in Bayesian models is based on simulation methods, results do not coincide 100%.

⁵Users should take into account that formal inference (hypothesis tests) in a Bayesian framework are based on Bayes factors.

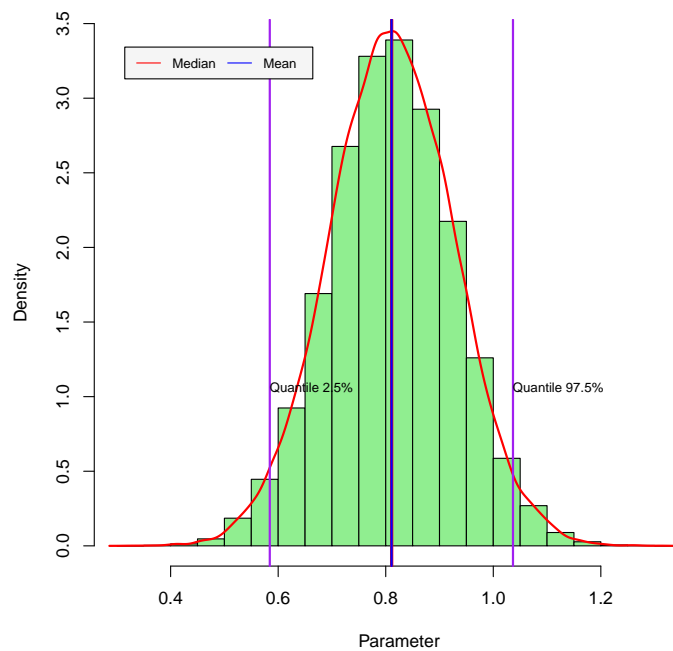


Figure 11: Posterior distribution: National team

of a soccer player, $\text{OptAge} = -\frac{\beta_{\text{Age}}}{2\beta_{\text{Age}^2}}$. We can estimate this using the posterior chains that can be downloaded from our GUI. This is in the file named *Posterior chains.csv*. We have that the mean value is equal to 24.31 years, and the 95% symmetric credible interval is (23.28, 25.36).

We can also see some convergence diagnostics from this application. In particular, the [Geweke \(1992\)](#) test indicates that there is no statistically significant difference at 5% between the first 10% of the posterior chains and the last 50% of the posterior chains. This is due to the fact that the absolute value of all the statistical tests are less than 1.96 (the value that defines the critical region in a normal distribution for a bilateral test at the 5% significance level). The [Raftery and Lewis \(1992\)](#) tests indicate dependence factors very close to 1 in all cases, and as a consequence lower than 5, which means a low level of autocorrelation of the posterior draws. Lastly, all the posterior chains passed the [Heidelberger and Welch \(1983\)](#) test, indicating that it seems that the posterior draws come from stationary distributions.

Let's assume that we only have the market value of soccer players whose value is greater than €1,000,000, which means that approximately 21.5% of our sample is censored. Estimating a normal-inverse gamma model without taking into account the censoring issue would mean inconsistent parameter estimates. For instance, we estimated a normal-inverse gamma model having as dependent variable $\log(\text{ValueCens})$, which is the censored dependent variable, using the same setting as the baseline framework. We found that age, squared age, national team, goals and experience are potentially relevant variables for predicting the market value, but this exercise suggests that squared experience is not relevant, a variable that was relevant in our previous estimation without censoring issues. Therefore, we estimated a Tobit model where $\log(\text{ValueCens})$ is the dependent variable, which is left censored at $\log(1,000,000) \approx 13.82$, with the same MCMC setting and hyperparameters as the baseline estimation. All convergence diagnostics seem good, and we got the same potentially relevant variables as in the baseline estimation, except for squared experience.

Now let's check if the marginal effects of the regressors are not constant over the support of the dependent variable. For instance, we want to check if the marginal effect of goals varies with the market value of the soccer player. So, we can estimate a Bayesian quantile regression. In particular, we estimated models at the 0.1, 0.5 (median) and 0.9 quantiles. We found that age, squared age, and national team are potentially relevant regressors to explain these quantiles. For instance, the age that maximizes the market value is approximately 24.5 years in all these three quantiles. However, goals is only relevant when we estimated the median model, which in general has better convergence diagnos-

tics and narrower credible intervals. Observe that experience is not relevant in quantile regressions, whereas this variable is relevant in mean regressions.

Lastly, we carried out a Bayesian bootstrap, which means that we did not assume any particular distribution for the dependent variable. In particular, we set 20,000 iterations with a resample size equal to 1,000. We used the same specification as in the normal-inverse gamma model.

The results show the posterior mean estimates, the highest posterior density credible intervals at 95%, and some percentiles that can be used to obtain the 95% symmetric credible interval. It seems that age, squared age, national team, goals, experience, and squared experience are statistically significant variables to explain the market value of a soccer player. Observe that these variables were also relevant in the normal-inverse gamma model. For instance, the highest density and symmetric credible intervals for national team are the same, (0.61, 1.08). This is also similar to the 95% credible interval using the normal-inverse gamma model. All convergence statistics seem good, which suggests that the posterior draws come from stationary distributions.

Binary response: Determinants of hospitalization in Medellín

We use the dataset named *2HealthMed.csv*, which was provided by [Ramírez Hassan et al. \(2013\)](#). Our dependent variable is a binary indicator with a value equal to 1 if an individual was hospitalized in 2007, and 0 otherwise.

The equation to enter in the main equation box is

$$\text{Hosp} \sim \text{SHI} + \text{Female} + \text{Age} + \text{Age}^2 + \text{Est2} + \text{Est3} + \text{Fair} + \text{Good} + \text{Excellent},$$

where SHI is a binary variable equal to 1 if the individual is in a subsidized health care program and 0 otherwise, Female is an indicator of gender, Age in years, Age² is squared age, Est2 and Est3 are indicators of socio-economic status, the reference is Est1, which is the lowest, and self perception of health status where bad is the reference.

We ran this application using a logit model with 30,000 MCMC iterations plus a burn-in equal to 10,000, a thinning parameter equal to 5, and a tuning parameter for the Metropolis–Hastings algorithm equal to 1.01. This implies an effective sample size equal to 6,000. It seems from our results that female and health status are relevant variables for hospitalization, as their 95% credible intervals do not cross 0. Women have a higher probability of being hospitalized than do men, and people with bad self perception of health condition also have a higher probability of being hospitalized. Observe that we can use the posterior chains, which can be downloaded from our GUI, to obtain the posterior distributions of the marginal effects without extra computational burden.

We also carried out this application using the probit model with the baseline setting of the logit model. We got the same results regarding potentially relevant predictors.⁶ However, the probit model does not require a tuning parameter in its MCMC algorithm, which in turn generates less autocorrelated chains.

Multivariate models

Continuous responses: The effect of institutions on per capita GDP

To illustrate the potential of our GUI to estimate multivariate models, we used the dataset provided by [Acemoglu et al. \(2001\)](#), who analyzed the effect of property rights on economic growth.

First of all, we used the dataset *5Institutions.csv* to estimate the following set of equations:

$$\log(\text{pcGDP95}_i) = \pi_0 + \pi_1 \log(\text{Mort}_i) + \pi_2 \text{Africa} + \pi_3 \text{Asia} + \pi_4 \text{Other} + e_{1i}, \quad (1)$$

$$\text{PAER}_i = \gamma_0 + \gamma_1 \log(\text{Mort}_i) + e_{2i}, \quad (2)$$

where pcGDP95, PAER and Mort are the per capita GDP in 1995, the average index of protection against expropriation between 1985 and 1995, and the settler mortality rate during the time of colo-

⁶Remember that in this model our GUI displays the posterior results according to the order in the equation.

nization. Africa, Asia and Other are dummies for continents, with America as the baseline group.

As there are different sets of regressors in each equation, and we suspect there is correlation between the stochastic errors of these two equations, we should estimate a seemingly unrelated regressions (SUR) model.

We should take into account that there are two equations: the first one has five regressors, including the intercept, and the second equation has two regressors (intercept plus the mortality rate). We used default values for the hyperparameters, this implies “vague” prior information, and hence an “objective” Bayesian approach.

We set 10,000 MCMC iterations plus 1,000 burn-in iterations, and a thinning parameter equal to 1. It seems that this setting gives posterior chains that converge to stationary distributions. All stationary tests do not reject the null hypothesis of “stationarity,” and the mixing properties look good (dependence factors close to 1, autocorrelation and trace plots seem to indicate no autocorrelation).

The most important parameters are the effect of the mortality rate on gross domestic product and property rights. Their 95% credible intervals are (-0.67, -0.29) and (-0.85, -0.35), respectively (second and seventh parameters). This suggests that the settler mortality rate during the time of colonization is negatively associated with economic growth and property rights. In addition, the 95% credible interval of the covariance between the stochastic errors of these two equations is (0.33, 0.88), which suggests that there is statistically significant evidence of correlation between the equations.

The previous set of equations can be considered as a restricted reduced form system, where the coefficients of the continents are set equal to 0 in the property rights equation. We can think in the following system of structural equations as producing the previous, but unrestricted, reduced form system,

$$\log(\text{pcGDP95}_i) = \beta_0 + \beta_1 \text{PAER}_i + \beta_2 \text{Africa} + \beta_3 \text{Asia} + \beta_4 \text{Other} + u_{1i}, \quad (3)$$

$$\text{PAER}_i = \alpha_0 + \alpha_1 \log(\text{pcGDP95}_i) + \alpha_2 \log(\text{Mort}_i) + u_{2i}. \quad (4)$$

We used the file *4Institutions.csv*, which has the structure to estimate multivariate Bayesian regressions using our GUI, to identify the causal effect of property rights on per capita GDP. In particular, we use the same MCMC and hyperparameters setting as in the previous exercise to obtain the posterior estimates of the reduced system without imposing zero restrictions of the effect of continents on property rights. The structural parameter β_1 is equal to π_1/γ_1 .⁷ We used the posterior draws automatically generated by our GUI to obtain the posterior chain of this structural parameter, which are the causal effects that [Acemoglu et al. \(2001\)](#) wanted to identify. The 95% credible interval is (0.56, 2.93), the posterior mean value is 1.12, and the median value is 0.98. If we estimate a multivariate system without taking into account the dummy variables associated with the continents, the causal effect has a 95% credible interval (0.68, 1.43) with posterior mean and median values equal to 0.94 and 0.97, respectively. Observe that the length of the second interval is shorter than the first. This is because the dummy variables of the continents are not statistically relevant for the property rights equation. As a consequence, the former estimation is less efficient.

Observe that we also obtain the posterior draws of the covariance matrix of these two reduced form equations from our GUI. All the convergence diagnostics indicate that the posterior draws (location and scale parameters) seem to come from stationary distributions.

Another way to identify the causal effect of property rights on per capita GDP is using instrumental variables. Therefore, we used the file *6Institutions.csv* to estimate Equation 3 using the mortality rate as an instrument for property rights. The equation to enter in the main equation box is

$$\log \text{pcGDP95} \sim \text{PAER} + \text{Africa} + \text{Asia} + \text{Other},$$

⁷Substituting Equation 4 into Equation 3 and comparing with Equation 1 yields $\pi_1 = \frac{\beta_1 \alpha_2}{1 - \beta_1 \alpha_1}$. Solving for the PAER as a function of the exogenous regressors in the structural system, and comparing with Equation 2, yields $\gamma_1 = \frac{\alpha_2}{1 - \beta_1 \alpha_1}$. Observe one needs independent equations ($\beta_1 \alpha_1 \neq 1$), and the exclusion restriction ($\alpha_2 \neq 0$).

and the equation to enter in the instrumental equation box is

$$\text{PAER} \sim \log \text{Mort}.$$

We used 20,000 MCMC iterations plus a burn-in equal to 5,000, and a thinning parameter equal to 5. So, the effective length of the posterior draws is 4,000. Using the default hyperparameters, the 95% credible interval of the coefficient associated with the endogenous variable, which are the first to be displayed in our descriptive and diagnostic statistics, is (0.55, 1.21), and the mean value is equal to 0.82. So, this is the effect of property rights on per capita GDP. Our GUI display next the posterior results associated with the instrumental equation, there we obtained a 95% credible interval equal to (-0.83, -0.35) for the effect of the mortality rate on the property rights. This suggests that the instrument is not weak. Then, we obtained the posterior results for the exogenous regressors in the main equation, which suggest that Africa and Asia dummies variables have negative effects on per capita GDP. Finally, we got the posterior estimates for the covariance matrix, which suggest that there is a negative covariance between the GDP equation and PAER equation, the 95% credible interval is (-1.50, -0.26).

All posterior draws seem to come from stationary distributions. However, there are high levels of autocorrelation in some posterior chains, as suggested by the dependence factors and posterior plots.

Hierarchical longitudinal models

Normal model: The relation between productivity and public investment

We used the dataset named *8PublicCap.csv* used by [Ramírez Hassan \(2017\)](#) to analyze the relation between public investment and gross state product in the setting of a spatial panel dataset consisting of 48 US states from 1970 to 1986. In particular, the specification to type into the main equation box of fixed effects is

$$\log(\text{gsp}) \sim \log(\text{pcap}) + \log(\text{pc}) + \log(\text{emp}) + \text{unemp},$$

where gsp is the gross state product, pcap is public capital, and pc is private capital all in US\$, emp is employment (people), and unemp is the unemployment rate in percentage.

We left empty the main equation box of random effects as we assumed that the unobserved heterogeneity is not associated with any particular regressors. This means that we control for the unobserved heterogeneity using just the constant terms. The variable which identifies the units is id.

We ran this application using 10,000 MCMC iterations plus a burn-in equal to 5,000 iterations, and a thinning parameter equal to 1. We also used the default values for the hyperparameters of the prior distributions. It seems that all posterior draws come from stationary distributions, as suggested by the diagnostics and posterior plots.

The 95% symmetric credible intervals for public capital, private capital, employment, and unemployment, are (-2.54e-02, -2.06e-02), (2.92e-01, 2.96e-01), (7.62e-01, 7.67e-01) and (-5.47e-03, -5.31e-03), respectively. The posterior mean elasticity estimate of public capital to gsp is -0.023, that is, an increase by 1% in public capital means a 0.023% decrease in gross state product. The posterior mean estimates of private capital and employment elasticities are 0.294 and 0.765, respectively. In addition, a 1% increase in the unemployment rate means a decrease of 0.54% in gsp. It seems that all these variables are statistically relevant. In addition, the posterior mean estimates of the variance associated with the unobserved heterogeneity and stochastic errors are 1.06e-01 and 1.45e-03. We obtained the posterior chain of the proportion of the variance associated with the unobserved heterogeneity (see Figure 12). The 95% symmetric credible interval is (0.98, 0.99) for this proportion, that is, unobserved heterogeneity is very important to explain the total variability.

Bayesian model averaging

Continuous response: Determinants of export diversification

We used the dataset provided by [Jetter and Ramírez Hassan \(2015\)](#) to analyze the determinants of export diversification. The dataset named *10ExportDiversificationHHI.csv* contains information about 36 potential determinants of export diversification measured using the Herfindahl–Hirschman Index (avghhi) for 104 countries (see [Jetter and Ramírez Hassan \(2015\)](#) for details). This setting implies 68.7 billion models (2^{36}).

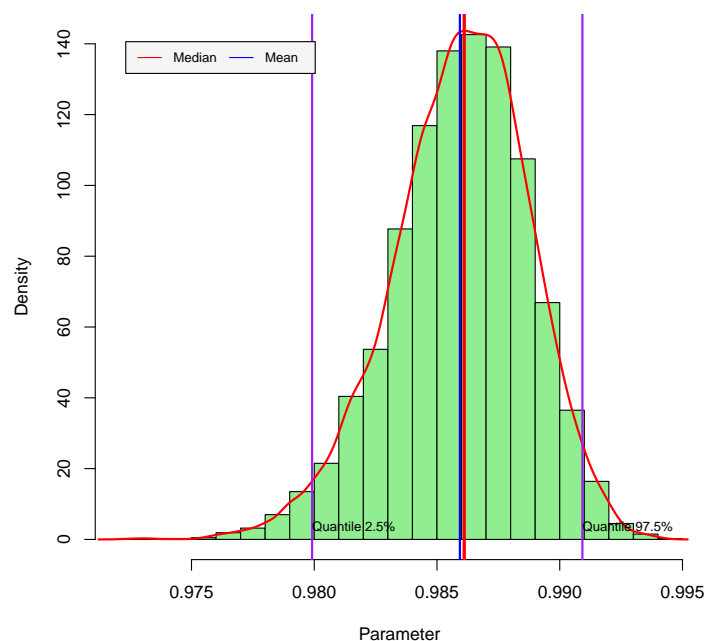


Figure 12: Posterior distribution: Proportion of variance associated with unobserved heterogeneity

We implemented three Bayesian model average (BMA) strategies: Bayesian information criterion approximation (BIC), Markov chain Monte Carlo model composition (MC^3), and instrumental variable (IVBMA). The former takes into account possible endogeneity between export diversification and gross domestic product.

Regarding BMA using the BIC approximation, we set 50 (default value) for OR. This parameter defines the number of best models to take into account in our BMA strategy. We obtained a table where we can see the posterior inclusion probability (PIP), expected value, standard deviation, and posterior mean estimates associated with the best models for each variable. The best models are defined using posterior model probabilities, which appear at the bottom of the table, where we also see the number of variables associated with each model as well as the coefficients of determination and BIC values. Our GUI also produces two csv files. The first one is *Best Models.csv*, where we have by row the best models, and the variables by columns, a 1 indicates the presence of the specific variable in the model's specification, and a 0 its absence. The last column in this file is the posterior model probability. The second one is *Descriptive Statistics.csv*, where we see the posterior inclusion probability, expected value, and standard deviation of each variable.

Following [Kass and Raftery \(1995\)](#)'s suggestions, we found that there is very strong evidence that being a former colony of Portugal, the total net primary enrollment, and the total natural resources rents as percentage of GDP are determinants of export diversification. Their expected values are 0.15, -0.006 and 0.008, respectively, which means that there are negative effects of having been a colony of Portugal and of having natural resources on export diversification. Recall that higher values of HHI indicate less diversification.

We also ran this application using the MC^3 strategy with 10,000 MCMC iterations. We got results similar to those with the BIC approximation.

We estimated an instrumental variable BMA to take into account possible endogeneity between export diversification and GDP using 20,000 MCMC iterations plus a burn-in equal to 5,000, where there is one endogenous variable (GDP). In particular, we used the files *11ExportDiversificationHHI.csv* and *12ExportDiversificationHHIInstr.csv*. The first file has the dependent variable in the first column (avhghi) followed by the endogenous variable (avgldpcap), the constant term (a column of 1's) and exogenous regressors. The second file has the instrumental variables, which are geographical, cultural,

and colonial factors.

Our GUI displays first the outcomes of the second stage equation (main equation), and then, the first stage equation (instrumental equation). We can download three csv files: *BMA Results First Stage.csv*, *BMA Results Second Stage.csv* and *Posterior chains.csv*. The first two files have the same structure: posterior inclusion probabilities and expected values. We can see from these files that educational levels and governance performance are the most important variables to foster gross domestic product (PIP=100), primary enrollment fosters export diversification (PIP=79.5), whereas natural resources discourages it (PIP=97.1). The latter file has the posterior draws where the name *beta* is associated with the variables in the main equation (second stage), and *gamma* is associated with the instrumental variable equation (first stage). Lastly, we have the posterior draws of the covariance matrix of the stochastic errors in the first and second stage equations. We have a 95% symmetric credible interval equal to (-0.014, 0.024), suggesting that there are no endogeneity issues.

Concluding remarks

The Bayesian statistical framework has become very popular among scientists since the computational revolution in the 1990's. In particular, computationally burdensome procedures such as Markov chain Monte Carlo algorithms can be easily implemented nowadays. However, most of the open source software to apply these procedures requires programming skills. This may be one reason why the Bayesian framework is not very popular among applied researchers and practitioners. In this paper, we introduced a graphical user interface to implement Bayesian regression analysis under different frameworks, explaining the basic theory, so that users can understand the basic principles of Bayesian statistics and apply them easily. Our objective has been to increase the popularity of the Bayesian statistical framework among applied researchers and practitioners.

Table 1: Graphical user interfaces to perform Bayesian regression analysis.

Name	Language	Models	Open source
ShinyStan	R+Stan	MCMC Implementation*	Yes
Bayesian regression: NP&P	MATLAB Compiler	Bayesian infinite-mixture regression Bayesian normal regression Hierarchical linear regression Binary regression Ordered regression Censoring regression Quantile regression Survival regression Density estimation Variable selection (spike-and-slab)	Yes
BugsXLA	OpenBUGS + Excel	Normal linear models GLM: Binomial GLM: Poisson GLM: Survival GLM: Multivariate categorical data Normal linear mixed Generalized linear mixed Bayesian variable selection Robust models	Yes
MATLAB toolkit: E&E⁺	MATLAB	Linear Regression Regression with non-spherical errors Regime switch regression Regression with restricted parameters Seemingly unrelated regression (SUR) Vector Autoregression (VAR) Instrumental variable Probit and logit Tobit Model Panel Data Analysis Stochastic search variable selection Highest posterior density (HPD) region Marginal likelihood of linear regression	No
Stata	Stata	MCMC implementation*	No
BayES	C++	Simple linear model Random-effects Random-coefficients Stochastic frontiers Inefficiency-effects Random-effects stochastic frontiers Dynamic stochastic frontier Probit and logit Random-effects probit and logit Multinomial probit and logit Ordered probit and logit Poisson and negative-binomial Type I Tobit Type II Tobit Seemingly unrelated regressions (SUR) Vector Autoregressive (VAR)	No

*User should define prior and likelihood.

⁺Toolkit on econometrics and economics teaching.

Table 2: Libraries and commands in BEsmarter GUI.

Univariate models			
Model	Library	Command	Reference
Normal	MCMCpack	MCMCregress	Martin et al. (2018)
Logit	MCMCpack	MCMClogit	Martin et al. (2018)
Probit	bayesm	rbprobitGibbs	Rossi (2017)
Multinomial(Mixed) Probit	bayesm	rmnpGibbs	Rossi (2017)
Multinomial(Mixed) Logit	bayesm	rmnlIndepMetrop	Rossi (2017)
Ordered Probit	bayesm	rordprobitGibbs	Rossi (2017)
Negative Binomial(Poisson)	bayesm	rnegbinRw	Rossi (2017)
Tobit	MCMCpack	MCMCtobit	Martin et al. (2018)
Quantile	MCMCpack	MCMCquantreg	Martin et al. (2018)
Multivariate models			
Model	Library	Command	Reference
Multivariate	bayesm	rmultireg	Rossi (2017)
Seemingly Unrelated Regression	bayesm	rsurGibbs	Rossi (2017)
Instrumental Variable	bayesm	rivGibbs	Rossi (2017)
Bivariate Probit	bayesm	rmvpGibbs	Rossi (2017)
Hierarchical longitudinal models			
Model	Library	Command	Reference
Normal	MCMCpack	MCMChregress	Martin et al. (2018)
Logit	MCMCpack	MCMChlogit	Martin et al. (2018)
Poisson	MCMCpack	MCMChpoisson	Martin et al. (2018)
Bayesian Bootstrap			
Model	Library	Command	Reference
Bayesian bootstrap	bayesboot	bayesboot	Baath (2018)
Bayesian model averaging			
Model	Library	Command	Reference
Normal (BIC)	BMA	bic.glm	Raftery et al. (2012)
Normal (MC ³)	BMA	MC3.REG	Raftery et al. (2012)
Normal (instrumental variables)	ivbma	ivbma	Lenkoski et al. (2013)
Logit (BIC)	BMA	bic.glm	Raftery et al. (2012)
Gamma (BIC)	BMA	bic.glm	Raftery et al. (2012)
Poisson (BIC)	BMA	bic.glm	Raftery et al. (2012)
Diagnostics			
Diagnostic	Library	Command	Reference
Trace plot	coda	traceplot	Plummer et al. (2016)
Autocorrelation plot	coda	autocorr.plot	Plummer et al. (2016)
Geweke test	coda	geweke.diag	Plummer et al. (2016)
Raftery & Lewis test	coda	raftery.diag	Plummer et al. (2016)
Heidelberger & Welch test	coda	heidel.diag	Plummer et al. (2016)

Table 3: Data sets templates in folder *DataSim*.

Univariate models		
Model	Data set file	Data set simulation
Normal	11SimNormalmodel.csv	11SimNormal.R
Logit	12SimLogitmodel.csv	12SimLogit
Probit	13SimProbitmodel.csv	13SimProbit.R
Multinomial(Mixed) Probit	14SimMultProbitmodel.csv	14SimMultinomialProbit.R
Multinomial(Mixed) Logit	15SimMultLogitmodel.csv	15SimMultinomialLogit.R
Ordered Probit	16SimOrderedProbitmodel.csv	16SimOrderedProbit.R
Negative Binomial(Poisson)	17SimNegBinmodel.csv	17SimNegBin.R
Tobit	18SimTobitmodel.csv	18SimTobit.R
Quantile	19SimQuantilemodel.csv	19SimQuantile.R
Multivariate models		
Model	Data set file	Data set simulation
Multivariate	21SimMultivariate.csv	21SimMultReg.R
Seemingly Unrelated Regression	22SimSUR.csv	22SimSUR.R
Instrumental Variable	23SimIV.csv	23SimIV.R
Bivariate Probit	24SimMultProbit.csv	24SimMultProbit.R
Hierarchical longitudinal models		
Model	Data set file	Data set simulation
Normal	31SimLogitudinalNormal.csv	31SimLogitudinalNormal.R
Logit	32SimLogitudinalLogit.csv	32SimLogitudinalLogit.R
Poisson	33SimLogitudinalPoisson.csv	33SimLogitudinalPoisson.R
Bayesian Bootstrap		
Model	Data set file	Data set simulation
Bayesian bootstrap	41SimBootstrapmodel.csv	41SimBootstrapmodel.R
Bayesian model averaging		
Model	Data set file	Data set simulation
Normal (BIC)	511SimNormalBMA.csv	511SimNormalBMA.R
Normal (MC ³)	512SimNormalBMA.csv	512SimNormalBMA.R
Normal (instrumental variables)	513SimNormalBMAivYXW.csv	513SimNormalBMAiv.R
	513SimNormalBMAivZ.csv	
Logit (BIC)	52SimLogitBMA.csv	52SimLogitBMA.R
Gamma (BIC)	53SimGammaBMA.csv	53SimGammaBMA.R
Poisson (BIC)	53SimPoissonBMA.csv	53SimPoissonBMA.R

Table 4: Real data sets in folder *DataApp*.

Univariate models		
Model	Data set file	Dependent variable
Normal	1ValueFootballPlayers.csv	log(Value)
Logit	2HealthMed.csv	Hosp
Probit	2HealthMed.csv	Hosp
Multinomial(Mixed) Probit	Fishing.csv	mode
Multinomial(Mixed) Logit	Fishing.csv	mode
Ordered Probit	2HealthMed.csv	MedVisPrevOr
Negative Binomial(Poisson)	2HealthMed.csv	MedVisPrev
Tobit	1ValueFootballPlayers.csv	log(ValueCens)
Quantile	1ValueFootballPlayers.csv	log(Value)
Multivariate models		
Model	Data set file	Dependent variable
Multivariate	4Institutions.csv	logpcGDP95 and PAER
Seemingly Unrelated Regression	5Institutions.csv	logpcGDP95 and PAER
Instrumental Variable	6Institutions.csv	logpcGDP95 and PAER
Bivariate Probit	7HealthMed.csv	$y = [\text{Hosp SHI}]'$
Hierarchical longitudinal models		
Model	Data set file	Dependent variable
Normal	8PublicCap.csv	log(gsp)
Logit	9VisitDoc.csv	DocVis
Poisson	9VisitDoc.csv	DocNum
Bayesian Bootstrap		
Model	Data set file	Dependent variable
Bayesian bootstrap	1ValueFootballPlayers.csv	log(Value)
Bayesian model averaging		
Model	Data set file	Dependent variable
Normal (BIC)	10ExportDiversificationHHI.csv	avghhi
Normal (MC ³)	10ExportDiversificationHHI.csv	avghhi
Normal (instrumental variables)	11ExportDiversificationHHI.csv	avghhi and avglgdpcap
	12ExportDiversificationHHIInstr.csv	
Logit (BIC)	13InternetMed.csv	internet
Gamma (BIC)	14ValueFootballPlayers.csv	Ln market value
Poisson (BIC)	15Fertile2.csv	ceb

Bibliography

- D. Acemoglu, S. Johnson, and J. Robinson. The colonial origins of comparative development: An empirical investigation. *The American Economic Review*, 91(5):1369–1401, 2001. [p]
- R. Baath. *Package bayesboot*, 2018. URL <https://CRAN.R-project.org/package=bayesboot>. [p]
- W. Chang. *Web Application Framework for R: Package shiny*. R Studio, 2018. URL <http://shiny.rstudio.com/>. [p]
- J. Geweke. *Bayesian Statistics*, chapter Evaluating the accuracy of sampling-based approaches to calculating posterior moments. Clarendon Press, Oxford, UK., 1992. [p]
- P. Heidelberger and P. D. Welch. Simulation run length control in the presence of an initial transient. *Operations Research*, 31(6):1109–1144, 1983. [p]
- M. Jetter and A. Ramírez Hassan. Want export diversification? educate the kids first. *Economic Inquiry*, 53(4):1765–1782, 2015. [p]
- G. Karabatsos. A menu-driven software package of bayesian nonparametric (and parametric) mixed models for regression analysis and density estimation. *Behavior Research Methods*, 49:335–362, 2016. [p]
- R. E. Kass and A. E. Raftery. Bayes factors. *Journal of the American Statistical Association*, 90(430):773–795, 1995. [p]
- A. Lenkoski, A. Karl, and A. Neudecker. *Package ivbma*, 2013. URL <https://CRAN.R-project.org/package=ivbma>. [p]
- A. D. Martin, K. M. Quinn, and J. H. Park. *Package MCMCpack*, 2018. URL <https://CRAN.R-project.org/package=MCMCpack>. [p]
- M. Plummer, N. Best, K. Cowles, K. Vines, D. Sarkar, D. Bates, R. Almond, and A. Magnusson. *Output Analysis and Diagnostics for MCMC*, 2016. URL <https://CRAN.R-project.org/package=coda>. [p]
- R Core Team. *R: A Language and Environment for Statistical Computing*. R Foundation for Statistical Computing, Vienna, Austria, 2018. URL <http://www.R-project.org/>. [p]
- A. Raftery and S. Lewis. One long run with diagnostics: Implementation strategies for Markov chain Monte Carlo. *Statistical Science*, 7:493–497, 1992. [p]
- A. Raftery, J. Hoeting, C. Volinsky, I. Painter, and K. Y. Yeung. *Package BMA*, 2012. URL <https://CRAN.R-project.org/package=BMA>. [p]
- A. Ramírez Hassan. The interplay between the Bayesian and frequentist approaches: a general nesting spatial panel data model. *Spatial Economic Analysis*, 12(1):92–112, 2017. [p]
- A. Ramírez Hassan, J. Cardona Jiménez, and R. Cadavid Montoya. The impact of subsidized health insurance on the poor in Colombia: Evaluating the case of Medellín. *Economía Aplicada*, 17(4): 543–556, 2013. [p]
- P. Rossi. *Package bayesm*, 2017. URL <https://CRAN.R-project.org/package=bayesm>. [p]
- M. Serna Rodríguez, A. Ramírez Hassan, and A. Coad. Uncovering value drivers of high performance soccer players. *Journal of Sport Economics*, Accepted manuscript, 2018. [p]
- Stan Development Team. *shinystan: Interactive visual and numerical diagnostics and posterior analysis for bayesian models.*, 2017. URL <http://mc-stan.org/>. R package version 2.3.0. [p]
- P. Woodward. BugsXLA: Bayes for the common man. *Journal of Statistical Software*, 14(5):1–18, 2005. [p]

Andrés Ramírez-Hassan
 Department of Economics
 School of Economics and Finance
 Universidad EAFIT
 Cra. 49, Medellín, Antioquia, Colombia
 e-mail: aramir21@eafit.edu.co
 URL: www.besmarter-team.org

Mateo Graciano-Londoño
Quantitative Analyst Department
Risk Vicepresidency
Protección SA
Cra. 49, 63 10, Medellín, Antioquia, Colombia.
e-mail: mgracian@proteccion.com.co
URL: www.besmarter-team.org