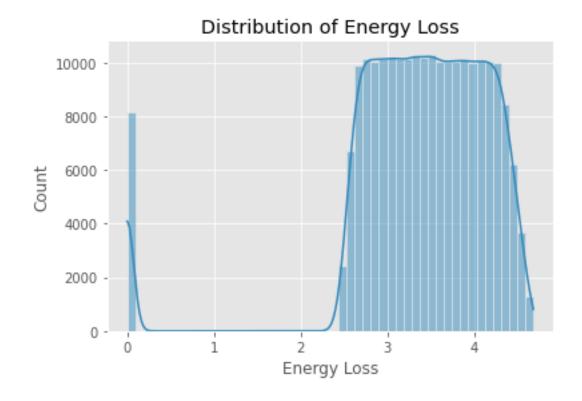
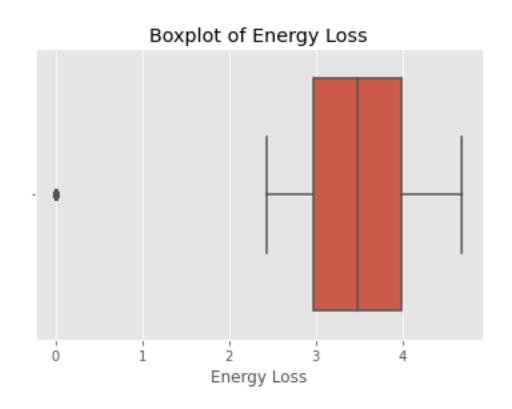
analysis

January 8, 2024

```
[21]: %matplotlib inline
      import numpy as np
      import matplotlib.pyplot as plt
      import pandas as pd
      from mpl_toolkits.mplot3d import Axes3D
      import plotly.graph_objs as go
      import seaborn as sns
      from sklearn.cluster import KMeans
      from sklearn.ensemble import IsolationForest
      from scipy.stats import shapiro
      from scipy.stats import sem, t
 [3]: file_path = 'muon_simulation_results.csv'
      df = pd.read_csv(file_path)
      df[['x', 'y', 'z']] = df['Position'].str.strip('[]').str.split(expand=True).
       →astype(float)
      threshold = 1
      df['Is_Cavity'] = (df['Energy_Loss'] < threshold) & (df['Energy_Loss'] != 0)</pre>
      df = df [df ['Energy_Loss'] != 0]
      df.head()
 [3]:
        {\tt Muon\_ID}
                                                  Position \
      1
               0 [157.75195142 203.93749687 31.43731061]
      2
               0 [157.71256088 203.85288034 31.47320531]
      3
               0 [157.66947658 203.76846241 31.50510131]
               0 [157.62839864 203.68207315 31.53424748]
               0 [157.58360973 203.59892122 31.56710641]
                                     Direction
                                                            Energy_Loss
                                                    Energy
      1 [-0.39390541 -0.84616522 0.35894701]
                                                604.747462
                                                               2.593000
      2 [-0.43084303 -0.84417936 0.31896002]
                                                601.880612
                                                               2.866850
      3 [-0.41077938 -0.86389257 0.29146169] 599.004357
                                                               2.876255
      4 [-0.44788913 -0.83151933 0.32858931] 595.834652
                                                               3.169705
      5 [-0.47346401 -0.82867732 0.29853934] 592.975050
                                                               2.859602
        Is Absorbed
                                                      z Is_Cavity
               False 157.751951 203.937497 31.437311
      1
                                                             False
```

```
2
                                                             False
               False 157.712561 203.852880 31.473205
      3
               False 157.669477 203.768462 31.505101
                                                             False
      4
               False 157.628399 203.682073 31.534247
                                                             False
      5
               False 157.583610 203.598921 31.567106
                                                             False
 [4]: energy_loss_stats = df['Energy_Loss'].describe()
      print(energy_loss_stats)
              218599.000000
     count
                   3.387053
     mean
     std
                   0.869905
                   0.000012
     min
     25%
                   2.972947
     50%
                   3.476681
     75%
                   3.983219
     max
                   4.685977
     Name: Energy_Loss, dtype: float64
[34]: plt.style.use('ggplot')
      sns.histplot(df['Energy_Loss'], bins=50 , kde=True)
      plt.xlabel('Energy Loss')
      plt.ylabel('Count')
      plt.title('Distribution of Energy Loss')
      plt.show()
      sns.boxplot(x=df['Energy_Loss'])
      plt.title('Boxplot of Energy Loss')
      plt.xlabel('Energy Loss')
      plt.show()
```





```
[35]: shapiro_test = shapiro(df['Energy_Loss'].sample(800))
      print(f"Shapiro-Wilk test:\nStatistics={shapiro_test[0]},__
       ⇔p-value={shapiro_test[1]}")
      skewness = df['Energy Loss'].skew()
      kurtosis = df['Energy_Loss'].kurt()
      print(f"Skewness: {skewness}")
      print(f"Kurtosis: {kurtosis}")
      correlation_matrix = df.drop(['Energy_Loss', 'Muon_ID', 'Is_Absorbed'], axis=1).
       ⇔corrwith(df['Energy_Loss'])
      print("\nCorrelation with Energy Loss:\n", correlation_matrix)
      confidence = 0.95
      data = df['Energy_Loss']
      n = len(data)
      mean = np.mean(data)
      std_err = sem(data)
      h = std_err * t.ppf((1 + confidence) / 2, n - 1)
      confidence_interval = (mean - h, mean + h)
      print(f"95% confidence interval for the mean of Energy Loss:

√{confidence_interval}")
     Shapiro-Wilk test:
     Statistics=0.8070188760757446, p-value=7.94901554398927e-30
     Skewness: -1.9993308216584464
     Kurtosis: 5.948566955037791
     Correlation with Energy Loss:
      Energy
                  0.098950
                  0.004754
     Х
                  0.001427
     У
                 -0.179825
     Is_Cavity
                 -0.765620
     dtype: float64
     95% confidence interval for the mean of Energy Loss: (3.3834066089285844,
     3.3906999794306167)
[40]: sns.pairplot(df.sample(80000), vars=['x', 'y', 'z', 'Energy_Loss'])
      plt.suptitle('Scatterplot Matrix for Position Variables and Energy Loss')
      plt.show()
      confidence = 0.95
      data = df['Energy_Loss']
      n = len(data)
      mean = np.mean(data)
      std_err = sem(data)
```

```
h = std_err * t.ppf((1 + confidence) / 2, n - 1)

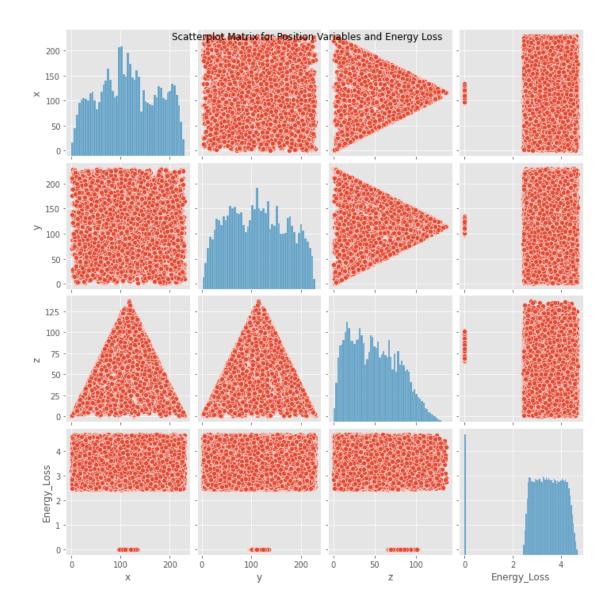
confidence_interval = (mean - h, mean + h)

print(f"95% confidence interval for the mean of Energy Loss:

confidence_interval}")
```

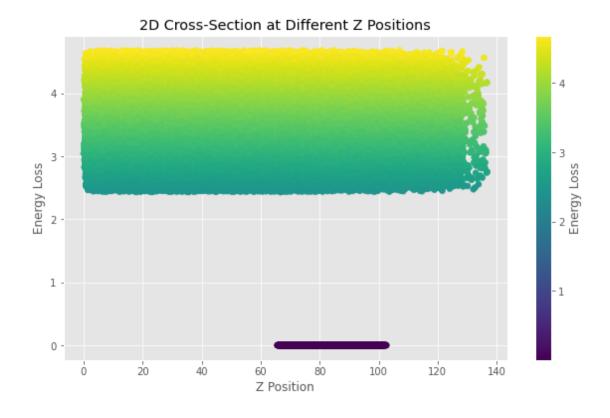
/opt/anaconda3/lib/python3.9/site-packages/seaborn/axisgrid.py:88: UserWarning:

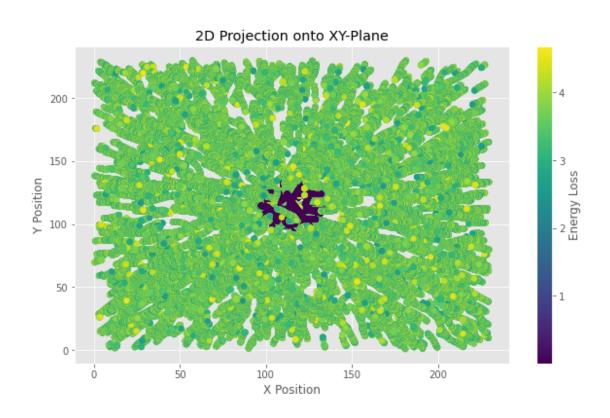
The figure layout has changed to tight

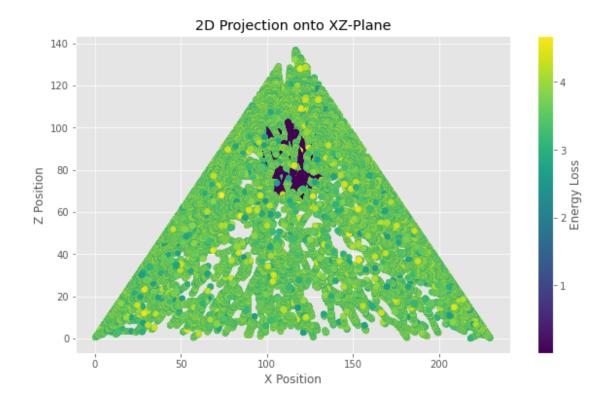


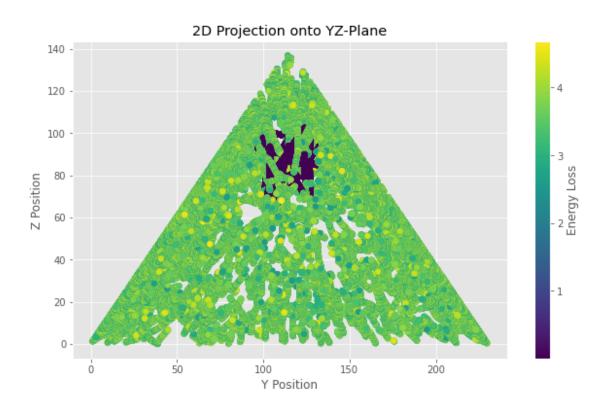
95% confidence interval for the mean of Energy Loss: (3.3834066089285844, 3.3906999794306167)

```
[37]: plt.figure(figsize=(10, 6))
      plt.scatter(df['z'], df['Energy_Loss'], c=df['Energy_Loss'], cmap='viridis')
      plt.colorbar(label='Energy Loss')
      plt.xlabel('Z Position')
      plt.ylabel('Energy Loss')
      plt.title('2D Cross-Section at Different Z Positions')
      plt.grid(True)
      plt.show()
      plt.figure(figsize=(10, 6))
      plt.scatter(df['x'], df['y'], c=df['Energy_Loss'], cmap='viridis')
      plt.colorbar(label='Energy Loss')
      plt.xlabel('X Position')
      plt.ylabel('Y Position')
      plt.title('2D Projection onto XY-Plane')
      plt.grid(True)
      plt.show()
      plt.figure(figsize=(10, 6))
      plt.scatter(df['x'], df['z'], c=df['Energy_Loss'], cmap='viridis')
      plt.colorbar(label='Energy Loss')
      plt.xlabel('X Position')
      plt.ylabel('Z Position')
      plt.title('2D Projection onto XZ-Plane')
      plt.grid(True)
      plt.show()
      plt.figure(figsize=(10, 6))
      plt.scatter(df['y'], df['z'], c=df['Energy_Loss'], cmap='viridis')
      plt.colorbar(label='Energy Loss')
      plt.xlabel('Y Position')
      plt.ylabel('Z Position')
      plt.title('2D Projection onto YZ-Plane')
      plt.grid(True)
      plt.show()
```





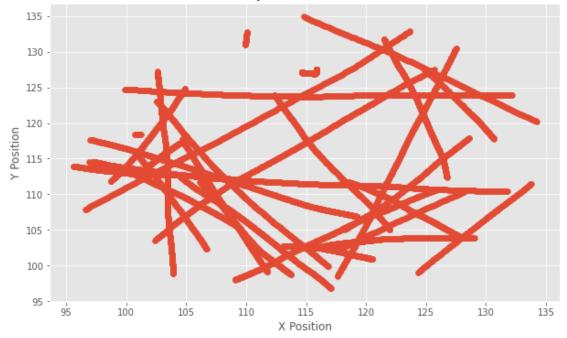


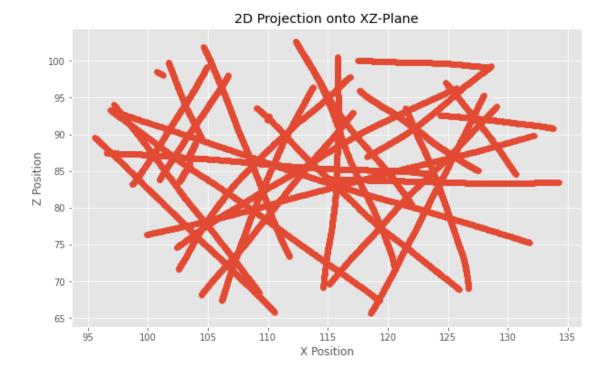


```
[]:
```

```
[38]: plt.figure(figsize=(10, 6))
    pos = df[df['Is_Cavity'] == True]
    plt.scatter(pos['x'], pos['y'])
    plt.xlabel('X Position')
    plt.ylabel('Y Position')
    plt.title('2D Projection onto XY-Plane')
    plt.grid(True)
    plt.show()
    plt.figure(figsize=(10, 6))
    plt.scatter(pos['x'], pos['z'])
    plt.xlabel('X Position')
    plt.ylabel('Z Position')
    plt.title('2D Projection onto XZ-Plane')
    plt.grid(True)
    plt.show()
```

2D Projection onto XY-Plane





```
[39]: # do not run this cell
      trace = go.Scatter3d(
          x=df['x'],
          y=df['y'],
          z=df['z'],
          mode='markers',
          marker=dict(
              size=5,
              color=df['Energy_Loss'],
              colorscale='Viridis',
              opacity=0.8
          )
      )
      layout = go.Layout(
          margin=dict(l=0, r=0, b=0, t=0)
      )
      fig = go.Figure(data=[trace], layout=layout)
      fig.show()
 []:
[]:
```

[]:[