# Towards A Synthetic Formulation of Multiparty Session Types

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### Background and Motivation

A Crash Course on Classic Multiparty Session Types

### What is wrong with this code?

```
func Worker(n int, resp chan int, err chan error) { ... }
func Master(regCh chan int, respCh chan []int, cErrCh chan error) {
  for {
    ubound := <-regCh
    workerChs := make([]chan int, ubound)
    errCh := make(chan error)
    for i := 0: i < ubound: i++ \{
      workerChs[i] = make(chan int)
      go Worker(i+1, workerChs[i], errCh)
    var res []int
    for i := 0; i < ubound; i++ \{
      select {
      case sql := <-workerChs[i]:</pre>
        res = append(res, sql)
      case err := <-errCh:
        cErrCh <- err
        return
      }}
    respCh <- res}}</pre>
```

### What is wrong with this code?

```
func Worker(n int, resp chan int, err chan error) { ... }
func Master(regCh chan int, respCh chan []int, cErrCh chan error) {
 for {
   ubour
          DEADLOCK!
   work
   errCł
          ORPHAN MESSAGES!
   for
     WO
     go
          NO RESOURCE CLEANUP!
   var
   for
          ...
     se'
     case sql := <-workerChs[i]:</pre>
       res = append(res, sql)
     case err := <-errCh:
       cErrCh <- err
       return
   respCh <- res}}</pre>
```

### What is wrong with this code?

```
func Worker(n int, resp chan int, err chan error) { ... }
func Master(regCh chan int, respCh chan []int, cErrCh chan error) {
  for {
    ubound := <-regCh
    worke
            Master needs to guarantee that all Workers are notified
    errCh
    for i
           when there is an error.
      wor
      go
    var res []int
    for i := 0: i < ubound: i++ {
      select {
      case sql := <-workerChs[i]:</pre>
        res = append(res, sql)
      case err := <-errCh:
        cErrCh <- err
        return
      }}
    respCh <- res}}</pre>
```

### Key Idea

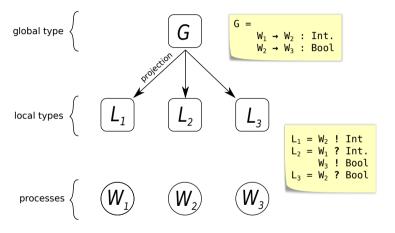
Multiparty Session Types prevent you from writing the code in the previous slide by enforcing syntactically that process implementations follow a given specification.

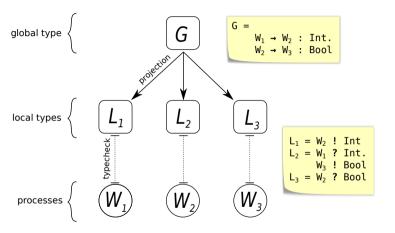
#### In a nutshell:

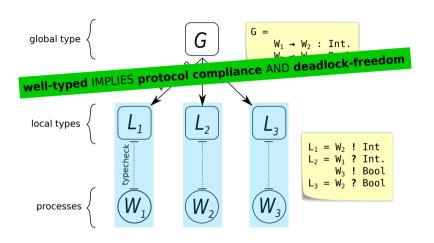
- 1. Global types: protocol specifications among a fixed number of different *roles*.
- 2. Role: sets of interactions that processes can do in a protocol.
- 3. Local types: protocol specifications from the point of view of a single role.
- 4. Projection: a partial function that extracts local type given a global types and a role.
- 5. <u>Well-formedness:</u> guarantees **deadlock-freedom**, usually defined in terms of *projectibility*.

processes  $\left\{ \begin{array}{cc} \left( W_{1} \right) & \left( W_{2} \right) & \left( W_{3} \right) \end{array} \right.$ 

processes  $\left\{ \begin{array}{cc} W_1 \\ \hline \end{array} \right\}$ 







### Global and Local Types

```
Roles
                               p, q, . . .
Sorts
                   S := bool \mid nat \mid \cdots
                                                               Basic data types.
Global Types G := p \rightarrow q : \{\ell_i(S_i).G_i\}_{i \in I}
                                                               Message communication.
                                                               Recursion.
                                                               Recursion variable.
                                                               End of protocol.
Local Types L := p!\{\ell_i(S_i).L_i\}_{i \in I}
                                                               Send message.
                          | \quad \mathsf{q}?\{\ell_i(S_i).L_i\}_{i\in I} \\ | \quad \mu \mathbf{X}.G 
                                                               Receive message.
                                                               Recursion.
                                                               Recursion variable.
                                                               End of protocol.
```

# Projection

$$\mathbf{p} \rightarrow \mathbf{q} : \{\ell_i(S_i).G_i\}_{i \in I} \upharpoonright \mathbf{r} = \left\{ \begin{array}{ll} \mathbf{q}! \{\ell_i(S_i).G_i \upharpoonright \mathbf{r}\}_{i \in I} & (\mathbf{r} = \mathbf{p} \land \qquad \land \mathbf{p} \neq \mathbf{q}) \\ \mathbf{p}? \{\ell_i(S_i).G_i \upharpoonright \mathbf{r}\}_{i \in I} & (\qquad \land \mathbf{r} = \mathbf{q} \land \mathbf{p} \neq \mathbf{q}) \\ \sqcap_{i \in I}(G_i \upharpoonright \mathbf{r}) & (\mathbf{r} \neq \mathbf{p} \land \mathbf{r} \neq \mathbf{q} \land \mathbf{p} \neq \mathbf{q}) \end{array} \right.$$

$$\mu \mathbf{X}.G \upharpoonright \mathbf{r} = \left\{ \begin{array}{ll} \mu \mathbf{X}.G \upharpoonright \mathbf{r} & (\mathbf{r} \in G) \\ \varnothing & (\mathbf{r} \notin G) \end{array} \right. \quad \mathbf{X} \upharpoonright \mathbf{r} = \mathbf{X} \qquad \varnothing \upharpoonright \mathbf{r} = \varnothing$$

# Projection

$$\begin{split} \mathbf{p} &\to \mathbf{q} : \{\ell_i(S_i).G_i\}_{i \in I} \upharpoonright \mathbf{r} = \left\{ \begin{array}{l} \mathbf{q}! \{\ell_i(S_i).G_i \upharpoonright \mathbf{r}\}_{i \in I} & (\mathbf{r} = \mathbf{p} \land \qquad \land \mathbf{p} \neq \mathbf{q}) \\ \mathbf{p}? \{\ell_i(S_i).G_i \upharpoonright \mathbf{r}\}_{i \in I} & (\qquad \land \mathbf{r} = \mathbf{q} \land \mathbf{p} \neq \mathbf{q}) \\ \sqcap_{i \in I}(G_i \upharpoonright \mathbf{r}) & (\mathbf{r} \neq \mathbf{p} \land \mathbf{r} \neq \mathbf{q} \land \mathbf{p} \neq \mathbf{q}) \end{array} \right. \\ \mu \mathbf{X}.G \upharpoonright \mathbf{r} = \left\{ \begin{array}{l} \mu \mathbf{X}.G \upharpoonright \mathbf{r} & (\mathbf{r} \in G) \\ \varnothing & (\mathbf{r} \not\in G) \end{array} \right. \quad \mathbf{X} \upharpoonright \mathbf{r} = \mathbf{X} \qquad \varnothing \upharpoonright \mathbf{r} = \varnothing \end{split}$$

$$\begin{split} &\mathsf{p}?\{\ell_{i}(S_{i}).L_{i}\}_{i\in I}\sqcap \mathsf{p}?\{\ell_{j}(S_{j}).L'_{j}\}_{j\in J}\\ &=\mathsf{p}?\{\ell_{i}(S_{i}).L_{i}\}_{i\in I\setminus J}\cup \{\ell_{j}(S_{j}).L'_{j}\}_{j\in J\setminus I}\cup \{\ell_{i}(S_{i}).L_{i}\sqcap L'_{i}\}_{i\in I\cap J} \\ &\mathsf{p}!\{\ell_{i}(S_{i}).L_{i}\}_{i\in I}\sqcap \mathsf{p}!\{\ell_{i}(S_{i}).L'_{i}\}_{i\in I}=\mathsf{p}!\{\ell_{i}(S_{i}).L_{i}\sqcap L'_{i}\}_{i\in I} \\ &\mu X.L\sqcap \mu X.L'=\mu X.(L\sqcap L') \qquad L\sqcap L=L \end{split}$$

### Projection

$$\mathsf{p} \to \mathsf{q} : \{\ell_i(S_i).G_i\}_{i \in I} \upharpoonright \mathsf{r} = \left\{ \begin{array}{ll} \mathsf{q}! \{\ell_i(S_i).G_i \upharpoonright \mathsf{r}\}_{i \in I} & (\mathsf{r} = \mathsf{p} \land \land \mathsf{p} \neq \mathsf{q}) \\ \mathsf{p}? \{\ell_i(S_i).G_i \upharpoonright \mathsf{r}\}_{i \in I} & (\land \mathsf{r} = \mathsf{q} \land \mathsf{p} \neq \mathsf{q}) \\ \sqcap_{i \in I}(G_i \upharpoonright \mathsf{r}) & (\mathsf{r} \neq \mathsf{p} \land \mathsf{r} \neq \mathsf{q} \land \mathsf{p} \neq \mathsf{q}) \end{array} \right.$$

$$\begin{array}{ll} \textbf{It gets complicated very quickly!} \\ \mu_{\mathbf{A}}.G_{\mathsf{r} \vdash \mathsf{r}} = \left\{ \begin{array}{ccc} \varnothing & & \mathsf{A} \vdash \mathsf{r} = \mathsf{A} & \varnothing \vdash \mathsf{r} = \varnothing \end{array} \right.$$

$$\begin{split} & \mathsf{p}? \{\ell_i(S_i).L_i\}_{i\in I} \sqcap \mathsf{p}? \{\ell_j(S_j).L_j'\}_{j\in J} \\ & = \mathsf{p}? \{\ell_i(S_i).L_i\}_{i\in I\setminus J} \cup \{\ell_j(S_j).L_j'\}_{j\in J\setminus I} \cup \{\ell_i(S_i).L_i\sqcap L_i'\}_{i\in I\cap J} \\ & \mathsf{p}! \{\ell_i(S_i).L_i\}_{i\in I} \sqcap \mathsf{p}! \{\ell_i(S_i).L_i'\}_{i\in I} = \mathsf{p}! \{\ell_i(S_i).L_i\sqcap L_i'\}_{i\in I} \\ & \mu \textbf{X}.L \sqcap \mu \textbf{X}.L' = \mu \textbf{X}.(L\sqcap L') \qquad L\sqcap L = L \end{split}$$

### What is the point of $\sqcap$ ?

Example:

```
\mu \textbf{\textit{X}}. \texttt{p} \rightarrow \texttt{q} : \left\{ \begin{array}{l} \mathsf{REQ}(\texttt{nat}). \texttt{q} \rightarrow \texttt{r} : \mathsf{REQ}(\texttt{bool}). \textbf{\textit{X}} \\ \mathsf{END}() \quad . \texttt{q} \rightarrow \texttt{r} : \mathsf{END}(). \mathsf{done} \end{array} \right\}
```

# What is the point of $\sqcap$ ?

Example:

$$\mu \textbf{\textit{X}}. \texttt{p} \rightarrow \texttt{q} : \left\{ \begin{array}{l} \mathsf{REQ}(\mathsf{nat}). \texttt{q} \rightarrow \texttt{r} : \mathsf{REQ}(\mathsf{bool}). \textbf{\textit{X}} \\ \mathsf{END}() \quad . \texttt{q} \rightarrow \texttt{r} : \mathsf{END}(). \mathsf{done} \end{array} \right\}$$

```
Projecting r
\mu X.(q?REQ(bool).X) \sqcap (q?END().\varnothing)
```

# What is the point of $\sqcap$ ?

Example:

$$\mu \pmb{X}. \mathbf{p} \rightarrow \mathbf{q} : \left\{ \begin{array}{l} \mathsf{REQ}(\mathsf{nat}). \mathbf{q} \rightarrow \mathbf{r} : \mathsf{REQ}(\mathsf{bool}). \pmb{X} \\ \mathsf{END}() \quad . \mathbf{q} \rightarrow \mathbf{r} : \mathsf{END}(). \mathsf{done} \end{array} \right\}$$

Projecting r

$$\begin{split} & \mu \pmb{X}.(\mathsf{q}?\mathsf{REQ}(\mathsf{bool}).\pmb{X}) \sqcap (\mathsf{q}?\mathsf{END}().\varnothing) \\ & = \mu \pmb{X}.\mathsf{q}? \left\{ \begin{array}{l} \mathsf{REQ}(\mathsf{bool}).\pmb{X} \\ \mathsf{END}() \end{array} \right. & \mathsf{done} \end{array} \right\} \end{split}$$

### Processes and Typing

### Process Typing (simplified)

Once we have local types, process typing is simple:

$$\begin{array}{ll} \text{T-SEND} & \\ \Gamma \vdash P : L_i & \Gamma \vdash e : S_i \quad i \in I \\ \hline \Gamma \vdash \mathsf{q} \mathrel{!} \ell_i \langle e \rangle . P : (\mathsf{p} ! \{\ell_i(S_i).L_i\}_{i \in I}) \end{array} & \begin{array}{l} \text{T-RECV} \\ \hline \Gamma, x_i : S_i \vdash P_i : L_i \quad \forall i \in I \\ \hline \Gamma \vdash \sum_{i \in I} \mathsf{p} ? \ell_i(x_i).P_i : (\mathsf{p} ? \{\ell_i(S_i).L_i\}_{i \in I}) \end{array} \\ \end{array}$$

### Problems with Classic Formulation

#### 1. Too syntactic:

- Processes and local types must align
- Too restrictive, rules out correct processes

- ...

#### 2. Unnecessarily complex:

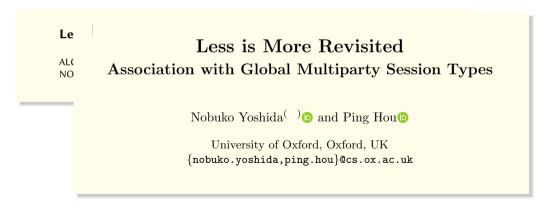
- Hard to implement/mechanise, e.g.:
  - Use of runtime coinductive global types: Our PLDI 2021 paper
  - Complex graph-based representation of MPST: Jacobs et al. (2022)
  - Graph-based reasoning and decision procedure for the equality of recursive types: Tirore et al. (2023)
- Hard to extend

# A Few Attempts at Simplifying the Theory

Less Is More: Multiparty Session Types Revisited

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### A Few Attempts at Simplifying the Theory



# HOW STANDARDS PROLIFERATE: (SEE: A/C CHARGERS, CHARACTER ENCODINGS, INSTANT MESSAGING, ETC.)

SITUATION: THERE ARE 14 COMPETING STANDARDS.





### Our Approach: Synthetic Typing

# Synthetic Behavioural Typing: Sound, Regular Multiparty Sessions via Implicit Local Types

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### Our Approach: Synthetic Typing

#### Syr Mu

#### Sun; Depar

Fran Depar

#### Goals:

- "Free" typing from being tied up to the syntax of local types.
- Avoid projection/merging/etc.
- A formal description of equality between global types to replace informally equating global types to their unfolding.
- Well-formedness/deadlock-freedom is decided by typeability.
- Mechanisation in Agda.

# Towards Synthetic MPST (WIP)

New judgement :  $\Gamma \vdash P : G \upharpoonright \mathsf{p}$ 

$$\begin{split} & \frac{\text{T-SEND}}{G \setminus \mathsf{p} \to \mathsf{q} = G'} \quad \frac{\Gamma \vdash P : G' \upharpoonright \mathsf{p} \quad \Gamma \vdash e : S}{\Gamma \vdash \mathsf{q} \: ! \: \ell(e).P : G \upharpoonright \mathsf{p}} \\ & \frac{\Gamma \vdash \mathsf{q} \: ! \: \ell(e).P : G \upharpoonright \mathsf{p}}{\Gamma \vdash \mathsf{E} : S} \\ & \frac{\forall (i \in I) \text{ s.t. } G \setminus \binom{\ell_i(S_i)}{\mathsf{q} \to \mathsf{p}} = G' \text{ we have } \Gamma, \pmb{x_i} : S_i \vdash P_i : G' \upharpoonright \mathsf{p}}{\Gamma \vdash \sum_{i \in I} \mathsf{q}?\ell_i(\pmb{x_i}).P_i : G \upharpoonright \mathsf{p}} \\ & \frac{\forall (i \in I) \text{ s.t. } G \setminus \binom{\ell_i(S_i)}{\mathsf{q} \to \mathsf{p}} = G' \text{ and } \mathsf{p} \neq \mathsf{r} \land \mathsf{q} \neq \mathsf{r} \text{ we have } \Gamma \vdash P : G' \upharpoonright \mathsf{r}}{\Gamma \vdash P : G \upharpoonright \mathsf{r}} \end{split}$$

Synthetic, in that G' occurs only in the premise, not in the conclusion. G' needs to be *synthesised* by using the rules of the operational semantics of global types.

### What is wrong with these rules?

$$\begin{split} & \frac{\text{T-SEND}}{G \setminus \mathsf{p} \to \mathsf{q} = G'} \quad \Gamma \vdash P : G' \upharpoonright \mathsf{p} \quad \Gamma \vdash e : S} \\ & \frac{G \setminus \mathsf{p} \to \mathsf{q} = G'}{\Gamma \vdash \mathsf{q} \,! \, \ell\langle e \rangle.P : G \upharpoonright \mathsf{p}} \\ & \frac{\text{T-RECV}}{\mathsf{T-RECV}} \\ & \frac{\forall (i \in I) \text{ s.t. } G \setminus \overset{\ell_i(S_i)}{\mathsf{q} \to \mathsf{p}} = G' \text{ we have } \Gamma, \pmb{x_i} : S_i \vdash P_i : G' \upharpoonright \mathsf{p}}{\Gamma \vdash \sum_{i \in I} \mathsf{q}?\ell_i(\pmb{x_i}).P_i : G \upharpoonright \mathsf{p}} \\ & \frac{\mathsf{T-SKIP}}{\mathsf{T-SKIP}} \\ & \frac{\forall (i \in I) \text{ s.t. } G \setminus \overset{\ell_i(S_i)}{\mathsf{q} \to \mathsf{p}} = G' \text{ and } \mathsf{p} \neq \mathsf{r} \land \mathsf{q} \neq \mathsf{r} \text{ we have } \Gamma \vdash P : G' \upharpoonright \mathsf{r}}{\Gamma \vdash P : G \upharpoonright \mathsf{r}} \end{split}$$

Hint: the problem is in these rules

$$\begin{aligned} & \text{T-RECV} \\ & \frac{\forall (i \in I) \text{ s.t. } G \setminus_{\mathbf{q} \to \mathbf{p}}^{\ell_i(S_i)} = G' \text{ we have } \Gamma, \mathbf{x_i} : S_i \vdash P_i : G' \upharpoonright \mathbf{p}}{\Gamma \vdash \sum_{i \in I} \mathbf{q}?\ell_i(\mathbf{x_i}).P_i : G \upharpoonright \mathbf{p}} \\ & \text{T-SKIP} \\ & \frac{\forall (i \in I) \text{ s.t. } G \setminus_{\mathbf{q} \to \mathbf{p}}^{\ell_i(S_i)} = G' \text{ and } \mathbf{p} \neq \mathbf{r} \land \mathbf{q} \neq \mathbf{r} \text{ we have } \Gamma \vdash P : G' \upharpoonright \mathbf{r}}{\Gamma \vdash P : G \upharpoonright \mathbf{r}} \end{aligned}$$

Hint 2: the problem is the same in both rules, let's focus on this one

```
\begin{aligned} &\mathsf{T}\text{-RECV} \\ &\frac{\forall (i \in I) \text{ s.t. } G \setminus \overset{\ell_i(S_i)}{\mathsf{q}} \to \mathsf{p} = G' \quad \text{we have } \ \Gamma, x_i : S_i \vdash P_i : G' \upharpoonright \mathsf{p}}{\Gamma \vdash \sum_{i \in I} \mathsf{q}?\ell_i(x_i).P_i : G \upharpoonright \mathsf{p}} \end{aligned}
```

What happens if *G* does not allow q to receive from p?

Let  $\mathcal{R}(\mathsf{p},\mathsf{q},\{\ell_i(S_i)\}_{i\in I},G)=\exists (i\in I)G',G\setminus \overset{\ell_i(S_i)}{\mathsf{q}}\to \mathsf{p}=G'$  – this means that an interaction between  $\mathsf{p}$  and  $\mathsf{q}$  is "ready" (i.e. can happen) in G.

$$\begin{array}{ccc} \text{T-SEND} \\ G \setminus \overset{\ell(S)}{\mathsf{p}} \to \mathsf{q} = G' & \Gamma \vdash P : G' \upharpoonright \mathsf{p} & \Gamma \vdash e : S \\ \hline \Gamma \vdash \mathsf{q} \ ! \ \ell\langle e \rangle . P : G \upharpoonright \mathsf{p} \end{array}$$

Let  $\mathcal{R}(\mathsf{p},\mathsf{q},\{\ell_i(S_i)\}_{i\in I},G)=\exists (i\in I)G',G\setminus \mathsf{q}^{\ell_i(S_i)}=G'$  – this means that an interaction between  $\mathsf{p}$  and  $\mathsf{q}$  is "ready" (i.e. can happen) in G.

$$\frac{\mathcal{R}(\mathsf{q},\mathsf{p},\{\ell_i(S_i)\}_{i\in I},G) \qquad \forall (i\in I) \text{ s.t. } G\setminus \overset{\ell_i(S_i)}{\mathsf{q}\to \mathsf{p}}=G' \text{ we have } \Gamma,x_i:S_i\vdash P_i:G'\upharpoonright \mathsf{p}}{\Gamma\vdash \sum_{i\in I}\mathsf{q}?\ell_i(x_i).P_i:G\upharpoonright \mathsf{p}}$$

Let  $\mathcal{R}(\mathsf{p},\mathsf{q},\{\ell_i(S_i)\}_{i\in I},G)=\exists (i\in I)G',G\setminus \mathsf{q}^{\ell_i(S_i)}=G'$  – this means that an interaction between  $\mathsf{p}$  and  $\mathsf{q}$  is "ready" (i.e. can happen) in G.

$$\begin{split} & \mathsf{T\text{-}SKIP} \\ & \mathcal{R}(\mathsf{q},\mathsf{p},\{\ell_i(S_i)\}_{i\in I},G) \land (\mathsf{r} \not\in \{\mathsf{p},\mathsf{q}\}) \\ & \frac{\forall (i\in I) \text{ s.t. } G \setminus \mathsf{q} \mathop{\rightarrow} \mathsf{p} = G' \text{ we have } \Gamma \vdash P : G' \upharpoonright \mathsf{r} }{\Gamma \vdash P : G \upharpoonright \mathsf{r}} \end{split}$$

Let  $\mathcal{R}(\mathsf{p},\mathsf{q},\{\ell_i(S_i)\}_{i\in I},G)=\exists (i\in I)G',G\setminus \mathsf{q}^{\ell_i(S_i)}=G'$  – this means that an interaction between  $\mathsf{p}$  and  $\mathsf{q}$  is "ready" (i.e. can happen) in G.

$$\frac{G \setminus \overset{\ell(S)}{\mathsf{p} \to \mathsf{q}} = G' \qquad \Gamma \vdash P : G' \upharpoonright \mathsf{p} \qquad \Gamma \vdash e : S}{\Gamma \vdash \mathsf{q} \; ! \; \ell\langle e \rangle . P : G \upharpoonright \mathsf{p}}$$

T-RECV

$$\frac{\mathcal{R}(\mathsf{q},\mathsf{p},\{\ell_i(S_i)\}_{i\in I},G) \qquad \forall (i\in I) \text{ s.t. } G\setminus \overset{\ell_i(S_i)}{\mathsf{q}\to \mathsf{p}} = G' \text{ we have } \Gamma, x_i:S_i\vdash P_i:G'\upharpoonright \mathsf{p}}{\Gamma\vdash \sum_{i\in I}\mathsf{q}?\ell_i(x_i).P_i:G\upharpoonright \mathsf{p}}$$
 
$$\mathsf{T\text{-SKIP}} \\ \mathcal{R}(\mathsf{q},\mathsf{p},\{\ell_i(S_i)\}_{i\in I},G) \wedge (\mathsf{r}\not\in \{\mathsf{p},\mathsf{q}\})$$
 
$$\underline{\forall (i\in I) \text{ s.t. } G\setminus \overset{\ell_i(S_i)}{\mathsf{q}\to \mathsf{p}} = G' \text{ we have } \Gamma\vdash P:G'\upharpoonright \mathsf{r}}$$
 
$$\Gamma\vdash P:G\upharpoonright \mathsf{r}$$

Let  $\mathcal{R}(\mathsf{p},\mathsf{q},\{\ell_i(S_i)\}_{i\in I},G)=\exists (i\in I)G',G\setminus \overset{\ell_i(S_i)}{\mathsf{q}}\to \mathsf{p}=G'$  – this means that an interaction between  $\mathsf{p}$  and  $\mathsf{q}$  is "ready" (i.e. can happen) in G.

T-RECV  $\mathcal{R}(\mathsf{q},\mathsf{p},\{\ell$ 

• The rules look more complex than with a syntactic approach, but computing  $G \setminus q \to p = G'$  is entirely mechanical by using the semantics of global types.

- The proof of subject reduction is greatly simplified (more in a few slides) with this formulation.
- No need of projection/merging.

T-SKIP  $\mathcal{R}(\mathsf{q},\mathsf{p},\{\ell_i(S_i)\}_{i\in I},G) \land (\mathsf{r} \not\in \{\mathsf{p},\mathsf{q}\})$   $\frac{\forall (i\in I) \text{ s.t. } G \setminus \mathsf{q} \to \mathsf{p} = G' \text{ we have } \Gamma \vdash P:G' \upharpoonright \mathsf{r}}{\Gamma \vdash P:G \upharpoonright \mathsf{r}}$ 

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# Semantics

# Lemmas

# Wrap Up

A Crash Course on Classic Multiparty Session Types

# Benefits of Synthetic Typing

# TODO