# Homework 4: Data Types and Functors in Haskell

# Required Problems

For this assignment, you're going to define a new type of list, called a Stream. This will duplicate a lot that you can do with lists, but will enforce that any Stream must be infinite. (The usual list type represents lists that may be infinite but may also have some finite length.)

In particular, in our implementation, streams will only have one constructor, whereas the list type has two constructors, [] (the empty list) and (:) (cons). In our setup, there is no such thing as an empty stream. So a stream is simply defined as an element followed by another stream:

data Stream a = Cons a (Stream a)

1. Write a function to convert a Stream to an infinite list:

```
streamToList :: Stream a -> [a]
```

2. To test your Stream functions in the succeeding exercises, it will be useful to have an instance of Show for Stream s. However, if you put deriving Show after your definition of Stream, as one usually does, the resulting instance will try to print an entire Stream, which, of course, will never finish. Instead, make your own instance of Show for Stream:

```
instance Show a => Show (Stream a) where
show...
```

which works by showing only a prefix of a stream- at most the first 20 elements.

3. Write a function:

```
streamRepeat :: a -> Stream a
```

which generates a stream containing infinitely many copies of the given element.

- 4. Make your Stream be an instance of Functor (as we did with binary trees in class), so that it applies an input function to every element in the Stream.
- 5. Write a function

```
streamIterate :: (a -> a) -> a -> Stream a
```

which generates a Stream from a "seed" of type a, which is the first element of the stream, and an "unfolding rule" that is a function taking an element of type a to another element of type a which specifies how to transform the seed into a new seed, to be used for generating the rest of the stream.

Example:

```
streamIterate ('x':) "o" == ["o", "xo", "xxo", "xxxo", "xxxxo", ...
```

#### 6. Write a function

```
streamInterleave :: Stream a -> Stream a -> Stream a
```

which interleaves the elements from 2 Streams. You will want streamInterleave to be lazy in its second parameter. This means that you should not deconstruct the second Stream in the function.

### Example:

```
streamInterleave (streamRepeat 0) (streamRepeat 1) ==
[0, 1, 0, 1, 0, 1, ...
```

7. Now that we have some tools for working with streams, let's create a few:

Define the stream

```
nats :: Stream Integer
```

which contains the infinite list of natural numbers 0, 1, 2, ...

8. Define the stream

```
powersoftwo :: Stream Integer
```

which corresponds to the powers of 2: 1, 2, 4, 8, 16, 32, 64, 128, . . . , where the  $n^{th}$  element in the stream is equal to  $2^n$ .

9. Define the stream

```
triangular :: Stream Integer
```

which corresponds to the triangular numbers: 0, 1, 3, 6, 10, 15, 21, 28, 36, 45, . . . , where the  $n^{th}$  element in the stream is equal to  $\frac{n(n+1)}{2}$ .

## Extra Credit Problems

10. Extra credit: Modify your Stream class so it is also of type Applicative, and define < \* > appropriately.