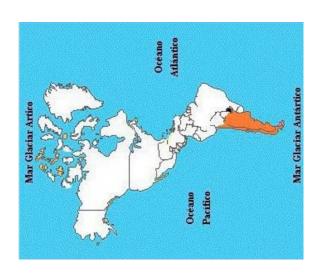
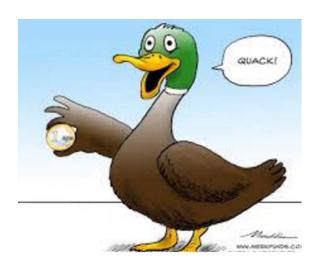
Vector space

axiomatic approach

(1) looks

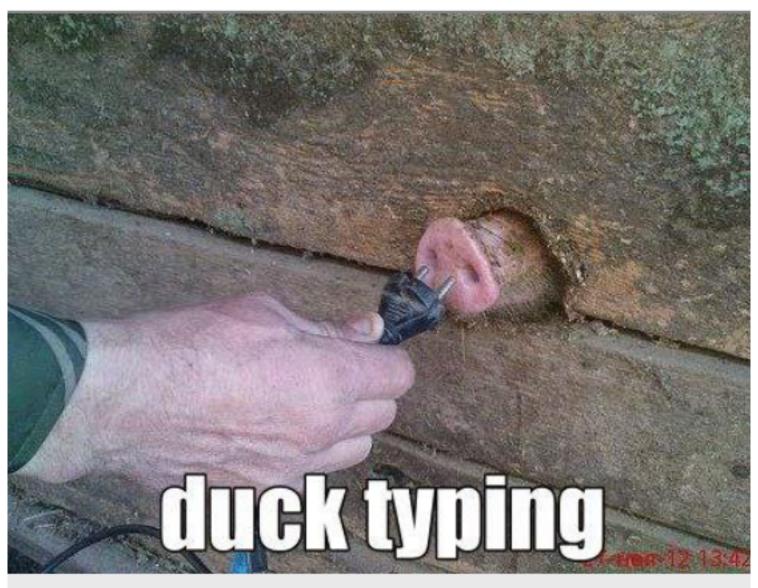


(2) quacks



=) duck.





A humorous and apt representation of duck typing. Source: Mastracci, 2014.* 🗨 🗀

A mathematical duck looks like...

A **vector space** is a nonempty set V of objects, called *vectors*, on which are defined two operations, called *addition* and *multiplication by scalars* (real numbers), subject to the ten axioms (or rules) listed below. The axioms must hold for all vectors \mathbf{u} , \mathbf{v} , and \mathbf{w} in V and for all scalars c and d.

- 1. The sum of \mathbf{u} and \mathbf{v} , denoted by $\mathbf{u} + \mathbf{v}$, is in V.
- 2. u + v = v + u.
- 3. (u + v) + w = u + (v + w).
- **4.** There is a **zero** vector **0** in V such that $\mathbf{u} + \mathbf{0} = \mathbf{u}$.
- **5.** For each **u** in V, there is a vector $-\mathbf{u}$ in V such that $\mathbf{u} + (-\mathbf{u}) = \mathbf{0}$.
- **6.** The scalar multiple of \mathbf{u} by c, denoted by $c\mathbf{u}$, is in V.
- 7. $c(\mathbf{u} + \mathbf{v}) = c\mathbf{u} + c\mathbf{v}$.
- 8. $(c+d)\mathbf{u} = c\mathbf{u} + d\mathbf{u}$.
- **9.** $c(d\mathbf{u}) = (cd)\mathbf{u}$.
- 10. 1u = u.

Ex. V= collection of all possible ducks differing only in Width