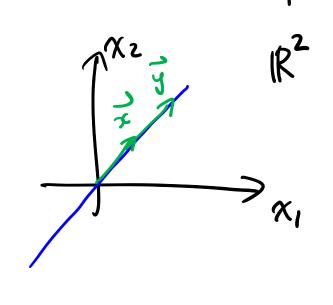
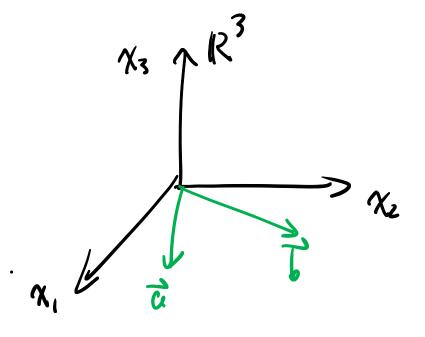
Lec 8 subspace.





Def A subspace H of IRⁿ is a subset of vectors in IRⁿ s.t.

(1) $\vec{O} \in H$ H cannot be empty (2) $\vec{U}, \vec{V} \in H$, then $\vec{U} + \vec{V} \in H$ closed under

(3) UEH, CEIR then CUEH closed under scalar mult.

addition

Ex. R. Possible subspaces.

IR 2 subspaces.

Ex. 12² possible subspaces.

 $\{0\}$ \mathbb{R}^2

Span{u}, u EIR, u +0

Ex. Sol set to hom. lin. sys.

A = 0

S. AERm×n

(1) 0 E S

(2) $\overrightarrow{x}, \overrightarrow{y} \in S$, $\overrightarrow{x} + \overrightarrow{y} \in S$

(3) CEIR, RES, CXES.

S is a subspace of R

what about $A \times = 6$

 $\{\vec{V}_1, ..., \vec{V}_K\} \subseteq \mathbb{R}^n$ Then span $\{\vec{V}_1, ..., \vec{V}_K\}$ is a subspace of \mathbb{R}^n .

Two important examples of subspace A ER mxn (1) Column space.

col(A) = Span of all Column Vectors of A.

Col(A) = Span fai, ..., and

a subspace of R^m

(2) Null space.

Null(A) = Sol Set of AX = 0.

a subspace of 1R"

$$\frac{1}{x} = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$$

$$\vec{b}_1 = \begin{bmatrix} 1 \\ 0 \end{bmatrix} \vec{b}_1 = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

$$\overrightarrow{X} \in \mathbb{R}^2$$
.

$$\vec{x} = x_1 \vec{b_1} + x_2 \vec{b_2} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}$$

$$\begin{bmatrix} \chi \\ \chi \end{bmatrix}_{\mathcal{B}} = \begin{bmatrix} 3 \\ 2 \end{bmatrix}$$

"Standard basis"

$$\sum_{X} = 3b_1 + 2b_2, \quad B = \{b_1, b_2\}$$

$$x_2 \qquad \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 \\ 2b \end{bmatrix}$$

$$x_3 \qquad \begin{bmatrix} x \\ y \end{bmatrix} = \begin{bmatrix} 3 \\ 2b \end{bmatrix}$$

$$x_4 = \begin{bmatrix} 3 \\ 4 \end{bmatrix}$$

$$x_4 = \begin{bmatrix} 3 \\ 4 \end{bmatrix}$$

$$x_5 = \begin{bmatrix} 4 \\ 7 \end{bmatrix}$$

Def A basis for a subspace H
of IRⁿ is an ordered set
of vectors

What is coordinate

