The Reaction Grid

Context for the cell list

- A cell list¹ is a data structure to find combinations of objects within a given cut-off distance of each other.
 - Cell size defined using a user defined reaction radius.
 - Enables efficient geometric search of nearby objects and combinatorial matching of nearby components.
- The cell list is integral in the incremental update.
- The cell list can be used in the rule mapping function φ .
- Other potential methods are bounding volume hierarchies², k-d trees³, etc.
- 1. (Slattery, 2022); 2. (Ericson, 2004); 3. (Bentley, 1975)

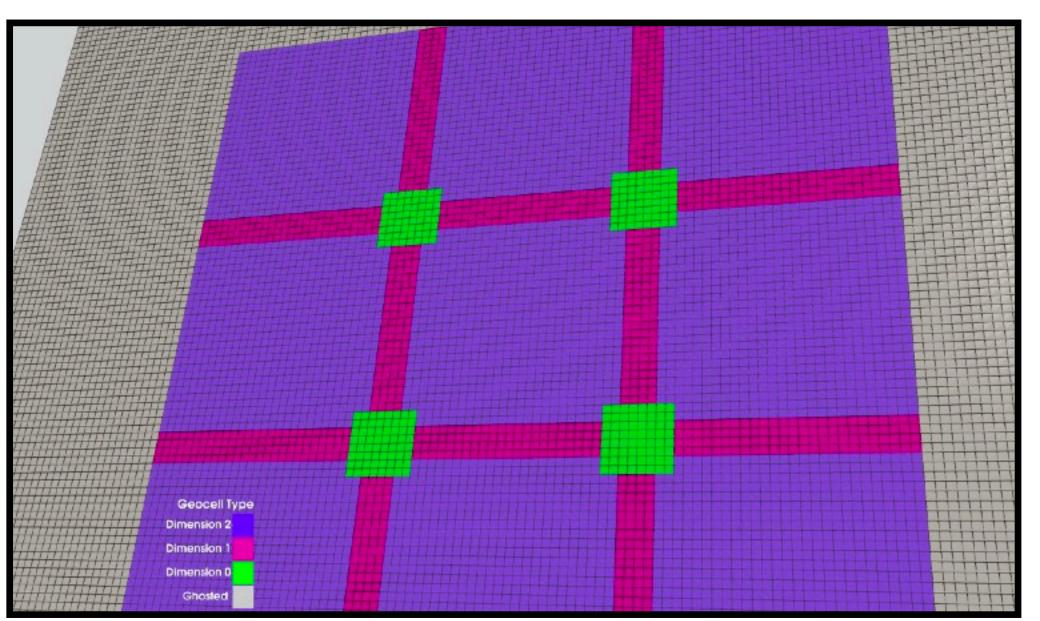


Figure 17: ECC overlaid with a "reaction grid" from a cell list and "ghost cells".

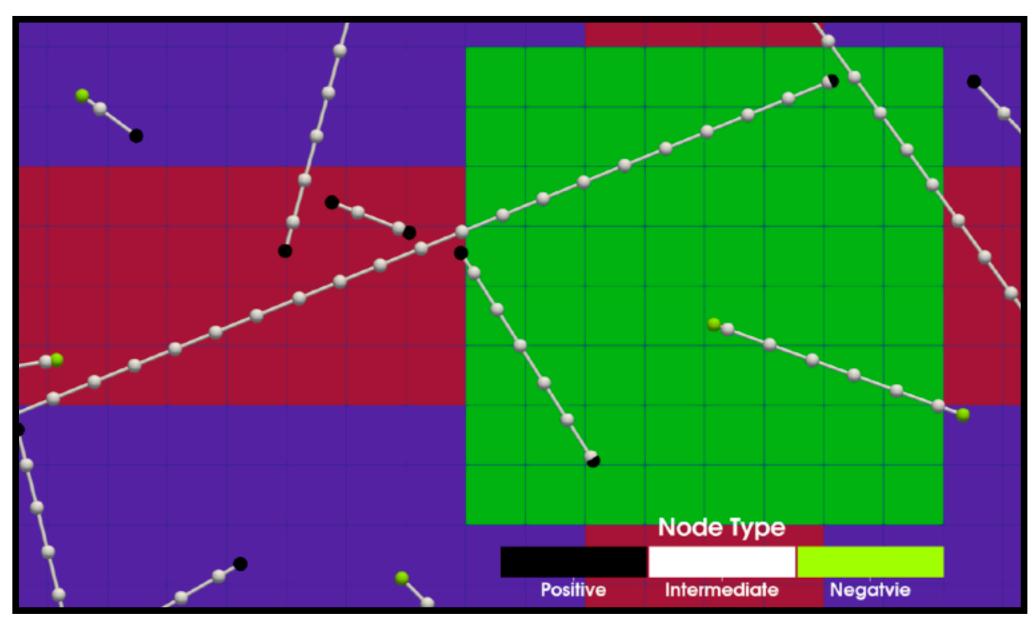


Figure 18: Zoomed in version with graph rules shown.

Original Approximate Algorithm

The first attempt at the approximation

- Differing dimensions can be processed separately.
- Potential for parallel processing over dimension and within a geometric cell.
- Reactions (rules) are spatially local and may be fired out of order at the cost of accuracy.

Original Approximate Spatially Embedded Hybrid Parameterized SSA/ODE Algorithm

```
while t \leq t_{max} do

foreach dimension d \in \{D_{max}, D_{max} - 1, \dots, 0\} do

using function \varphi map rule instances to the geocells of the expanded cell complex;

ParFor expanded geocell c_i \in ExpandedCellComplex(d) do

run Exact Hybrid Parameterized SSA/ODE algorithm for \Delta t in c_i;

t + = \Delta t;
```

Algorithm 2

- Good for larger simulations.
- Requires more details to fully address the problem.