UNIVERSITY OF TORONTO FACULTY OF APPLIED SCIENCE AND ENGINEERING FINAL EXAMINATION, DECEMBER 2021

CIV102F – Structures and Materials – An Introduction to Engineering Design

Examiners --- A. Kuan and E.C. Bentz

Permissible Aids: Non-programmable calculator, printed or handwritten notes

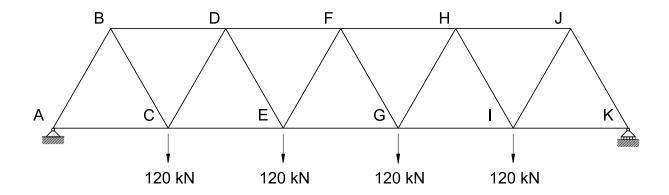
IMPORTANT INSTRUCTIONS

- 1. You have a total of 2.5 hours to complete and submit the final exam.
- 2. There are four questions on the exam. Attempt all questions; any questions left blank will receive a grade of zero. Part marks will be awarded for incomplete answers.
- 3. Report all final answers using slide-rule precision (i.e., four significant figures if the first digit is a "1", three otherwise).
- 4. If you need more space, you may write on the back side of the page. Indicate this on the front side of the page so none of your work is missed.
- 5. Write neatly and draw a box around your final answers.

Full Name:	 	
Student Number:		

Question No.	Score	Possible Points
1		34
2		31
3		25
4		20
Total		110

1. The truss shown below supports a 30 m pedestrian bridge and is made from steel hollow structural sections with a yield stress of 350 MPa. When the bridge is crowded with people, it supports four 120 kN loads as shown below. **Each member is 6 m long.**



1(a). Calculate the axial force in each member of the truss due to the 120 kN loads. Indicate the calculated member forces on the provided drawing. Use the convention +ve for tension and -ve for compression. Use the provided space below for intermediate/sample calculations if needed. (10 marks)

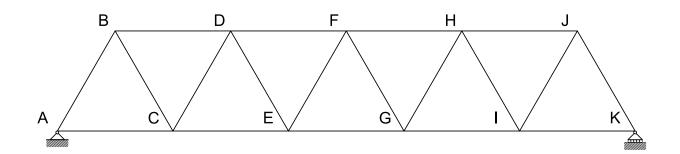
1(b). Each of the horizontal chord members are HSS $203\times203\times6.4$, and each of the diagonal web members are HSS $152\times152\times6.4$. Is the truss <u>safe</u> under the 120 kN loads? Yes or no? At what value of the loads will the structure be on the boundary between safe and unsafe? (6 marks)

Note: When solving this problem, you do not need to check if the slenderness ratio, L/r, exceeds the allowable limit of 200.

1(c). Using the Method of Virtual Work, calculate the vertical deflection of $\underline{\textbf{Joint F}}$ due to the application of the 120 kN loads. Use the provided drawing of the truss to determine the virtual forces, and fill in the following table to perform your calculations. Recall that E = 200,000 MPa for steel. Note that the table lists the members for only one half of the truss. (10 marks)

Note: Two blank columns have been provided for intermediate calculations if needed.

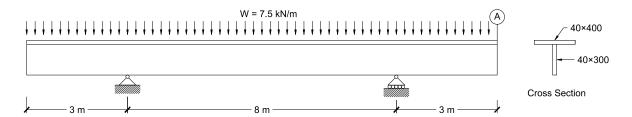
Member	Member Force	Area		Length	$\Delta 1$	Virtual Force	Work
Wember	(kN)	(mm ²)		(mm)	(mm)	(kN)	(J)
AB							
ВС							
CD		3610					
DE							
EF				6000			
BD							
DF		4000					
AC		4900					
CE							
EG		4900		6000			



1(d). Consider the situation where a smaller crowd of people is standing on the bridge. When standing still, the resulting point loads on the structure will be 90 kN each instead of the 120 kN loads considered in parts (a) to (c).

Using your answer from part (c), calculate the midspan displacement under this smaller load and the resulting natural frequency of the loaded bridge. What will the maximum midspan displacement be if the crowd starts moving, producing loads of 90 ± 30 kN at a frequency of 3.5 Hz? Will any of the members yield or buckle? When performing your calculations, use a damping ratio of $\beta = 0.02$. (8 marks)

2. The timber T-beam shown below has been fabricated by gluing together two pieces of wood. The beam is 14 m long, is supported by two supports 8 m apart, and is subjected to a uniformly distributed load, which includes self weight, of 7.5 kN/m. The wood has an ultimate tensile strength of 70 MPa, an ultimate compressive strength of 50 MPa, and a Young's modulus of 11,000 MPa. All dimensions are in mm unless indicated otherwise.



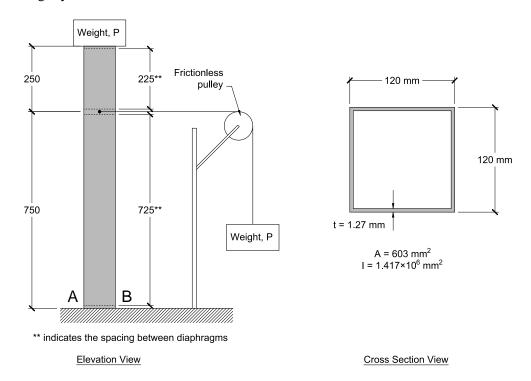
2(a). Draw the shear force and bending moment diagrams for the beam. Calculate and show important values. Use the course convention when drawing your bending moment diagram. (5 marks)

2(b). Determine the location of the centroidal axis and the value of I for the cross-section. (5 marks) *Note: there is more space at the top of page 7 for you to complete this calculation.*

2(c). Determine the max	ximum flexural comp	ressive stress, the m	aximum flexural ten	sile stress, and the
maximum shear stress v stresses occur. (8 marks		m. indicate on the pi	rovided drawing whe	ere tnese maximum

2(d). Draw the curvature diagram and calculate the vertical displacement of the beam at the midspan. Also determine the slope of the beam at point A, located at the far right side of the structure. (7 marks)
Note: report only the magnitudes of the slope and displacement.
2(e). Calculate the factor of safety against a tension failure and the factor of safety against a compression failure (do not check the FOS against a shear failure). Using these two values,
determine the overall factor of safety. Will the overall factor of safety increase or decrease if the
beam is flipped upside down? Explain. (6 marks)

3. Although the design-build project in CIV102 has traditionally involved building a bridge, another possibility is to build a tower. Consider the 1 m tall tower structure shown below. The tower is loaded using two weights which each have a value of P. One weight is applied to the top of the tower, subjecting it to an axial compression. The second weight applies a horizontal force to the tower 750 mm above the base using a pulley system. The tower has four diaphragms whose spacings are shown in the figure, and the base of the tower is rigidly connected to a table below. All dimensions are in mm unless indicated otherwise.



The matboard has the following properties:

Tensile Strength	$\sigma^{+}_{ult} = 30 \text{ MPa}$	Young's Modulus	E = 4000 MPa
Compressive Strength	$\sigma_{ult} = 6 \text{ MPa}$	Poisson's Ratio	$\mu = 0.2$
Shear Strength	$\tau_{\rm ult} = 4~MPa$	Thickness	t = 1.27 mm

3(a). Calculate the reaction forces if P = 100 N. At the base of the structure, calculate the tensile stress at point A and the compressive stress at point B caused by the combined loading. Determine where the axial stress equals zero at the base, and state its location relative to the left side of the tower (i.e., from point A). (7 marks)

3(b). Calculate the values of P causing a compression failure (P ₁) and a tension failure (P ₂). (4 marks)
3(c). Calculate the values of P causing plate buckling failures due to flexural compression. Consider both
possible plate buckling cases (P ₃ and P ₄). (4 marks) Note: Use the clear distance between edges to find "b" when using the plate buckling equations.

3(d). Calculate Q and the values of P causing a matboard shear failure (P ₅) and a shear buckling failure (5 marks)	P ₆).
3(e). What value of P will cause the tower to fail? What will be the cause of failure? (2 marks)	
3(f). The shear buckling equation presented in class was derived for a beam that is carrying bend moments and shears forces only. Will this equation underestimate or overestimate the critical shear strucker which also carries an axial compression? Explain. (3 marks)	

4. The reinforced concrete beam shown in the photo below was tested by Ms. Nicole Butkovic on Nov. 26, 2021, as part of her MASc research project. The specimen was uniformly loaded from below using a series of hydraulic jacks – a schematic explaining the loading apparatus can be found below. Because the loads were applied from below, the self-weight of the beam should be neglected when performing your calculations. The south region of the beam did not contain any shear reinforcement, while the north region of the beam contained two-leg 10M stirrups spaced apart at 170 mm.

All dimensions are in mm unless indicated otherwise.

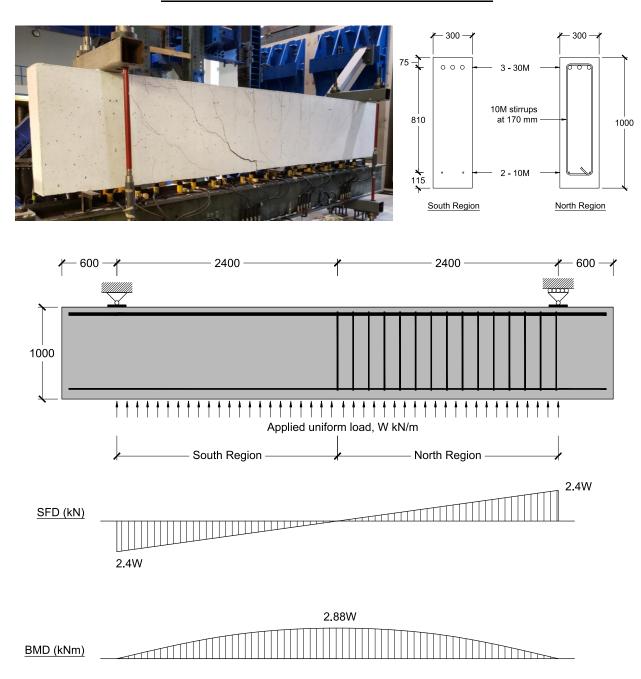


Photo of tested beam (top left), cross section details (top right), elevation view (middle), SFD and BMD showing key values (bottom).

The compressive strength of the concrete at the time of testing was f_c ' = 41 MPa, and the yield strengths of the 10M and 30M steel bars were f_y = 400 MPa. The Young's modulus of the concrete can be taken as E_c = 28,000 MPa.

4(a). Calculate the highest value of the bending moment and corresponding value of W which can be <u>safely</u> resisted by the beam so that the tensile stress in the longitudinal reinforcement does not exceed $0.6 \times f_y = 240$ MPa and the compressive stress in the concrete does not exceed $0.5 \times f_c' = 20.5$ MPa. Neglect the longitudinal steel in compression when performing your calculations. (8 marks)
4(b). Calculate the value of W which would cause the longitudinal reinforcement to yield and hence cause a flexural failure. (2 marks)

4(c). Calculate the highest shear force and corresponding value of W which will cause a shear failure in the south region of the beam which does not contain shear reinforcement. (3 marks)
4(d). Calculate the highest shear force and corresponding value of W which will cause a shear failure in the north region of the beam which contains shear reinforcement. (4 marks)
4(e). Using your results from questions 4(b) to 4(d), predict the value of W which causes failure of the beam. Does the beam fail in flexure or shear? State approximately where the failure takes place. (3 marks)