

MAT292 – Deferred Final Examination – January 29, 2022

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Time allotted: 150 minutes

Full Name

Student Number

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Signature

You are allowed to access the following “OK” aids during the exam. Everything not listed here is **NOT OK**.

- The course textbook
- Your own lecture notes
- Any content that can be found directly on the course’s Quercus page, with the exception of external links (i.e. any links outside of Quercus).
 - As an example: You can access the lecture slides available on Quercus.
 - As a non-example: You can’t access youtube, even if there is a link to it somewhere on the course page.
- Any calculator listed as Type 3 on the faculty’s list: <https://undergrad.engineering.utoronto.ca/exams/exam-types-permitted-calculators/>

This exam contains 13 pages (including this title page). Once the exam starts, make sure you have all of them.

In Section I, only answers are required. No justification necessary.

In Section II and Section III, you need to justify your answers.

Answers without justification won’t be worth points, unless a question says “no justification necessary”.

You can use pages ??–13 to complete questions. In such a case, **MARK CLEARLY** that your answer “continues on page X” **AND** indicate on the additional page which questions you are answering.

	Short	True/False	Long answer						
Question	Q1-Q6	Q7-Q11	Q12/13	Q14	Q15	Q16/Q17	Q18	Q19	Total
Marks	19	10	10	10	10	12	8	10	89

!!!! THERE IS A TABLE ON PAGE 14!!!!

GOOD LUCK! YOU GOT THIS!

SECTION I Provide the final answer. No justification necessary.

1. (3 marks) For $r > 0$ and $K > T > 0$, identify and classify the equilibrium points of the following autonomous ODE.

$$y' = -r \left(1 - \frac{y}{T}\right) \left(1 - \frac{y}{K}\right) y$$

List the equilibria from smallest to largest.

Solution:

$y = 0$ is stable, $y = T$ is unstable, $y = K$ is stable.

Equilibrium	Classification

2. (2 marks) Consider the following IVP

$$y'(t) + \frac{e^t}{(t-1)(t-6)} y(t) = \frac{t^5}{t-3} \quad y(2) = 5$$

Interval:

What is the maximal interval of t for which you can guarantee that the solution to this IVP exists?

Solution: This is a linear ODE. The largest interval that contains $t = 2$ on which the functions involved are continuous is $(1, 3)$. Based on E-U-Theorem for linear ODEs, this is the largest interval we can guarantee.

3. (2 marks) Write a constant in the box such that for ALL solutions except for the trivial solution $y(t) = 0$, we have

$$|y(t)| \rightarrow +\infty \quad \text{for} \quad t \rightarrow +\infty$$

$$y'' - y' + \boxed{} y = 0$$

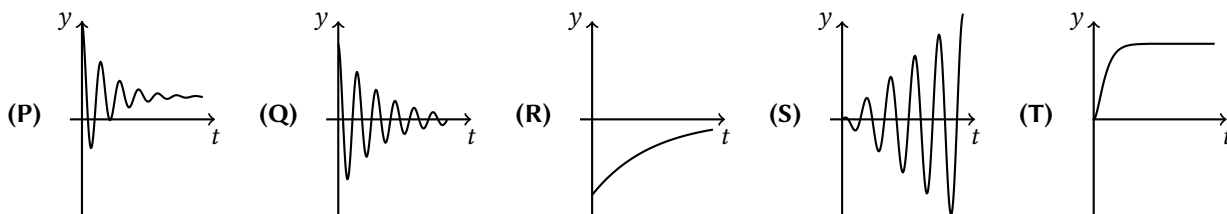
Solution: If we call the missing parameter a , then the characteristic polynomial has roots $\frac{1 \pm \sqrt{1-4a}}{2}$. We can't have complex roots since that would mean that solutions will always oscillate back to zero. Instead, we need two positive roots (or one single positive root). We can achieve this by picking any a that makes the expression in the root less than one without making it negative. That means any $a \in (0, 1/4]$ works. Note that $a = 0$ does not work since in that case we have nonzero constant solutions.

4. (2 marks) State the inverse Laplace Transform of $Y(s) = \frac{e^{-2s}}{s-1} H(s)$ in terms of the function $h(t)$.

$$\mathcal{L}^{-1} \left\{ \frac{e^{-2s}}{s-1} H(s) \right\} =$$

Solution: The inverse laplace transform of $\frac{e^{-2s}}{s-1}$ is $u_2(t)e^{t-2}$ (time shift property). Now use convolution theorem and write this as $(u_2(t)e^{t-2}) * h(t)$ (or the integral expression for convolution). Alternatively, $(e^{t-2}) * u_2(t)h(t)$ also works.

5. Consider these graphs depicting solutions of ODEs of the form $ay'' + by' + cy = f(t)$.



(a) (2 marks) Which graph/graphs can describe a free oscillator involving a mass of 2 kg , a spring constant of 24 N/m and a damping coefficient of 14 N/s/m ?

Solution: This describes the ODE $2y'' + 14y' + 24y = 0$. The characteristic polynomial has two negative roots, so the solutions are exponentials with negative exponent. The only such graph is (R).

(b) (2 marks) Which graph/graphs can describe a forced damped oscillator with **nonzero constant external force**?

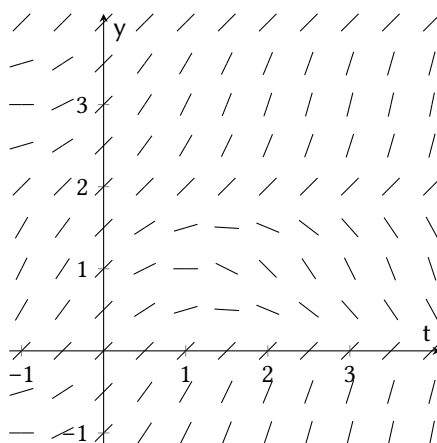
Solution: Since the external force is constant, resonance like in (S) is not possible. (Q) and (R) aren't possible since it depicts a free oscillator. The other two, (P) and (T) depict under- and overdamped oscillators with nonzero constant external force.

(c) (2 marks) For what value of p is (S) a plot of a solution to $y'' + 3y = \cos(pt)$?

$p =$

Solution: (S) depicts resonance or, as an equation, a solution of the form $t \sin(at)$. This is only possible if the frequency of the oscillator and the external force match, which is achieved for $p = \sqrt{3}$.

6. (4 marks) Consider the ODE $y' = f(t, y)$ whose direction field is plotted below.



With initial value $y(1) = 2$, approximate $y(2)$ using Euler's Method with a single step.
Choose the value closest to your estimate.

- ☐ 0.00 ☐ 0.25 ☐ 0.50 ☐ 0.75 ☐ 1.00 ☐ 1.25 ☐ 1.50 ☐ 1.75
☐ 2.00 ☐ 2.25 ☐ 2.50 ☐ 2.75 ☐ 3.00 ☐ 3.25 ☐ 3.50 ☐ 3.75

With initial value $y(1) = 1$, approximate $y(2)$ using **Improved** Euler's Method with a single step.
Choose the value closest to your estimate.

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☐ 2.00 ☐ 2.25 ☐ 2.50 ☐ 2.75 ☐ 3.00 ☐ 3.25 ☐ 3.50 ☐ 3.75

Solution: For the first one, the slope at the point $(1, 2)$ is 1. So we take a step of size 1 with slope 1 and get to the point $(2, 3)$. The estimate is $y(2) \approx 3$.

For the second one, the slope at $(1, 1)$ is 0. We take a step of size 1 with slope 0 to get to $(2, 1)$. The slope sample there is -1 . We take the average of both slope samples, which is $-1/2$. Starting again and taking a step at that slope we get to $(2, 0.5)$. Therefore, the estimate is $y(2) \approx 0.5$.

SECTION II For each of the following statements, decide if it is true or false. Then justify your choice.

Remember: A statement is only true if you can guarantee it is ALWAYS true given the information.

In other words: If something is “only true under certain circumstances”, it is still false.

7. (2 marks) If $f(t, y)$ is continuous for all t and all y and never zero, then $y' = f(t, y)$ can be solved using separation of variables.

Solution: This is not true for $f(t, y) = 1 + t^2 + y^2$

8. (2 marks) Consider the IVP $y' = f(t, y)$ with $y(0) = 0$. When using Euler's method to approximate $y(10)$, a smaller step size will always lead to a smaller error in our approximation.

Solution: This is not true. Sometimes we get very lucky for a large step size.

9. (2 marks) For all square matrices A , we have $\lim_{t \rightarrow \infty} e^{-tA} = 0$

Solution: Not even correct for scalars, i.e. 1×1 matrices. Take $A = [-1]$ for example.

10. (2 marks) If the constant-coefficient ODE $ay'' + by' + cy = 0$ has ONE periodic solution (not the zero solution), then ALL solutions are periodic.

Solution: This is true. Periodic solutions can only appear if the roots of the characteristic polynomial are purely imaginary $r = \pm \nu i$. This means all solutions are just linear combinations of sines and cosines and therefore periodic.

11. (2 marks) Consider $\vec{x}(t) = [x_1(t), x_2(t), \dots, x_n(t)]$ and the system $\vec{x}'(t) = P(t)\vec{x}(t) + \vec{g}(t)$ where $P(t)$ is an $n \times n$ matrix and $\vec{g}(t) = [g_1(t), g_2(t), \dots, g_n(t)]$.

There must be at least one solution to this system such that $\vec{x}(0) = [0, \dots, 0]$.

Solution: This is not true. We don't know if $\vec{g}(t)$ and/or $P(t)$ are continuous, so the E-U-Theorem for Systems doesn't apply. A counterexample is any system for which $\vec{g}(t)$ and/or $P(t)$ are not continuous at $t = 0$.

SECTION III Justify all your answers, unless it **specifically** says that you do not need to justify.

12. (4 marks) Find the maximum of the solution to this IVP:

$$y' + ty = 0 \quad y(\sqrt{2}) = \frac{1}{e}$$

Solution: Using separation of variables or integrating factor, the general solution is $y(t) = Ce^{-t^2/2}$. Matching the initial value, we get $C = 1$. The maximum of $y(t) = e^{-t^2/2}$ is $y(0) = 1$.

Maximum:

13. (6 marks) Consider the ODE $y' = f(y)$ where $f(y)$ is given by the phase plot on the right.

(a) You do NOT need to justify your answer to this part.

If $y(t)$ is a solution to this ODE with $y(0) = 2.5$, then

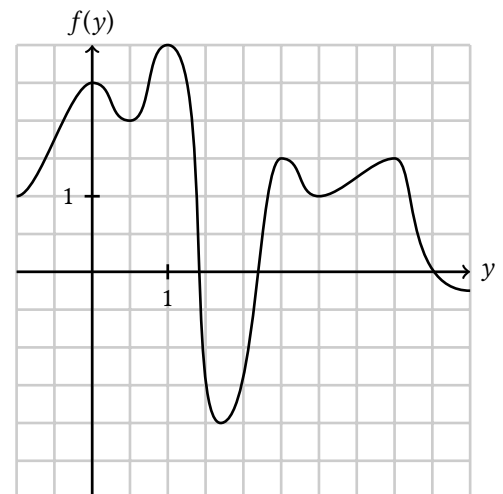
$$\lim_{t \rightarrow \infty} y(t) =$$

4.5

(b) Explain and justify your answer to this part.

Assume $y(t)$ is a solution to this ODE with $y(0.5) = 2$. Is y concave up, concave down, or neither at the point $(t, y) = (0.5, 2)$?

Solution: From $y' = f(y)$ we get (by chain rule) that $y'' = f'(y)y' = f'(y)f(y)$. At the point $y = 2$, we have $f(y) < 0$ and $f'(y) > 0$. So the product is negative. Therefore $y'' < 0$ and the function is concave down whenever it has value 2.



☐ concave UP

☐ concave DOWN

☐ neither (inflection point)

14. There is a yet another zombie outbreak in a remote town in Northern Saskatchewan. We denote by $H(t)$ the number of humans and by $Z(t)$ the number of zombies in town. Every individual in town is either a human or a zombie. t is measured in days. The following effects are given:

- Every day, each human kills n zombies, where $n \geq 1$ is an unknown parameter.
- Every day, each zombie bites 2 humans, and as a result transforms them into zombies.
- Every day, 3 humans arrive from out of town.
- Every day, 5 zombies get lost in the forest and never come back (i.e. they leave town).

(a) (4 marks) Set up a system of ODEs. **You must explain your system to receive full points.**

$$\begin{bmatrix} H(t) \\ Z(t) \end{bmatrix}' = \begin{bmatrix} 0 & -2 \\ -n & 2 \end{bmatrix} \begin{bmatrix} H(t) \\ Z(t) \end{bmatrix} + \begin{bmatrix} 3 \\ -5 \end{bmatrix}$$

(b) (2 marks) Find the two eigenvalues of the matrix that you just defined. Your answers should depend on the parameter n . **You do not need to justify, just state the two eigenvalues.**

$$\lambda_1 = 1 + \sqrt{1 + 2n} > 0$$

$$\lambda_2 = 1 - \sqrt{1 + 2n} < 0$$

(c) (4 marks) For each of the following four scenarios, discuss if it is possible or not.

Assume that the initial population $[H(0), Z(0)]$ is NOT proportional to one of the eigenvectors.

The number of humans and zombies will converge to a fixed, finite limit.

Solution: Impossible. Since the eigenvalues have different signs, the equilibrium is unstable. So unless we start on one of the eigenvector lines (which is not the case), the equilibrium will never be reached.

The zombies will win eventually, i.e. humans will go extinct.

Solution: Possible, in particular for small n . Depending on the initial value, the zombies might win (since the positive eigenvalue line points in their favour)

The humans will win eventually, i.e. zombies will go extinct.

Solution: Possible, in particular for large n . Depending on the initial value, the humans might win (since the positive eigenvalue line points in their favour)

The number of humans and zombies will cycle endlessly, without either of them becoming extinct.

Solution: Impossible. This would only happen for two purely imaginary eigenvalues.

15. Consider the IVP

$$y'' + 3y' + 2y = \delta(t - 5) - u_{10}(t) \quad y(0) = 0 \quad y'(0) = \frac{1}{2}$$

(a) (5 points) Find the Laplace Transform $Y(s)$ of the solution to this IVP. Simplify as much as possible.

Solution: Applying the Laplace Transform on both sides and using the table:

$$s^2 Y(s) - y'(0) - sy(0) + 3(sY(s) - y(0)) + 2Y(s) = e^{-5s} - \frac{e^{-10s}}{s}$$

Plugging in the initial values:

$$s^2 Y(s) - \frac{1}{2} + 3sY(s) + 2Y(s) = e^{-5s} - \frac{e^{-10s}}{s}$$

Rearranging

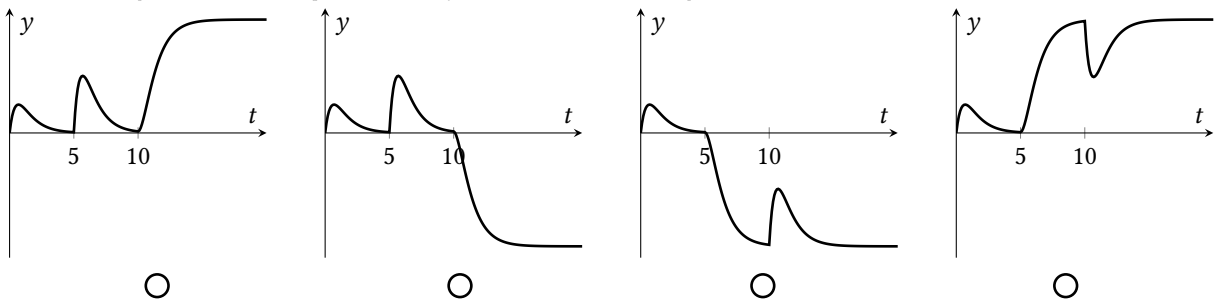
$$Y(s) = \frac{1}{s^2 + 3s + 2} \left(e^{-5s} - \frac{e^{-10s}}{s} + \frac{1}{2} \right)$$

(b) (2 points) Describe how you would now find $y(t)$. You do NOT need to actually find $y(t)$, just describe the general steps that are necessary.

Solution: Use *partial fraction decomposition* to split the fractions. Then use *timeshift property* and the *table* to find the relevant functions.

(c) (3 points) Even without finding the actual equation for $y(t)$ you should be able to tell which of these four plots shows the solution to this IVP. Make a choice and justify.

Do NOT try to find the equation for $y(t)$. It would be very tedious to do so.



Initially, the oscillator moves up due to $y'(0) = \frac{1}{2}$. It is then hit by a positive impulse at $t = 5$ and finally at $t = 10$ a negative force is applied that doesn't go away.

There are now several ways to solve this by way of exclusion. One such way is:

Due to the negative force, only the middle two graphs can be considered. Of the two middle graphs, only the first one has the impulse before the constantly applied force. So that's the one.

The second graph is the correct answer.

16. Consider a continuous function $g(t)$ that has Laplace Transform $G(s)$ and define $f(t) = \int_0^t g(u) du$.

(a) (2 marks) Using the Fundamental Thm. of Calculus, we know that $f'(t) = \boxed{g(t)}$ and $f(0) = \boxed{0}$.

You don't need to justify your answer for part (a).

(b) (3 marks) Use your answer from part (a) and a formula from the table to express the Laplace Transform of $f(t)$ in terms of $G(s)$.

Solution: By the derivative rule for the Laplace Transform: $G(s) = \mathcal{L}\{g(t)\} = \mathcal{L}\{f'(t)\} = sF(s) - f(0) = sF(s)$
Therefore $F(s) = \frac{G(s)}{s}$.

17. In this question, we want to verify that the following equation holds:

$$\mathcal{L}\{t^n\} = \frac{n!}{s^{n+1}}, \quad s > 0 \quad \text{for all integers } n \geq 0$$

In this question you are not allowed to use the table of Laplace transforms.

(a) (3 marks) Assume $n = 0$. Show, using the definition of Laplace Transform, that $\mathcal{L}\{1\} = \frac{1}{s}$, $s > 0$

Solution:

$$\mathcal{L}\{1\} = \int_0^\infty 1 \cdot e^{-st} dt = \lim_{b \rightarrow \infty} \int_0^b e^{-st} dt = \lim_{b \rightarrow \infty} \left[-\frac{1}{s} e^{-sb} + \frac{1}{s} e^{-s \cdot 0} \right] = \frac{1}{s}$$

Note that the last step required using $s > 0$ to get limit zero.

(b) (3 marks) Use int. by parts and the definition of the Laplace Transform to show $\mathcal{L}\{t^n\} = \frac{n}{s} \mathcal{L}\{t^{n-1}\}$, $s > 0$

Solution: We use IBP with $u = t^n$, $dv = e^{-st}$, $du = nt^{n-1}$, $v = -\frac{1}{s} e^{-st}$.

$$\begin{aligned} \mathcal{L}\{t^n\} &= \int_0^\infty t^n e^{-st} dt = \lim_{b \rightarrow \infty} \int_0^b t^n e^{-st} dt = \lim_{b \rightarrow \infty} \left(\left[-t^n \frac{1}{s} e^{-st} \right]_0^b + \int_0^b \frac{1}{s} n t^{n-1} e^{-st} dt \right) \\ &= \lim_{b \rightarrow \infty} \left(b^n \frac{1}{s} e^{-sb} \right) + \frac{n}{s} \int_0^\infty t^{n-1} e^{-st} dt = \frac{n}{s} \mathcal{L}\{t^{n-1}\} \end{aligned}$$

Note that the last step required using $s > 0$ and the fact that the exponential term e^{-bs} dominates the polynomial b^n . The remaining integral is then the definition of the desired Laplace transform.

(c) (1 mark) Explain briefly how the results from part (a) and part (b) give you the formula stated at the top.

Solution: This can be shown using proof by induction. Part (a) gives the base case, whereas part (b) is the induction step.

18. Consider the following differential equation: $x^2 \frac{d^2 y}{dx^2} - x \frac{dy}{dx} + y = 0$.

Assume $x > 0$ and denote $t = \ln x$. Using the chain rule for $y = y(x(t))$, we can observe that $\frac{dy}{dx} = \frac{dy}{dt} \frac{dt}{dx}$ and therefore

$$\frac{dy}{dx} = \frac{1}{x} \frac{dy}{dt}$$

- (a) (2 marks) Use chain rule again to show that

$$\frac{d^2 y}{dx^2} = \frac{1}{x^2} \left(\frac{d^2 y}{dt^2} - \frac{dy}{dt} \right)$$

Solution: Use product rule, then chain rule for the second term.

$$\frac{d^2 y}{dx^2} = \frac{d}{dx} \left(\frac{1}{x} \frac{dy}{dt} \right) = \frac{d}{dx} \left(\frac{1}{x} \right) \frac{dy}{dt} + \frac{1}{x} \frac{d}{dx} \left(\frac{dy}{dt} \right) = -\frac{1}{x^2} \frac{dy}{dt} + \frac{1}{x} \frac{d^2 y}{dt^2} \frac{dt}{dx} = -\frac{1}{x^2} \frac{dy}{dt} + \frac{1}{x} \frac{d^2 y}{dt^2} \frac{1}{x}$$

In the last step, we used that $t = \ln x$ and therefore $\frac{dt}{dx} = 1/x$

Factoring gives the desired answer.

- (b) (2 marks) Substitute our results into the original ODE to show that

$$\frac{d^2 y}{dt^2} - 2 \frac{dy}{dt} + y = 0$$

Solution: No magic here, it's just plugging in both things and regrouping.

- (c) (3 mark) Find the general solution to the ODE in part (b) to obtain $y(t)$.

Solution: This is a second order linear homogeneous ODE with constant coefficients.

The characteristic polynomial $r^2 - 2r + 1 = 0$ has one repeated root $r = 1$.

The general solution is therefore $y(t) = c_1 e^t + c_2 t e^t$.

$y(t) =$

- (d) (1 mark) Use the $y(t)$ that you just found to state $y(x)$.

Solution: Plug in $t = \ln x$ to get $y(x) = c_1 e^{\ln x} + c_2 \ln x e^{\ln x} = c_1 x + c_2 x \ln x$.

$y(x) =$

19. Consider the following partial differential equation with initial and boundary conditions:

$$\begin{aligned}u_{xx} &= u_{tt}, & 0 < x < \pi, & \quad t \geq 0 \\u(x, 0) &= \sin x, & u_t(x, 0) &= 0 \\u(0, t) &= u(\pi, t) = 0.\end{aligned}$$

Assume the solution factorizes as follows: $u(x, t) = X(x)T(t)$.

(a) (2 marks) Using the PDE, fill in the three blanks.

$$\frac{T''(t)}{T(t)} = \frac{X''(x)}{X(x)} = -\lambda$$

(b) (2 marks) Find two ODEs, as well as two boundary conditions for $X(x)$ and an initial condition for $T(t)$.

$$\begin{aligned}X''(x) &= -\lambda X(x) & X(0) &= 0 & X(\pi) &= 0 \\T''(t) &= -\lambda T(t) & T'(0) &= 0\end{aligned}$$

(c) (4 marks) Show that nontrivial solutions to these boundary and initial value problems are given by

$$X_n(x) = \sin nx \quad T_n(t) = \cos nt \quad \text{where } n = 1, 2, \dots$$

Solution: Both equations are second order linear homogenous ODEs with constant coefficients. They have the same characteristic polynomial $r^2 + \lambda = 0$ with roots $r = \pm \sqrt{\lambda}i$.

The general solutions are $X(x) = c_1 \cos \sqrt{\lambda}x + c_2 \sin \sqrt{\lambda}x$ and $T(t) = c_1 \cos \sqrt{\lambda}t + c_2 \sin \sqrt{\lambda}t$

Consider $X(0) = 0$. This requires $0 = c_1 \cos 0 + c_2 \sin 0$ which gives $c_1 = 0$. We are left with $X(x) = c_2 \sin \sqrt{\lambda}x$.

Consider $X(\pi) = 0$. This requires $0 = c_2 \sin \sqrt{\lambda}\pi$. $c_2 = 0$ would give the trivial solution. We want nontrivial solutions as the question states. So we must have $\sqrt{\lambda}\pi = n\pi$ for some integer n . This is only possible if $\sqrt{\lambda} = n$. Since the square root is always nonnegative and since $n = 0$ would again give the trivial solution, we can only have positive integers. Therefore we get solutions $X_n(x) = \sin nx$ for $n = 1, 2, \dots$

Consider $T'(0) = 0$. This requires $0 = T'(t) = -c_1 \sin 0 + c_2 \cos 0$, giving $c_2 = 0$. Using the value for λ that we already found, we get solutions $T_n(t) = \cos nt$

(d) (1 mark) Explain briefly why the following function solves the PDE: $u(x, t) = \sum_{n=1}^{\infty} c_n \sin nx \cos nt$ **Solution:**

This is using the superposition principle. Since the PDE is linear and homogeneous, any linear combination of solutions gives a solution.

(e) (1 mark) Consider the initial condition $u(x, 0) = \sin x$. State the solution $u(x, t)$ matching this initial condition.

Solution: Using part (d) we want $\sin x = u(x, 0) = \sum_{n=1}^{\infty} c_n \sin nx \cos 0 = \sum_{n=1}^{\infty} c_n \sin nx$

This condition is obviously matched if $c_1 = 1$ and all other coefficients are zero. As an alternative to “solving by inspection”, use the formulas for Fourier Coefficients.

The solution therefore is $u(x, t) = \sin(x) \cos(t)$.

TABLE 5.3.1

Elementary Laplace transforms.

	$f(t) = \mathcal{L}^{-1}\{F(s)\}$	$F(s) = \mathcal{L}\{f(t)\}$
1.	1	$\frac{1}{s}, \quad s > 0$
2.	e^{at}	$\frac{1}{s-a}, \quad s > a$
3.	$t^n, \quad n = \text{positive integer}$	$\frac{n!}{s^{n+1}}, \quad s > 0$
4.	$t^p, \quad p > -1$	$\frac{\Gamma(p+1)}{s^{p+1}}, \quad s > 0$
5.	$\sin at$	$\frac{a}{s^2 + a^2}, \quad s > 0$
6.	$\cos at$	$\frac{s}{s^2 + a^2}, \quad s > 0$
7.	$\sinh at$	$\frac{a}{s^2 - a^2}, \quad s > a $
8.	$\cosh at$	$\frac{s}{s^2 - a^2}, \quad s > a $
9.	$e^{at} \sin bt$	$\frac{b}{(s-a)^2 + b^2}, \quad s > a$
10.	$e^{at} \cos bt$	$\frac{s-a}{(s-a)^2 + b^2}, \quad s > a$
11.	$t^n e^{at}, \quad n = \text{positive integer}$	$\frac{n!}{(s-a)^{n+1}}, \quad s > a$
12.	$u_c(t)$	$\frac{e^{-cs}}{s}, \quad s > 0$
13.	$u_c(t)f(t-c)$	$e^{-cs}F(s)$
14.	$e^{ct}f(t)$	$F(s-c)$
15.	$\int_0^t f(t-\tau)g(\tau) d\tau$	$F(s)G(s)$
16.	$\delta(t-c)$	e^{-cs}
17.	$f^{(n)}(t)$	$s^n F(s) - s^{n-1}f(0) - \dots - f^{(n-1)}(0)$
18.	$t^n f(t)$	$(-1)^n F^{(n)}(s)$

You can wait with filling in this page until you are back on the Zoom call with us.
We will then let you know when to fill in the page.

We at U of T want you to feel proud of what you accomplish as a student. Please respect all of the hard work you've done by making sure that the work you do is your own.

We don't expect you to score perfectly on the assessments and there will be some things that you may not know. Using an unauthorized resource or asking someone else for the answer robs you of the chance later to feel proud of how well you did because you'll know that it wasn't really your work that got you there.

Success in university isn't about getting a certain mark, it's about becoming the very best person you can by enriching yourself with knowledge, strengthening yourself with skills, and building a healthy self-esteem based on how much you've grown and achieved. No one assessment captures that but your conscience will stay with you forever.

Make yourself and your loved ones proud of the student that you are by conducting yourself honestly at all times. Hold each other accountable to these standards.

In submitting this assessment ...	Short sentences
... I confirm that my conduct regarding this test adheres to the Code of Behaviour on Academic Matters .	I know the Code.
... I confirm that I have not acted in such a way that would constitute cheating, misrepresentation, or unfairness, including but not limited to, using unauthorized aids and assistance, impersonating another person, and committing plagiarism.	I didn't cheat.
... I confirm that the work I am submitting in my name is the work of no one but myself.	This is only my work.
... I confirm that all pages have been handwritten by myself.	I wrote all pages.
... I confirm that I have not received help from others, whether directly or indirectly.	I didn't receive help.
... I confirm that I have not provided help to others, whether directly or indirectly.	I didn't provide help.
... I confirm that I have only used the aids marked as "OK" on the cover page.	I only used "OK" aids.
... I am aware that not disclosing another student's misconduct despite my knowledge is an academic offence.	I know I must report cheating.

In this box, handwrite the sequence of short sentences (starting with "I know the Code. I didn't cheat...").

Your student number

Your signature

Submission date