

University of Toronto  
Faculty of Applied Science and Engineering

Final Exam  
December 2012

ECE253 – Digital and Computer Systems

Examiner – Prof. Stephen Brown

**Print:**

First Name . . . . . Last Name . . . . .

Student Number . . . . .

1. There are **7** questions and **18** pages. Do **all** questions. The duration of the exam is 2.5 hours.
2. **ALL WORK IS TO BE DONE ON THESE SHEETS.** Use the back of the pages if you need more space. Be sure to indicate clearly if your work continues elsewhere.
3. Closed book. One 2-sided hand-written aid sheet is permitted.
4. No calculators are permitted.

1 [20]	
2 [15]	
3 [10]	
4 [10]	
5 [15]	
6 [15]	
7 [10]	
Total [95]	

1. Short answers:

[3 marks]

(a) Convert the following decimal numbers to 16-bit 2's complement.

i. -800

**Answer** .....

ii. -5120

**Answer** .....

iii. -1028

**Answer** .....

[2 marks]

(b) Consider the addition of 2 four-bit signed numbers  $s_3s_2s_1s_0 = a_3a_2a_1a_0 + b_3b_2b_1b_0$ . Give a logic expression for a function  $z$  that should be set to 1 only when the sum  $S$  is a valid 2's complement result.

**Answer** .....

[2 marks]

(c) What are the differences between the Nios II *ldw* and *ldwio* instructions?

**Answer** .....

.....  
.....  
.....

[3 marks]

(d) Assuming that interrupts are enabled for the Nios II processor, list the steps that the processor takes in response to an IRQ signal being asserted by an I/O device. Describe the various processor registers that are affected, and so on.

**Answer** .....

.....  
.....  
.....  
.....  
.....  
.....  
.....  
.....

[2 marks]

- (e) Use Boolean algebra to derive a minimal sum-of-products expression for the function  $f$ , below. In the boxes on the left specify the number of any identity that you used in that step. Identity numbers are shown at the end of this exam. Use as few steps as possible.

**Identity**

$$f = x_1x_2 + x_3(\bar{x}_1 + \bar{x}_2)$$

.....

.....

.....

.....

.....

.....

.....

.....

[2 marks]

- (f) Use Boolean algebra to show that the following equality is valid. In the boxes on the left specify the number of any identity that you used in that step. Identity numbers are shown at the end of this exam. Use as few steps as possible.

**Identity**

$$\bar{k} \cdot x_3x_4 + k \cdot (x_3 + x_4) = x_3x_4 + k \cdot (x_3 + x_4)$$

.....

.....

.....

.....

.....

.....

.....

.....

.....

.....

[3 marks]

- (g) Consider the function  $f$  shown in the Karnaugh map below. Give both a minimal SOP and POS expression for this function.

		$x_1x_2$			
		00	01	11	10
$x_3x_4$	00	1	0	0	1
	01	0	0	0	0
	11	1	1	1	0
	10	1	1	0	1

**SOP** .....

**POS** .....

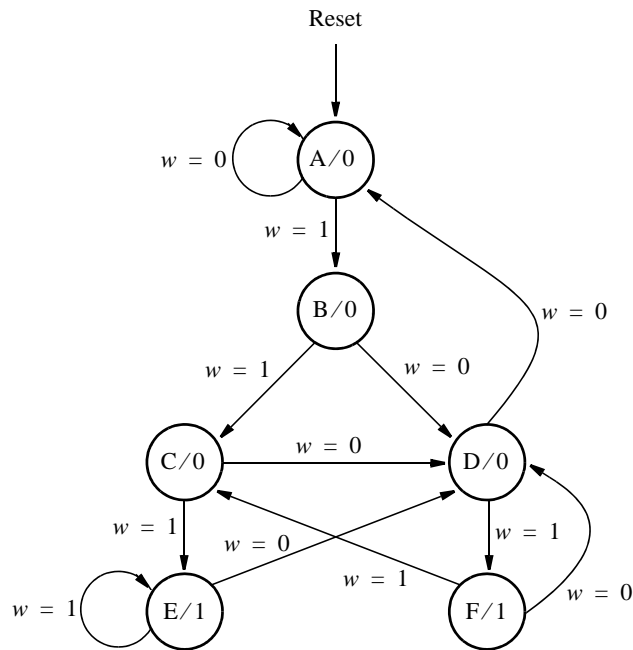
[3 marks]

- (h) Derive and draw a circuit that implements the function  $f = x_3 + x_1x_2$  using only 2-to-1 multiplexers. Your circuit should have **only** 2-to-1 multiplexer symbols, and no logic gates. Use the simplest circuit possible.

## 2. Finite State Machines:

[10 marks]

(a) Consider the state diagram shown below.



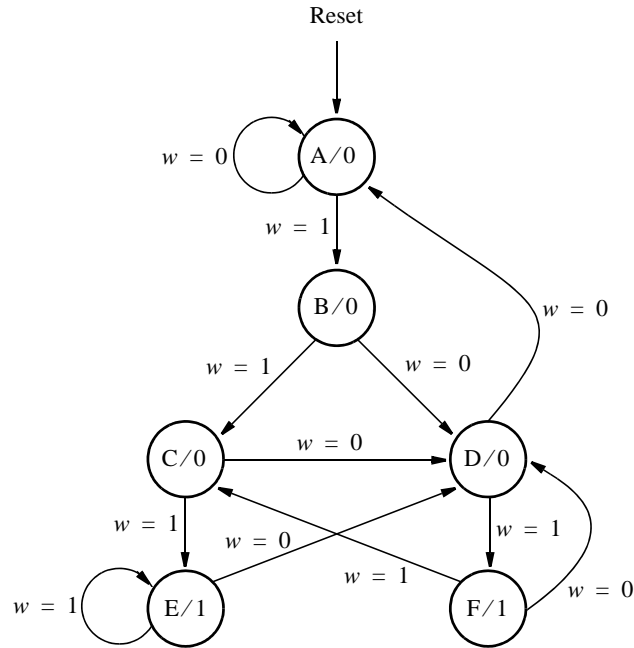
Write complete Verilog code that represents this FSM. Use separate **always** blocks for the state table and the state flip-flops, as done in lectures. Describe the FSM output, which is called  $z$ , using either continuous assignment statement(s) or an **always** block (at your discretion). Assign any state codes that you wish to use. Write your Verilog code in the space below and on the following page.

**Answer:**

**Answer** for Question 2 FSM Verilog code continued. . .

[5 marks]

(b) The state diagram for this question is shown again below.



Assume that a one-hot code is used with the state assignment

$$y_5y_4y_3y_2y_1y_0 = 000001(A), 000010(B), 000100(C), 001000(D), 010000(E), 100000(F)$$

i. Write a logic expression for the signal  $Y_1$ , which is the input of state flip-flop  $y_1$ .

**Answer** .....

ii. Write a logic expression for the signal  $Y_3$ , which is the input of state flip-flop  $y_3$ .

**Answer** .....

### 3. Assembly Language Trace:

[10 marks]

Consider the assembly language program shown below, which was also explained in lectures. This code calls the recursive subroutine named FINDSUM to sum the numbers from 0 to  $N$ . In this code  $N$  is set to the value 2. Note that the address that each instruction would have in memory, assuming that the program starts at address 00000000, is shown to the left of the code.

```

        .text
        .global _start
_start:
00000000    movia    sp, 0x20000
00000008    mov     r2, r0
0000000C    ldw     r4, N(r0)           # data is passed to subroutine in r4
00000010    call    FINDSUM            # result will be in r2
        END:
00000014    br      END                # wait here

        FINDSUM:
00000018    bne     r4, r0, RECURSE
0000001C    add     r2, r0, r0
00000020    ret
        RECURSE:
00000024    subi    sp, sp, 8
00000028    stw     r4, 0(sp)
0000002C    stw     ra, 4(sp)
00000030    subi    r4, r4, 1
00000034    call    FINDSUM

00000038    ldw     r4, 0(sp)
0000003C    add     r2, r4, r2
00000040    ldw     ra, 4(sp)
00000044    addi    sp, sp, 8
00000048    ret

        .data
        N:
        .word      2
        .end

```

If this program is executed on the Nios II processor, what would be the values of the Nios II registers shown below when the program reaches, but has not yet executed, the instruction **add** r2, r0, r0. Also show in the space on the next page the contents of the stack in memory at this point in time.

pc

ra

sp



Answer space for the contents of the stack in memory. For memory values that are not known, if any, write N/A in the corresponding box.

Memory Address	Content
.....	
.....	
.....	
.....	
.....	
.....	
.....	
20000 .....	

#### 4. Assembly Language Debug:

[10 marks]

The Nios II program shown below performs a bubble sort—you implemented such an algorithm in Lab 7. Recall that the data, as shown on the next page, is stored in memory at the location LIST. The first item at LIST is the number of words to be sorted. The list is sorted by the program “in place” in the memory, in descending order. Unfortunately, this code contains some errors. Place an **X** to the left of each instruction that is erroneous, and indicate to the right of the instruction how you would fix this error. Assume that the program is loaded into memory starting at address 0. The code for the SWAP subroutine is on the following page.

		Suggested correction
	<b>.text</b>	
	<b>.global</b> _start	
	_start:	
<input type="checkbox"/>	<b>movia</b> sp, 0	.....
<input type="checkbox"/>	<b>movia</b> r9, LIST	.....
	BEGIN_SORT:	
<input type="checkbox"/>	<b>ldw</b> r20, 0(r9)	.....
	RESTART_SORT:	
<input type="checkbox"/>	<b>add</b> r18, r0, r0	.....
<input type="checkbox"/>	<b>addi</b> r19, r0, 1	.....
<input type="checkbox"/>	<b>addi</b> r4, r9, 4	.....
	SORT_LOOP:	
<input type="checkbox"/>	<b>call</b> SWAP	.....
<input type="checkbox"/>	<b>mov</b> r18, r2	.....
<input type="checkbox"/>	<b>addi</b> r19, r19, 1	.....
<input type="checkbox"/>	<b>addi</b> r4, r4, 1	.....
<input type="checkbox"/>	<b>beq</b> r19, r20, SORT_LOOP	.....
<input type="checkbox"/>	<b>addi</b> r20, r20, -1	.....
<input type="checkbox"/>	<b>bne</b> r18, r0, RESTART_SORT	.....
	END:	
	<b>br</b> END	

```
# SWAP list elements
# Register r4 has the address of the first element to swap, and
# register r4 + 4 is the address of the other element
# Return 1 in register r2 if swap performed, otherwise return 0
```

		Suggested correction
	SWAP:	
	<b>addi</b> sp, sp, -8	.....
	<b>stw</b> r5, 0(sp)	.....
	<b>stw</b> r6, 4(sp)	.....
	<b>add</b> r2, r0, r0	.....
	<b>ldw</b> r5, 0(r4)	.....
	<b>ldw</b> r6, 4(r4)	.....
	<b>bgt</b> r5, r6, SKIP_SWAP	.....
	<b>stw</b> r6, 0(r4)	.....
	<b>stw</b> r5, 4(r4)	.....
	<b>addi</b> r2, r0, 1	.....
	SKIP_SWAP:	
	<b>addi</b> sp, sp, 8	.....
	<b>ldw</b> r5, 0(sp)	.....
	<b>ldw</b> r6, 4(sp)	.....
	<b>eret</b>	.....
	<b>.data</b>	
	LIST:	
	<b>.word</b> 10, 0, 1, 2, 3, 4, 5, 6, 7, 8, 9	
	<b>.end</b>	

5. Assembly Language Subroutine:

[15 marks]

The Nios II processor does not include any hardware for performing a *division* operation, but the Nios II assembly language defines a divide instruction, as:

**div** rC, rA, rB

The result is defined as the integer operation  $rC = rA/rB$ . Since the **div** instruction isn't implemented in the Nios II processor, you are to write a subroutine, called **DIVIDE**, that performs a division operation. The inputs to **DIVIDE** should be passed to the subroutine in registers  $r4$  and  $r3$ , and the result should be returned in register  $r2$ . The result should have the integer quotient of  $r4/r3$  in the least-significant halfword of  $r2$ , and the remainder should be in the most-significant halfword of  $r2$ . Assume that  $r4$  and  $r3$  contain unsigned values, and that  $r3 \neq 0$ .

You need to provide a main program that calls your **DIVIDE** subroutine. Part of this main program is shown below; fill in the rest of the code. The values of arguments  $A$  and  $B$  that are used to produce the result  $C = A/B$  are stored in memory as shown in the code—your main program needs to load these values from memory and pass them to the subroutine. Write the code for **DIVIDE** in the space on the next page. Include **meaningful comments** in your code!

```
.text
.global _start
_start:
```

```
END:
    br    END          # wait here

.data
A:
    .word 10
B:
    .word 3
.end
```

Answer space for the DIVIDE subroutine.

```
        .global    DIVIDE
DIVIDE:
```

## 6. Exception Handler:

[15 marks]

Consider the Nios II main program shown below. It enables interrupts for the pushbutton KEYs (but the interrupt service routine for the pushbutton KEYs isn't used in this question), and then initializes some registers and calls the **div** instruction. As we said in the previous question, the **div** instruction is not implemented in the Nios II processor. This means that when the processor tries to execute this instruction an exception occurs, and the processor automatically branches to the exception handler address (0x20).

```
.text
.global _start
_start:
    movia    sp, 0x20000          # stack starts from a large memory address

    # assume that we need pushbutton KEY interrupts to be enabled
    movia    r15, 0x10000050      # KEY base address
    movi     r7, 0b01010         # set interrupt mask bit for KEY3 and KEY1
    stwio    r7, 8(r15)          # interrupt mask register is (base + 8)

    # enable Nios II processor interrupts
    movi     r7, 0b010           # set interrupt mask bit for irq1 (KEYs port)
    wrctl    ienable, r7         # write to control register
    movi     r7, 1
    wrctl    status, r7          # turn on Nios II interrupt processing

DO_DIV:
    movi     r4, 10
    movi     r3, 3
    div      r2, r4, r3

    # there would be additional code here in a real program ...
IDLE:
    br       IDLE
.end
```

You are to write the exception handler for this main program, in the space on the next page. The exception handler has to check whether it has been called due to an **IRQ**, or due to an exception. If an exception, then your code has to check if the exception has been caused by the **div** instruction. If this is the cause of the exception, then simply call the **DIVIDE** subroutine that you wrote in Question 5. This means that your solution for this question works only for the exact instruction **div r2, r4, r3**, because these are the registers used in your **DIVIDE** subroutine. Make sure that you return properly from the exception handler to the main program, with the division result in the right register. Include **meaningful comments** in your code!

To check if the exception is caused by a **div** instruction, you need to know the format of the **OPCODE** for **div**, which would be produced by the Assembler for this program. The **OPCODE** format of the Nios II **div** instruction is shown at the end of this exam.

Answer space for the exception handler. Fill in the missing parts of the code.

```
        .section    .exceptions, "ax"
        .global     EXCEPTION_HANDLER
EXCEPTION_HANDLER:
        rdctl       et, ipending
        beq         et, r0, SKIP_DEC      # it is an exception, not an IRQ
        subi        ea, ea, 4             # decrement ea by one instruction for IRQ
SKIP_DEC:
        subi        sp, sp, .....       # save registers, then check for div instruction
```

```
CHECK_irq1:                                # KEYs are interrupt level 1
        andi        r22, et, 0b10
        beq         r22, r0, END_ISR      # other irq levels not handled in this code
        call        KEY_ISR               # code for this ISR is not shown here
END_ISR:
                                           # restore registers
```

```
.end
```

7. Exception Handler (Advanced):

[10 marks]

In Question 6 you called your `DIVIDE` subroutine from Question 5 to implement the division operation. But your `DIVIDE` subroutine works only for the exact instruction `div r2, r4, r3`. If the operand registers are not exactly `r2, r4, r3`, then your `DIVIDE` subroutine can't be used to implement the `div` instruction. For this question you are to write a somewhat more general `DIVIDE` subroutine that will work for any register operands from `r2` to `r6`. For example, it has to work with `div r2, r3, r4`, or `div r6, r2, r3`, or `div r5, r4, r2`, and so on. This means that your new `DIVIDE` subroutine has to examine the `OPCODE` that caused the exception to determine what register operands are involved. Assume that only registers in the range of `r2` to `r6` will be used, and make the same assumptions as for Question 5 regarding the division operation ( $rC = rA/rB$ , unsigned integers, argument  $rB \neq 0$ , quotient and remainder in `rC`).

Complete the code below (additional space is provided on the next page). Think about the comments that are shown in the code—they provide a *hint* about how your `DIVIDE` subroutine can access the contents of registers `rA`, `rB`, and `rC`. Include **meaningful comments** in your code!

```

.global    DIVIDE
DIVIDE:
    subi    sp, sp, 28    # reserve space on the stack
    stw     r2, 8(sp)     # r2 saved at sp + 2 words
    stw     r3, 12(sp)    # r3 saved at sp + 3 words
    stw     r4, 16(sp)    # r4 saved at sp + 4 words
    stw     r5, 20(sp)    # r5 saved at sp + 5 words
    stw     r6, 24(sp)    # r6 saved at sp + 6 words

```



**Answer** for Question 7 DIVIDE code continued...

### Boolean Identities

- 12a.  $x \cdot (y + z) = x \cdot y + x \cdot z$  *Distributive*  
 13a.  $x + x \cdot y = x$  *Absorption*  
 14a.  $x \cdot y + x \cdot \bar{y} = x$  *Combining*  
 15a.  $\overline{x \cdot y} = \bar{x} + \bar{y}$  *DeMorgan's theorem*  
 16a.  $x + \bar{x} \cdot y = x + y$   
 17a.  $x \cdot y + y \cdot z + \bar{x} \cdot z = x \cdot y + \bar{x} \cdot z$  *Consensus*

### Nios II div Instruction OPCODE Format

31	30	29	28	27	26	25	24	23	22	21	20	19	18	17	16	15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
A					B					C					0x25					0					0x3a						