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Coordinate Systems 1

1.1 Cartesian Coordinates

Definition:

• Position vector

$$\mathbf{R} = x\mathbf{a}_x + y\mathbf{a}_y + z\mathbf{a}_z \tag{1}$$

• Differential length elements

$$\mathbf{dl}_x = \mathbf{a}_x dx, \quad \mathbf{dl}_y = \mathbf{a}_y dy, \quad \mathbf{dl}_z = \mathbf{a}_z dz$$
 (2)

• Differential surface elements

$$dS_x = a_x dy dz, \quad dS_y = a_y dz dx, \quad dS_z = a_z dx dy$$
(3)

• Differential volume elements

$$dV = dxdydz (4)$$

1.2 Cylindrical Coordinates

Definition:

• Position vector

$$\mathbf{R} = r\mathbf{a}_r + z\mathbf{a}_z \tag{5}$$

• Differential length elements

$$\mathbf{dl}_r = \mathbf{a}_r dr, \quad \mathbf{dl}_\phi = \mathbf{a}_\phi r d\phi, \quad \mathbf{dl}_z = \mathbf{a}_z dz$$
 (6)

• Differential surface elements

$$\mathbf{dS}_r = \mathbf{a}_r dz dr, \quad \mathbf{dS}_\phi = \mathbf{a}_\phi r dz d\phi, \quad \mathbf{dS}_z = \mathbf{a}_z dr d\phi \tag{7}$$

Spherical Coordinates 1.3

Definition:

Electric Field $\mathbf{2}$

Coloumb's Law

Definition:

$$\mathbf{F}_{12} = \frac{q_1 q_2}{4\pi\epsilon_0} \frac{\mathbf{R}_2 - \mathbf{R}_1}{|\mathbf{R}_2 - \mathbf{R}_1|^3} \tag{8}$$

2.2 **Guass Law**

Definition:

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0} \tag{9}$$

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$$\oint_S \mathbf{E} \cdot \mathbf{dS} = \frac{Q_{\text{enc}}}{\epsilon_0}$$
(9)

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- 3 Electrostatics
- 3.1
- 4 Magnetostatics
- 4.1
- 5 Faraday's Law, Ampere-Maxwell Law
- 5.1
- 6 Currents
- 6.1