TRADES

TRADES v2.10.0 by Luca Borsato - 2016

Most of the information can be found in the paper by Borsato et al. (2014) and at the webpage TRADES@ESPG.

Feel free to use or modify the code, but please citeBorsato et al. (2014).

Comments are welcome!

TRADES@github

WARNING:

only tested on a Unix/Linux machine (i.e., Centos Rocks 5.3, Ubuntu > 12.04 and derivatives)

Please use gfortran version greater than 4.8.1 . Previous versions could fail to compile.

MPI/open-MPI required in order to compile the PolyChord library. In the future this will be fixed.

openMP required to compile parallel versions TRADES

TRADES user guide

- 1. Introduction
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Introduction

We have developed a computer program (in Fortran 90, openMP, and MPI) for determining the possible physical and dynamical configurations of extra-solar planetary systems from observational data, known as TRADES, which stands for TRAnsits and Dynamics of Exoplanetary Systems.

The program TRADES models the dynamics of multiple planet systems and reproduces the observed transit times (T_0 , or mid-transit times) and radial velocities (RVs). These T_0 s and RVs are computed during the integration of the planetary orbits.

Hereafter, I will use the reduced chi-squared ($\chi^2_r = \chi^2/\mathrm{dof}$) as the fitness parameter, but it would be also possible to use a $\chi^2_{\mathrm{w,dof}}$ weighted/scaled by the number of each type of data set: transits and radial velocities.

We have developed TRADES from zero because we want to avoid black-box programs, it would be easier to parallelize it with openMP, and include additional algorithms.

To solve the inverse problem, TRADES can be run in different modes:

• integration:

it runs a simple integration of the orbits of the planetary system calculating the T_0s and the RVs.

• grid search:

TRADES samples the orbital elements of one perturbing body (all the parameters are allowed in the grid, but remember that the number of simulations will increase hugely). The grid parameters can be evenly sampled on a fixed grid by setting the number of steps, or the step size, or by a number of points chosen randomly within the parameter bounds. For any given set of values, the orbits are integrated, and the residuals between the observed and computed $T_0 s$ and RVs are computed. For each combination of the parameters, the LM algorithm can be called and the best case is the one with the lowest residuals (lowest reduced chi-squared = $\chi^2/\text{dof} = \chi_{\rm r}^2$).

• Levenberg-Marquardt (LM , lmdif from MINPACK) algorithm:

After an initial guess on the orbital parameters of the perturber, which could be provided by the previously described grid approach, the LM algorithm exploits the Levenberg-Marquardt minimization method to find the solution with the lowest residuals. The LM algorithm requires the analytic derivative of the model with respect to the parameters to be fitted. Since the T_0 s are determined by an iterative method and the radial velocities are computed using the

numerical integrator, we cannot express these as analytic functions of fitting parameters. We have adopted the method described in Moré et al. (1980) to compute the Jacobian matrix, which is determined by a forward-difference approximation. The <code>epsfcn</code> parameter, which is the parameter that determines the first Jacobian matrix, is automatically selected in a logarithmic range from the machine precision up to 10^{-6} ; the best value is the one that returns the lower $\chi^2_{\rm r}$. This method has the advantage to be scale invariant, but it assumes that each parameter is varied by the same <code>epsfcn</code> value (e.g., a variation of 10% of the period has a different effect than a variation of the same percentage of the argument of pericenter).

• genetic algorithm (GA or PIK , we used the implementation named PIKAIA , Charbonneau 1995):

the GA mode searches for the best orbit by performing a genetic optimization (e.g. Holland 1975; Goldberg 1989), where the fitness parameter is set to the inverse of the χ^2_r . This algorithm is inspired by natural selection which is the biological process of evolution. Each generation is a new population of *offspring* orbital configurations, that are the result of *parent* pairs of orbital configurations that are ranked following the fitness parameter. A drawback of the GA is the slowness of the algorithm, when compared to other optimizers. However, the GA should converge to a global solution (if it exists) after the appropriate number of iterations.

At the moment if the GA after the predefine iteration has a fitness (or χ_r^2) higher than 1000, it will continue (it stops if it reaches the iteration step with fitness lower than 1000 or if it reaches fitness <= 1.).

• particle swarm optimization (PSO , Tada 2007):

the PSO is another optimization algorithm that searches for the global solution of the problem; this approach is inspired by the social behavior of bird flock and fish school (e.g., Kennedy & Eberhart 1995; Eberhart 2007). The fitness parameter used is the same as the GA , the inverse of the $\chi^2_{\rm r}$. For each *particle*, the next step (or iteration) in the space of the fitted parameters is mainly given by the combination of three terms: random walk, best *particle* position (combination of parameters), and best *global* position (best orbital configuration of the all particles and all iterations).

• PolyChord (PC , Handley et al., 2015):

PolyChord is a novel nested sampling algorithm tailored for high dimensional parameter spaces. In addition, it can fully exploit a hierarchy of parameter speeds such as is found in CosmoMC and CAMB. It utilises slice sampling at each iteration to sample within the hard likelihood constraint of nested sampling. It can identify and evolve separate modes of a posterior semi-independently and is parallelised using openMPI. PolyChord is available for download at PolyChord-CCPForge

In each mode, TRADES compares observed transit times ($T_{0,\rm obs}$) and radial velocities (RV $_{\rm obs}$) with the simulated ones ($T_{0,\rm sim}$ and RV $_{\rm sim}$). From version 1.1.2 of TRADES, it is possible to use different set of RV, with different RV offset (the so-called gamma point); TRADES will compute a γ for each RV data set.

The *grid* search is a good approach in case that we want to explore a limited subset of the parameter space or if we want to analyze the behavior of the system by varying some parameters, for example to test the effects of a growing mass for the perturbing planet.

GA and PSO are good methods to be used in case of a wider space of parameters. The orbital solution determined with the GA or the PSO method is eventually refined with the LM mode.

PC is well described in the paper by Handle et al. (2015), and it uses a Bayesian approach with the nested sampling. It works also on parameter bounds, but it would be better to limit the boundaries, and not used them as wide as those for GA and PSO.

For each mode, but PC , TRADES can perform a **bootstrap** analysis to calculate the interval of confidence of the best-fit parameter set. We generate a set of T_0 s and RVs from the fitted parameters, and we add a Gaussian noise having the calculated value (of T_0 s and RVs) as the mean and the corresponding measurement error as variance, scaled by the $\sqrt{\chi^2_{\rm reduced}}$. We fit each new set of observables with the LM with default options. We iterate the whole process thousands of times to analyze the distribution for each fitted parameter.

For the mathematical and computational description see Borsato et al. (2014).

- TRADES source is available at github.com/lucaborsato/trades.
 Download the .zip file or clone the repository (see github help).
- 2. Extract the .zip file in your drive or enter the cloned repository. It should contain a README.md file, bin/, src/, and pytrades/ folders.

The src/ folder should countains the following f90 source files:

- o Module source files: parameters.f90 random_trades.f90 convert_type.f90 lin_fit.f90 celestial_mechanics.f90 init_trades.f90 statistics.f90 timing.f90 rotations.f90 sort.f90 gls_module.f90 eq_motion.f90 output_files.f90 numerical_integrator.f90 radial_velocities.f90 transits.f90 ode_run.f90 derived_parameters_mod.f90 fitness_module.f90 grid_search.f90 lm.f90 pikaia.f90 util_sort.f90 util_qmc.f90 opti_pso.f90 gaussian.f90 bootstrap.f90 PolyChord_driver.f90 driver.f90
- o PolyChord folder PolyChord/ with source files: utils.f90 abort.F90 settings.f90 params.f90 array_utils.f90 priors.f90 mpi_utils.F90 calculate.f90 random_utils.F90 chordal_sampling.f90 run_time_info.f90 clustering.f90 read_write.f90 feedback.f90 generate.F90 ini.f90 nested_sampling.F90
- o Old main TRADES file (DO NOT USED IT, to be converted into a library asap): trades.f90
- simple integration+ LM +bootstrap main: trades_int_lm_bootstrap.f90
- o simple grid main: trades_grid.f90
- o simple PIK and PSO main: trades_pik_pso.f90
- o **simple** PC **main:** trades_polychord.f90
- o Makefile: Makefile
- python script to create example simulation folder: createSimFile.py
 Look at section 6. for the pytrades/ folder (install and execution).
- 3. Edit the Makefile with your Fortran 90 MPI compiler, and with the needed compiling options.
 - o flag cc for the compiler to use. From the implementation of Pc the mpif90 must be used;
 - flag CFLAGS for the compiler options;
 from the implementation of PC the -ccp preprocessor option must be used
 add options or uncomment following rows for other debugging options
 - flag COPT for the compiler optimization
 from the implementation of PC the -ccp preprocessor option must be used
 - o flag CFLAGS2 for the opemMP version
 - flag TARGET_SER_X is relative path and executable name for the serial program
 - flag TARGET_OMP_X is relative path and executable name for the openMP parallel program
 - flag TARGET_MPIOMP is relative path and executable name for the MPI+openMP parallel program (it compiles only old trades.f90)
 - o flag TARGET_PC is relative path and executable name for the PC program

4. To compile:

- o serial-debug mode, type: make serial_debug It creates a executable file trades_s_xxx and trades_polychord in the bin/ folder.
- o serial-release mode, type: make serial_release
 It creates a executable file trades_s_xxx and trades_polychord in the bin/ folder.
- o openMP-debug mode, type: make omp_debug
 It creates a executable file trades_o_xxx and trades_polychord in the bin/ folder.
- o openMP-release mode, type: make omp_release

 It creates a executable file trades_o_xxx and trades_polychord in the bin/ folder.
- o openMP-MPI-debug mode, type: make mpi_omp_debug
 It creates a executable file trades_mo and trades_polychord in the bin/ folder.

o openMP-MPI-release mode, type: make mpi_omp_release

It creates a executable file trades_mo and trades_polychord in the bin/ folder.

Remember to type make clean to remove *.o and *.mod files before re-compiling TRADES .

Remember to type make clean_libchord to remove PolyChord files and library.

Remember to type make cleanall to remove *.o , *.mod , and all the executable files before re-compiling TRADES .

To compile in parallel mode the openMP libraries must be properly installed (as suggested by your Linux distribution) and the MPI (Open-MPI) libraries and compilers.

2016-01-28 WARNING:

If the MPI compiler is different from the compiler used for the module mpi.mod , the program will fail to compile. Please, change properly your Fortran-MPI in the Makefile .

How to run TRADES

Different ways to launch TRADES:

- export the path of the executable (trades_s, trades_o, and trades_mo) in your ~/.bahsrc o ~/.profile:
 export PATH=\$PATH:/path/to/trades/executables
- it is possible to execute trades from the bin/ folder by typing:

```
./trades_s_xxx
./trades_o_xxx
./trades_polychord
./trades_mo
```

WARNING:

Before running TRADES in parallel with open-MP (trades_o_xxx) remember to set the number of cpus (Ncpu) to use by exporting:

```
OMP_NUM_THREADS=Ncpu
export OMP_NUM_THREADS
```

Put this in a script or type it in a terminal; in short way:

```
export OMP_NUM_THREADS=Ncpu
```

In order to use trades with MPI+openMP remember to specify the <code>OMP_NUM_THREADS</code> and the MPI processes <code>mpiexec - n N_mpi_process trades_mo ...</code>

If TRADES has been launched without any arguments, it will search for the needed files in the current folder: e.g.:

```
cd /home/user/Simulation/
trades_s_xxx
```

it is equal to type:

```
cd /home/user/Simulation/
trades_s_xxx .
```

or:

```
cd /home/user/
trades_s_xxx /home/user/Simulation/
```

In any of these three cases, TRADES will write the output files in the folder /home/user/Simulation/

Provide orbital elements (and boundaries) in the bodies file.

```
Algorithm selection in arg.in:
progtype:

1. grid
2. integration + LM + bootstrap
3. PIKAIA (+ LM + bootstrap)
4. PSO (+ LM + bootstrap)
5. PolyChord
```

Files needed by TRADES

In the src/ folder you can find the createSimFile.py python script that allows to create all the files needed by TRADES . The files are based on Kepler-9 system, with the original data T_0 and RV) from the discovery paper by Holman et al. (2010).

List of the files with explanation:

```
arg.in bodies.lst star.dat b.dat c.dat lm.opt pikaia.opt pso.opt PolyChord.opt obsRV.dat NB2_observations.dat NB3_observations.dat
```

arg.in : file with program arguments, needed for the integration, fitting type, output files.
 Example file arg.in .

2. bodies.1st: file with list of the files with the parameters for each body.

The first column is always the file name of the body, followed by 0 or 1 for each parameter. 0 means do not fit it, 1 means fit it.

The first row is always the star file with the Mass and Radius fitting parameter type.

From the second row, each line is the body file name followed by the parameters to fit in this order:

 $\verb|mass radius| period eccentricity| argument_of_pericenter| mean_anomaly| inclination| longitude_of_node|.$

Remember that the number of the lines of this file has to match the NB parameter in the arg.in file.

Example file bodies.1st

 star.dat: Mass (and sigma) and Radius (and sigma) of the star in Solar units. First row the Mass, second the Radius.

In the code will be identified with the id == 1.

Example file star.dat

b.dat: file with parameters of the planet in the second row of the bodies.lst, that is in the code will be identified with the id == 2.

Each row is a different parameter (3 columns + flag for grid), in the order:

```
mass min max [M_Jup]
radius min max [R_Jup]
period min max [days]
semi-major_axis min max [au]
eccentricity min max
argument_of_pericenter min max [deg]
mean_anomaly min max [deg]
time_of_pericenter_passage min max [JD]
inclination min max [deg]
longitude_of_node min max [deg]
```

When not specified the \min max values are set by default (i.e. eccentricity < 1, angles between 0 and 360 deg, inclination between 0 and 180 deg, radius < 5 R_Jup, and mass < 1 M_Sun in 'M_Jup. In the grid mode the mean of the columns is: \min max step type. The step is used as true step, or step number, and so on accordingly to the fourth column type. Keywords for column 4 are: ss (means step size), rn (random number), and sn (step number). Alternatives: semi-major axis in au instead of period (set period greater than 9000000. , while setting semi-major axis equal to 999. will let

you use the period); time of passage at pericentre is used if mean anomaly is greater than 999. , while set time of passage at pericentre greater than 9.8 to use mean anomaly . Example file [b.dat'] (trades example/b.dat)

• c.dat : same as file b.dat , but with different parameter values for the body in the third row in bodies.lst , that is in the code will be identified with the id == 3.

Example file c.dat

3. lm.opt : parameter options for the Levenberg-Marquardt algorithm; they are based on the original manual. Keep it as it for standard analysis.

Example file 1m.opt

4. pikaia.opt : parameter options for the GA algorithm. The most important parameters to tune are

(1pik) the number of individuals (row 1, ctrl(1)), that is the number of set of parameters for each generation;

(2pik) the number of generation (row 2, ctrl(2)), that is the number of iteration that GA has to perform, the last iteration returns the best set of parameters;

(3pik) the seed (row 13), that is a integer number that defines the seed for the random generator, if you keep the same value it repeat the same analysis;

(4pik) the wrtAll (row 14) is a parameter that defines if you want to that the GA writes all the individuals for each generation, set it to 1 to write, 0 not write;

(5pik) the nGlobal (row 15) is the number of global search to perform with the GA, each search returns a solution, and the seed of each analysis is different (seed + i, i=1..nGlobal).

Example file pikaia.opt

5. pso.opt: parameter options for the PSO algorithm. The rows 1, 2, 4, 5, and 6 are the same parameters explained for the pikaia.opt file.

In particular:

(1pso) row 1 and (2pik) 2 are exactly the same as in pikaia.opt;

(3pso) row 3 is an integer that specifies when write a summary during the PSO analysis;

(4pso) row 4 is the same as (4pik) row 14 in pikaia.opt;

(5pso) row 5 is the same as (5pik) row 15 in pikaia.opt ;

(6pso) row 6 is the same as (3pik) row 13 in ${\tt pikaia.opt}$.

Example file pso.opt

6. Polychord.opt: parameter options for the PC algorithm. It is quite well self explained; for further information check the Polychord webpage.

Example file PolyChord.opt

7. obsRv.dat: list of radial velocities (RVs) data.

Columns description:

- (1) RV observation time (JD, or time in same units of the integration time);
- (2) observed RVs in meter per seconds;
- (3) observed RV uncertainties in meter per seconds;
- (4) ID of the RV dataset, so if you have only one dataset set all column to 1 , else increas value untill the number of different datasets, i.e., 1 , 2 for 2 datasets (2 different facilities, or one facility before and after upgrade).

Example file obsRV.dat

8. NB2_observations.dat : list of transit times (T_0 s) observed for planet in the second row of bodies.lst , i.e., b.dat is planet 2.

Columns description:

- (1) transit epoch (N), an integer number that identifies the transit w.r.t. a reference transit time $T_{\rm ref}$ and refined by a linear ephemeris of kind: $T_N = T_{\rm ref} + P_{\rm ref} \times N$;
- (2) the transit time (T_0) in JD or the same time unit of the integration/epoch/start time;
- (3) the uncertainty on the $\,T_0\,$. Example file $\,$ NB2_observations.dat
- 9. NB3_observations.dat : same kind of file NB2_observations.dat , but for the planet in the third row of

```
bodies.lst , i.e., c.dat is planet 3. Example file NB3_observations.dat
```

10. derived_boundaries.dat : this file a special file.

If you have some derived parameters (or other values) that can reduce your parameter space you have to create this file in your simulation folder.

if the argument secondary_parameters in arg.in file is set to 0, this file will not be used.

If secondary_parameters = 1 , but the file does not exist it will not be used (no derived parameters will be checked).

The file should have a line for each parameter, the name in the first column (please keep it short), the min and the max value in the 2nd and 3rd column. Keep last line empty so the code can determine the end of file.

derived_boundaries.dat example:

```
# name phase_min phase_max
ph2 34. 180.
ph3 180. 270.
```

In order to use the derived parameters you have to modify by your own the derived_parameters_mod.f90 . In fitness module.f90 check which subroutines/fuctions will be called to 'check derived' or 'fix derived' parameters.

Output files by TRADES

Each algorithm will write different files, and depends on the flag used in the arg.in and in the *.opt files. Each file should have an self-explaning header.

1. integration: depends only on arg.in file

```
\label{local_model} \# ID\_\#LM\_rotorbit.dat \ , \quad \# ID\_\#LM\_NB\#\_elements.dat \ , \quad \# ID\_\#LM\_NB\#\_tra.dat \ , \\ \# ID\_\#LM\_gls\_output.dat
```

 $\#ID_\#LM_rotorbit.dat$, if wrtorb = 1, where #ID is the simulation ID, #LM is the Levenberg-Marquardt flag (lmon = 0 or 1). Columns: 1 Time in JD; 2 Light-Time Travel Effect in days (llmon = 0); 3:3+NB*6 {X,Y,Z,VX,VY,VZ} for each body (NB=number of bodies); last column is the radial velocity (RV) of the star due to the planets in m/s.

#ID_#LM_constants.dat , if wrtcon = 1 , naming convenction as previous. Columns: 1 Time in JD; 2 momentum; 3 delta between initial and current momentum; 4 Total Energy; 5 delta between initial and current Total Energy.

```
\label{eq:lower_scargle} $$\#\text{ID}_\#\text{LM}_gls\_output.dat} \ , \ it \ is \ the \ output \ of \ the \ General \ Lomb-Scargle(GLS) \ applied \ to \ the \ residuals: \\ res = RV_{obs} - RV_{sim} \ .
```

#ID_#LM_NB#_elements.dat , if wrtel = 1 , naming convenction as previous, plus the body id NB#, starting from 2 to the number of bodies used. Columns: 1 Time in JD; 2 Period in days, 3 semi-major axis in astronomical unit (au), 3 eccentricity, 4 inclination in degrees, 4 mean anomaly in degrees, 5 argument of the pericenter in degrees, 6 longitude of the node in degrees, 7 true anomaly in degrees, 8 difference between time of refence (epoch) and time of the passage of pericenter tau in days

#ID_#LM_NB#_tra.dat , if idtra > 0 , naming convenction as previous. Columns: 1 trasit time, 2 LTE, 3 firt contact time, 4 second contact time, 5 third contact time, 6 fourth contact time, 7:7+NB*6 state vector {X,Y,Z,VX,VY,VZ} for each body (NB=number of bodies).

Python Library

TRADES can now be used in python scripts, thanks to f2py.

In the <code>src/</code> folder there is the <code>pytrades_lib.f90</code> that is the library that interface <code>TRADES</code> to python.

Compile:

- cd src/
- debug mode: make pyomp_debug

• release mode: make pyomp_release

It creates the pytrades_lib.so and it copies it into the folder ../pytrades/

Check if in the src/ folder there is an hidden file .f2py_f2cmap that contains one row: dict(real=dict(sp='float', dp='double'))

Run scripts:

In folder pytrades/ : pytrades_lib.so , constants.py , ancillary.py , trades_pso2emcee.py .

The script to run is trades_pso2emcee.py , that shows how to call the pytrades_lib and how to combine PSO algorithm with emcee .

Run as python trades_pso2emcee.py -h for instruction on the all the command line arguments to provide.

The ancillary.py file has different functions to write and read output files from PSO and emcee and other stuff helpful to manage the output of the simulations.

Check also other files in the pytrades folder to understand how to use the python library.

TO BE CONTINUED

Changes/Log

sorry, I will not be able to report all the small changes...

```
TRADES 2.10.0
```

From the python library (pytrades_lib) it is possible to initialise TRADES without read files and given a set of orbital parameters, times of radial velocities, and transit epochs (integer numbers that identify each transit w.r.t. a transit of reference) it returns the simulated radial velocities and transit times.

To use this feature I added in the folder pytrades a test file trades_test_20161116.py. Be aware that the radial velocities and transit times have been read from 2 files, so modify it accordingly to your file/data.

Added more files in pytrades folder and added files to plot and summarise simulation with emcee .

```
TRADES 2.9.1
```

Small bugfixes in check of the physical parameters.

Added optional argument for debug in the output subroutine in ode_run .

```
TRADES 2.9.0
```

Introduced flag in arg.in file: oc_fit .

oc_fit = F is false, it means that the difference between the observed transit times ($T0_obs$) and the simulated ($T0_sim$) is used to compute the χ^2 ;

oc_fit = T is true, it means that χ^2 is computed from the amplitude of the TTV, based on the O-C for the observed (oc_obs) and simulated data (oc_sim):

```
OC_obs = T0_obs - T0_lin, obs , where T0_lin, obs is the linear ephemeris of the observed data and
```

```
OC_sim = TO_sim - TO_lin, sim , where TO_lin, sim is the linear ephemeris of the simulated transit times.
```

```
TRADES 2.8.0
```

Python library of TRADES has been tested and now is public.

In bodies.1st file user can specify if a planet should transit or not.

At the end of each planet row (after 0/1 fit-flag and before the #), user adds a T (or leaves blank) if planet is allowed to transit, otherwise adds an F.

Example:

```
in bodies.lst row b.dat 1 0 0 0 0 0 0 0 T is equal to b.dat 1 0 0 0 0 0 0 : planet b could transit. in bodies.lst row b.dat 0 0 0 1 0 0 0 0 F : planet b could not transit (in case it discards the solution).
```

Converted all logical values in a consistent way.

TRADES 2.7.0

Fitting parameters examples:

```
in bodies.lst row b.dat 1 0 0 0 0 0 0 0 0 : mass_planet / mass_star
in bodies.lst row b.dat 0 0 0 1 0 0 0 0 : eccentricity
in bodies.lst row b.dat 1 0 0 1 1 0 0 0 : mass_planet / mass_star , e*cos(w) , e*sin(w)
in bodies.lst row b.dat 0 0 0 0 1 1 1 0 : argument_of_pericenter , mean longitude (lambda) , inclination
in bodies.lst row b.dat 1 0 0 1 1 1 1 1 : mass_planet / mass_star , e*cos(w) , e*sin(w) , lambda ,
i*cos(lN) , i*sin(lN)
```

TRADES 2.6.0

The old main trades.f90 has been replaced (still in the sources, it compiles) by small easier-to-understand mains. As for the version 2.5.1 the user has to change the arg.in accordingly to the purpose. See.

During RV fit, TRADES will run a GLS periodogram (Zechmeister and Kurster, 2009) and look for peaks close ($\protect\ P = \protect\ P = \pro$