Physics HW 2

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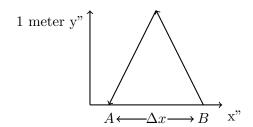
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1 The Invariant

s'' frame

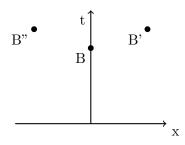


$$\Delta t^{2} - (-\Delta x)^{2}$$

$$= (2\sqrt{1 + \frac{\Delta x^{2}}{4}})^{2} - (-\Delta x)^{2}$$

$$= (4 - \Delta x)^{2} - (\Delta x)^{2}$$

$$= 4$$



2 Michelson-Morley experiment

In the stationary frame speed, time, and length are constant

$$L_x = L_y$$

In the frame with motion, though

$$t_y = 2\sqrt{l^2 + \frac{\Delta x^2}{4}}$$

$$t_y = 2\sqrt{l^2 + \frac{(\beta t_y)^2}{4}}$$

$$t_y^2 = 4(l^2 + \frac{(\beta t_y)^2}{4})$$

$$t_y^2 = 4l^2 + \beta^2 t_y^2$$

$$t_y^2 - \beta^2 t_y^2 = 4l^2$$

$$t_y^2 (1 - \beta^2) = 4l^2$$

$$t_y = \frac{2l}{\sqrt{1 - \beta^2}}$$

$$t_x = \frac{l'}{1+\beta} + \frac{l'}{1-\beta}$$

$$t_x = \frac{l'[(1-\beta) + (1+\beta)]}{1-\beta^2}$$

$$t_x = \frac{2l'}{1-\beta^2}$$

$$l = \gamma l'$$

$$l' = \frac{l}{\gamma}$$

$$t_x = \frac{2l}{\gamma(1 - \beta^2)}$$

$$t_x = \frac{2l\sqrt{1 - \beta^2}}{1 - \beta^2}$$

$$t_x = \frac{2l}{\sqrt{1 - \beta^2}}$$

$$t_x = t_y$$

4 Provisions in space

$$\beta = \frac{1}{2}$$

$$\gamma = \frac{1}{\sqrt{1 - 0.5^2}}$$

$$\gamma = \frac{1}{\sqrt{0.75}}$$

$$t = 20 \text{ years}$$

$$20 = \gamma t$$

$$t = 20\sqrt{0.75}$$

$$t = 10\sqrt{3} \text{ years}$$

$$t = 6322 \text{ days}$$

6322 meals.

3 Moving Balls

B because the length contraction will occur on the axis of movement.

$$\beta_x = \frac{\beta_x' + \beta}{1 + \beta \beta'}$$

$$\beta_x' = \frac{\beta_x'' + \beta'}{1 + \beta' \beta_x''}$$

$$\beta_x' = \frac{0.9 + 0.9}{1 + 0.9(0.9)}$$

Velocity Addition

$$\beta_x' = 0.994475$$

$$\beta_x = \frac{(0.994475) + 0.9}{1 + 0.9(0.994475)}$$

$$\beta_x = 0.999708c$$

5

6 Break down of Galilean 8 Euclidean "slope" transfor-Transformations mations

$$t' = \gamma t$$

$$0.99t = t\sqrt{1 - \beta^2}$$

$$0.99 = \sqrt{1 - \beta^2}$$

$$0.99^2 = 1 - \beta^2$$

$$\beta = \sqrt{1 - 0.99^2}$$

$$\beta = 0.141$$

0.141c

7 Temporal order

All time-like events are in theory physically possible. In this case all time like events can be mapped to each other by Lorenz transformations and preserve the order where an even A that causes B will occur before B. Similarly light-like scenarios, with sufficient distance, will be able to preserve order of events. The issue comes when you reach space-like intervals where you exceed the speed of light. This is obviously impossible to physically happen, but also breaks down causation because if A is to occur, it will have caused B before it happens.

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} G & -BG \\ BG & G \end{pmatrix} \begin{pmatrix} x' \\ y' \end{pmatrix}$$

$$\begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} Gx' - BGy' \\ BGx' + Gy' \end{pmatrix}$$

$$x = Gx' - BGy'$$

$$x = Gx' - Gy' \tan \theta$$

$$G \equiv \frac{1}{\sqrt{1 + B^2}}$$

$$G = \frac{1}{\sqrt{1 + \tan^2 \theta}}$$

$$G = \cos \theta$$

$$x = x' \cos \theta - y' \cos \theta \tan \theta$$

$$x = x' \cos \theta - y' \sin \theta$$

$$y = x' \sin \theta + y' \cos \theta$$

$$\sqrt{x^{2} + y^{2}}
= \sqrt{(x'\cos\theta - y'\sin\theta)^{2} + (x'\sin\theta + y'\cos\theta)^{2}}
= \sqrt{x'^{2}\cos^{2}\theta + y'^{2}\sin^{2}\theta + x'^{2}\sin^{2}\theta + y'^{2}\cos^{2}\theta}
= \sqrt{x'^{2}(\cos^{2}\theta + \sin^{2}\theta) + y'^{2}(\sin^{2}\theta + \cos^{2}\theta)}
= \sqrt{x'^{2} + y'^{2}}$$