## 机器学习第二次作业

### 1、BP 公式推导

BPI: 
$$a_{1}^{L} = \frac{e^{\frac{z_{1}^{L}}{2}}}{\frac{z}{k}e^{\frac{z_{1}^{L}}{2}}} = \frac{c}{\sqrt{2}} \frac{3c}{\sqrt{2}} \frac{3c}{\sqrt{2}} \frac{3c}{\sqrt{2}}$$

$$S_{1}^{L} = \frac{3c}{\sqrt{2}} = \frac{3c}{\sqrt{2}} \frac{$$

BP2: 
$$S_{j}^{L} = \frac{\partial C}{\partial Z_{j}^{L}} = \frac{\partial C}{\partial Z_{t}^{L}} \cdot \frac{\partial Z_{t}^{L}}{\partial A_{1}^{L}} \cdot \frac{\partial A_{1}^{L}}{\partial A_{1}^{L}} \cdot \frac{\partial A_{1}^{L}}{\partial Z_{1}^{L}}$$

$$= \sum_{k=1}^{n^{L}} W_{nk}^{L} ReLU(Z_{k}^{L}) + b_{n}^{L}$$

$$= \sum_{j=1}^{n^{L}} S_{i}^{L} W_{n}^{L} \cdot \frac{\partial C}{\partial Z_{i}^{L}} \cdot \frac{\partial C}{\partial Z_{i}^{L}} \cdot \frac{\partial A_{1}^{L}}{\partial A_{1}^{L}} \cdot \frac{\partial A_{1}^{L}}{\partial Z_{1}^{L}}$$

$$= \sum_{k=1}^{n^{L}} W_{nk}^{L} ReLU(Z_{k}^{L}) + b_{n}^{L}$$

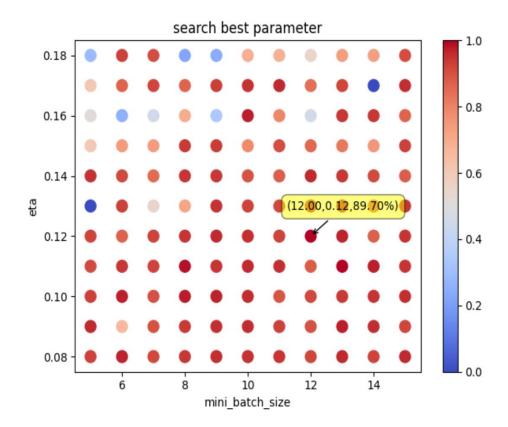
$$S_{1}^{L} = \sum_{j=1}^{n^{L}} S_{i}^{L} W_{n}^{L} \cdot \frac{\partial C}{\partial Z_{i}^{L}} \cdot \frac{\partial C}{\partial Z_{i}^{L}$$

BP3: 先推导例数第2层的代价函数对偏置的导数 36-1 - 3C 22 36-1 : 3c = 8 x x = 8i : 3c = ST 再推平一般形式  $\frac{\partial C}{\partial b_i^{l-1}} = \frac{\partial C}{\partial z_i^l} \frac{\partial z_i^l}{\partial b_i^{l-1}} = S_i^l \times l = S_i^l$ : 3c = 8L 图 IC 36-1=8L

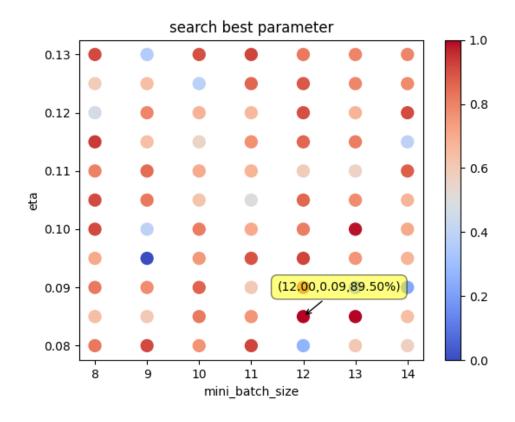
# 2、编程题

```
(1)将 sigmoid 函数改为 ReLU 函数
def ReLU(z):
   """ReLU 承徵"""
   return np.where(z < 0, 0, z)
def ReLU prime(z):
   """ReLU 函数的导数"""
   return np.where (z < 0, 0, 1)
(2) 更改损失为交叉熵损失,最后一层用 softmax 函数表示
def fn(a, y):
   """交叉熵损失函数"""
   sums = 0
   for zi in a:
      sums += np.exp(zi)
   sums = np.log(sums)
   return np.sum(-y * (a - sums))
def feedforward(self, a):
   """前向传播"""
   for b, w in zip(self.biases[:-1],
self.weights[:-1]):
      a = ReLU(np.dot(w, a) + b)
   a = np.dot(self.weights[-1], a) + self.biases[-
1]
   return a
(3) 采用网格搜索寻找比较好的超参数
# 网格搜索大致好的超参数
x  scatter = np.arange(5, 16, 1)
y scatter = np.linspace(0.08, 0.18, 11)
results = {}
\# x \ scatter = np.arange(5, 7, 1)
# y scatter = np.linspace(0.08, 0.10, 3)
# results = {}
```

```
for x in x scatter:
   for y in y scatter:
      training data, validation data, test data =
load data.load data wrapper()
       training data = training data[0:5000]
      test data = test data[0:1000]
      net = network.Network([784, 15, 10],
cost=network.CrossEntropyCost)
       res = net.SGD(training data, 10, x, y,
                   evaluation data=test data,
                   monitor training accuracy=True,
monitor evaluation accuracy=True)
       accuracy = max([i / 1000 \text{ for } i \text{ in } res[1]])
       results [(x, y)] = accuracy
marker size = 100 # default: 20
best point = max(results, key=results.get)
best acc = max(results.values())
worst acc = min(results.values())
colors = [results[x] for x in results.keys()]
colors = np.array(colors)
colors = 1-((best acc - colors)/(best acc -
worst acc))
[Y, X] = np.meshgrid(y scatter, x scatter)
X = X.reshape(len(X.reshape(-1, 1)))
Y = Y.reshape(len(Y.reshape(-1, 1)))
plt.figure()
plt.scatter(X, Y, marker size, c=colors,
cmap=plt.cm.coolwarm)
plt.annotate('(%.2f,%.2f,%.2f%%)' % (best point[0],
best point[1], best acc*100),
           xy=best point, xytext=(-30, 30),
textcoords='offset pixels',
           bbox=dict(boxstyle='round,pad=0.5',
fc='yellow', alpha=0.5),
           arrowprops=dict(arrowstyle='->',
connectionstyle='arc3,rad=0'))
plt.colorbar()
plt.xlabel('mini batch size')
plt.ylabel('eta')
plt.title('search best parameter')
plt.show()
```



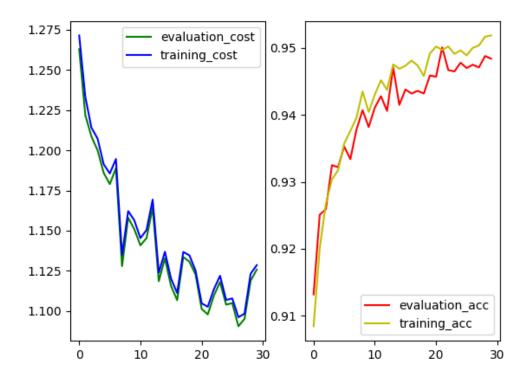
继续缩小超参数区间找到最好的大致区间



(4) 采用隐含层有 15 个神经元的网络,在大致区间进行试验,找到

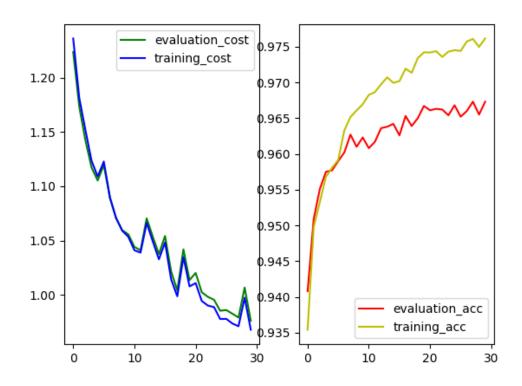
#### 最好的结果。

```
training data, validation data, test data =
load data.load data wrapper()
net = network.Network([784, 15, 10],
cost=network.CrossEntropyCost)
y = net.SGD(training_data, 30, 9, 0.1, lambda1=0.3,
           evaluation data=validation data,
           monitor training cost=True,
           monitor evaluation cost=True,
           monitor training accuracy=True,
           monitor evaluation accuracy=True)
x = np.arange(30)
y0 = [i \text{ for } i \text{ in } y[0]]
y1 = [i/10000 \text{ for } i \text{ in } y[1]]
y2 = [i \text{ for } i \text{ in } y[2]]
y3 = [i/50000 \text{ for } i \text{ in } y[3]]
plt.subplot(1, 2, 1)
plt.plot(x, y0, 'g', label='evaluation cost')
plt.plot(x, y2, 'b', label='training_cost')
plt.title("The change of cost")
plt.legend()
plt.subplot(1, 2, 2)
plt.plot(x, y1, 'r', label='evaluation acc')
plt.plot(x, y3, 'y', label='training acc')
plt.title("The change of accuracy")
plt.legend()
```



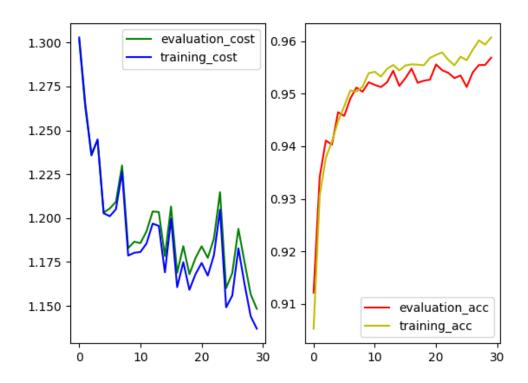
由图可知,损失函数在验证集和训练集上都在下降。并且精度在验证 集和训练集上精度都接近 95%,结果不错。

(5) 将隐含层改为 30 个神经元



由图可以看出,损失函数得到了进一步的下降,训练集的精度提升到97.5%,但验证集的精度只是提升到了96.5%,出现了过拟合现象。此时可以通过正则化或者减小中间层的神经元数量来解决

## (6) 正则化



正则化加上降低隐藏层神经元,过拟合现象降低了。但感觉也不是很好。可能没找到更好的超参数