Diabetes Prediction with Incomplete Patient Data

Hao Yi Ong, Dennis Wang, Xiao Song Mu

CS 221 Aritificial Intelligence: Principles and Techniques Class Project

Introduction

- Given a set of electronic health records, we want to have a smart predictor that prompts high-risk patients to obtain Type II Diabetes testing
- Traditional Kaggle Practice Fusion Diabetes Classification Challenge:
- Patients all have a standard database and a full medical record
- I.e., exact same tests taken, same variables recorded, etc.
- In practice, however, records may be incomplete or wrong:
- Not everyone has taken the same tests and gotten regular checkups
- Database inconsistencies or errors in inputting data may exist
- Predictor must be able to accurately classify based on incomplete or erroneous medical records to be useful

Diabetes Prediction

Given

- Training set containing standardized, de-identified patient medical records
- Testing set containing de-identified patient medical records with missing information and unknown erroneously recorded data

Learn

- Bayesian network structure encoding the conditional dependencies between medical record variables
- Bayesian network parameters encoding the conditional probabilities for each variable

To minimize the error rate, including false positives and false negatives, on classifying whether a patient has Type II Diabetes

Evaluation Criteria

- Baseline of logistic regression
- Feature vector with basic data including height, weight, body mass index...
- Cross validation with 10%-hold-out on the training data
- Obtained a false positive rate of 0.7% and false negative rate of 15.3% for a total error rate of 16% (84% accuracy)
- Oracle
- Ideal oracle would be experienced physicians who have correctly advised patients to test for diabetes given their medical history
- Infeasible time-wise and financially for the scope of our project
- Use as surrogate measures the test accuracies of established diabetes tests vetted by the US Department of Health and Human Services
- Specifically, HBA1c, FPG, and OGTT, which have 85–95% accuracy

Problem Formulation

The design variables for our truss optimization are:

- Cross sectional areas $a \in \mathbf{R}^m$, where $a_i \in \mathbf{R}$ is the area of the i^{th} bar
- Coordinates $x \in \mathbf{R}^{2n}$, where $x_j \in \mathbf{R}^2$ are the coordinates of the j^{th} node

Our problem data are:

- ullet Loading forces $F\in {f R}^{2n}$, where $F_j\in {f R}^2$ is the load on the j^{th} node
- Material densities $\rho_1, \ldots, \rho_m \in \mathbf{R}$ of bars
- Young's moduli $E_1, \ldots, E_m \in \mathbf{R}$ characterizing the elasticities of the bars
- Bar lengths $L_1, \ldots, L_m \in \mathbf{R}$, which are dependent on node coordinates x
- Force mapping matrix $P(\mathcal{X}) \in \mathbf{R}^{m \times 2n}$, which relates loads F to the internal stresses experienced by the bars, $f \in \mathbf{R}^m$; implicit in P is an adjacency matrix relating each bar to its attachment points
- Stiffness matrix $K(\mathcal{X}, a, L)$, which determines the amount of flex in the truss

$$K = \sum_{i=1}^{m} \frac{E_i a_i}{L_i^2} p_i p_i^T,$$

where p_1, \ldots, p_m are the columns of the force mapping matrix P

Our truss design optimization is further characterized by the following variables, whose relations contain all of the physics of the problem:

- Node deflections $u \in \mathbf{R}^{2n}$ due to the truss flexing under loads F, where $u_j \in \mathbf{R}^2$ is the deflection of the j^{th} node; by Hooke's Law, we have the force balance F = Ku
- Internal stress $f_i \in \mathbf{R}$ experienced by each bar due to the node deflections

$$f_i = -\frac{E_i a_i}{L_i^2} p_i^T u, \quad i = 1, \dots, m$$

• Stored elastic energy $\Theta = \frac{1}{2}F^Tu$, which we minimize in order to maximize the truss stiffness

An Alternating Convex Optimization Approach

The minimization of Θ in (a, x) that follows from our formulation above is non-convex. As a heuristic to solve the optimization problem, we first optimize over the bar sizes a, and then over the node coordinates x:

• We perform a linear change of coordinates to cast the bar sizing problem as a second-order cone program (SOCP) in $w, v \in \mathbf{R}^m$:

$$w_i + v_i = -\frac{1}{2} \left(u^T P \right)_i f_i,$$

$$w_i - v_i = a_i$$

The value of $w_i + v_i$ is therefore the spring energy stored in the i^{th} bar

• Holding x constant, find the bar cross sectional areas a that minimize Θ :

minimize
$$\Theta = 1^T (w + v)$$

subject to $Pf + F = 0$

$$M(w - v) \le d$$

$$\|(v_i, \frac{L_i}{\sqrt{\pi}} f_i)\| < w_i, \quad i = 1, \dots, m$$
(1)

(Cont'd)

• Holding a constant, find a set of displacements $y \in \mathbf{R}^{2n}$ that "shift" the node coordinates x from their original positions and minimize Θ :

$$\begin{array}{ll} \text{minimize} & \Theta = \mathbf{1}^T \left(w + v \right) \\ \text{subject to} & Pf + F = 0 \\ & \frac{1}{2} \left(\left(w_i - v_i \right) - 1 \right) = \frac{p_i^T y_i}{L_i}, \quad i = 1, \ldots, m \\ & \left\| \left(v_i, \frac{L_i}{\sqrt{E_i a_i}} f_i \right) \right\|_2 \leq w_i, \quad i = 1, \ldots, m \\ & \|y_i\|_2 \leq \epsilon_i, \quad i = 1, \ldots, m \\ & g \left(y \right) = 0, \end{array} \tag{2}$$

where g(y) = 0 enforces truss symmetry, and $||y_i||_2 \le \epsilon_i$ restrict node shifts.

In our heuristic, we first discretize the physical space as in traditional approaches to obtain $\hat{\mathcal{D}}$, and alternate between solving (1) and (2) in each iteration:

given
$$\mathcal{X}^{\mathsf{fixed}}$$
, \mathcal{F} , $\hat{\mathcal{D}}$
Generate set of node coordinates x^0 from $\hat{\mathcal{D}}$, set $x := x^0$

repeat

1. Given x , obtain a and Θ_1 as the solution to and objective of (1)

2. Given a , obtain y and Θ_2 as the solution to and objective of (2), set $x := x + y$

3. **break if** Θ_1 and Θ_2 converge

Example: Bridge Design

This problem has 791 variables and 219 constraints. Out of several solvers, SCS was the fastest at 0.3 s per iteration (vs. 2.0 s with SeDuMi at comparable accuracy requirements). SCS's speed advantage scales with problem size (~100 times faster than SeDuMi with 16000 variables, 4000 constraints).

Conclusion

return a, x

Our alternating convex optimization approach presents a promising tool to solving the non-convex truss design problem. Future work should extend the model to 3-D and compare this approach to other existing methods.

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