# Lecture 2 – Syntax and Semantics (1)

COSE212: Programming Languages

Jihyeok Park



2023 Fall





### We learn language features of **Scala**:

- Basic Features
  - Built-in Data Types
  - Variables
  - Functions
  - Conditionals
- Object-Oriented Programming (OOP)
  - Case Classes
- Algebraic Data Types (ADTs)
  - Pattern Matching
- Functional Programming (FP)
  - First-class Functions
  - Recursion
- Immutable Collections
  - Lists
  - Options and Pairs
  - Maps and Sets
  - For Comprehensions

### Programming Languages



### Definition (Programming Language)

A **programming language** is defined by

- Syntax: a grammar that defines the structure of programs
- Semantics: a set of rules that defines the meaning of programs

We will learn how to define the **syntax** and **semantics** of a programming language.

We define a programming language for **arithmetic expressions** (AE) as the running example.

### Arithmetic Expressions



Let's consider the arithmetic expressions (AE) supporting **addition** and **multiplication** of integers:

- 4 + 2
- 1 \* 24
- -42 + 4 \* 10
- $\bullet$  (1 + 2) \* (2 + 3)
- . . .

There are **infinitely many** AEs.

How to define all the valid AEs (syntax)?

How to define the expected result of each AE (semantics)?

#### Contents



### 1. Syntax

Backus-Naur Form (BNF) Concrete Syntax of AE Abstract Syntax of AE Concrete vs. Abstract Syntax

#### 2. Semantics

### Contents



### 1. Syntax

Backus-Naur Form (BNF) Concrete Syntax of AE Abstract Syntax of AE Concrete vs. Abstract Syntax

#### Semantics

# Backus-Naur Form (BNF)



### Backus-Naur Form (BNF) is a notation for context-free grammar:

- A nonterminal has a name and a set of production rules consisting of sequences of terminals and nonterminals.
- A **terminal** is a symbol that appears in the final output.

For example, we can define a nonterminal <number> with its production rules to represent all integers (allowing leading zeros) as follows:

### Concrete Syntax of AE



Let's define the **concrete syntax** of AE in BNF:

It determines whether a given string is a valid AE or not. For example, (1+2)\*3 is a valid AE:

```
<expr> \Rightarrow <expr>*<expr> \Rightarrow (<expr>)*<expr>
\Rightarrow (<expr>+<expr>)*<expr> \Rightarrow (1+<expr>)*<expr> \Rightarrow (1+2)*<expr> \Rightarrow (1+2)*3
\Rightarrow (1+2)*3
```

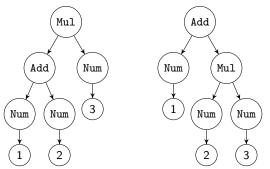
### Abstract Syntax of AE



Let's define the abstract syntax of AE in BNF:

It captures only the essential structure of AE rather than the details.

The abstract syntax trees (ASTs) of (1+2)\*3 and 1+2\*3 are as follows:



### Concrete vs. Abstract Syntax



While **concrete syntax** is the **surface-level** representation of programs, **abstract syntax** is the **essential** representation of programs.

There might be **multiple** concrete syntax for the **same** abstract syntax:

```
\begin{array}{ccccc} e & ::= & n & & \text{(Num)} \\ & & | & e+e & \text{(Add)} \\ & & | & e*e & \text{(Mul)} \end{array}
```

# Concrete vs. Abstract Syntax



While **concrete syntax** is the **surface-level** representation of programs, **abstract syntax** is the **essential** representation of programs.

There might be multiple concrete syntax for the same abstract syntax:

### Contents



### 1. Syntax

Backus-Naur Form (BNF)
Concrete Syntax of AE
Abstract Syntax of AE
Concrete vs. Abstract Syntax

#### 2. Semantics

#### Semantics



There exist many different kinds of semantics:

- Axiomatic semantics defines the meaning of a program by specifying the properties that hold after its execution.
- Denotational semantics defines the meaning of a program by mapping it to a mathematical object that represents its meaning.
- Operational semantics defines the meaning of a program by specifying how it executes on a machine.
- ...

In this course, we will focus on **operational semantics**, and there are two different representative styles:

- Big-Step (Natural) Semantics defines the meaning of a program by specifying how it executes on a machine in one big step.
- Small-Step (Reduction) Semantics defines the meaning of a program by specifying how it executes on a machine step-by-step.

#### Inference Rules



Operational semantics is defined by inference rules.

An inference rule consists of multiple premises and one conclusion:

$$\frac{premise_1}{conclusion} \frac{premise_2}{conclusion} \cdots \frac{premise_n}{conclusion}$$

meaning that "if all the premises are true, then the conclusion is true":

$$premise_1 \land premise_2 \land \cdots \land premise_n \implies conclusion$$

For example,

$$\frac{A \Longrightarrow B \Longrightarrow C}{A \Longrightarrow C}$$

means that "if A implies B, and B implies C, then A implies C".

# Big-Step (Natural) Semantics of AE



$$\vdash e \Rightarrow n$$

It means that "the expression e evaluates to the number n".

Let's define the big-step (natural) semantics of AE:

Num 
$$\frac{}{\vdash n \Rightarrow n}$$

$$e::=n \qquad ext{(Num)} \ | e+e \quad ext{(Add)} \qquad \Longrightarrow \ | e*e \quad ext{(Mul)}$$

$$ADD \xrightarrow{\vdash e_1 \Rightarrow n_1 \qquad \vdash e_2 \Rightarrow n_2} \\ \vdash e_1 + e_2 \Rightarrow n_1 + n_2$$

$$\texttt{MUL} \; \frac{\vdash e_1 \Rightarrow \textit{n}_1 \quad \vdash e_2 \Rightarrow \textit{n}_2}{\vdash e_1 * e_2 \Rightarrow \textit{n}_1 \times \textit{n}_2}$$

# Big-Step (Natural) Semantics of AE



$$Num \frac{}{\vdash n \Rightarrow n}$$

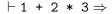
$$\text{Num} \; \frac{}{\vdash n \Rightarrow n} \qquad \text{Add} \; \frac{\vdash e_1 \Rightarrow n_1 \quad \vdash e_2 \Rightarrow n_2}{\vdash e_1 + e_2 \Rightarrow n_1 + n_2} \qquad \text{Mul} \; \frac{\vdash e_1 \Rightarrow n_1 \quad \vdash e_2 \Rightarrow n_2}{\vdash e_1 * e_2 \Rightarrow n_1 \times n_2}$$

$$MUL \frac{\vdash e_1 \Rightarrow n_1 \qquad \vdash e_2 \Rightarrow n_2}{\vdash e_1 * e_2 \Rightarrow n_1 \times n_2}$$

Let's prove  $\vdash$  (1 + 2) \* 3  $\Rightarrow$  9 by drawing a **derivation tree**:

$$\begin{array}{c} \text{Num} \\ \text{Add} \\ \text{Mul} \\ \hline \\ -1 \Rightarrow 1 \\ \hline \\ -1 + 2 \Rightarrow 3 \\ \hline \\ -(1 + 2) * 3 \Rightarrow 9 \\ \end{array}$$

Let's prove  $\vdash 1 + 2 * 3 \Rightarrow 7$  by drawing a **derivation tree**:



### Small-Step (Reduction) Semantics of AE



$$e \rightarrow e$$

It means that "the one-step evaluation result of e is e".

Let's define the small-step (reduction) semantics of AE:

 $rac{e_1 o e_1'}{e_1 + e_2 o e_1' + e_2} \quad rac{e_1 o e_1'}{e_1 * e_2 o e_1' * e_2}$ 

# Small-Step (Reduction) Semantics of AE



$$\frac{e_1 \to e_1'}{e_1 + e_2 \to e_1' + e_2} \qquad \qquad \frac{e_2 \to e_2'}{n_1 + e_2 \to n_1 + e_2'}$$

$$\frac{e_2 \to e_2'}{n_1 + e_2 \to n_1 + e_2'}$$

$$\overline{n_1 + n_2 \rightarrow n_1 + n_2}$$

$$rac{e_1
ightarrow e_1'}{e_1st e_2
ightarrow e_1'st e_2}$$

$$\frac{e_1 \to e_1'}{e_1 * e_2 \to e_1' * e_2} \qquad \qquad \frac{e_2 \to e_2'}{n_1 * e_2 \to n_1 * e_2'}$$

$$\overline{n_1*n_2\to n_1\times n_2}$$

Let's prove  $(1 + 2) * 3 \rightarrow^* 9$  by showing a **reduction sequence**:

(Note that  $\rightarrow^*$  denotes the reflexive-transitive closure of  $\rightarrow$ .)

$$(1 + 2) * 3 \rightarrow 3 * 3 \rightarrow$$

$$\rightarrow$$

Let's prove  $(1 + 2) * 3 \rightarrow^* 9$  by showing a **reduction sequence**:

$$1 + 2 * 3 \rightarrow$$

$$\rightarrow$$

### Summary



### 1. Syntax

Backus-Naur Form (BNF) Concrete Syntax of AE Abstract Syntax of AE Concrete vs. Abstract Syntax

#### 2. Semantics

### Next Lecture



• Syntax and Semantics (2)

Jihyeok Park
jihyeok\_park@korea.ac.kr
https://plrg.korea.ac.kr