

171 HW5

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I tried doing as much work in markdown as possible, but it got very math-y so I used latex for part of it. The first set of problems (9.9, 13.8, and 14.1) are done in markdown. The second set of problems (8.8, 8.10, 8.28, 9.20, and 13.13) are done in latex. I couldn't merge the two too cleanly, but it is what it is.

9.9

note: I'll be referring to goals and axioms as Gx and Ax where x is the identifier.

- a) $G1: 7 \leq 3 + 9$; $A8\{x1 / 7, z1 / (3 + 9)\}$
 $G2: 7 \leq y1$; $A4\{x2 / 7, y1 / (7 + 0)\}$ (success)
 $G3: 7 + 0 \leq 3 + 9$; $A8\{x3 / (7 + 0), z3 / (3 + 9)\}$
 $G4: 7 + 0 \leq y3$; $A6\{x4 / 7, y4 / 0, y3 / (0 + 7)\}$ (success)
 $G5: 0 + 7 \leq 3 + 9$; $A7\{w5 / 0, x5 / 7, y5 / 3, z5 / 9\}$
 $0 \leq 3$; $A1$ (success)
 $7 \leq 9$; $A2$ (success)
 $G1, G3, G5$ (success)
- b) infer from $A1, A2, A7$ $\{w / 0, x / 7, y / 3, z / 9\}$
 $A9: 0 + 7 \leq 3 + 9$
infer from $A9, A6, A8$ $\{x1 / 0, y1 / 7, x2 / (0 + 7), y2 / (7 + 0), z2 / (3 + 9)\}$
 $A10: 7 + 0 \leq 3 + 9$
infer from $A4, A10, A8$
 $\{x3 / 7, x4 / 7, y4 / (7 + 0), z4 / (3 + 9)\}$
 $A11: 7 \leq 3 + 9$

13.8

- a) $P(\text{Toothache}) = 0.108 + 0.012 + 0.016 + 0.064$
 $= 0.2$
- b) $P(\text{Cavity}) = \langle 0.2, 0.8 \rangle$
 $= 0.108 + 0.012 + 0.072 + 0.008$
 $= 0.2$
- c) $P(\text{Toothache} | \text{Cavity}) = \langle (0.108 + 0.012) / 2, (0.072 + 0.008) / 0.2 \rangle$
 $= \langle 0.6, 0.4 \rangle$
 $= .6$
- d) $P(\text{Cavity} \vee \text{Catch}) = 0.108 + 0.012 + 0.016 + 0.064 + 0.072 + 0.144$
 $= 0.416$
therefore,
 $P(\text{Cavity} | \text{Toothache} \vee \text{Catch}) = \langle (0.108 + 0.012 + 0.072) / 0.416, (0.016 + 0.064 + 0.144) / 0.416 \rangle$
 $= \langle 0.4615, 0.5384 \rangle$

13.13

note: I originally did this problem in latex, but when merging the pdfs, I got a font type error so I ended up posting an image of the latex output to markdown. Sorry if it's messy.

13.13

$$\begin{aligned}
 P(\text{TestA} = \text{pos} \mid \text{Virus} = \text{Present}) &= .95 \\
 P(\text{TestA} = \text{pos} \mid \text{Virus} = \text{Absent}) &= .1 \\
 P(\text{TestB} = \text{pos} \mid \text{Virus} = \text{Present}) &= .9 \\
 P(\text{TestB} = \text{pos} \mid \text{Virus} = \text{Absent}) &= .05 \\
 P(\text{Virus} = \text{Present}) &= .01 \\
 P(\text{Virus} = \text{Present} \mid \text{TestA} = \text{pos}) \\
 &= \frac{P(\text{TestA} = \text{pos} \mid \text{Virus} = \text{Present}) \times P(\text{Virus} = \text{Present})}{P(\text{TestA} = \text{pos} \mid \text{Virus} = \text{Present}) \times P(\text{Virus} = \text{Present}) + P(\text{TestA} = \text{pos} \mid \text{Virus} = \text{Absent}) \times P(\text{Virus} = \text{absent})} \\
 &= \frac{.0095}{.1085} = .088 \\
 P(\text{Virus} = \text{Present} \mid \text{TestB} = \text{pos}) \\
 &= \frac{P(\text{TestB} = \text{pos} \mid \text{Virus} = \text{Present}) \times P(\text{Virus} = \text{Present})}{P(\text{TestB} = \text{pos} \mid \text{Virus} = \text{Present}) \times P(\text{Virus} = \text{Present}) + P(\text{TestB} = \text{pos} \mid \text{Virus} = \text{Absent}) \times P(\text{Virus} = \text{absent})} \\
 &= \frac{.009}{.0585} = .15
 \end{aligned}$$

Figure 1:

14.1

- a) let RV C have domain {a, b, c}

In the network, C is the root and X1, X2, X3 are the children.

CPT for C:

C	P(C)
a	1/3
b	1/3
c	1/3

CPT for Xi

C	Xi	P(C)
a	heads	.2
b	heads	.6
c	heads	.8

- b) “ P(X1=tails, X2=heads, X3=heads | C=a) = .8 * .2 * .2 = .032 P(2 heads, 1 tails | C=a) = 3 * .032 = .096 P(" " " | C=b) = .432 P(" " " | C=c) = .384

therefore, b is most likely to be drawn “

hw5

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8.8

Jim \neq *George*
Spouse(*Jim*, *Laura*)
 $\forall X : X \neq \textit{Jim} \wedge \textit{Spouse}(X, \textit{Laura})$
therefore *Spouse*(*George*, *Laura*)

8.10

a) $\textit{Occupation}(\textit{Emily}, \textit{Surgeon}) \vee \textit{Occupation}(\textit{Emily}, \textit{Lawyer})$
b) $\textit{Occupation}(\textit{Joe}, \textit{Actor}) \wedge \exists! X : X \neq \textit{Actor} \wedge \textit{Occupation}(\textit{Joe}, X)$
c) $\forall X : \textit{Occupation}(X, \textit{Surgeon}) \Rightarrow \textit{Occupation}(X, \textit{Doctor})$
d) $\forall X : \textit{Occupation}(X, \textit{Lawyer}) \Rightarrow \textit{Customer}(\textit{Joe}, X)$
e) $\exists! X : \textit{Boss}(X, \textit{Emily}) \Rightarrow \textit{Occupation}(X, \textit{Lawyer})$
f) $\exists X, \forall Y (\textit{Occupation}(X, \textit{Lawyer}) \Rightarrow (\textit{Customer}(Y, X) \Rightarrow \textit{Occupation}(Y, \textit{Doctor})))$
g) $\forall X, \exists Y : \textit{Occupation}(X, \textit{Surgeon}) \Rightarrow \textit{Customer}(X, Y)$

8.28

b) $\neg \textit{Wrote}(\textit{Gershwin}, \textit{Eleanor Rigby.})$
d) $\exists X : \textit{Wrote}(\textit{Joe}, X)$
g) $\forall X, \exists Y : \textit{Sings}(Y, X, \textit{Revolver}) \Rightarrow Y \neq \textit{Gershwin}$
h) $\forall X, \exists Y : \textit{Wrote}(\textit{Gershwin}, X) \Rightarrow \textit{Sings}(\textit{Gershwin}, X, Y) k) \forall X, \exists Y, \exists Z : \textit{Sings}(\textit{McCartney}, X, Y) \Rightarrow (\textit{CopyOf}(Z, Y) \wedge \textit{Owns}(\textit{Joe}, Z))$