

# Cryptographic Authentication for GPS Communications

AA 272 Global Positioning System

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# Overview

- Motivation
- Problem Statement
- Approach
- Demonstration
- Results and Findings
- Improvements



# Motivations



- Security concerns associated with GPS communications
- Integrity of location-based services
- Potential threats to data accuracy

## Status

onGnssStatusChanged: SATELLITE\_STATUS |  
[Satellites:

Constellation = GPS, Svid = 19, Cn0DbHz = 37.26122, Elevation = 78.0, Azimuth = 196.0, hasEphemeris = true, hasAlmanac = true, usedInFix = true, carrierFrequencyHz = 1.57542003E9

Constellation = GPS, Svid = 17, Cn0DbHz = 31.919926, Elevation = 70.0, Azimuth = 51.0, hasEphemeris = true, hasAlmanac = true, usedInFix = true, carrierFrequencyHz = 1.57542003E9

Constellation = GALILEO, Svid = 2, Cn0DbHz = 27.61021, Elevation = 67.0, Azimuth = 359.0, hasEphemeris = true, hasAlmanac = true, usedInFix = true, carrierFrequencyHz = 1.57542003E9

Constellation = GALILEO, Svid = 2, Cn0DbHz = 21.75385, Elevation = 67.0, Azimuth = 359.0, hasEphemeris = true, hasAlmanac = true, usedInFix = false, carrierFrequencyHz = 1.17645005E9

Constellation = GLONASS, Svid = 18, Cn0DbHz = 40.533543, Elevation = 60.0, Azimuth =

*GnssLogger, Google Pixel 6*

# Motivations

- Security concerns associated with GPS communications
- Integrity of location-based services
- Potential threats to data accuracy
- **Solution: Authentication**



# Cryptography - Symmetric Message Authentication

- Used for “Integrity”, not “confidentiality”
  - In GPS applications, this prevents GPS signal spoofing or message alteration.



- CBC-MAC
- HMAC
- ...

# Problems

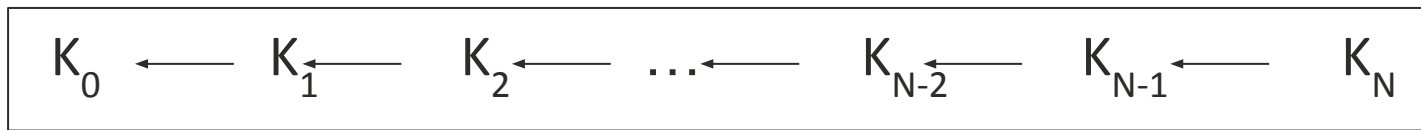
- Problem 1: **Key Lost**
- Problem 2: **Replay Attack**
  - **Definition:** Intercepting secure network communication to manipulate the recipient.
  - **Process:** Cybercriminal captures and fraudulently resends or delays the message.
  - **Risk:** Advanced decryption skills not required; success achieved through message replay.



# Approach: TESLA Algorithm



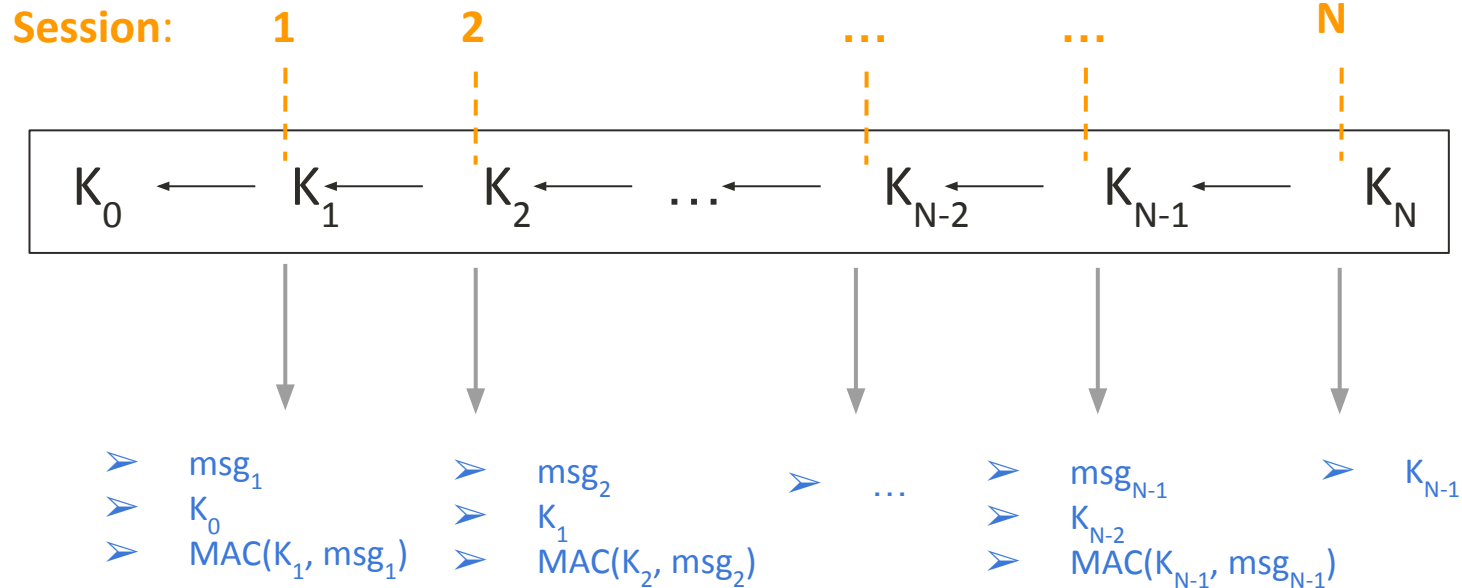
- Key Chain:  $[K_0, K_1, K_2, K_3, \dots, K_N]$
- Establish a key for each session, which is a type of code that is only valid for one transaction and can't be used again.



- $K_{N-1} = F(K_N),$
  - $K_{N-2} = F(K_{N-1})$
  - $\dots$
  - $K_0 = F(K_1)$
- $F$  : Secure Hash Algorithm  
256-bit (**SHA-256**)

# Approach: TESLA Algorithm

- Key Distribution is delayed by one session.



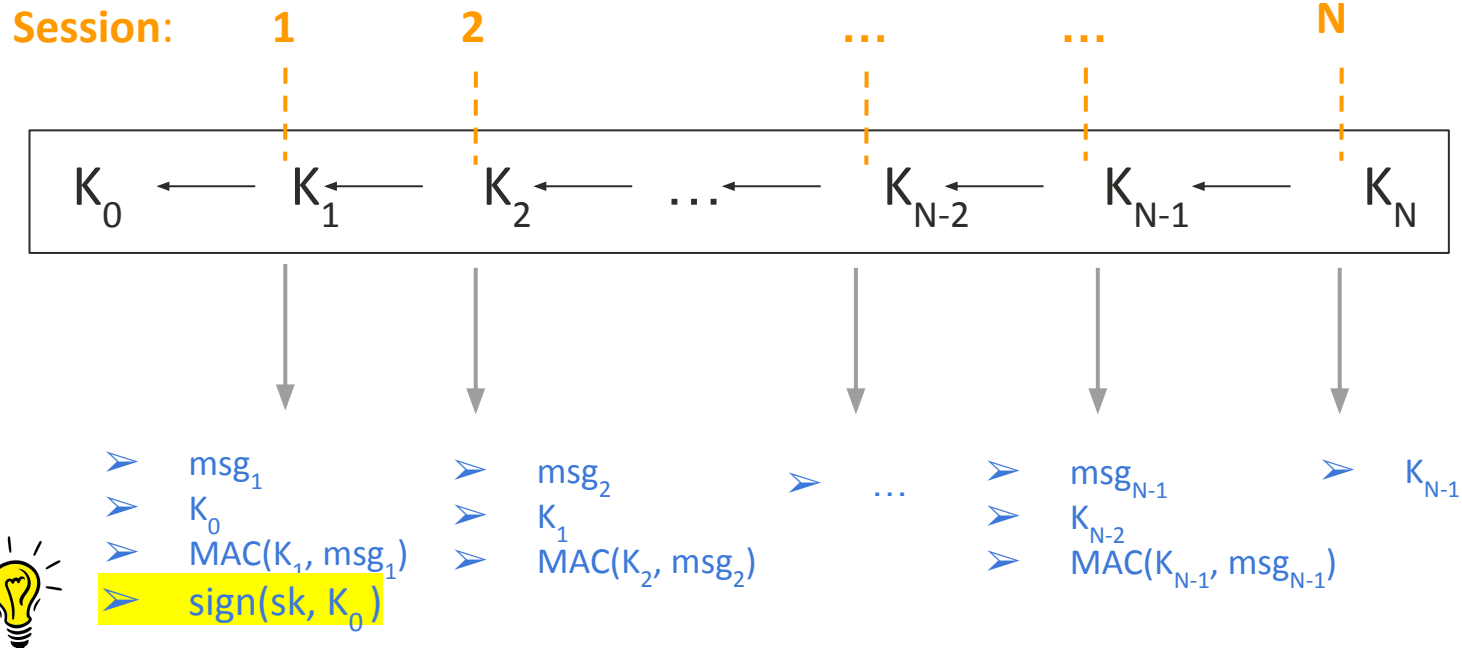




Do we take  $K_0$  for granted?

# Approach: TESLA Algorithm

- Key Distribution is delayed by one session.



# Approach: TESLA Algorithm

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## Algorithm 1 TESLA Sender

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```
1: Generate key chain:  $[K_0, K_1, K_2, \dots, K_N]$ 
2: for  $i \leftarrow 1$  to  $N$  do
3:    $mac_i \leftarrow MAC(K, msg_i)$ 
4:   Send ( $msg_i, K_{i-1}, mac_i$ )
5:   if  $i = 1$  then
6:      $sig \leftarrow Sign(sk, K_0)$ 
7:     Send ( $sig$ )
8:   end if
9: end for
```

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## Algorithm 2 TESLA Receiver

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```
1:  $msg_{prev}, mac_{prev}$ 
2: for  $i \leftarrow 1$  to  $N$  do
3:    $msg \leftarrow msg_i$ 
4:    $K_{prev} \leftarrow K_{i-1}$ 
5:    $mac \leftarrow mac_i$ 
6:   if  $i = 1$  then
7:     verify ( $pk, sig, K_0$ )
8:   else
9:     verify ( $K_{prev}, msg_{prev}, mac_{prev}$ )
10:  end if
11:   $msg_{prev} \leftarrow msg$ 
12:   $mac_{prev} \leftarrow mac$ 
13: end for
```

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How do we validate public key (pk)?

# Solution 1:

Every receiver stores  $pk(s)$  for all GPS satellites.

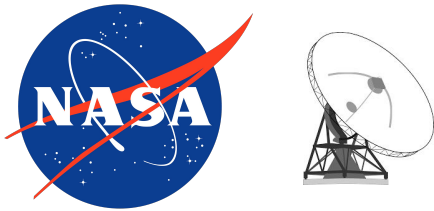
- Cons:
  - requires  $pk$  integrity at each receiver
  - requires timely updates when new satellites are launched

# Better Solution:

- Use certificates issued by trusted third parties to deliver pk(s)

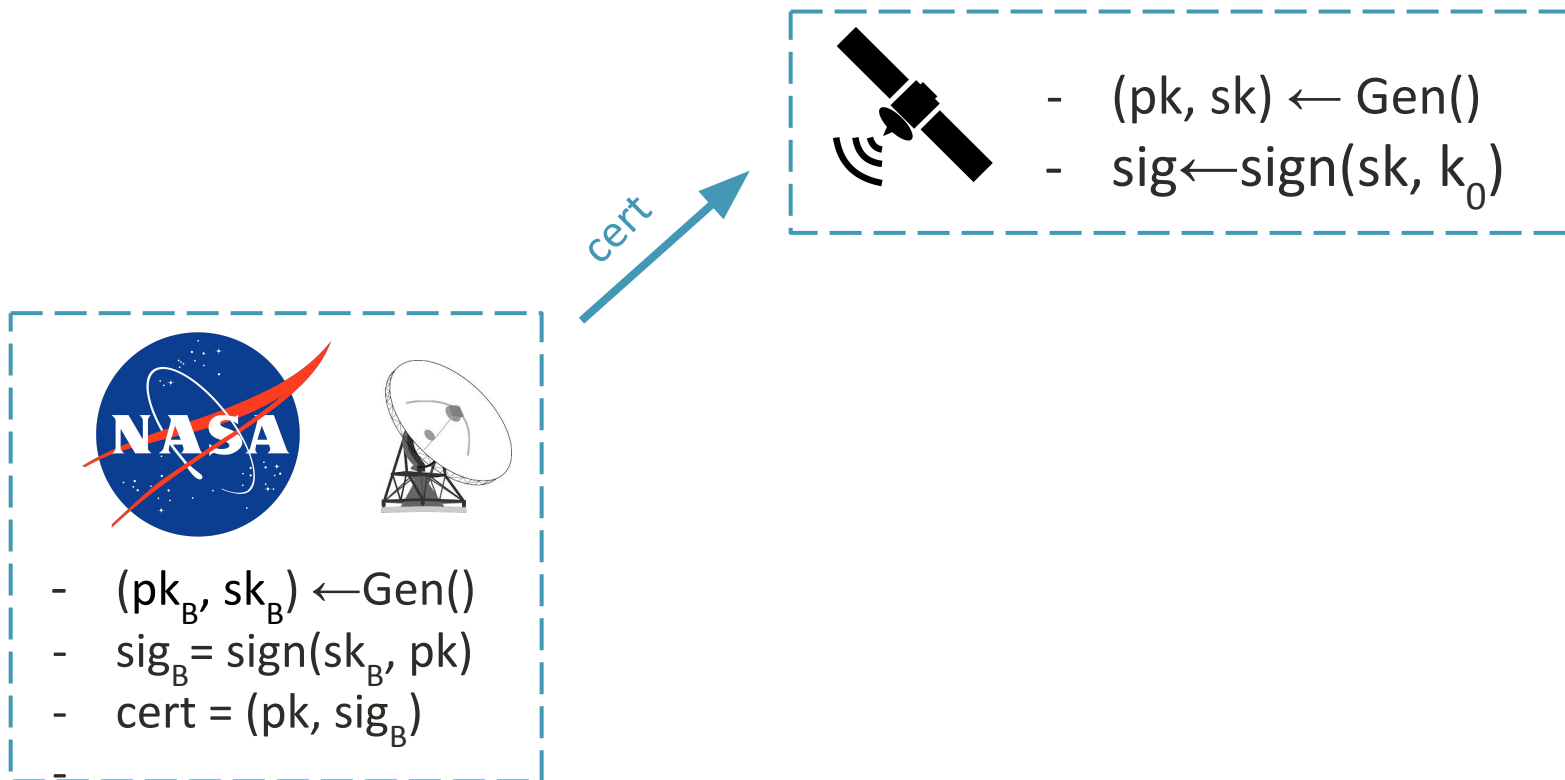


# Secret Key & Public Key



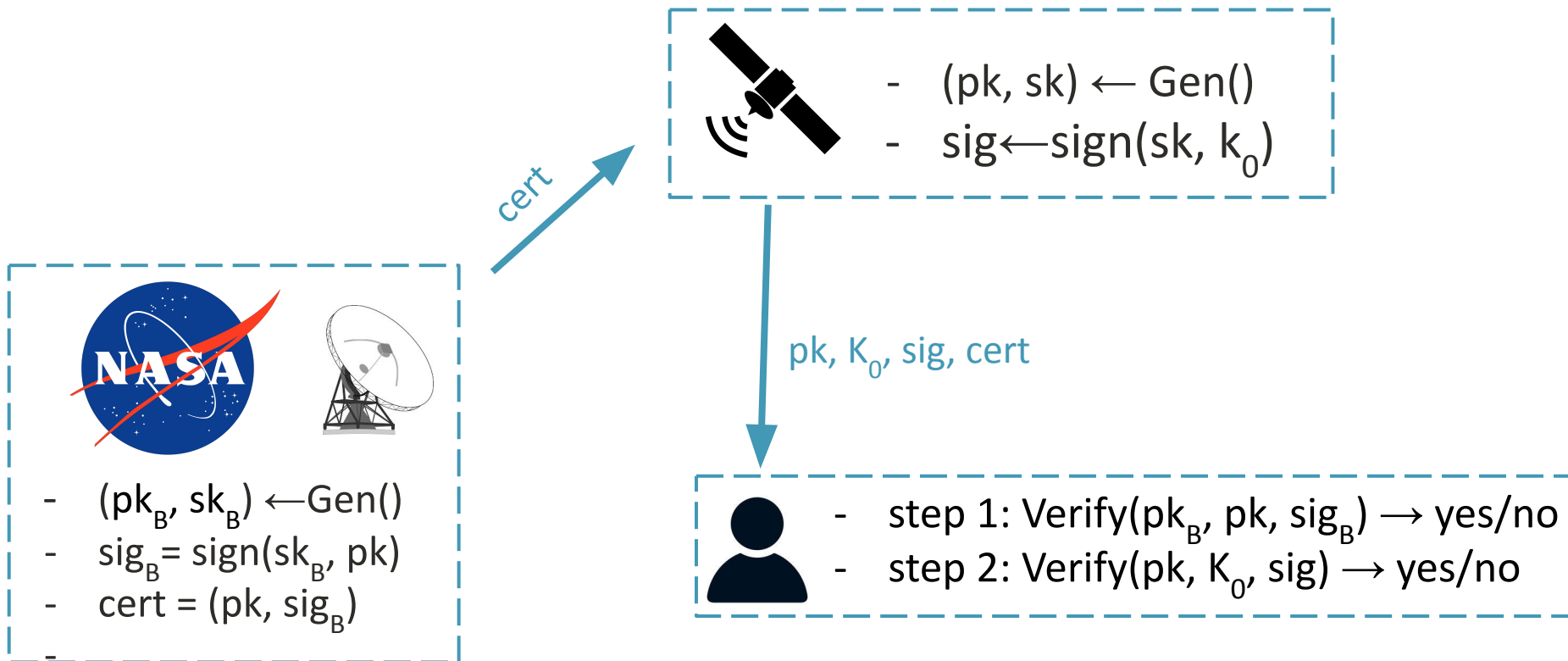
- $(pk_B, sk_B) \leftarrow \text{Gen}()$
- $\text{sig}_B = \text{sign}(sk_B, pk)$
- $\text{cert} = (pk, \text{sig}_B)$

# Secret Key & Public Key





# Secret Key & Public Key



# Implementation

- Sender

```
key_auth = key_chain[session]
key_send = key_chain[session-1].hex()
print("Entered session: ", session)
file_name = input("Enter filename to send: ")
with open(file_name, 'rb') as file:
    file_data_b = file.read()
    file_data = file_data_b.decode('utf-8')
hm = hmac.HMAC(key_auth, hashes.SHA256())
hm.update(file_data.encode('utf-8'))
mac = hm.finalize().hex()
if session == 1:
    signature = private_key.sign(
        key_send.encode('utf-8'),
        padding.PSS(
            mgf=padding.MGF1(hashes.SHA256()),
            salt_length=padding.PSS.MAX_LENGTH
        ),
        hashes.SHA256()
    )
    sndr_socket.send((key_send+" "+file_data+" "+mac+" "+pem_public_key.hex()+" "+signature.hex()).encode('utf-8'))
else:
    sndr_socket.send((key_send+" "+file_data+" "+mac).encode('utf-8'))
print("Key sent in session", session, "is", key_send)
print("Just info: Message", file_data, "can only be authenticated with key", key_auth.hex())
print("Session", session, "finished.")
```

# Implementation

- Receiver

```
# Verify the prev_msg with received key
hm = hmac.HMAC(key, hashes.SHA256())
hm.update(prev_msg.encode())
try:
    hm.verify(prev_mac)
    print("Message received in session", session-1, prev_msg, "is authenticated.")
    prev_msg = msg
    prev_key = key
    prev_mac = mac
    print("Session", session, "finished.")
except InvalidSignature:
    print("MAC is not valid. Message is spoofed.")
    print("Received message", msg, "is discarded.")
    session -= 1
    print("Downgraded session to id", session, "to sync with gps.")
```

# Implementation

- Certification

```
with open(sat_pk_path, 'rb') as sat_pk_file:
    pem_public_key_sat = sat_pk_file.read()

public_key_sat = serialization.load_pem_public_key(
    pem_public_key_sat,
    backend=default_backend()
)

issuer = x509.Name([
    x509.NameAttribute(NameOID.COMMON_NAME, u"nasa"),
])
certificate = x509.CertificateBuilder().subject_name(
    issuer
).issuer_name(
    issuer
).public_key(
    public_key_sat
).serial_number(
    x509.random_serial_number()
).not_valid_before(
    datetime.datetime.utcnow()
).not_valid_after(
    # Valid for 1 year
    datetime.datetime.utcnow() + datetime.timedelta(days=365)
).sign(private_key_nasa, hashes.SHA256(), default_backend())

# Serialize certificate
pem_certificate = certificate.public_bytes(encoding=serialization.Encoding.PEM)

cert_path = "cert.pem"
with open(cert_path, 'wb') as cert_file:
    cert_file.write(pem_certificate)
    print("Certificate generated for satellite public key")
```

# Demonstration

Github Repo: [https://github.com/jw4149/GPS\\_Project/tree/main](https://github.com/jw4149/GPS_Project/tree/main)

```
[(base) jiayangwang@DNA80d9da code % python satellite.py] [(base) jiayangwang@DNA80d9da code % python receiver.py]
Entered session: 1
Receiver ready.
Enter filename to send: data1.txt
Entered session: 1
Key sent in session 1 is af069be81c78a8a55f096c4016d2d472af1131a884ce9f29f9a7068e7889500f
Received message gps_millis:1273611504445.0,gnss_id:gps,sv_id:2,corr_pr_m:20774577.36402971,x
Just info: Message gps_millis:1273611504445.0,gnss_id:gps,sv_id:2,corr_pr_m:20774577.36402971,
_sv_m:-11867755.90150921,y_sv_m:-21956297.905915044,z_sv_m:9801130.518319722
will be verified in next session.
,x_sv_m:-11867755.90150921,y_sv_m:-21956297.905915044,z_sv_m:9801130.518319722
Session 1 finished.
can only be authenticated with key ccc45cd05b2e6ce787d6bd926865a5f7ba7fbc8b5d55cc606927ce1f
Entered session: 2
1d82621
Received message gps_millis:1273611506892.0,gnss_id:gps,sv_id:2,corr_pr_m:20774577.36402971,x
Enter filename to send: data2.txt
_sv_m:-11867767.90150921,y_sv_m:-21956299.905915044,z_sv_m:9801143.518319722
Key sent in session 2 is ccc45cd05b2e6ce787d6bd926865a5f7ba7fbc8b5d55cc606927ce1f1d82621
will be verified in next session.
Just info: Message gps_millis:1273611506892.0,gnss_id:gps,sv_id:2,corr_pr_m:20774577.36402971,
Message received in session 1 gps_millis:1273611504445.0,gnss_id:gps,sv_id:2,corr_pr_m:207745
,x_sv_m:-11867767.90150921,y_sv_m:-21956299.905915044,z_sv_m:9801143.518319722
77.36402971,x_sv_m:-11867755.90150921,y_sv_m:-21956297.905915044,z_sv_m:9801130.518319722
can only be authenticated with key afdcdf9b061eb4f4ab09f4b51795a60ebc5902e8c60a89ebc79e15022
is authenticated.
cf03ce9
Session 2 finished.
Entered session: 3
Message received in session 2 gps_millis:1273611506892.0,gnss_id:gps,sv_id:2,corr_pr_m:20774577.36402971,x
Enter filename to send: data3.txt
_sv_m:-11867767.90150921,y_sv_m:-21956299.905915044,z_sv_m:9801143.518319722 will be verified
Key sent in session 3 is afdcdf9b061eb4f4ab09f4b51795a60ebc5902e8c60a89ebc79e15022cf03ce9
in next session.
Just info: Message gps_millis:1273611509763.0,gnss_id:gps,sv_id:2,corr_pr_m:20774577.36402971,
MAC is not valid. Message is spoofed.
,x_sv_m:-11867771.90150921,y_sv_m:-21956302.905915044,z_sv_m:9801150.518319722
Received message gps_millis:1273611506892.0,gnss_id:gps,sv_id:2,corr_pr_m:20774577.36402971,x
can only be authenticated with key 529a5baec6c17f381965068857ce98827d32c4e04c541ccf247a5529f
_sv_m:-11867771.90150921,y_sv_m:-21956299.905915044,z_sv_m:9801143.518319722 is discarded.
b30c015
Downgraded session to id 2 to sync with gps.
Session 3 finished.
Entered session: 3
Received message gps_millis:1273611509763.0,gnss_id:gps,sv_id:2,corr_pr_m:20774577.36402971,x
Just info: Message gps_millis:1273611509763.0,gnss_id:gps,sv_id:2,corr_pr_m:20774577.36402971,
_sv_m:-11867771.90150921,y_sv_m:-21956302.905915044,z_sv_m:9801150.518319722
will be verified in next session.
,x_sv_m:-11867771.90150921,y_sv_m:-21956302.905915044,z_sv_m:9801150.518319722
Message received in session 2 gps_millis:1273611506892.0,gnss_id:gps,sv_id:2,corr_pr_m:207745
can only be authenticated with key 529a5baec6c17f381965068857ce98827d32c4e04c541ccf247a5529f
77.36402971,x_sv_m:-11867767.90150921,y_sv_m:-21956299.905915044,z_sv_m:9801143.518319722
is authenticated.
b30c015
Session 3 finished.
```

# Improvements

- Message loss handling
- Signal-Level Authentication
- ...

# References

Petovello, M. (2017), GNSS Solution. Q: What is navigation message authentication?

Fernández-Hernández, I., Rijmen, V., Seco-Granados, G., Simon, J., Rodríguez, I., & Calle, J. D. (2016). A navigation message authentication proposal for the Galileo open service. *NAVIGATION: Journal of the Institute of Navigation*, 63(1), 85-102.

Lo, S. C., & Enge, P. K. (2010, May). Authenticating aviation augmentation system broadcasts. In *IEEE/ION position, location and navigation symposium* (pp. 708-717). IEEE.

# Questions?