

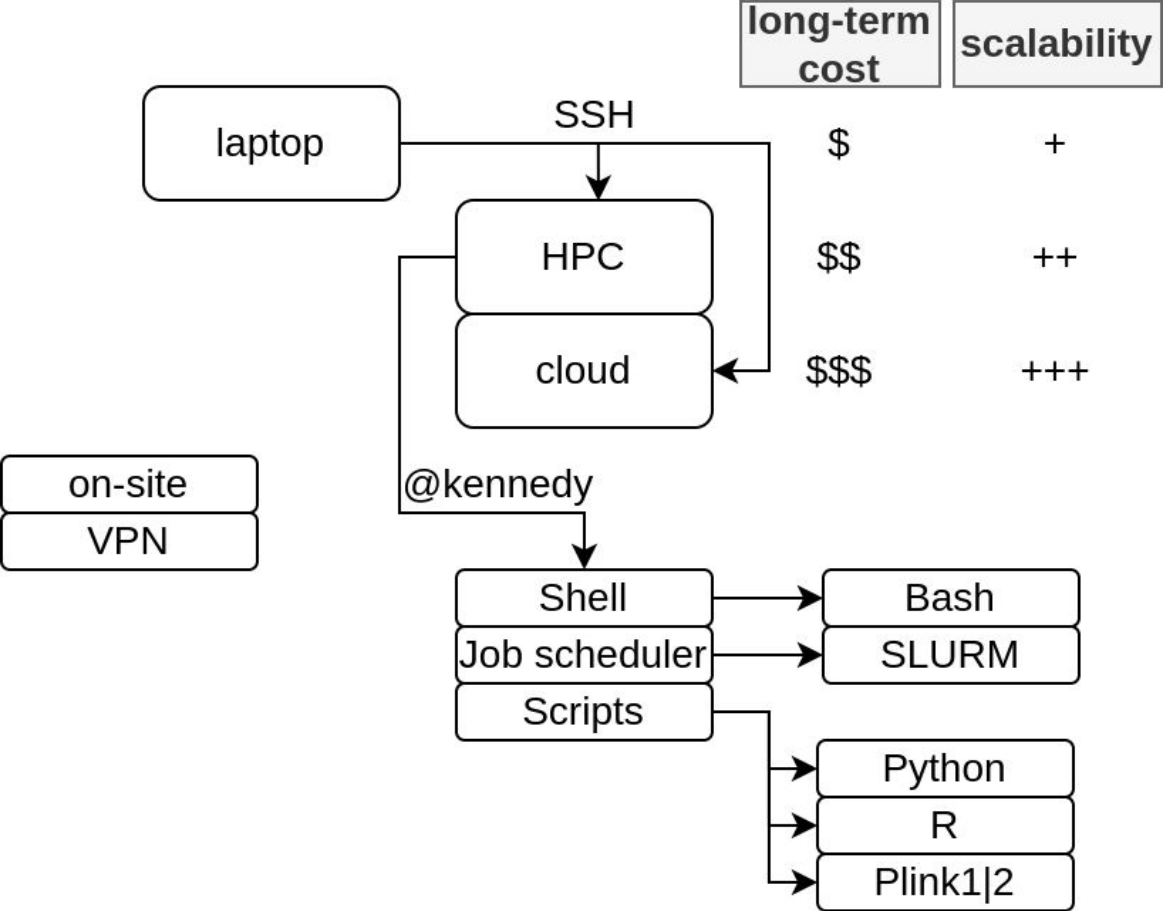
Lecture 1 - GWAS Statistics + Polygenic Risk Scores (PRS)

Wed, Mar 20, 9-10AM

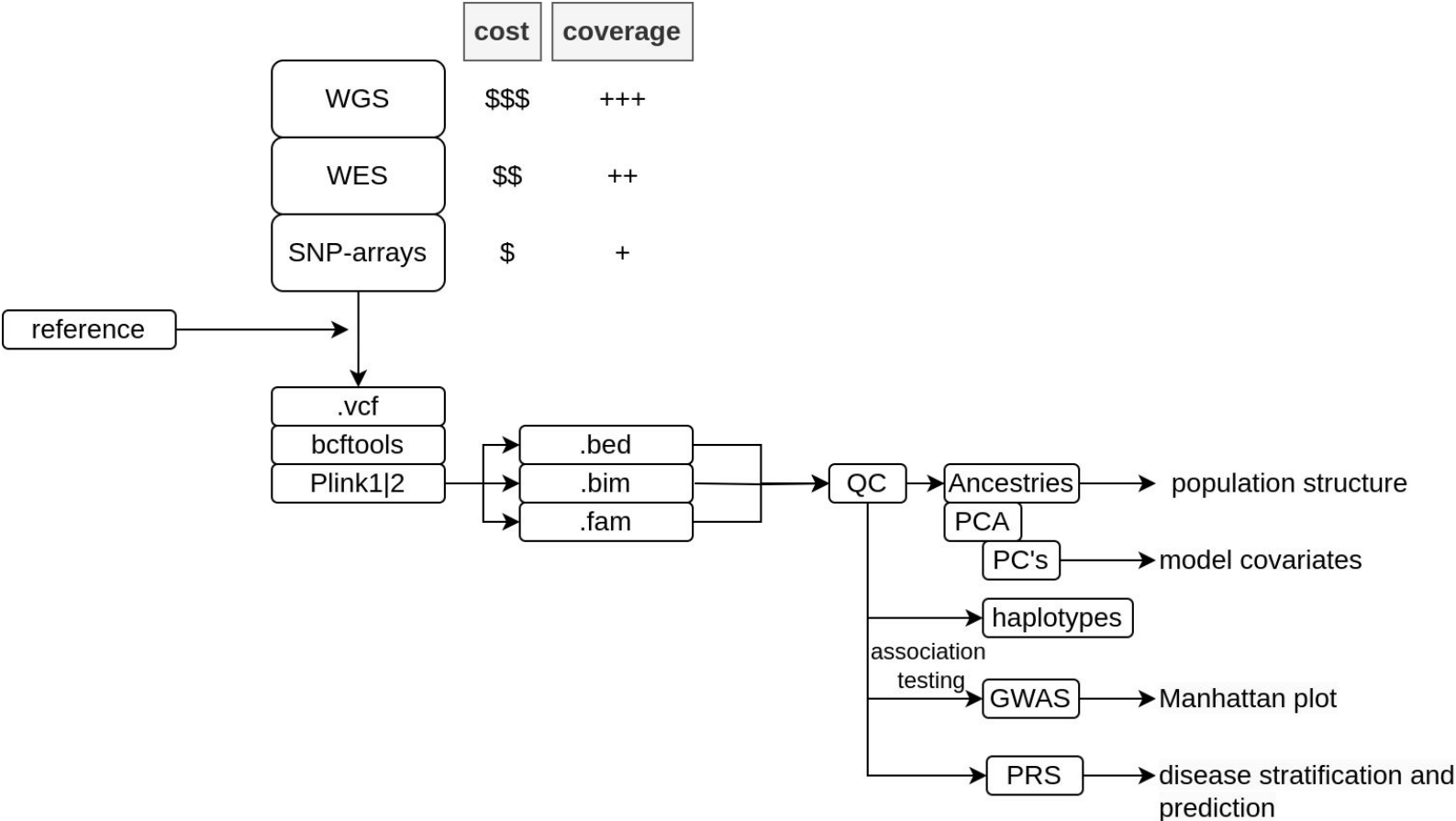
Recap

HPC | GWAS

Recap: HPC + SSH



Recap: GWAS

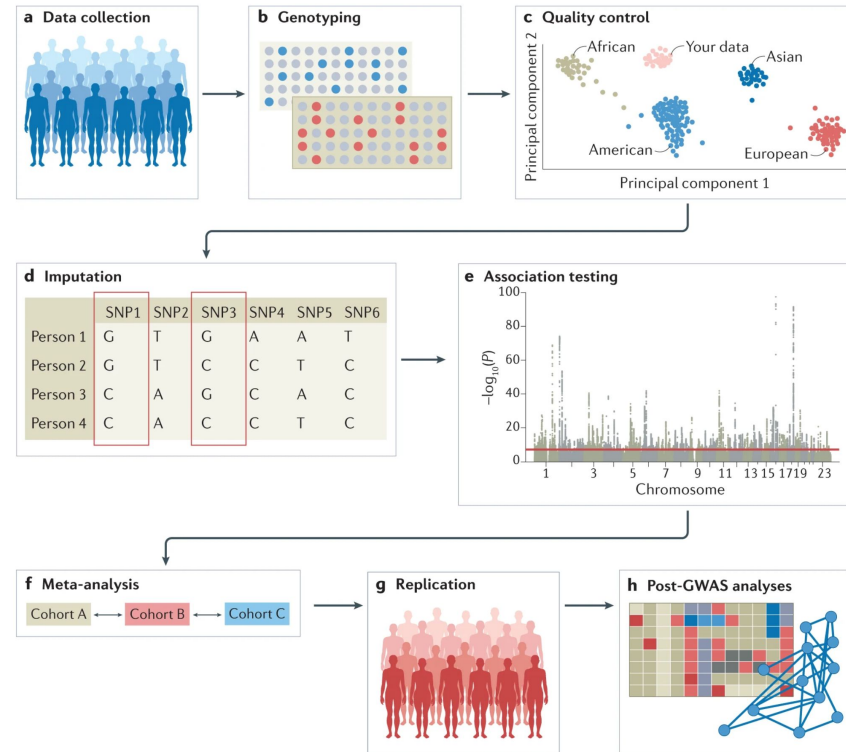


GWAS

Genome-wide Association Studies

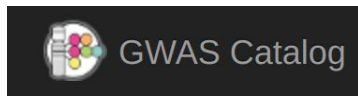
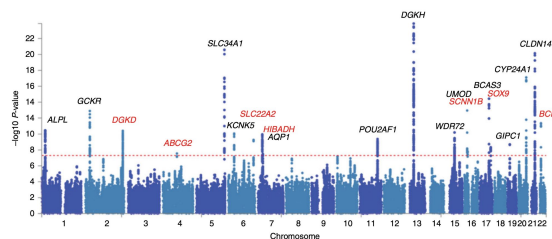
Genome-wide Association studies (GWAS)

Single nucleotide polymorphism (SNP): This is a variation in a single nucleotide (i.e., **A**, **C**, **G**, or **T**) that occurs at a specific position in the genome. A SNP usually exists as two different forms (e.g., **A** vs. **T**). These different forms are called alleles. A SNP with two alleles has three different genotypes (e.g., **AA**, **AT**, and **TT**).



Data sources & repositories

Summary statistics

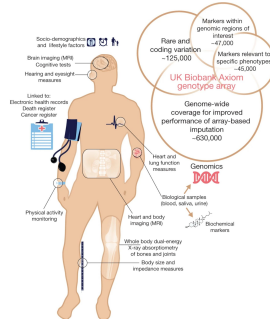


general GWAS data repository



specific for GWAS Chronic Kidney Disease

Individual-level



Genotype data

	SNP1	SNP2	SNP3	SNP4
Individual 1	AT	CG	TT	CC
Individual 2	TA	GG	GT	CA
Individual 3	TT	CC	GT	CA
Individual 4	TT	CC	GG	AA



Testing for associations

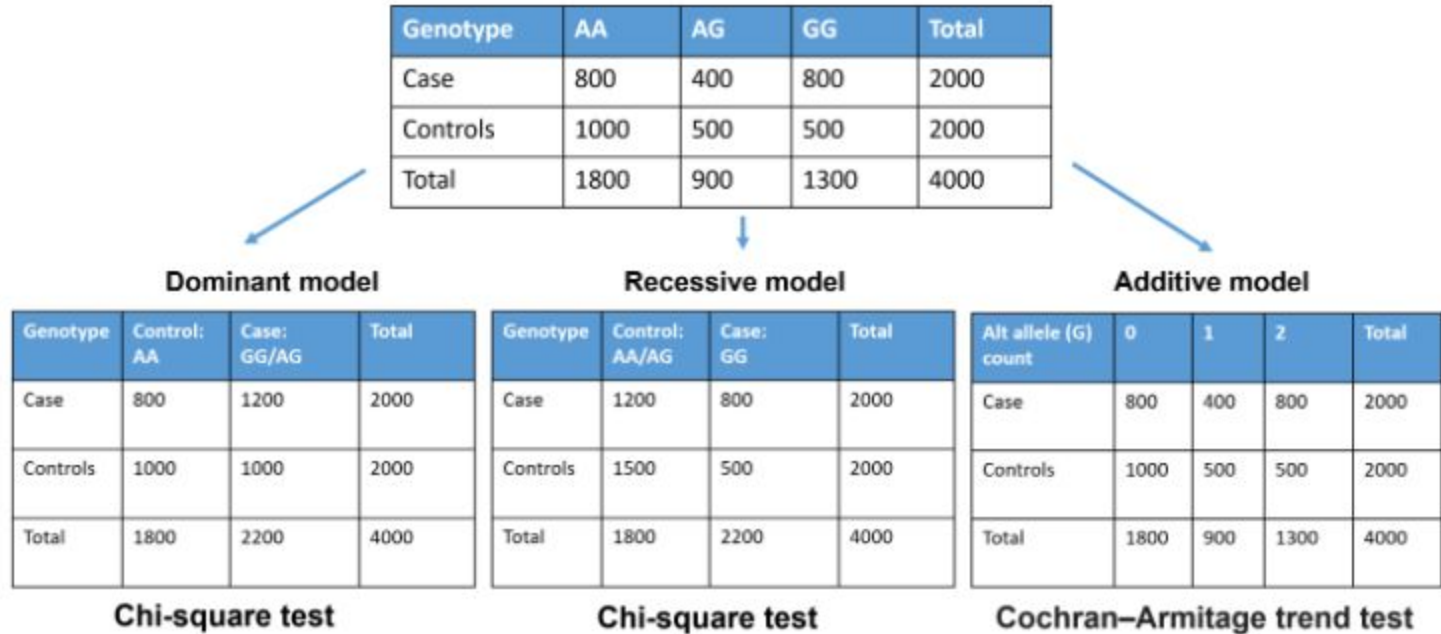
Genetic models

Genetic models	AA	AG	GG
Additive model	0	1	2
Dominant model	0	1	1
Recessive model	0	0	1

- Additive model (ADD)
- Dominant model (DOM)
- Recessive model (REC)

Testing for associations

Contingency table



Testing for associations

Quantitative traits

$$y = G\beta_G + X\beta_X + e$$

- G is the genotype matrix.
- β_G is the effect size for variants.
- X and β_X are covariates and their effects.
- e is the error term.

Binary traits

$$\text{logit}(p) = G\beta_G + X\beta_X + e$$

Testing for associations

Quantitative trait

$$y = G\beta_G + X\beta_X + e$$

Height

Genotype
(allele count/
dosage)

Covariates

Age

Sex

PCs ...

$$\begin{bmatrix} 181 \\ 152 \\ 162 \\ 177 \\ 148 \\ 165 \end{bmatrix} \sim \begin{bmatrix} 1 \\ 0 \\ 2 \\ 2 \\ 0 \\ 1 \end{bmatrix} + \begin{bmatrix} 81 \\ 52 \\ 62 \\ 77 \\ 48 \\ 65 \end{bmatrix} + \begin{bmatrix} 1 \\ 2 \\ 1 \\ 2 \\ 2 \\ 1 \end{bmatrix} + \begin{bmatrix} \dots \\ \dots \\ \dots \\ \dots \\ \dots \\ \dots \end{bmatrix}$$

Binary trait

$$\log(p/1-p) = G\beta_G + X\beta_X + e$$

Type2
diabetes

Genotype
(allele count/
dosage)

Covariates

Age

Sex

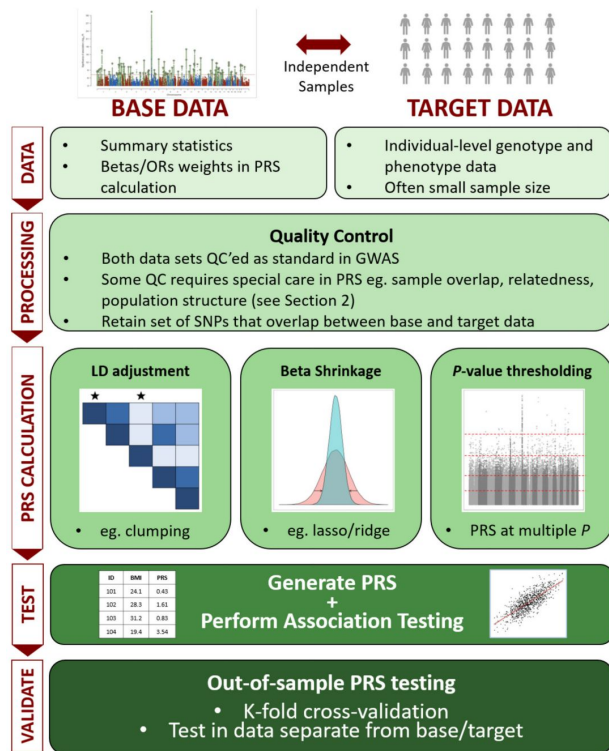
PCs ...

$$\begin{bmatrix} 1 \\ 0 \\ 1 \\ 1 \\ 0 \\ 1 \end{bmatrix} \sim \begin{bmatrix} 1 \\ 0 \\ 2 \\ 2 \\ 0 \\ 1 \end{bmatrix} + \begin{bmatrix} 181 \\ 152 \\ 162 \\ 177 \\ 148 \\ 165 \end{bmatrix} + \begin{bmatrix} 1 \\ 2 \\ 1 \\ 2 \\ 2 \\ 1 \end{bmatrix} + \begin{bmatrix} \dots \\ \dots \\ \dots \\ \dots \\ \dots \\ \dots \end{bmatrix}$$

Polygenic Risk Scores

stratification & disease trajectories

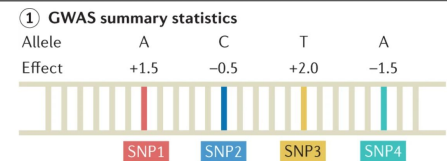
Common workflow - single-trait PRS



Polygenic risk scores (PRS)

$$PRS_i = \sum_{j \in J} \beta_j G_{ij}$$

i -th individual
 j -th variant
 G : genotype
 β : effect size

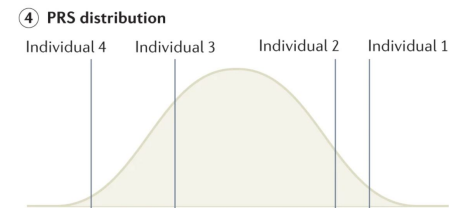


② Genotype data

	SNP1	SNP2	SNP3	SNP4
Individual 1	AT	CG	TT	CC
Individual 2	TA	GG	GT	CA
Individual 3	TT	CC	GT	CA
Individual 4	TT	CC	GG	AA

③ Polygenic risk score

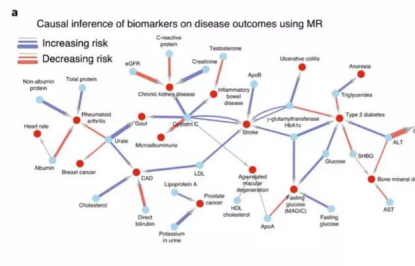
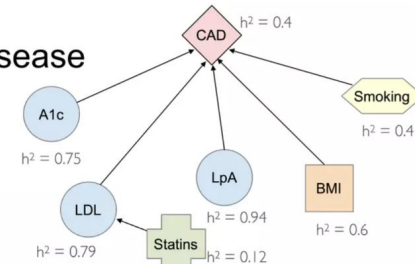
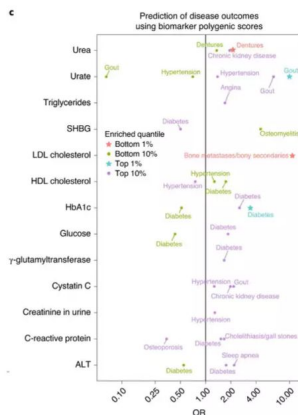
Individual 1	1.5	-	0.5	+	4.0	-	0.0	=	5.0
Individual 2	1.5	-	0.0	+	2.0	-	1.5	=	2.0
Individual 3	0.0	-	1.0	+	2.0	-	1.5	=	-0.5
Individual 4	0.0	-	1.0	+	0.0	-	3.0	=	-4.0



Common workflow - multi-trait PRS

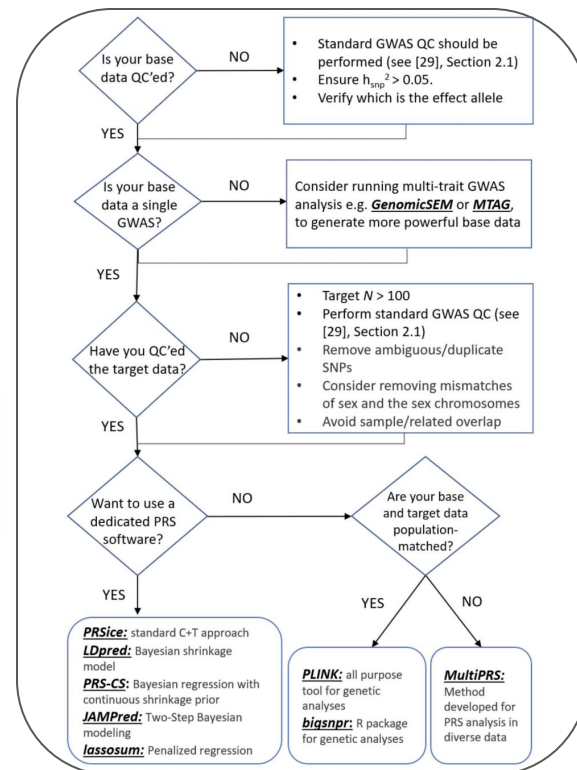
- Multiple observations suggest “biomarkers → disease” links

- PRS-PheWAS analysis
- Biomarkers are more heritable than disease
- Mendelian Randomization



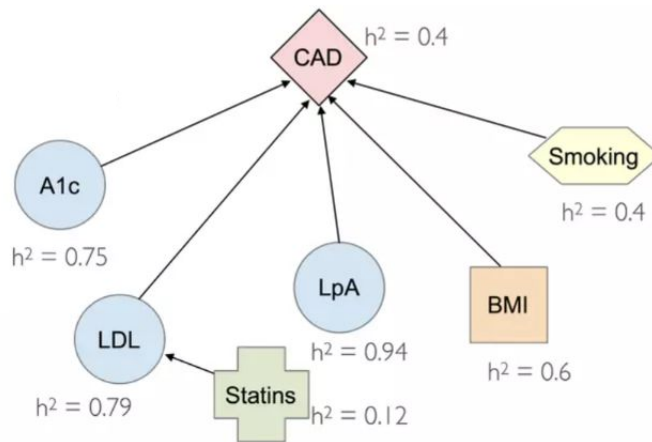
- Multi-PRS is a weighted sum of PRSs

$$\text{i.e. } w_1(\text{PRS}_1) + w_2(\text{PRS}_2) + w_3(\text{PRS}_3) + \dots$$

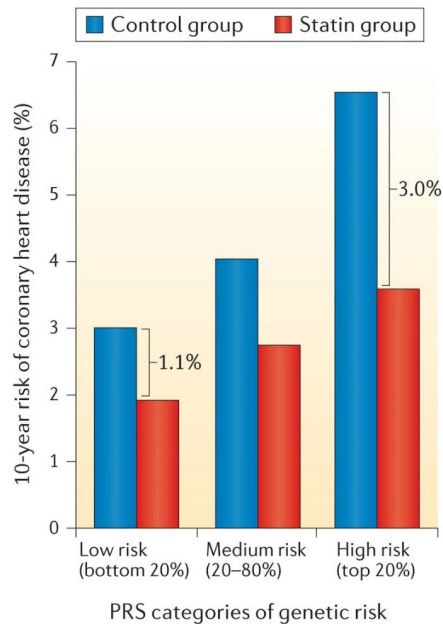


Common workflow - multi-trait PRS

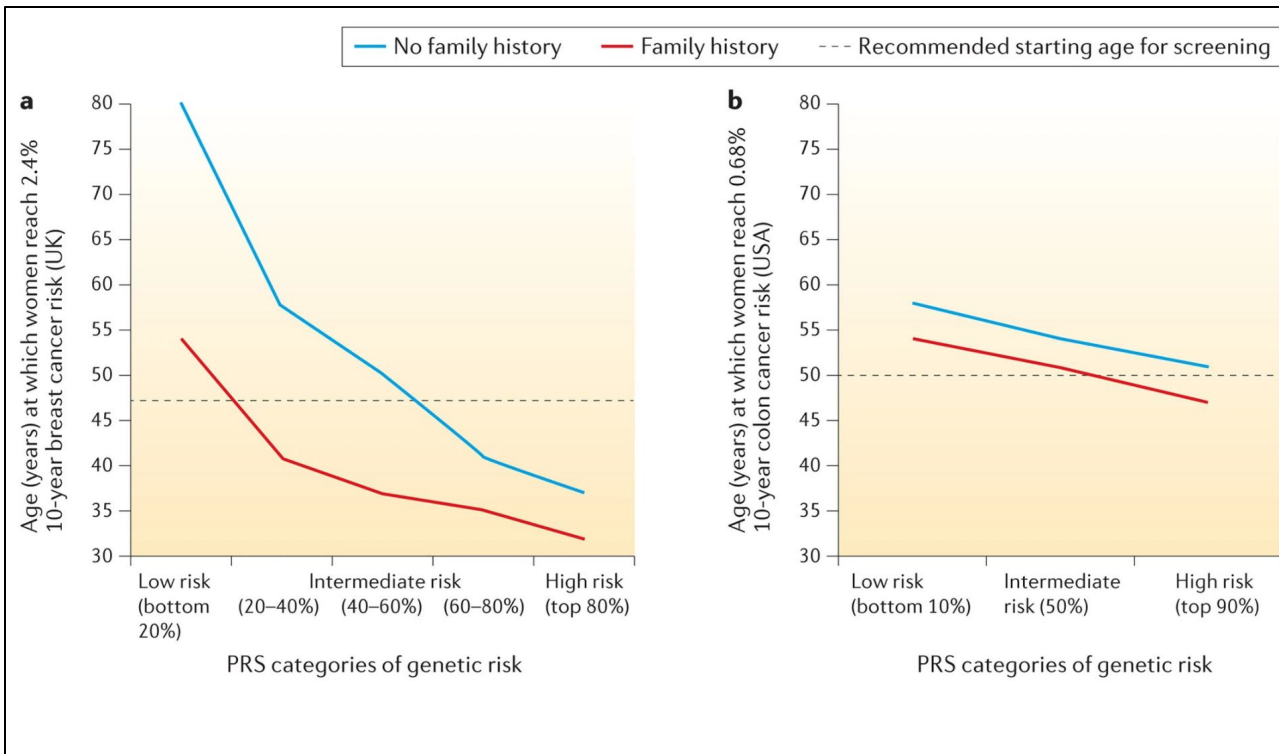
- Multi-PRS is a weighted sum of PRSs
i.e. $w_1(\text{PRS}_1) + w_2(\text{PRS}_2) + w_3(\text{PRS}_3) + \dots$



Case study - disease stratification

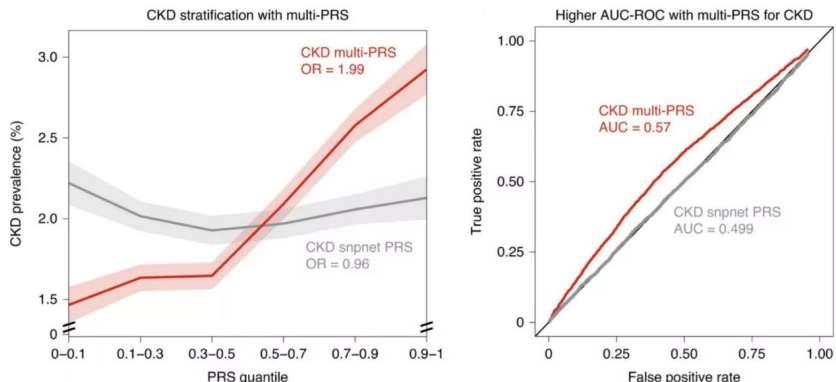


ARR (%)	1.1	1.3	3.0
RRR	0.36	0.32	0.46

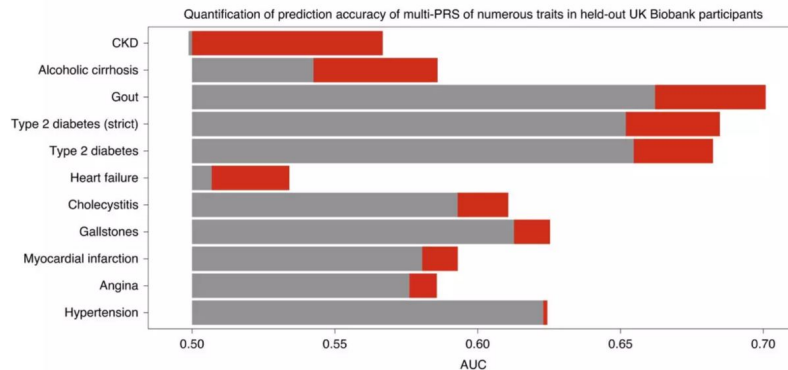


Case study - multi-trait PRS improves disease prevalence prediction

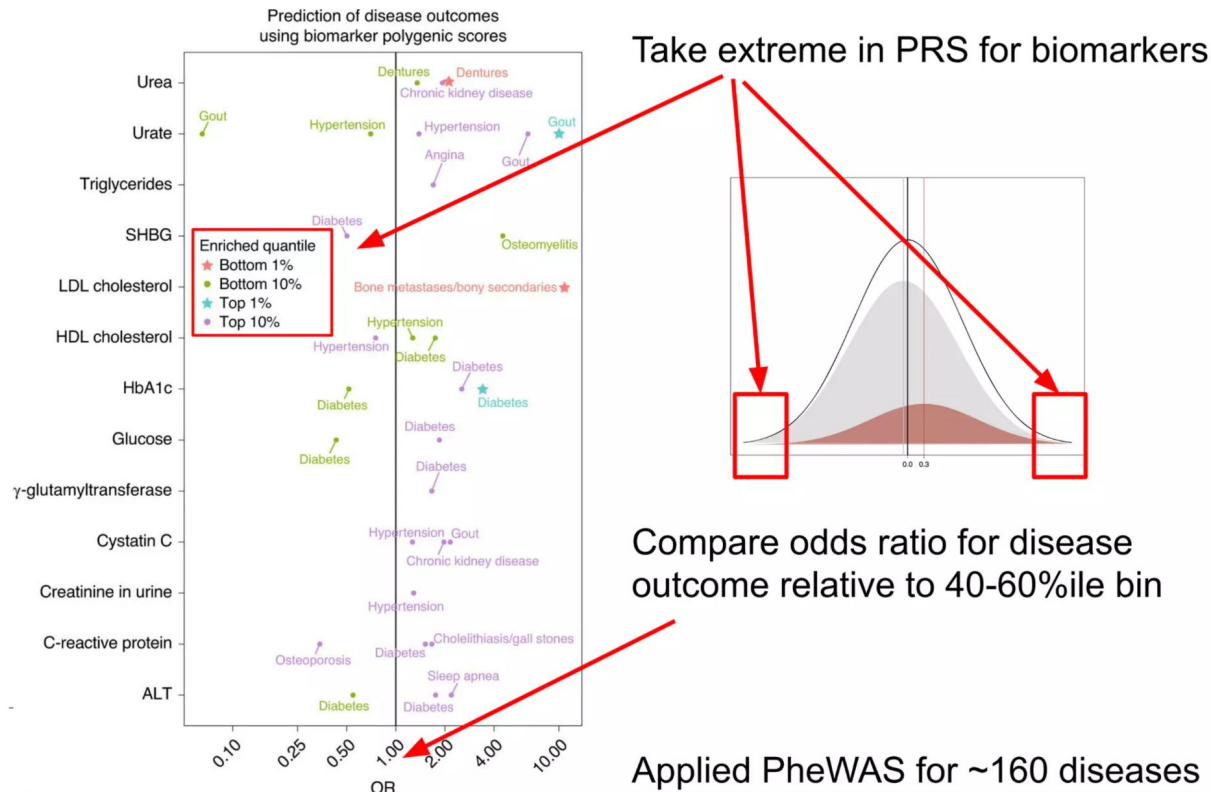
Chronic kidney disease (CKD)



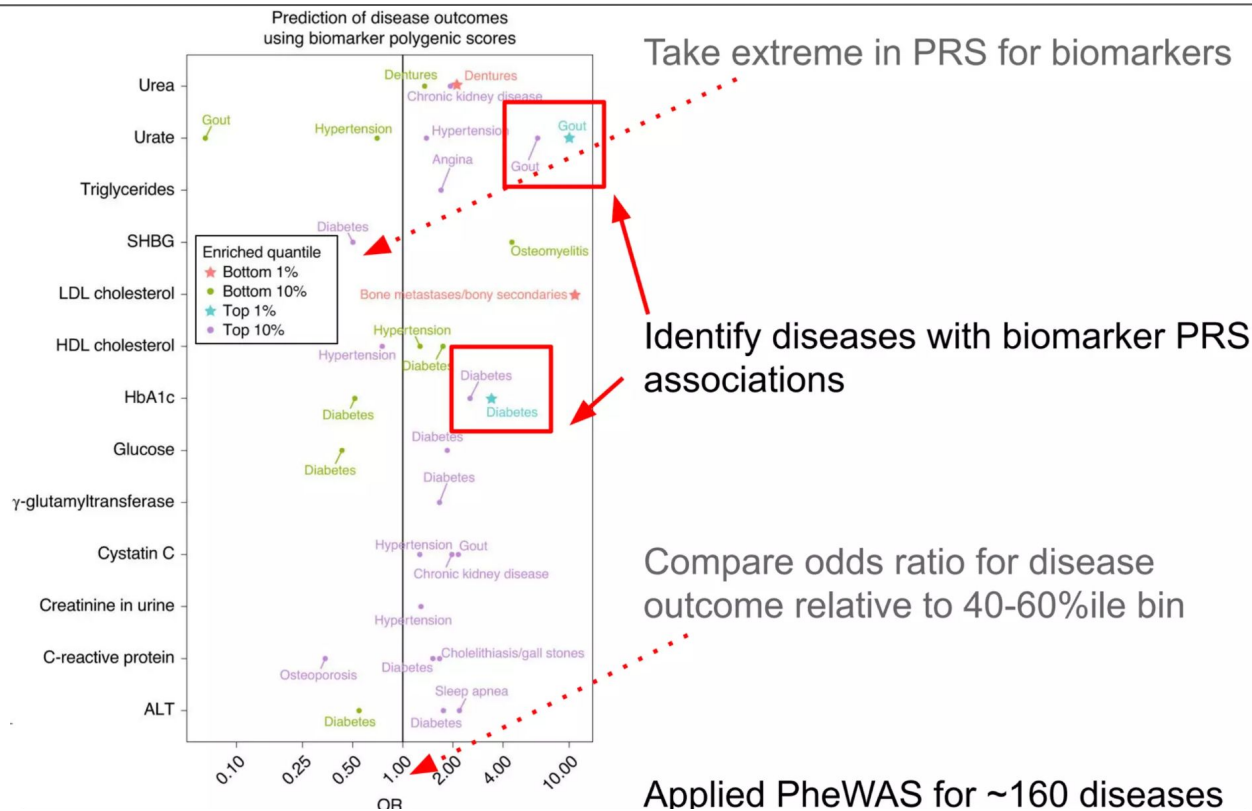
Other diseases in UK Biobank



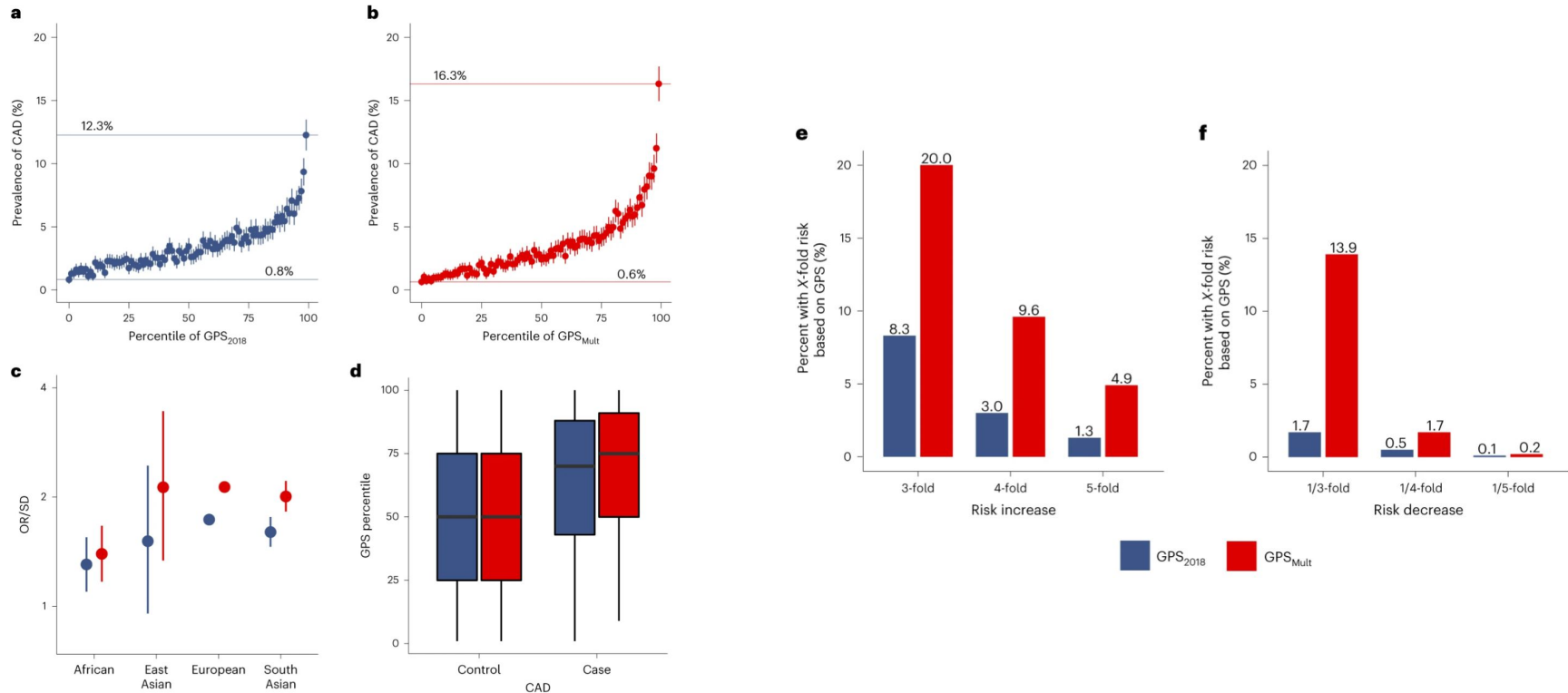
Use of PRS for trait / disease prediction



Use of PRS for trait / disease prediction

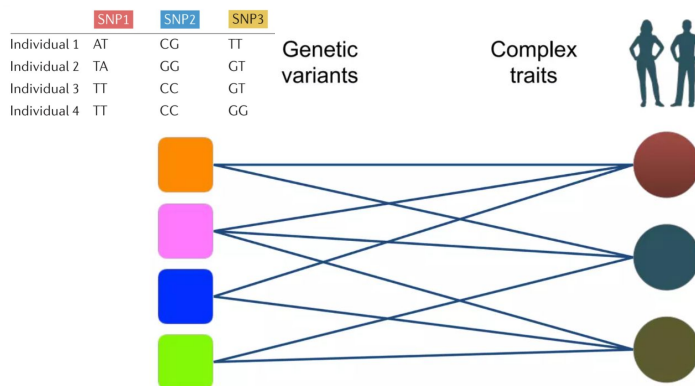


Limitations - ethnicity / ancestry



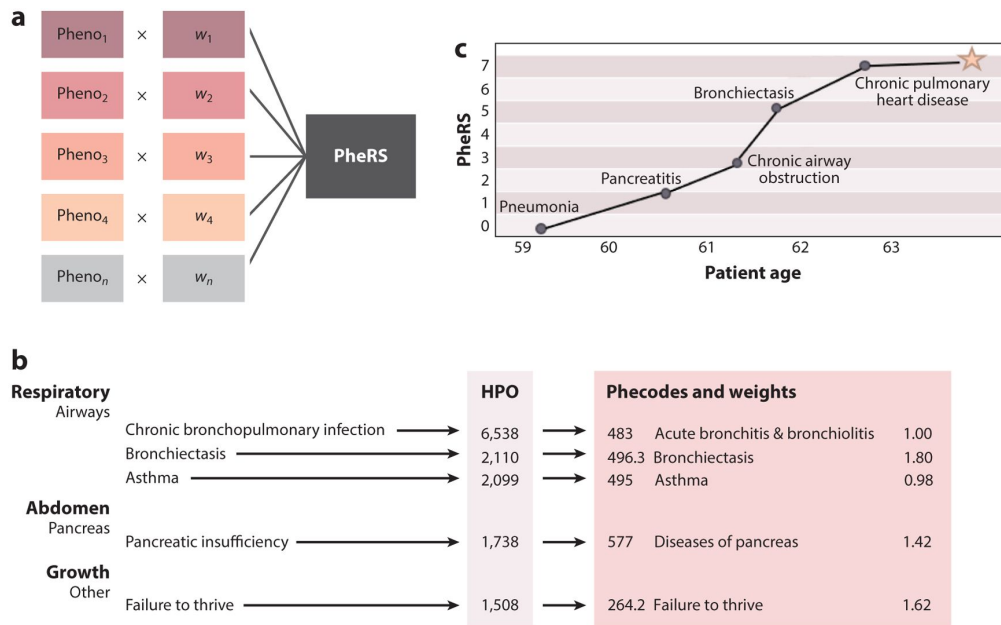
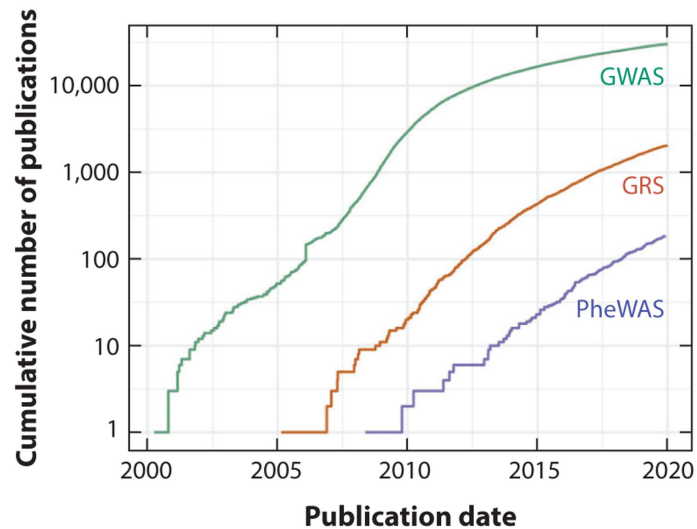
Limitations - polygenicity & pleiotropy

- Polygenicity: many variants - one trait
- Pleiotropy: one variant - many traits



- Large number of associations in population-based cohorts
- Can we group them together for enhanced interpretation?

Going further - EHR's & PRS



Summary

Two complementary approaches to improve predictive performance:

- Sample size → increase in **statistical power**
 - Multi-trait PRS analysis

Why does multi-PRS work?

- Quantitative traits have more power
- **Genetic correlation** between biomarkers and disease

The multi-trait PRS model:

Genetics → Biomarkers (molecular traits) → Disease