

SPACE-TIME DISCRETISATION OF THE

WAVE EQUATION

$$\frac{\partial^2 y}{\partial t^2} = \alpha^2 \frac{\partial^2 y}{\partial x^2}$$
 Poe

DISCRETISATION OF LAPLACIAND

San ym =
$$\frac{y_{m-1} - 2y_m + y_{m+1}}{\Delta_{x}^{2}}$$
 => INTERNAL POINTS $\frac{\partial^{2}}{\partial n^{2}}$ $\frac{\partial^{2}}{\partial n^{2}}$ LAPLACIAN

$$\left(S_{222}y_{m} = \frac{y_{m-2} - Ly_{m-1} + 6y_{m} - Ly_{m+1} + y_{m+2}}{\Delta_{2}^{u}}\right)$$

$$\frac{LND6FWEO!}{S_{22}} = \frac{y_{m-2} - Ly_{m-1} + 6y_{m} - Ly_{m+1} + y_{m+2}}{\Delta_{2}^{u}}$$

$$\frac{LND6FWEO!}{S_{22}} = \frac{1}{2} \frac{LND6FWEO!}{DIRICHLET}$$

$$\frac{1}{2} \frac{1}{2} \frac{1}{2}$$

y = y(x,t) $x \in [0,L]$ $(x,t) \mapsto \vec{y}(t) \in \mathbb{R}^{M-1} \xrightarrow{n} \vec{y} \vec{y}$

$$Sany_0 = \frac{y_{-1} - 2y_0 + y_1}{3a^2} = \frac{-2y_0 + 2y_1}{3a^2}$$

$$Sa.y_0 = 0 \rightarrow y_{-1} = y_1$$

For Neumann?

Sanyo =
$$\frac{y-1-2y_0+y_1}{4a^2}$$
 $= \frac{-2y_0+2y_1}{5a^2}$

Sanyo = $0 \rightarrow y-1=y_1$

STIFF STRING

AFTER SPATIAL DISCRETISATION, PROCEED WITH TIME

INTEGRATION

$$\ddot{y} = \alpha^2 \, \text{Dan } \ddot{y}$$

$$\frac{y^{n+1}-2y^n+y^{n-1}}{n^2} = a^2 \underbrace{\sum_{n=2}^{\infty} 2n} y^n$$

$$\frac{\partial^2 y}{\partial t^2} = d^2 \frac{\partial^2 y}{\partial n} y + S(x - x_f) + (t)$$

 $\ddot{y}(t) = d^2 \sum_{i=1}^{n} x_i \dot{y} + \vec{J} f(t)$ SPREADING OPENATION



- · GONDITIONALLY STABLE! (WHAT IS THE STABILITY CONDITION HERE!)

reavines two previous STOVED IN STEPS to BE MEMORY, NO MOLE