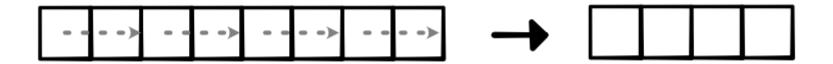
## Module 4.3 - Advanced NNs

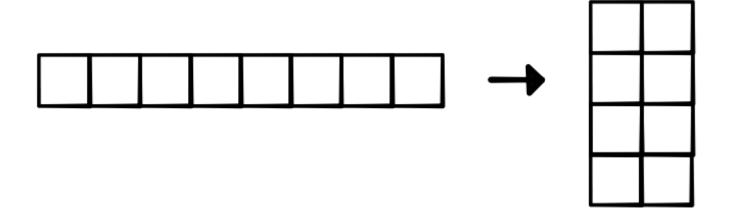
# "Pooling"

Reduction applied to each region:



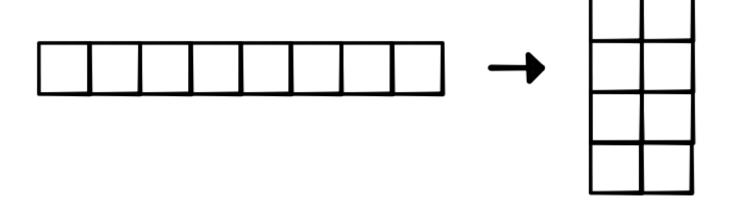
### Simple Implementation

- Ensure that it is contiguous
- Use View to "fold" the tensor



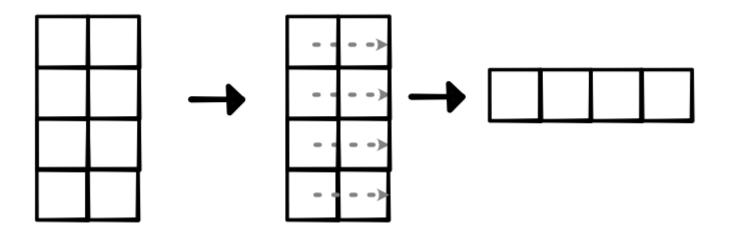
#### Why does folding work?

- View requires "contiguous" tensor
- View(4, 2) makes strides (2, 1)



# Simple Implementation

Reduce along created fold



# Quiz

#### **Gradient Flow**

- Layers that are used get more updates
- Gradient signals which aspect was important
- Can have extra layers

#### More Reductions

- Heading for a max reduction
- Heading for a softmax output
- Quick detour

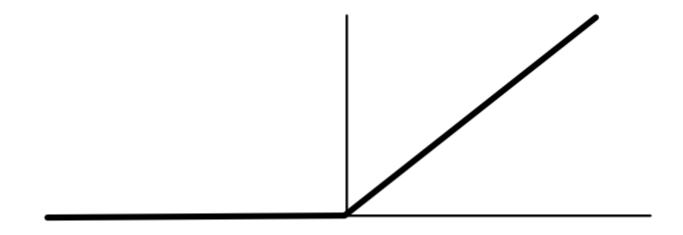
# ReLU, Step, Sigmoid

#### Basic Operations

- Introduced in Module-0
- Widely used in ML
- What is it?

## Simple Function: ReLU

Main "activation" function

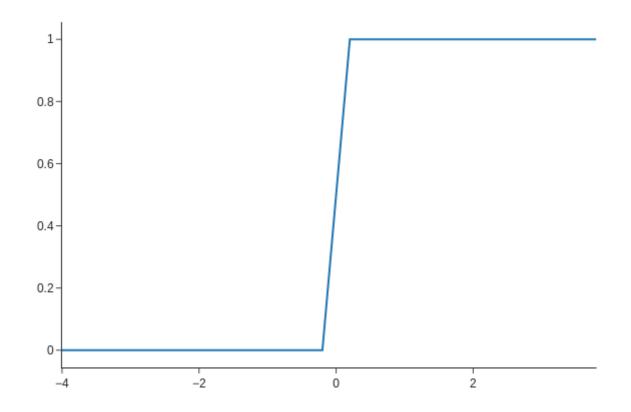


Primarily used to split the data.

#### Simple Function: Step

Step function f(x) = x > 0 determines correct answer

Derivative of ReLU



#### ReLU

Mathematically,

$$ReLU(x) = max\{0, x\}$$

Simplest max function.

## Step

Mathematically,

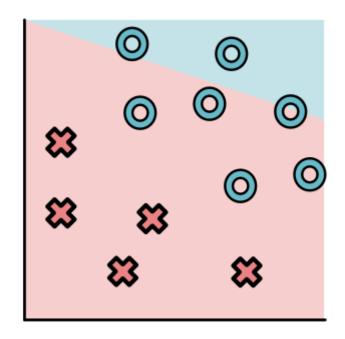
$$step(x) = x > 0 = \arg\max\{0, x\}$$

Simplest argmax function.

#### Relationship

Step is derivative of ReLU

$$ext{ReLU}'(x) = egin{cases} 0 & ext{if } x \leq 0 \ 1 & ext{ow} \end{cases}$$
  $ext{step}(x) = ext{ReLU}'(x)$ 



Loss of step tells us how many points are wrong.

#### Derivative of Step?

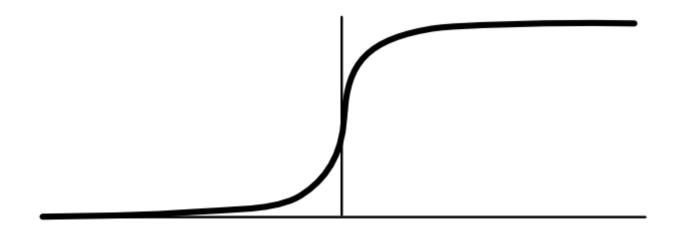
Mathematically,

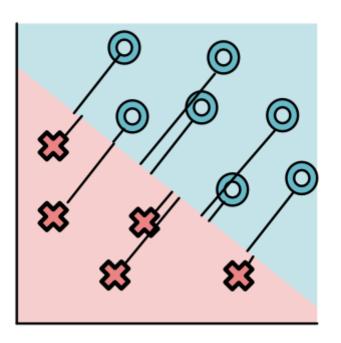
$$ext{step}'(x) = egin{cases} 0 & ext{if } x \leq 0 \ 0 & ext{ow} \end{cases}$$

Not a useful function to differentiate

# Altenative Function: Sigmoid

Used to determine the loss function





## Soft (arg)max?

Would be nice to have a version that with a useful derivative

$$sigmoid(x) = softmax\{0, x\}$$

Useful soft version of argmax.

# Max, Argmax, Softmax

## Challenge

How do we generalize sigmoid to multiple outputs?



### Max reduction

- Max is a binary associative operator
- $\max(a,b)$  returns  $\max$  value
- Generalized  $\operatorname{ReLU}(a) = \max(a,0)$

### Max Pooling

- Common to apply pooling with max
- Sets pooled value to "most active" in block
- Forward code is easy to implement

### Max Backward

- Unlike sum, max throws away other values
- Only top value gets used
- Backward needs to know this.

## Argmax

- Function that returns argmax, one-hot
- Generalizes step



### Max Backward

- First compute argmax
- Only send gradient to argmax gradinput
- Everything else is 0

#### Ties

- What if there are two or more argmax's?
- Max is non-differentiable, like ReLU(0).
- Short answer: Ignore, pick one

#### HW

- When writing tests for max, ties will break finitedifferences
- Suggestion: perturb your input by adding a small amount of random noise.

### Soft argmax?

- Need a soft version of argmax.
- Generalizes sigmoid for our new loss function
- Standard name -> softmax

### Softmax

$$\operatorname{softmax}(\mathbf{x}) = \frac{\exp \mathbf{x}}{\sum_{i} \exp x_{i}}$$

## Sigmoid is Softmax

$$\operatorname{softmax}([0,x])[1] = \frac{\exp x}{\exp x + \exp 0} = \sigma(x)$$

### Softmax

Softmax



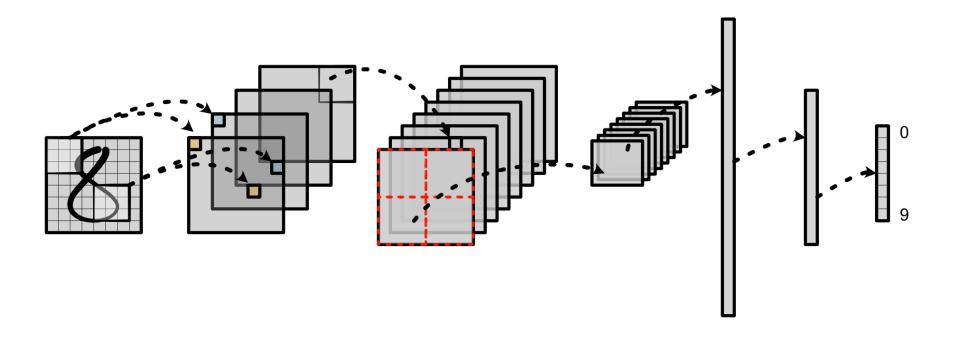
### Review

- ReLU -> Max
- Step -> Argmax
- Sigmoid -> Softmax

## Softmax

### Network

#### Network



## Softmax Layer

- Produces a probability distribution over outputs (Sum to 1)
- Derivative similar to sigmoid
- Lots of interesting practical properties

### Softmax in Context

- Not a map!
- Gradient spreads out from one point to all.

### Softmax

• (Colab)

[https://colab.research.google.com/drive/1EB7MI\_3gzAR1g

# Soft Gates

### **New Methods**

- Sigmoid and softmax produce distributions
- Can be used to "control" information flow

## Example

Returns a combination of x and y

$$f(x, y, r) = x * \sigma(r) + y * (1 - \sigma(r))$$

### Gradient is controlled

$$egin{array}{ll} f_x'(x,y,r) &= \sigma(r) \ f_y'(x,y,r) &= (1-\sigma(r)) \ f_r'(x,y,r) &= (x-y)\sigma'(r) \end{array}$$

#### **Neural Network Gates**

Learn which one of the previous layers is most useful.

$$egin{aligned} r &= NN_1 \ x &= NN_2 \ y &= NN_3 \end{aligned}$$

#### **Gradient Flow**

- Layers that are used get more updates
- Gradient signals which aspect was important
- Can have extra layers

## Selecting Choices

- Gating gives us a binary choice
- What if we want to select between many elements?
- Softmax!

# Softmax Gating

Combines many elements of X based on R

$$f(X,R) = X \times softmax(R)$$

# Softmax Gating

• Brand name: Attention

# Example: Translation

Show example

Example: GPT-3

Show example

