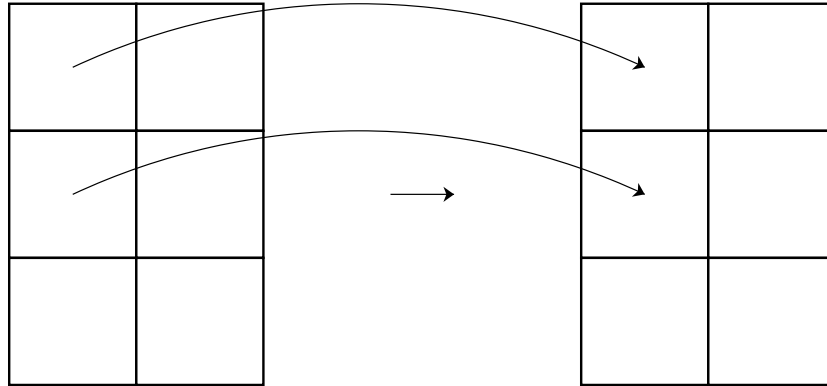




# Module 2.3 - Advanced Tensors

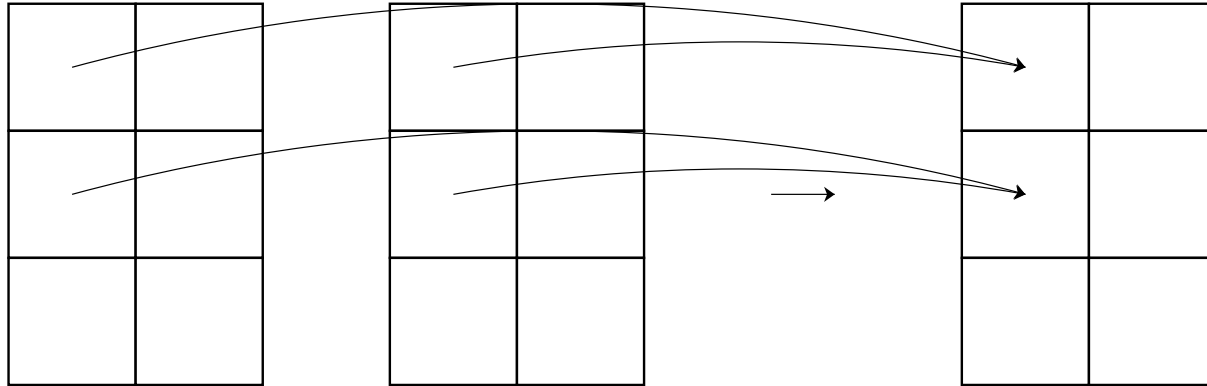


# Map



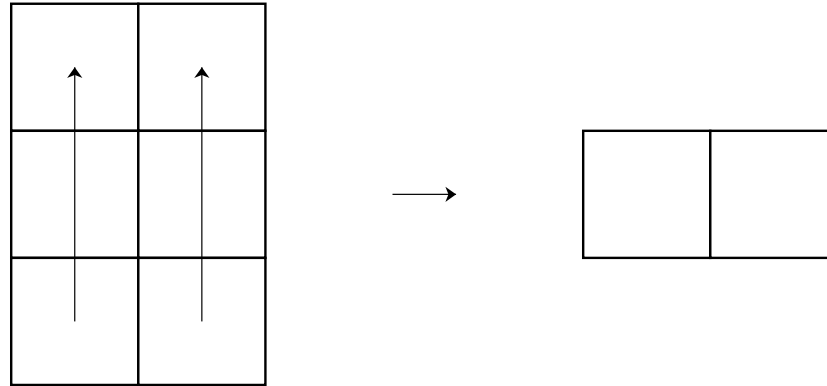


# Zip





# Reduce







# Quiz



# Outline

- Broadcasting
- Gradients
- Tensor Puzzles



# Broadcasting



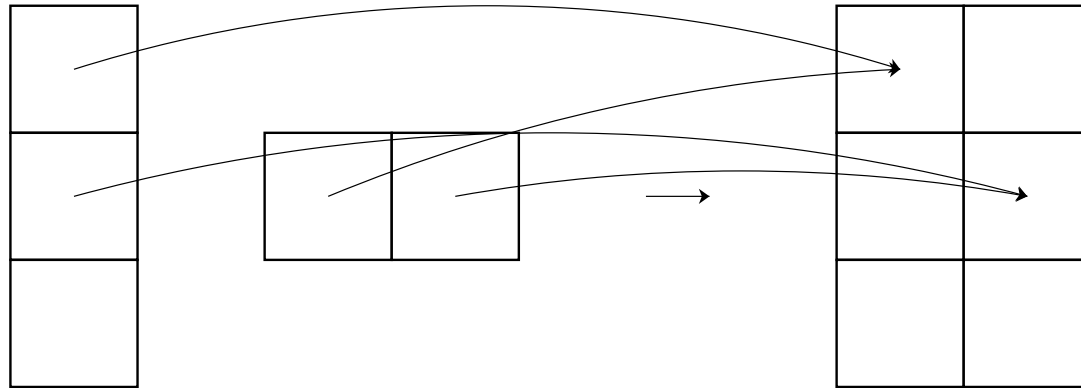
# Motivation: Scalar Addition

$$\textit{vector1} + 10$$





# Zip Broadcasting





# Rules

- **Rule 1:** Dimension of size 1 broadcasts with anything
- **Rule 2:** Extra dimensions of 1 can be added with `view`
- **Rule 3:** Zip automatically adds starting dims of size 1



# Applying the Rules

- $(3, 4, 5) \mid (3, 1, 5) \Rightarrow (3, 4, 5)$
- $(3, 4, 1) \mid (3, 1, 5) \Rightarrow (3, 4, 5)$
- $(3, 4, 1) \mid (1, 5) \Rightarrow (3, 4, 5)$
- $(3, 4, 1) \mid (3, 5) \Rightarrow X$



# Broadcasting Example

3	4	1
	1	5
-----		
3	4	5





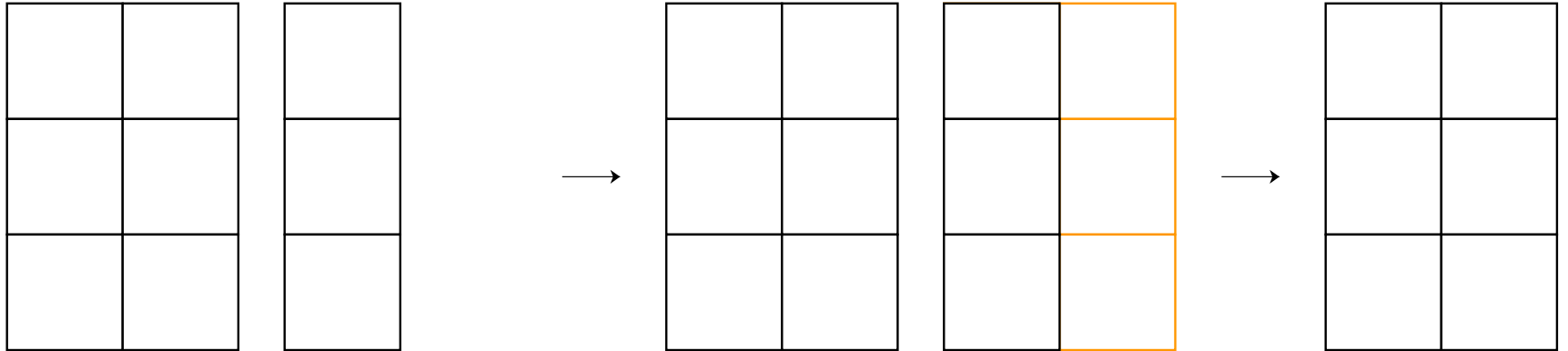
# Matrix-Vector

```
x = minitorch.tensor([[1, 2], [3, 4], [5, 6]])  
y = minitorch.tensor([[1], [3], [5]])  
z = x + y  
z.shape
```

(3, 2)



# Matrix-Vector





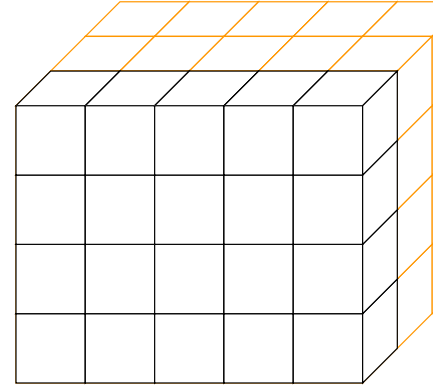
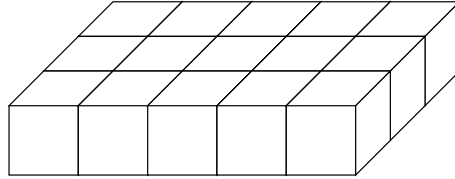
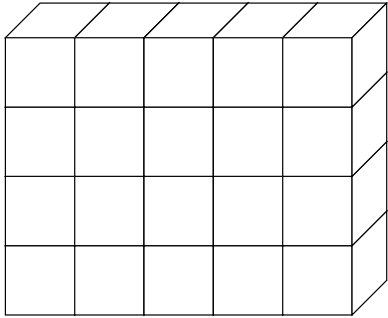
# Matrix-Matrix

```
x = minitorch.zeros((4, 5))  
y = minitorch.zeros((3, 1, 5))  
z = x + y  
z.shape
```

(3, 4, 5)



# Matrix-Matrix







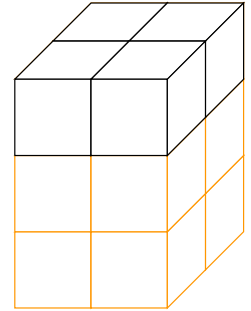
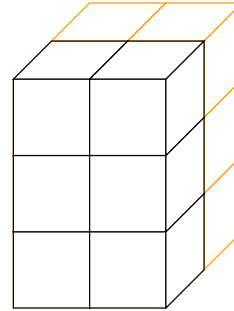
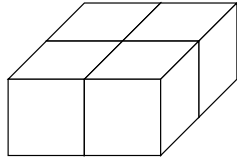
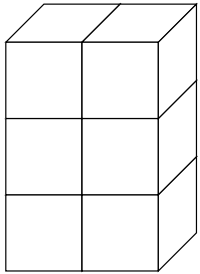
# "Matrix multiplication"

```
x = minitorch.zeros((3, 2))  
y = minitorch.zeros((2, 1, 2))  
z = (x * y).sum(2)  
z.shape
```

```
(2, 3, 1)
```



# "Matrix multiplication"





# Implementation

- Never create an intermediate value.
- Implicit map between output space / input space



# Functions

- `shape_broadcast` - create the broadcast dims
- `broadcast_index` - map from broadcasted to original value





# Tensor Puzzles



# Special PyTorch Syntax

(Not available in minitorch)

```
import torch

x = torch.tensor([1, 2, 3])
print(x.shape)
print(x[None].shape)
print(x[:, None].shape)
```

```
torch.Size([3])
torch.Size([1, 3])
torch.Size([3, 1])
```



# Tensor Function

```
x = torch.arange(10)
print(x)
```

```
y = torch.arange(4)
print(y)
```

```
tensor([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
tensor([0, 1, 2, 3])
```



# Tensor Function

```
x = torch.where(  
    torch.tensor([True, False]),  
    torch.tensor([1, 1]),  
    torch.tensor([0, 0]),  
)  
print(x)
```

```
tensor([1, 0])
```





# Tensor Puzzles

## Tensor Puzzles



Q&A

