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# Advances in SRF cavity architectures for quantum computing

**Tanay Roy**

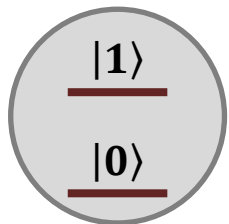
SQMS division, Fermilab

Quantum Technologies for Fundamental Physics Workshop, Erice, Italy

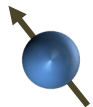
3 Sep 2023

Report number: FERMILAB-SLIDES-23-283-SQMS

# Basic Requirements for a Quantum Computer

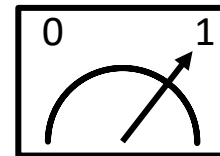


Quantum two  
level systems

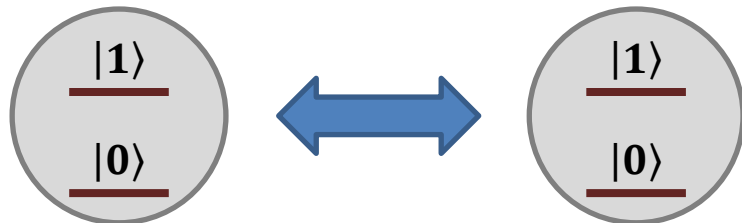


$$\alpha|0\rangle + \beta|1\rangle$$

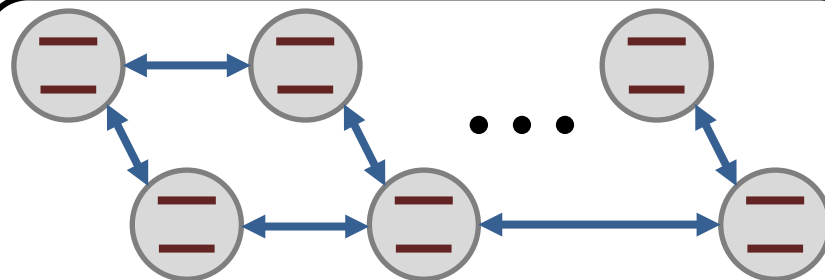
Create arbitrary  
states



Measure  
quantum states



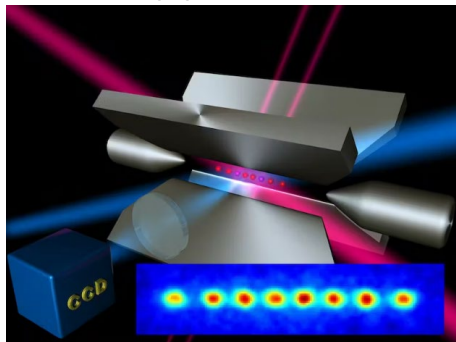
Couple multiple qubits



Scalable architecture

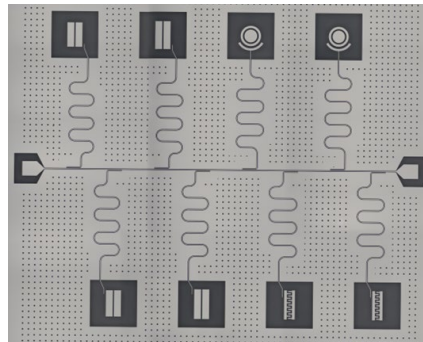
# Different Platforms

Trapped ions



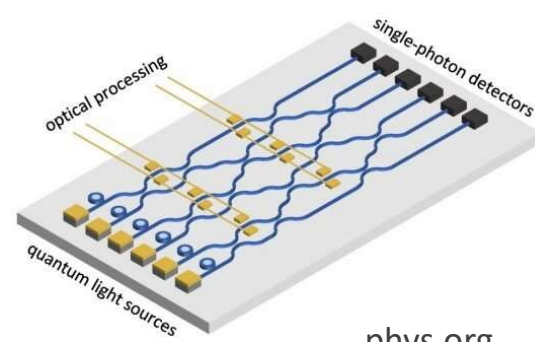
laserfocusworld.com

Superconducting circuits



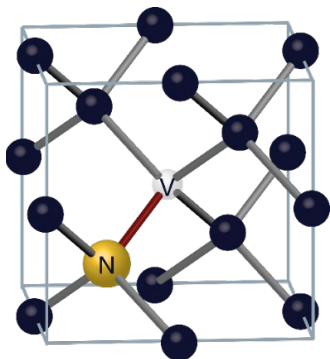
SQMS

Photonic crystals



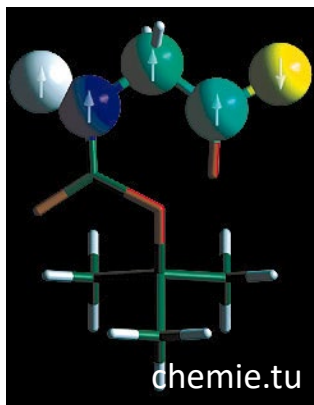
phys.org

NV centers



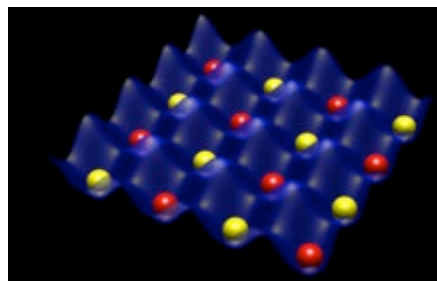
phys.org

NMR



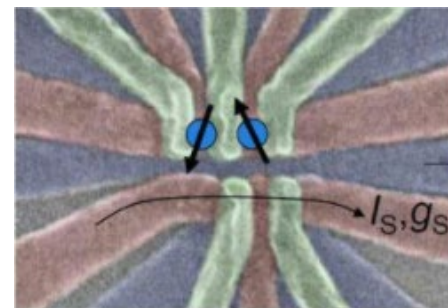
chemie.tu

Neutral atoms



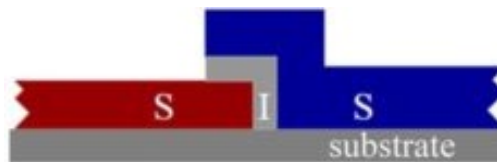
NIST

Quantum dots



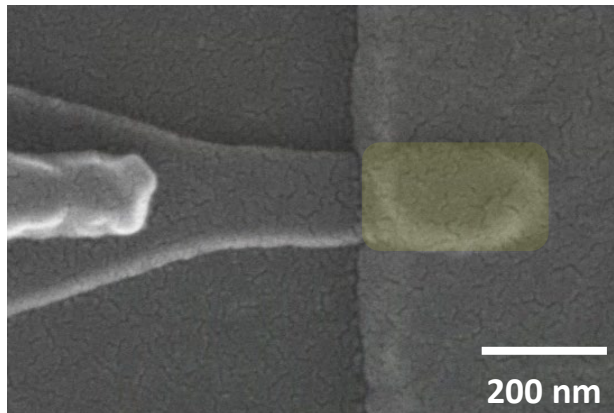
sciencemag.org

# Superconducting Circuits



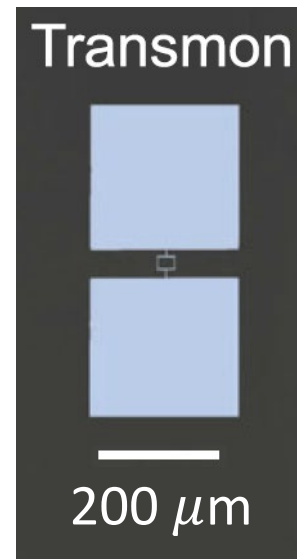
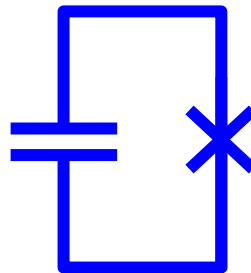
Josephson Junction

Lossless nonlinear inductor

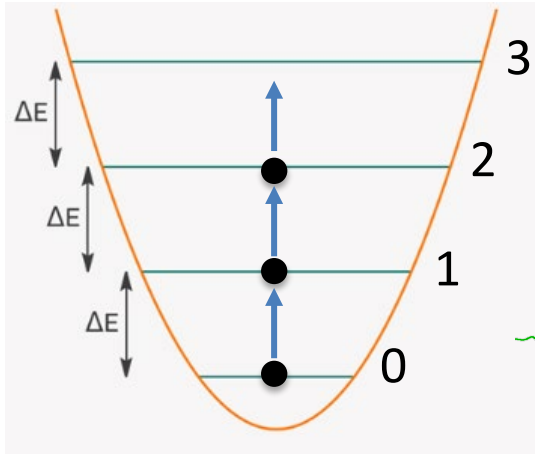


$$L_J(I) = \frac{\varphi_0}{(I_0^2 - I^2)^{1/2}}$$

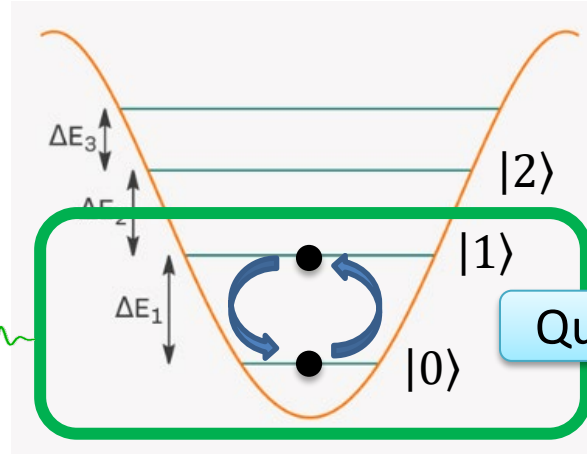
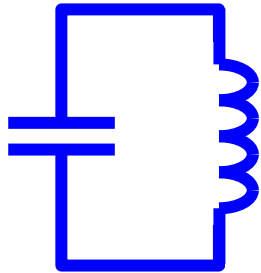
Transmon



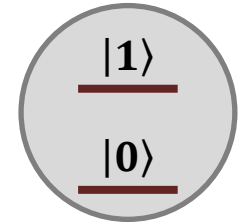
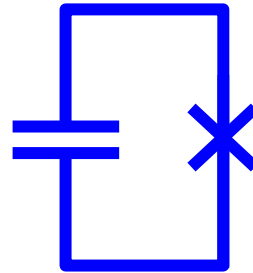
# Transmon: Anharmonic Oscillator



Harmonic Oscillator



Anharmonic Oscillator



# Operating Temperature

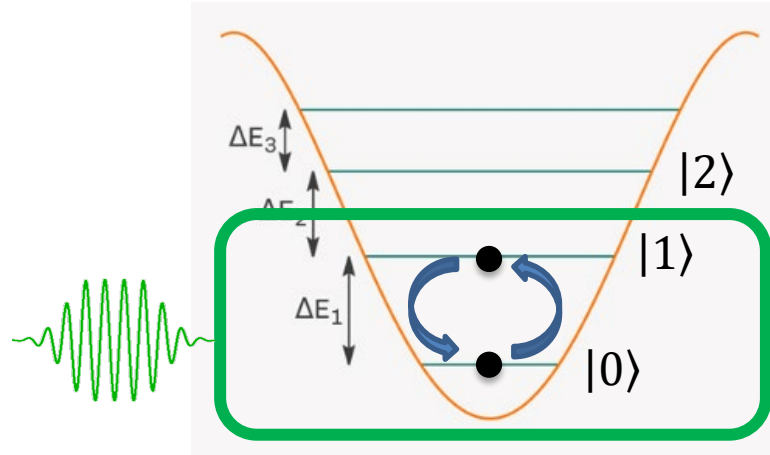
$$f_{01} \approx \frac{1}{2\pi\sqrt{L_J C}}$$

$\sim 5 \text{ GHz}$

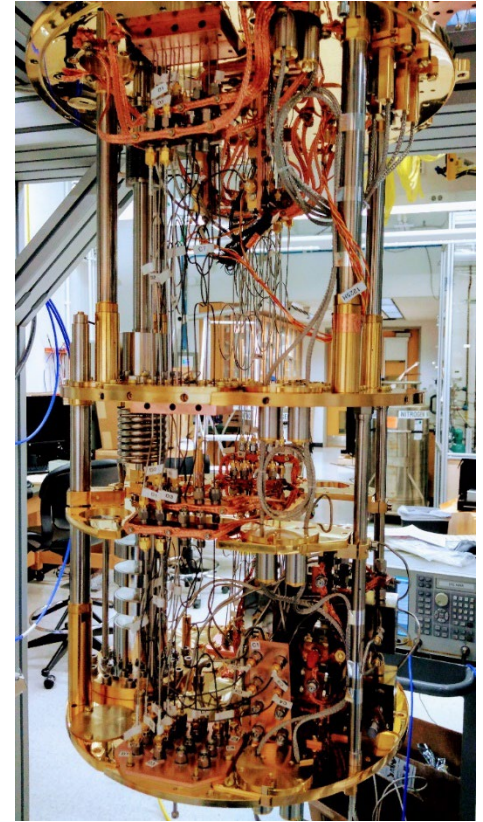
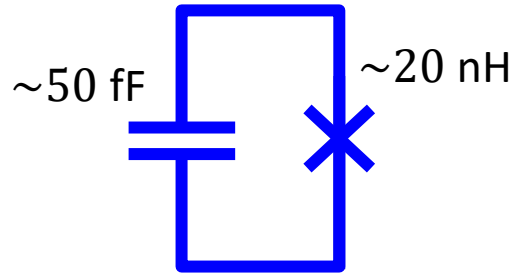
$$k_B T \ll h f_{01}$$

20 mK

$\sim 240 \text{ mK}$



Anharmonic Oscillator

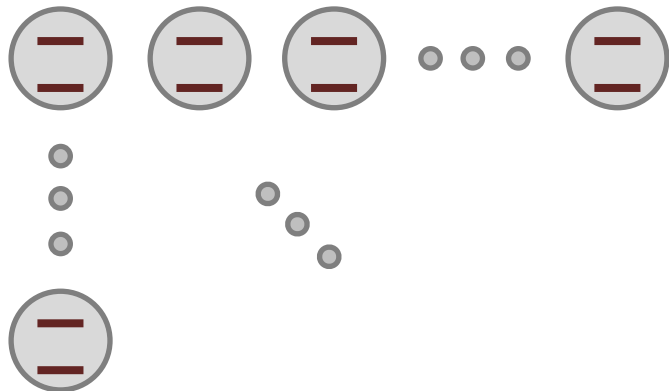


Dilution fridge  $\sim 10 \text{ mK}$



# Traditional Multi-qubit Architecture

Linear or planar geometry

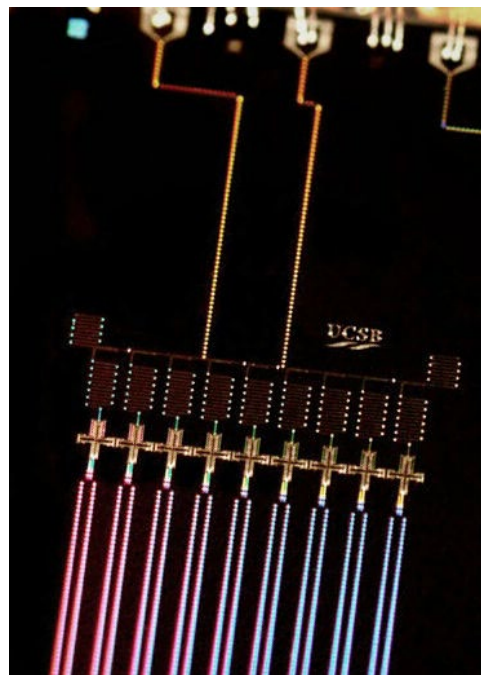


Computational space:  $2^N$

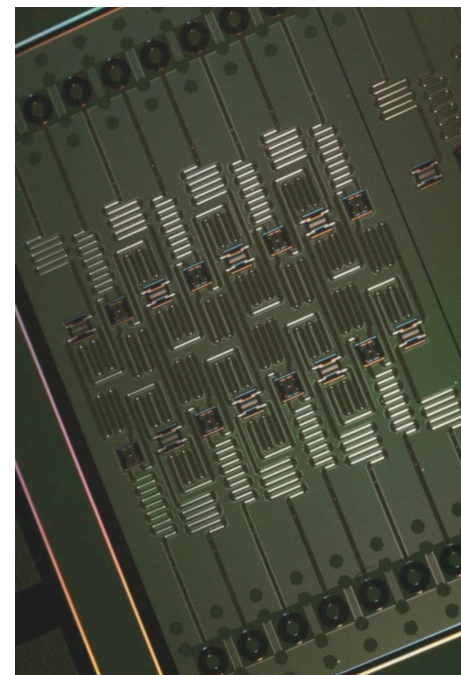
Can we do **better**?

Scaling:  $d^N$ ,  $d > 2$

**Qudit**



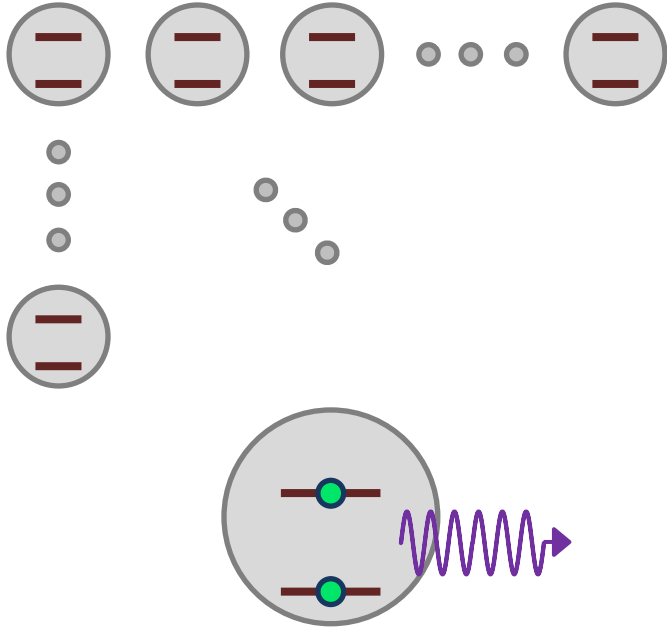
UCSB, Nature 519 (7541)



IBM

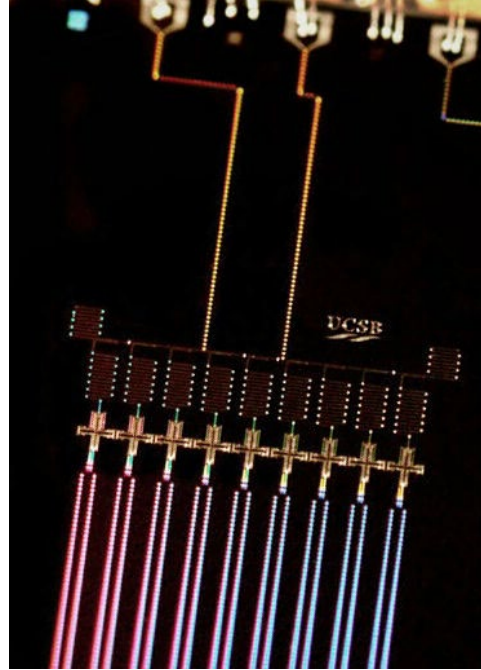
# Problem of Relaxation

Linear or planar geometry

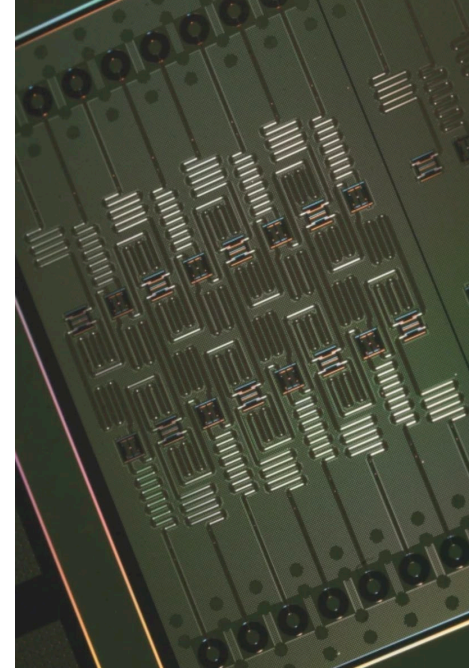


$$T_1 \sim 100 \mu\text{s}$$

Q: a few  $10^6$



UCSB, Nature 519 (7541)

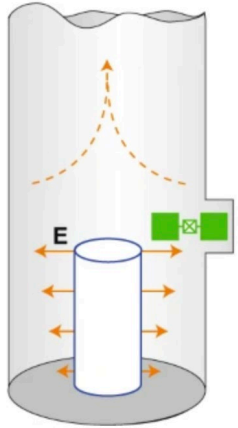


IBM

Can we do **better**?

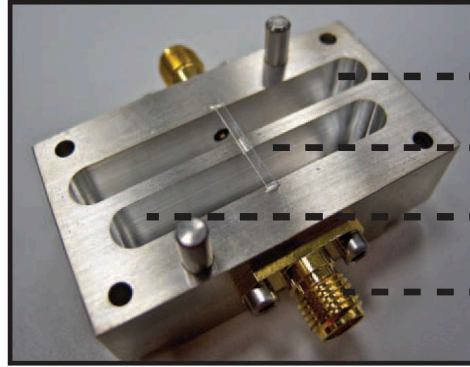


# Zoo of Cavities



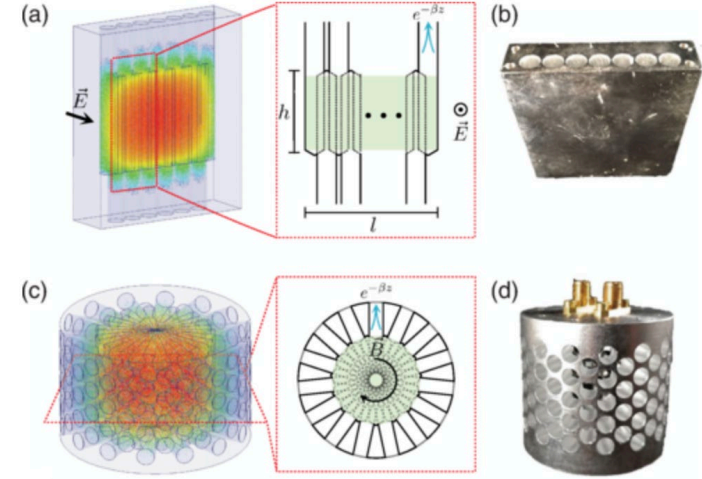
Nat. Phys. 16, 247

Yale, U. Pittsburgh



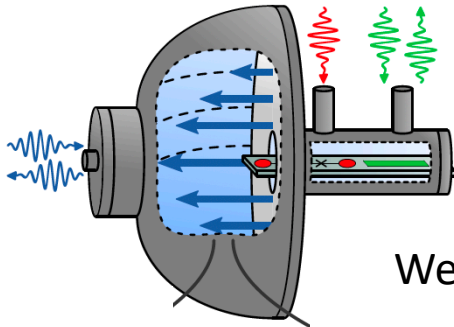
- cavity 1
- transmon qubit
- cavity 2
- cavity coupler

Science 342, 6158



PRL 127, 107701

U. Chicago, Rutgers



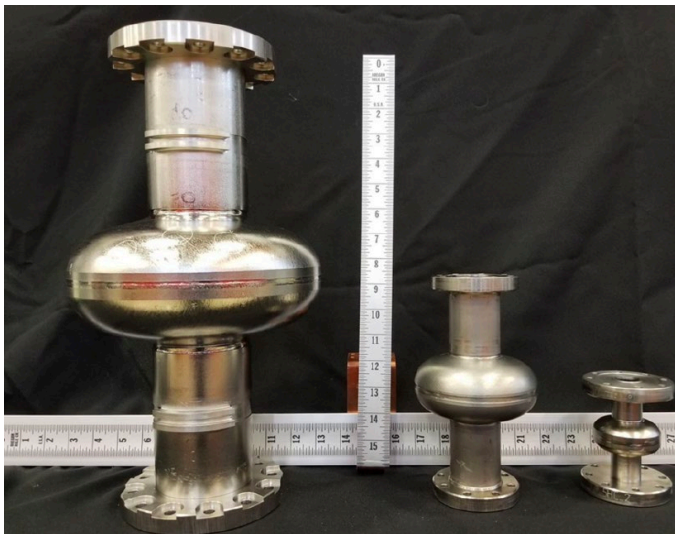
Weizmann

Under  
exploration

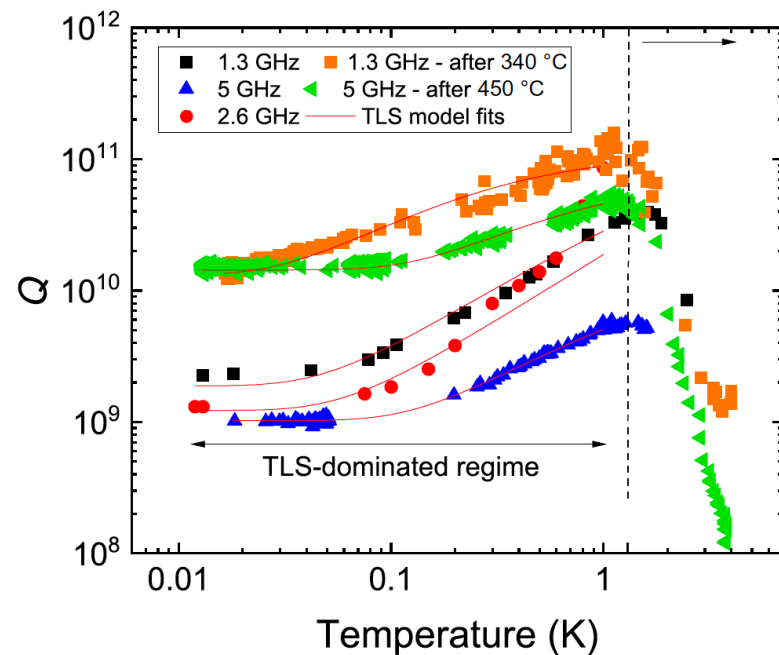
arXiv:2302.06442

Tanay Roy - Fermilab

# High-Q 3D SRF Cavities



Romanenko et al. PRApplied 13, 034032



1.3 GHz SRF:  $Q > 10^{11}$  at 1 K



$T_1 > 2$  s

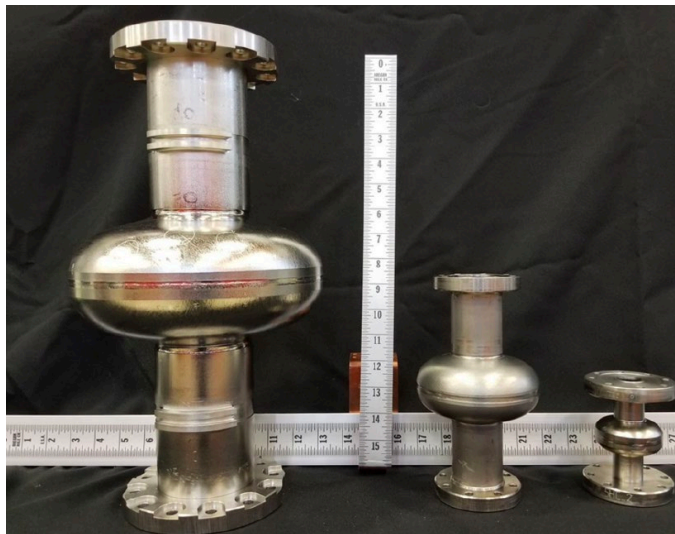
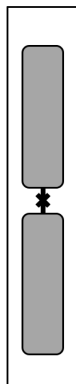
5 GHz SRF:  $Q > 10^{10}$  at 10 mK



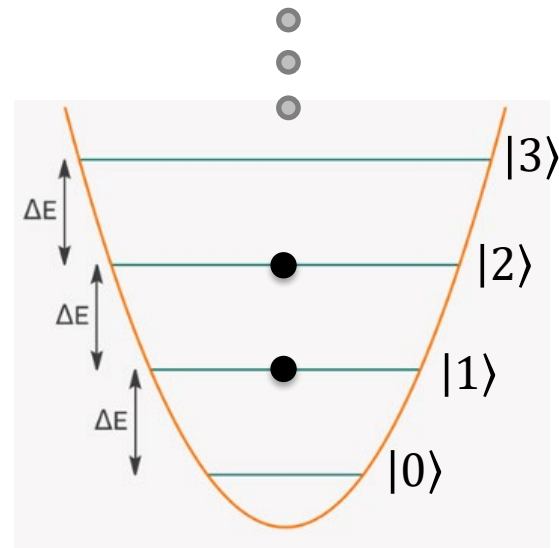
$T_1 > 300$  ms

**>1000 times better than  
transmons**

# High-Q 3D Cavities as Qudits



Romanenko et al. PRApplied 13, 034032



**Qudit**

Still much better than transmon qubits

$$T_1^{|1\rangle} > 300 \text{ ms}$$

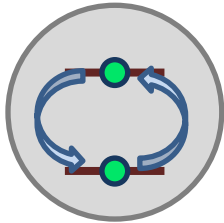
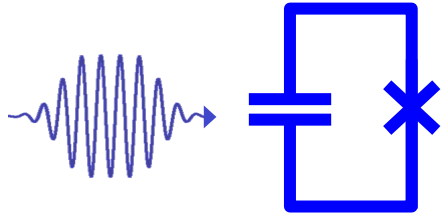
$$T_1^{|2\rangle} > 150 \text{ ms}$$

$$T_1^{|n\rangle} > T_1^{|1\rangle}/n$$

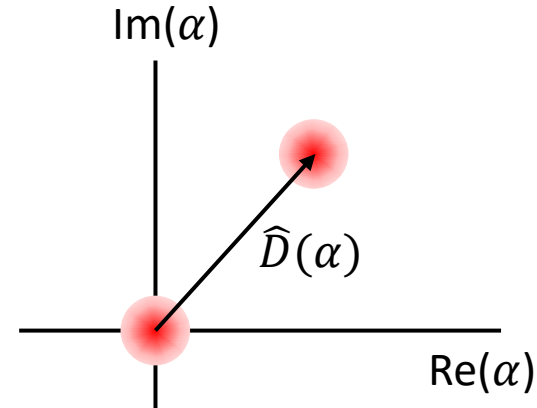
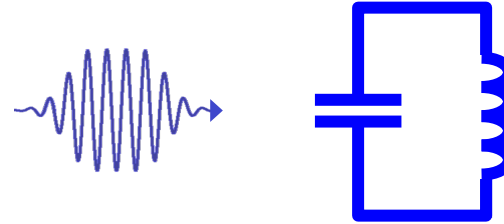
$$T_1^{|10\rangle} > 30 \text{ ms}$$

# Transmon vs. Cavity Drive

Qubit:  $\alpha|0\rangle + \beta|1\rangle$



Qudit:  $\alpha_0|0\rangle + \alpha_1|1\rangle + \dots + \alpha_d|d\rangle$



# Qudit Operation

$$|0\rangle \xrightarrow{\mathcal{D}(\alpha=1)} \alpha_0|0\rangle + \alpha_1|1\rangle + \cdots + \alpha_d|d\rangle$$

$$|1\rangle \rightarrow e^{i\pi}|1\rangle \quad \downarrow$$

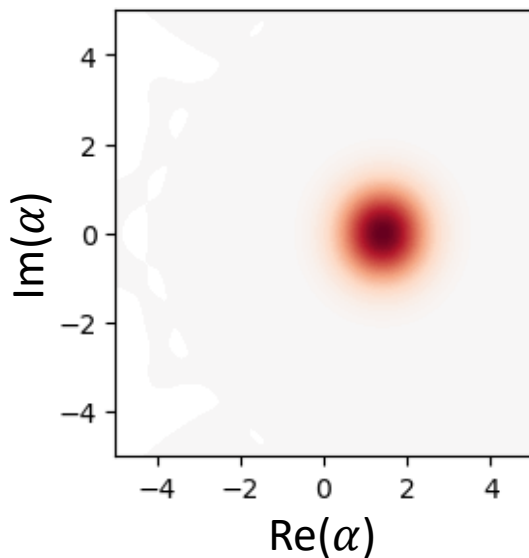
Quantum state

$$\alpha_0|0\rangle - \alpha_1|1\rangle + \cdots + \alpha_d|d\rangle$$

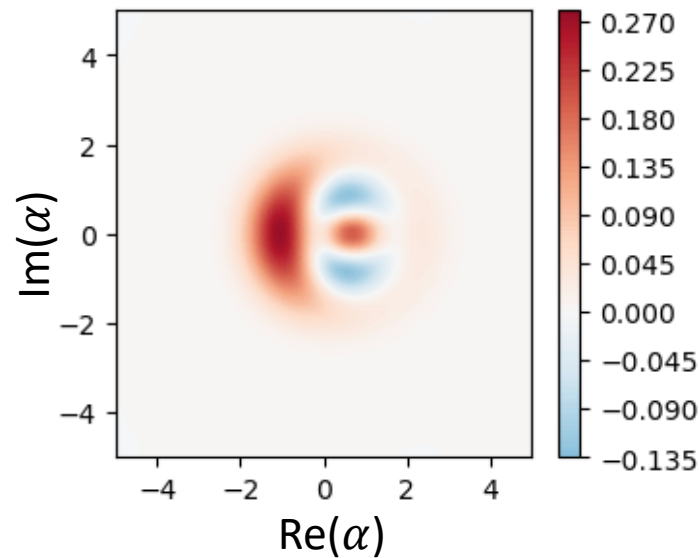
$$|n\rangle \rightarrow e^{i\theta}|n\rangle$$

Selective number-dependent arbitrary phase (SNAP) gate

PRL 115, 137002 (2015)

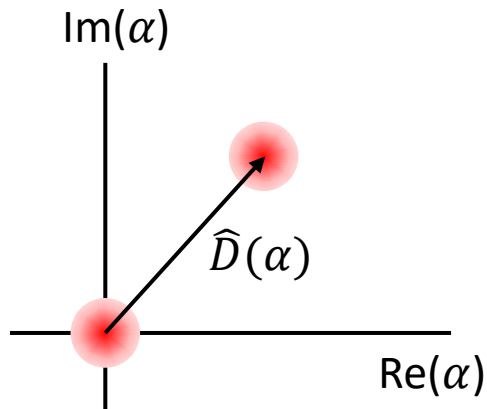


$$|1\rangle \rightarrow e^{i\pi}|1\rangle$$





# Universal Gate Set



$$\text{Qudit: } \alpha_0|0\rangle + \alpha_1|1\rangle + \dots + \alpha_d|d\rangle$$



SNAP gate

$$\text{Qudit: } \alpha_0 e^{i\theta_0}|0\rangle + \alpha_1 e^{i\theta_1}|1\rangle + \dots + \alpha_d e^{i\theta_d}|d\rangle$$

Cavity drive



SNAP

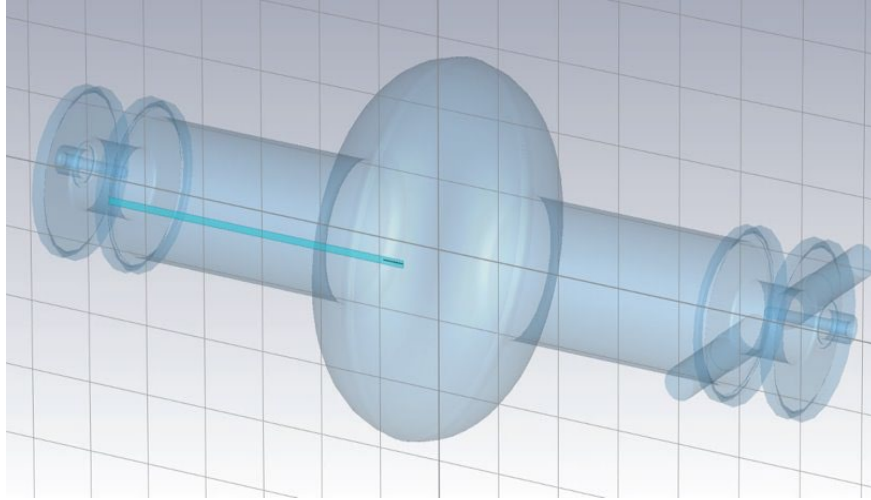


Universal control

Unconditional  
operation on cavity

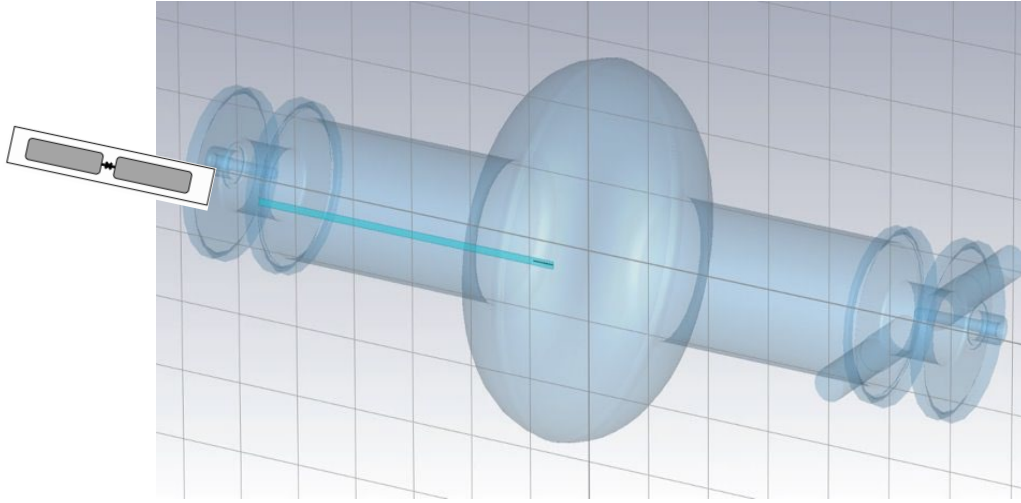
Conditional operation on  
cavity enabled by a transmon

# First Milestone



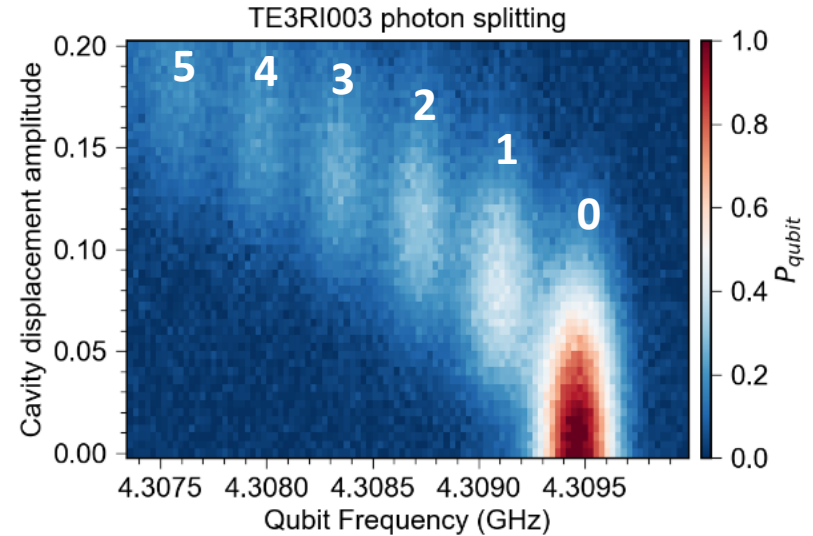
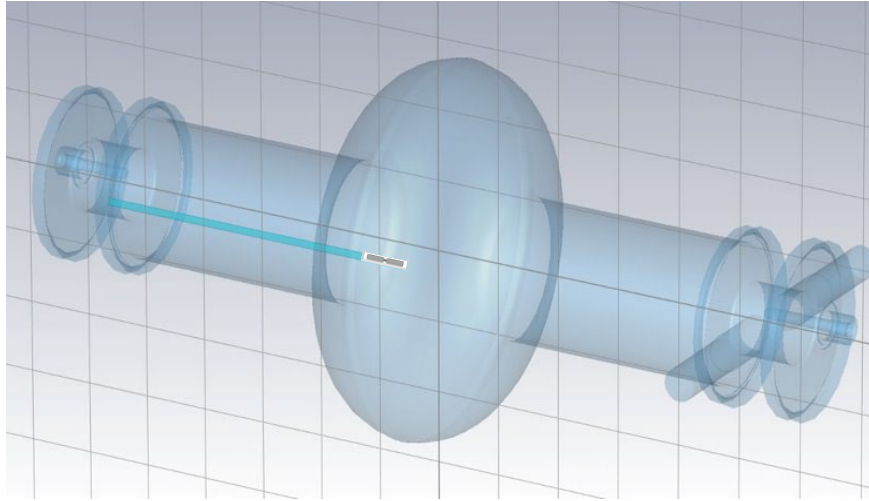
Incorporate Transmon into a  
TESLA cavity

# First Milestone



Incorporate Transmon into a  
TESLA cavity

# First Milestone

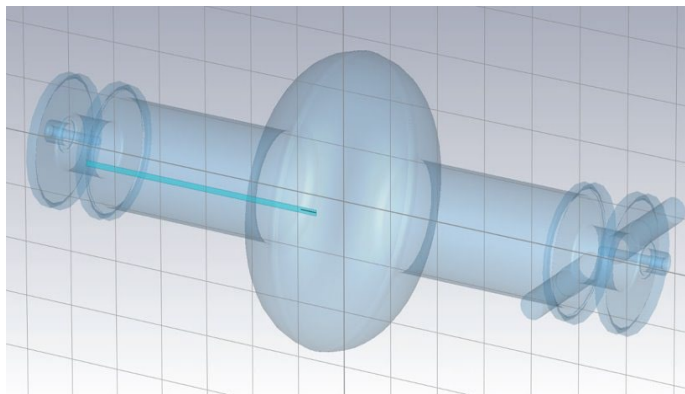


Incorporate Transmon into a  
TESLA cavity

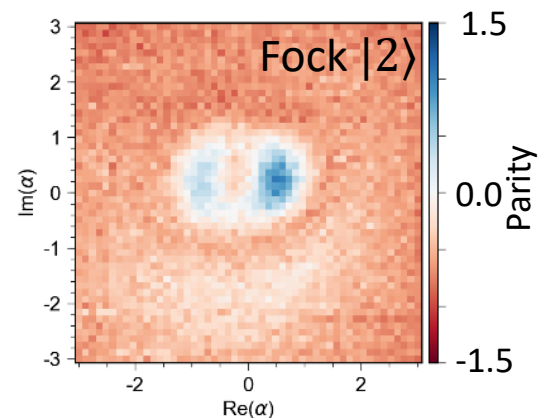
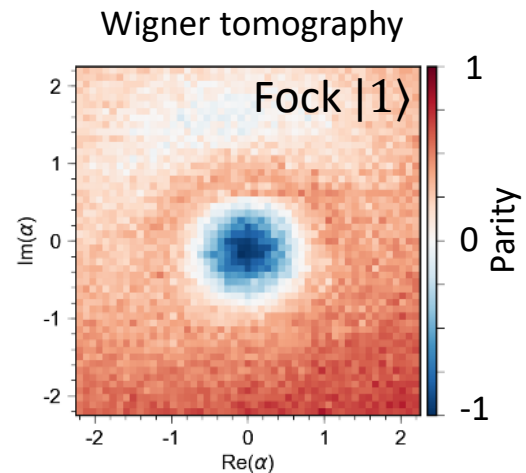
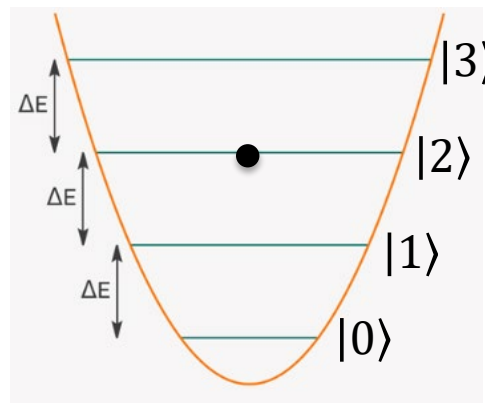
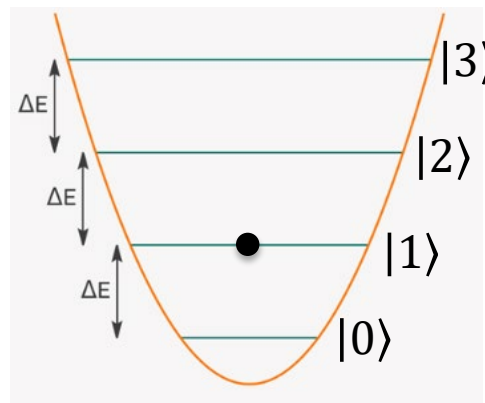
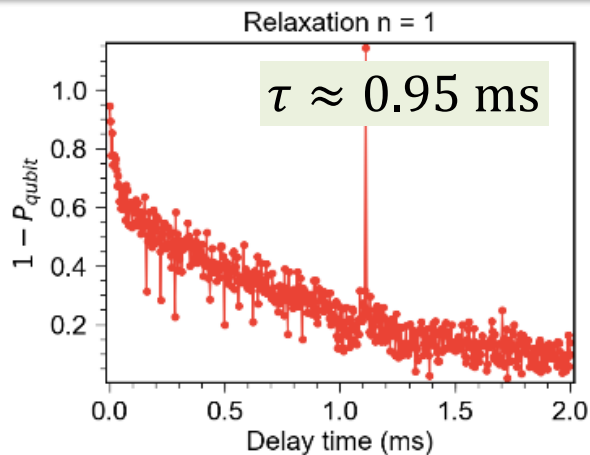
Achieved photon counting

Key to Dark Matter detection

# Second Milestone



Prepare quantum states





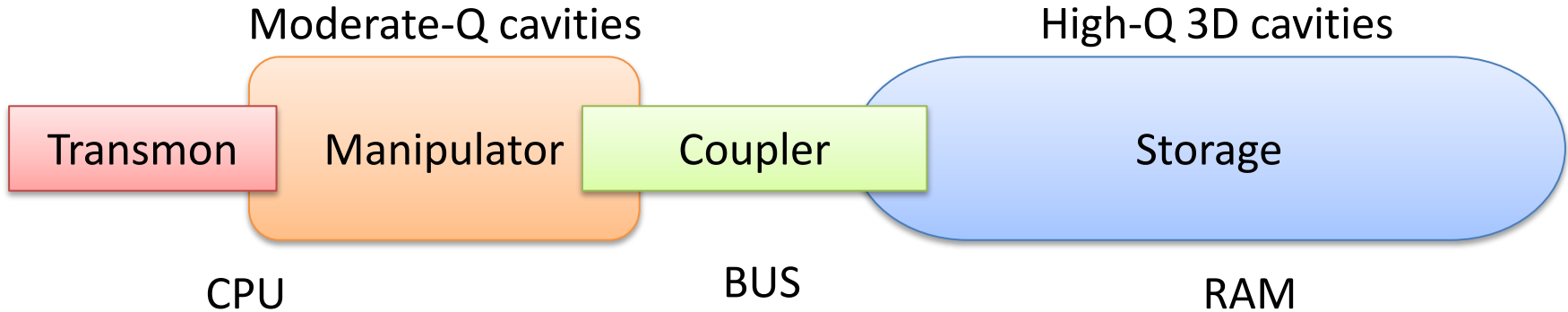
# Multiqudit Architecture

Crosstalk issues



Faster scaling:  $d^N > 2^N$

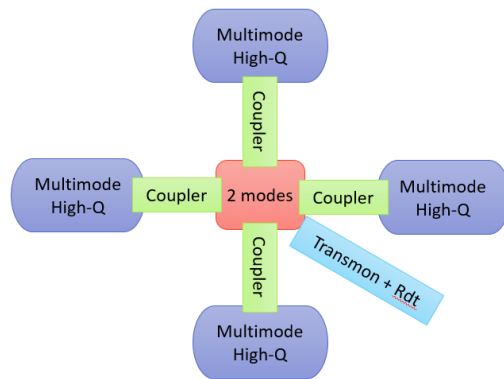
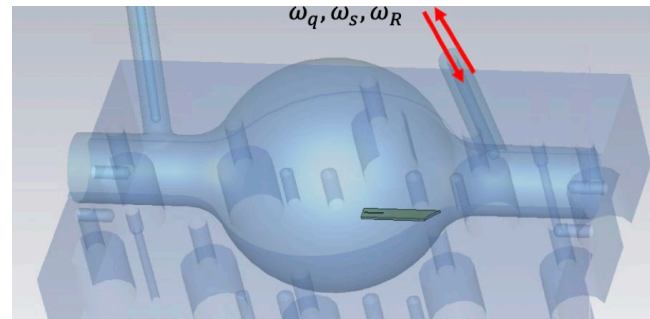
All-to-all coupling



# Outlook

- ❖ Improve single-cell devices
  - Optimize transmon design, placement
  - Investigate other SRF cavity geometries
- ❖ Scaling up
  - Develop modular architecture
  - Connect several modules

Find new applications



# Brand New SQMS Facility at Fermilab





# Thank You!

