

Relating insomnia symptoms and genetic data

Research notes

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1 Preliminary remarks about Bayesian probability theory

Bayesian probability theory is not just a set of new, better recipes meant to replace old ones. It also requires a different – and simpler – mindset about problems of inference.

The only purpose of Bayesian theory is to give the probability of some statements – more exactly, ‘propositions’ (Copi et al. 2014; Barwise et al. 2003) – given other statements that may concern data, facts, hypotheses. For example, Bayesian theory can tell us that hypothesis A has probability x given some data D and initial information I , while hypothesis B has probability y given the same conditions:

$$P(A|D, I) = x, \quad P(B|D, I) = y.$$

That’s all there is to it. We can then use these probabilities as we like; in particular, we can use them within decision theory to choose courses of action (Raiffa et al. 2000; Pratt et al. 1996; Sox et al. 2013). But notions like ‘statistical significance’, ‘acceptance level’, ‘confidence’, and similar are foreign to Bayesian theory; or at best they’re just secondary notions.

Another important characteristic of Bayesian theory is that it’s an extension of formal logic, the truth calculus. In fact we’ll call it *probability calculus* from now on.

In formal logic, to prove a theorem we need some axioms to start from. These may partly include experimental facts or data, but they always also include assumptions that are purely conjectural. It’s impossible to avoid this conjectural element (see for example Harding 1976). This impossibility is well known in modern science; we can quote Poincaré (1992):

But upon more reflection we realize the position held by hypothesis; we see that the mathematician wouldn't know how to do without it, and the experimenter can't do without it at all (Introduction)

Every generalization is a hypothesis (ch. IX, p. 176)

Duhem (1991):

In sum, the physicist can never subject an isolated hypothesis to experimental test, but only a whole group of hypotheses; when the experiment is in disagreement with his predictions, what he learns is that at least one of the hypotheses constituting this group is unacceptable and ought to be modified; but the experiment does not designate which one should be changed (§ VI.2, p. 187)

Unlike the reduction to absurdity employed by geometers, experimental contradiction does not have the power to transform a physical hypothesis into an indisputable truth; in order to confer this power on it, it would be necessary to enumerate completely the various hypotheses which may cover a determinate group of phenomena; but the physicist is never sure he has exhausted all the imaginable assumptions (§ VI.3, p. 190)

the realization and interpretation of no matter what experiment in physics imply adherence to a whole set of theoretical propositions (§ VI.5, p. 200)

Medawar (1963):

the starting point of induction, naive observation, innocent observation, is a mere philosophic fiction. There is no such thing as unprejudiced observation

Jeffreys [quote][ref]. Likewise, in the probability calculus we need to specify initial probabilities. These may originate in data, but they always also include additional assumptions. The motto 'let the data speak for themselves' is simply impossible.

The difference between Bayesian methods and traditional methods is *not* that the former need additional assumptions while the latter don't. Rather, Bayesian methods make these assumptions explicit, while traditional methods hide them. This is the reason why many traditional results can be obtained as special cases of Bayesian ones.

The previous remarks may appear pedantic, but they're important lest we misuse Bayesian methods.

2 When genes keep you awake...

[Luca's memoranda:]

- Use of partial exchangeability *has to* distinguish also between men and women: see Gehrman et al. (2013 p. 327).
- This study could also be used to detect most relevant genes, by eliminating them in turn (and in pairs etc) and checking the ensuing predictions.
- Is it computationally possible to use a 'nonparametric model'? It would avoid unwarranted assumptions and phenomena like over-training.

Bibliography

- (‘de X’ is listed under D, ‘van X’ under V, and so on, regardless of national conventions.)
- Barwise, J., Etchemendy, J. (2003): *Language, Proof and Logic*. (CSLI, Stanford). Written in collaboration with Gerard Allwein, Dave Barker-Plummer, Albert Liu. First publ. 1999.
- Copi, I. M., Cohen, C., McMahon, K. (2014): *Introduction to Logic*, 14th ed. (Pearson, Harlow, UK). First publ. 1953.
- Duhem, P. (1914): *La Théorie Physique : son objet – sa structure*, 2nd ed. (Marcel Rivière, Éditeur, Paris). http://virtualbooks.terra.com.br/freebook/fran/la_theorie_physique.htm. First publ. 1906. Transl. as Duhem (1991).
- (1991): *The Aim and Structure of Physical Theory*, Transl. of the 2nd ed. (Princeton University Press, Princeton). Transl. of Duhem (1914) by P. P. Wiener. First publ. in French 1906.
- Gehrman, P. R., Pfeiffenberger, C., Byrne, E. M. (2013): *The role of genes in the insomnia phenotype*. *Sleep Med. Clin.* **8**³, 323–331.
- Harding, S. G., ed. (1976): *Can Theories Be Refuted?* (D. Reidel, Dordrecht).
- Medawar, P. B. (1963): *Is the scientific paper a fraud?* *Listener* **70**, 377–378.
- Poincaré, H. (1905): *Science and Hypothesis*. (Walter Scott, London). Transl. of Poincaré (1992) by W. J. Greenstreet; with a Preface by J. Larmor. First publ. 1902. Partly repr. in **poincare1913_r1958**.
- (1992): *La science et l’hypothèse*. (Éditions de la Bohème, Rueil-Malmaison, France). <http://gallica.bnf.fr/document?0=N026745>. First publ. 1902; transl. as Poincaré (1905).
- Pratt, J. W., Raiffa, H., Schlaifer, R. (1996): *Introduction to Statistical Decision Theory*, 2nd pr. (MIT Press, Cambridge, USA). First publ. 1995.
- Raiffa, H., Schlaifer, R. (2000): *Applied Statistical Decision Theory*, reprint. (Wiley, New York). First publ. 1961.
- Sox, H. C., Higgins, M. C., Owens, D. K. (2013): *Medical Decision Making*, 2nd ed. (Wiley, New York). First publ. 1988.