## ElementSets from MeshConnectivity

## VertexOneRing, Faces from Neighborhoods(M)

$$M\colon \operatorname{TriangleMesh} \\ x_i\in\mathbb{R}^3 \\ V, E, F = ElementSets(M) \\ UpdateStep(v0, v1, v2, d) = \begin{cases} P & \text{if } s_{1,1} < 0 \text{ and } s_{2,1} < 0 \\ \min(d_{v1} + \|xI\|, d_{v2} + \|x2\|) & \text{otherwise} \end{cases} \\ \text{where} \\ v0, v1, v2 \in V \\ d_i \in \mathbb{R} \\ x1 = x_{v1} - x_{v0} \\ x2 = x_{v2} - x_{v0} \\ X = \begin{bmatrix} x1 & x2 \end{bmatrix} \\ t = \begin{bmatrix} d_{v1} & d_{v2} \end{bmatrix}^T \\ Q = (X^T \ X)^{-1} \\ 1 = \begin{bmatrix} 1 \\ 1 \end{bmatrix} \\ p = \frac{1^T \ Q \ t + \sqrt{(1^T \ Q \ t)^2 - 1^T \ Q \ 1 \cdot (t^T \ Q \ t - 1)}}{1^T \ Q \ 1} \\ n = X \ Q \ (t - p \cdot 1) \\ s = Q \ X^T \ n \end{cases} \\ GetNextLevel(U) = v - s \\ \text{where} \\ U_i \subset V \\ s = \bigcup_i U_i \\ v = VertexOneRing(s) \\ GetRangeLevel(U, a, b) = \bigcup_{i=0}^b U_i \text{ where } U_j \subset V, a, b \in \mathbb{Z}, \text{ index} \\ GetLevelSequence}(U) = \begin{cases} sequence(U, n) & \text{if } |n| \neq 0 \\ 0 & \text{otherwise} \end{cases} \\ \text{where} \end{cases}$$

 $U_i \subset V$ 

n = GetNextLevel(U)