vec, inversevec, diag, svd from linearalgebra

ElementSets from MeshConnectivity

NeighborVerticesInFace, Faces, VertexOneRing, OrientedVertices from Neighborhoods(M)

$$\begin{split} M: & \operatorname{TriangleMesh} \\ & \bar{x}_i \in \mathbb{R}^3 \operatorname{ rest pos in } 3D \\ & x_i \in \mathbb{R}^2 \operatorname{ current pos in } 2D \\ & \varepsilon \in \mathbb{R} \operatorname{ eps} \\ & psd : \mathbb{R}^{p \times p} \to \mathbb{R}^{p \times p}, \operatorname{ sparse} \\ \\ & V, E, F = ElementSets(M) \\ & m_r(f) = [br - ar \quad cr - ar] \\ & \operatorname{where} \\ & f \in F \\ & a, b, c = OrientedVertices(f) \\ & n = (\bar{x}_b - \bar{x}_a) \times (\bar{x}_c - \bar{x}_a) \\ & b1 = \frac{\bar{x}_b - \bar{x}_a}{\|\bar{x}_b - \bar{x}_a\|} \\ & b2 = \frac{n}{\|x_b - \bar{x}_a\|} \\ & b2 = \frac{n}{\|x_b - \bar{x}_a\|} \\ & ar = \begin{pmatrix} 0 \\ 0 \\ 0 \end{pmatrix} \\ & cr = \begin{pmatrix} (\bar{x}_b - \bar{x}_a) \cdot b1 \\ (\bar{x}_c - \bar{x}_a) \cdot b2 \end{pmatrix} \\ & S(f, x) = \begin{cases} \infty & \text{if } |m| \leq 0 \\ A \left(\|J\|^2 + \|J^{-1}\|^2 \right) & \text{otherwise} \end{cases} \\ & \text{where} \\ & f \in F \\ & x_i \in \mathbb{R}^2 \\ & a, b, c = OrientedVertices(f) \\ & m = [x_b - x_a - x_c - x_a] \\ & A = \frac{1}{2}|m_r(f)| \\ & J = mm_r(f)^{-1} \\ & e = \sum_{i \in F} S_i(x) \\ & H = \sum_{i \in F} psd \left(\frac{\partial^2 S_i(x)}{\partial x^2} \right) \\ & G = \frac{\partial e}{\partial x} \end{aligned}$$