arccos, atan2 from trigonometry

ElementSets from MeshConnectivity

Faces, Vertices, Edges, OppositeFaces, OppositeVertices, NeighborVerticesInFace, OrientedVertices from Neighborhoods(M)

$$N: \text{TriangleMeth} \\ x_i \in \mathbb{R}^3 \\ V.E.F = ElementScis_i(M) \\ VertexNormal_i(i) = \left( \sum_{j \in S} \frac{(x_j - x_j) \times (x_i - x_j)}{|x_i - x_i|^2} \right) \\ \text{where } j, k = \text{NeighborVerticeInFace}(f, i) \text{ where } i \in V \\ \emptyset(i, f) = \operatorname{arccos}\left( \frac{(x_j - x_j) \times (x_i - x_j)}{|x_i - x_i|} \right) \\ \text{where } i \in V \\ i \in V \\ f \in F \\ j, k = \text{NeighborVerticeInFace}(f, i) \\ \text{arcs}(f) = \frac{1}{2} |(x_j - x_j) \times (x_i - x_j)| \\ \text{where } f \in F \\ i, k = CointedVerticeif(f) \\ N(f) = \frac{(x_j - x_j) \times (x_j - x_j)}{2 \text{ arcs}(f)} \\ \text{where } f \in F \\ i, k = \text{CointedVerticeif}(f) \\ R(g) = \frac{1}{2} |(x_j - x_j) \times (x_j - x_j)| \\ \text{where } f \in F \\ i, k = \text{CointedVerticeif}(f) \\ R(g) = \frac{1}{2} |(x_j - x_j) \times (x_j - x_j)| \\ \text{where } e \in E \\ i, j = \text{Vertice}(g) \\ \emptyset(g) = \pi - \text{atance}[(N_i \times N_i], N_i \cdot N_g) \\ \text{where } e \in E \\ f_{j, f_j} = \text{OppositeFace}(g) \\ N_{j_j} = N(f_j) \\ N_{j_j} = N$$