



## The Strucplot Framework: Visualizing Multi-way Contingency Tables with `vcd`

David Meyer, Achim Zeileis, and Kurt Hornik  
Wirtschaftsuniversität Wien, Austria

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### Abstract

This paper has been published in the Journal of Statistical Software (Meyer, Zeileis, and Hornik 2006) and describes the “strucplot” framework for the visualization of multi-way contingency tables. Strucplot displays include hierarchical conditional plots such as mosaic, association, and sieve plots, and can be combined into more complex, specialized plots for visualizing conditional independence, GLMs, and the results of independence tests. The framework’s modular design allows flexible customization of the plots’ graphical appearance, including shading, labeling, spacing, and legend, by means of “graphical appearance control” functions. The framework is provided by the R package `vcd`.

*Keywords:* contingency tables, mosaic plots, association plots, sieve plots, categorical data, independence, conditional independence, HSV, HCL, residual-based shading, `grid`, R.

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## 1. Introduction

In order to explain multi-dimensional categorical data, statisticians typically look for (conditional) independence structures. Whether the task is purely exploratory or model-based, techniques such as mosaic and association plots offer good support for visualization. Both visualize aspects of (possibly higher-dimensional) contingency tables, with several extensions introduced over the last two decades, and implementations available in many statistical environments. A *mosaic plot* (Hartigan and Kleiner 1984) is basically an area-proportional visualization of (typically, observed) frequencies, composed of tiles (corresponding to the cells) created by recursive vertical and horizontal splits of a rectangle. Thus, the area of each tile is proportional to the corresponding cell entry *given* the dimensions of previous splits. An *association plot* (Cohen 1980) visualizes the standardized deviations of observed frequencies from those expected under a certain independence hypothesis. Each cell is represented by a rectangle that has (signed) height proportional to the residual and width proportional to

the square root of the expected counts, so that the area of the box is proportional to the difference in observed and expected frequencies.

Extensions to these techniques have mainly focused on the following aspects.

1. Varying the shape of bar plots and mosaic displays to yield, e.g., double-decker plots (Hofmann 2001), spine plots, or spinograms (Hofmann and Theus 2005).
2. Using residual-based shadings to visualize log-linear models (Friendly 1994, 2000) and significance of statistical tests (Meyer, Zeileis, and Hornik 2003; Zeileis, Meyer, and Hornik 2005).
3. Using pairs plots and trellis-like layouts for marginal, conditional and partial views (Friendly 1999).
4. Adding direct user interaction, allowing quick exploration and modification of the visualized models (Unwin, Hawkins, Hofmann, and Siegl 1996; Theus 2003).
5. Providing a modular and flexible implementation to easily allow user extensions (Meyer *et al.* 2003, 2006).

Current implementations of mosaic displays can be found, e.g., for SAS (SAS Institute Inc. 2005), ViSta (Young 1996), MANET (Unwin *et al.* 1996), Mondrian (Theus 2003), R (R Development Core Team 2006), and S-PLUS (Insightful Inc. 2005). For R, currently three implementations do exist in the packages **graphics** (in base R), **vcd** (Meyer *et al.* 2006), and **iplots** (Urbanek and Wichtrey 2006), respectively. Table 1 gives an overview of the available functionality in these systems. Most environments are available on Windows, MacOS, and Linux/Unix variants, except **MANET** which is only available for the Macintosh platforms.

	SAS	S-PLUS	R			ViSta	MANET	Mondrian
			base	vcd	iplots			
Basic functionality	×	×	×	×	×	×	×	×
Shape				×		×	×	
Res.-based shadings	×		×	×	(×)		(×)	(×)
Highlighting				×	×	×	×	×
Conditional views	×			×		×	×	
Interaction					×	×	×	×
Linking					×	×	×	×
Extensible design				×				
Language	SAS	S	R	R	R/Java	XLisp	C++	Java

Table 1: Comparison of current software environments.

Figures 1 to 4 illustrate some of these extensions. Figure 1 shows the results from a double-blind clinical trial investigating a new treatment for rheumatoid arthritis, using an extended mosaic plot with residual-based shading based on the maximum statistic: clearly, the new treatment is effective. The dark blue cell indicates that the rate of treated patients showing marked improvement is significant at the 1% level. Figure 2 visualizes the well-known UCB

admissions data by means of a conditional association plot. The panels show the residuals from a conditional independence model (independence of gender and admission, given department), stratified by department. Clearly, the situation in department A (more women/less men accepted than would be expected under the null hypothesis) causes the rejection of the hypothesis of conditional independence. Figure 3 illustrates the conditional independence of premarital and extramarital sex, given gender and marital status. The  $\chi^2$  test of independence, based on the permutation distribution, rejects the null hypothesis: possibly, because the tendency of people to have extramarital sex when they had premarital sex is particularly marked among married people? The rate of such women and men is significant at the 0.01 and 0.1 level, respectively. Finally, Figure 4 visualizes the “Survival on the Titanic” data using a double-decker plot. Here, a binary response (survival of the disaster) is to be explained by other factors (class, gender, and age). The gray boxes represent the proportion of survived passengers in a particular stratum. The proportions of saved women and children are indeed higher than those of men, but they clearly decrease from the 1st to the 3rd class. In addition, the proportion of saved men in the 1st class is higher than in the others.

This paper describes the `strucplot` framework provided by the `vcd` package for the R environment for statistical computing and graphics, available from the Comprehensive R Archive Network (<http://CRAN.R-project.org/>). The framework integrates displays such as mosaic, association, and sieve plots by their unifying property of being flat representations of contingency tables. These basic plots, as well as specialized displays for conditional independence, can be used both for exploratory visualization and model-based analysis. Exploratory techniques include specialized displays for the bivariate case, as well as pairs and trellis-type displays for higher-dimensional tables. Model-based tools include methods suitable for the visualization of conditional independence tests (including permutation tests), as well as for the visualization of particular GLMs (logistic regression, log-linear models). Additionally, two of the framework’s further strengths are its flexibility and extensibility: graphical appearance aspects such as shading, labeling, and spacing are modularized by means of “graphical appearance control” (*grapcon*) functions, allowing fine-granular customization and user-level extensions.

The remainder of the paper is organized as follows. In Section 2, we give an overview of the `strucplot` framework, describing the hierarchy of the main components and the basic functionality. In Section 3, we demonstrate how (residual-based) shadings support the visualization of log-linear models and the results of independence tests. Also, we explain step-by-step how the concepts of generating and *grapcon* functions can be combined to provide a flexible customization of complex graphical displays as created by the `strucplot` framework. Sections 4 and 5 discuss in detail the labeling and spacing features, respectively. Section 6 exemplifies the framework in the analysis of a four-way data set. Section 7 concludes the work.

## 2. The `strucplot` framework

The `strucplot` framework in the R package `vcd`, used for visualizing multi-way contingency tables, integrates techniques such as mosaic displays, association plots, and sieve plots. The main idea is to visualize the tables’ cells arranged in rectangular form. For multi-way tables, the variables are nested into rows and columns using recursive conditional splits, given the margins. The result is a “flat” representation that can be visualized in ways similar to a two-dimensional table. This principle defines a class of conditional displays which allows for

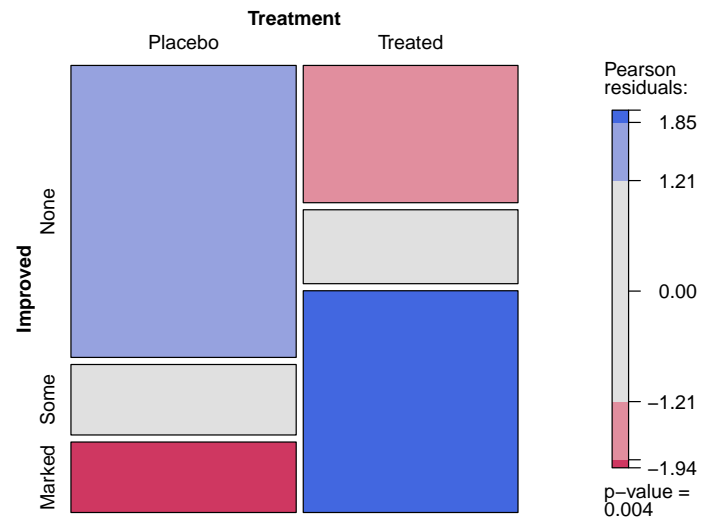


Figure 1: Mosaic plot for the Arthritis data.

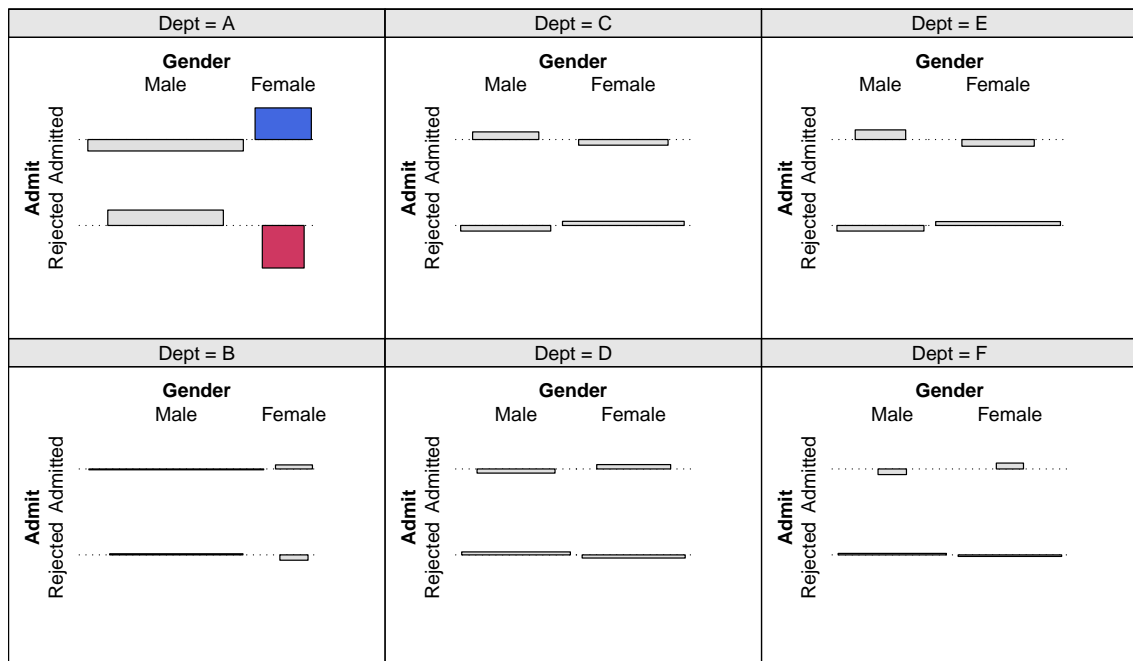


Figure 2: Conditional association plot for the UCBAAdmissions data.

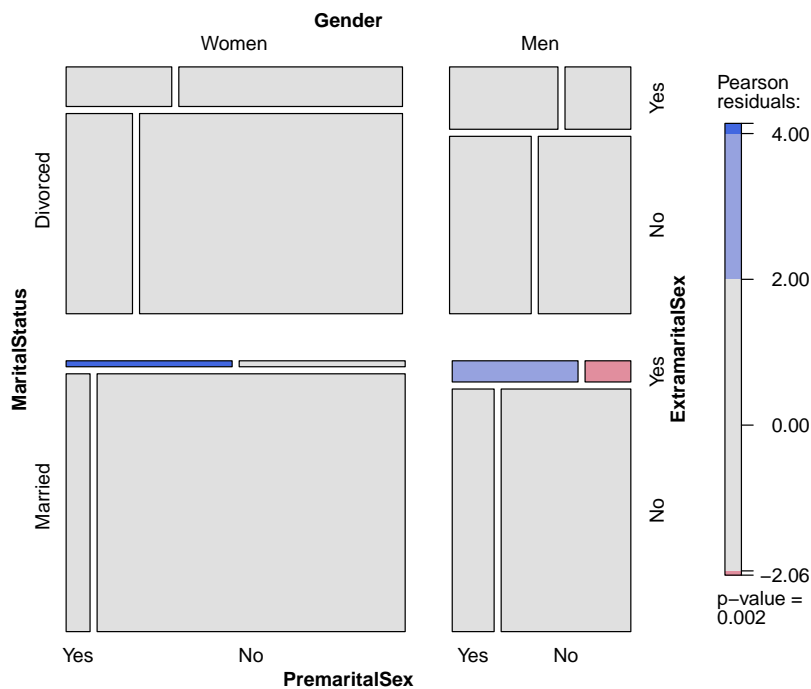


Figure 3: Mosaic plot for the PreSex data.

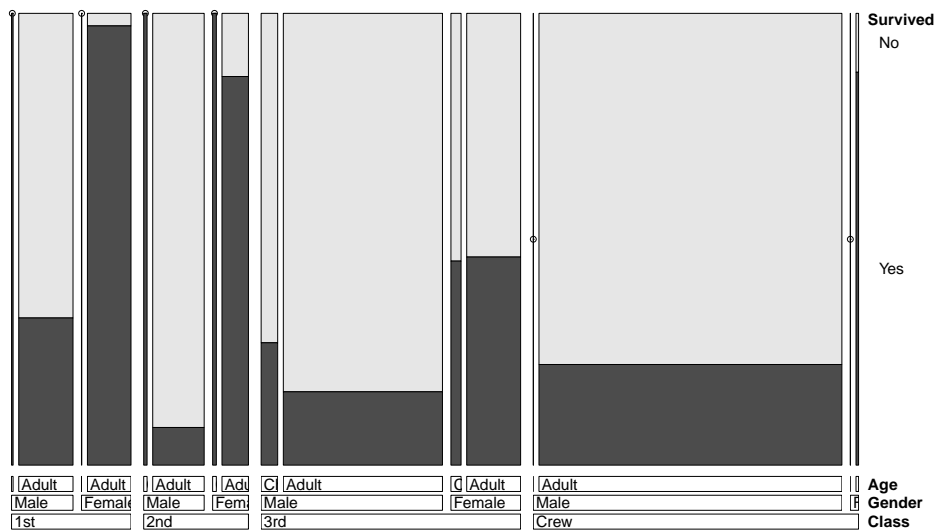


Figure 4: Double-decker plot for the Titanic data.

granular control of graphical appearance aspects, including:

- the content of the tiles
- the split direction for each dimension
- the graphical parameters of the tiles’ content
- the spacing between the tiles
- the labeling of the tiles

The strucplot framework is highly modularized: Figure 5 shows the hierarchical relationship between the various components. On the lowest level, there are several groups of workhorse and parameter functions that directly or indirectly influence the final appearance of the plot (see Table 2 for an overview). These are examples of *grapcon* functions. They are created by generating functions (*grapcon generators*), allowing flexible parameterization and extensibility (Figure 5 only shows the generators). The generator names follow the naming convention *group\_foo()*, where *group* reflects the group the generators belong to (strucplot core, labeling, legend, shading, or spacing). The workhorse functions (created by *struc\_foo()*, *labeling\_foo()*, and *legend\_foo()*) directly produce graphical output (i.e., “add ink to the canvas”), whereas the parameter functions (created by *spacing\_foo()* and *shading\_foo()*) compute graphical parameters used by the others. The *grapcon* functions returned by *struc\_foo()* implement the core functionality, creating the tiles and their content. On the second level of the framework, a suitable combination of the low-level *grapcon* functions (or, alternatively, corresponding generating functions) is passed as “hyperparameters” to *strucplot()*. This central function sets up the graphical layout using grid viewports (see Figure 6), and coordinates the specified core, labeling, shading, and spacing functions to produce the plot. On the third level, we provide several convenience functions such as *mosaic()*, *sieve()*, *assoc()*, and *doubledecker()* which interface *strucplot()* through sensible parameter defaults and support for model formulae. Finally, on the fourth level, there are “related” *vcd* functions (such as *cotabplot()* and the *pairs()* methods for table objects) arranging collections of plots of the strucplot framework into more complex displays (e.g., by means of panel functions).

## 2.1. Mosaic, association, and sieve plots

As an example, consider the *HairEyeColor* data containing two polytomous variables (hair and eye color), as well as one (artificial) dichotomous gender variable (*Sex*). The “flattened” contingency table can be obtained using the *structable()* function (quite similar to *ftable()* in base R, but allowing the specification of split directions):

```
> (HEC <- structable(Eye ~ Sex + Hair, data = HairEyeColor))
```

		Eye Brown	Blue	Hazel	Green
Sex	Hair				
Male	Black	32	11	10	3
	Brown	53	50	25	15

Group	Grapcon generator	Description
strucplot core	<code>struc_assoc()</code> <code>struc_mosaic()</code> <code>struc_sieve()</code>	core function for association plots core function for mosaic plots core function for sieve plots
labeling	<code>labeling_border()</code> <code>labeling_cboxed()</code>  <code>labeling_cells()</code> <code>labeling_conditional()</code>  <code>labeling_doubledecker()</code> <code>labeling_lboxed()</code> <code>labeling_left()</code> <code>labeling_left2()</code> <code>labeling_list()</code>	border labels centered labels with boxes, all labels clipped, and on top and left border  cell labels border labels for conditioning variables and cell labels for conditioned variables draws labels for doubledecker plot left-aligned labels with boxes left-aligned border labels left-aligned border labels, all labels on top and left border draws a list of labels under the plot
shading	<code>shading_binary()</code> <code>shading_Friendly()</code> <code>shading_hcl()</code> <code>shading_hsv()</code> <code>shading_max()</code>  <code>shading_sieve()</code>	visualizes the sign of the residuals implements Friendly shading (based on HSV colors) shading based on HCL colors shading based on HSV colors shading visualizing the maximum test statistic (based on HCL colors) implements Friendly shading customized for sieve plots (based on HCL colors)
spacing	<code>spacing_conditional()</code>  <code>spacing_dimequal()</code> <code>spacing_equal()</code> <code>spacing_highlighting()</code> <code>spacing_increase()</code>	increasing spacing for conditioning variables, equal spacing for conditioned variables equal spacing for each dimension equal spacing for all dimensions increasing spacing, last dimension set to zero increasing spacing
legend	<code>legend_fixed()</code> <code>legend_resbased()</code>	creates a fixed number of bins (similar to <code>mosaicplot()</code> ) suitable for an arbitrary number of bins (also for continuous shadings)

Table 2: Available grapcon generators in the strucplot framework

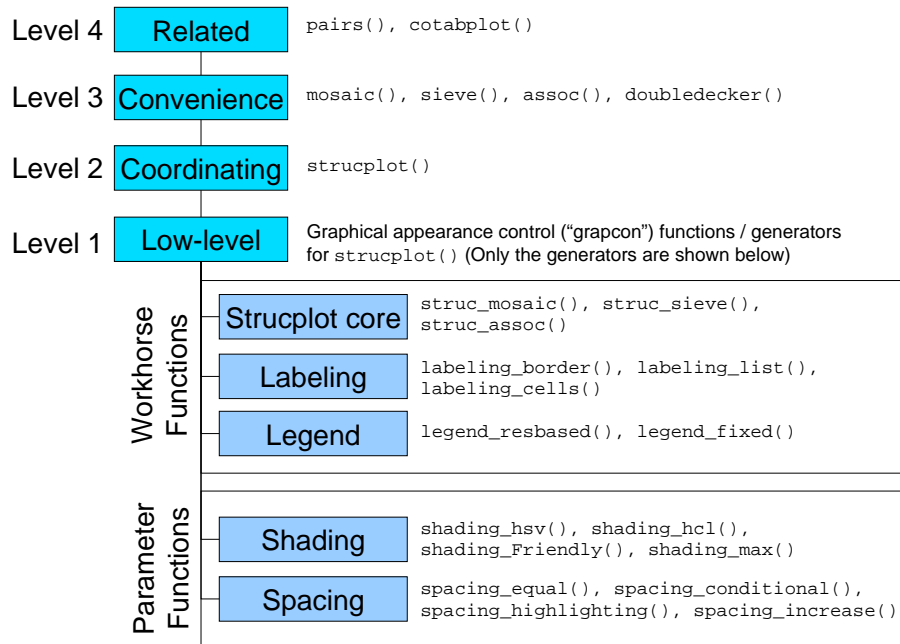


Figure 5: Components of the strucplot framework.

	Red	10	10	7	7
	Blond	3	30	5	8
Female	Black	36	9	5	2
	Brown	66	34	29	14
	Red	16	7	7	7
	Blond	4	64	5	8

Let us first visualize the contingency table by means of a mosaic plot. The effect of

```
> mosaic(HEC)
```

equivalent to

```
> mosaic(~Sex + Eye + Hair, data = HairEyeColor)
```

depicts the observed frequencies of the `HairEyeColor` data. If there are zero entries, tiles have zero area and are, additionally, marked by small bullets (see, e.g., Figure 4). By default, these cells are not split further. The bullets help distinguishing very small cells from zero entries, and are particularly useful when color shadings come into play (see the example using the `Bundesliga` data in Section 3.3). Note that in contrast to, e.g., `mosaicplot()` in base R, the default split direction and level ordering in all strucplot displays correspond to the textual representation produced by the print methods. It is also possible to visualize the expected values instead of the observed values (see Figure 8):



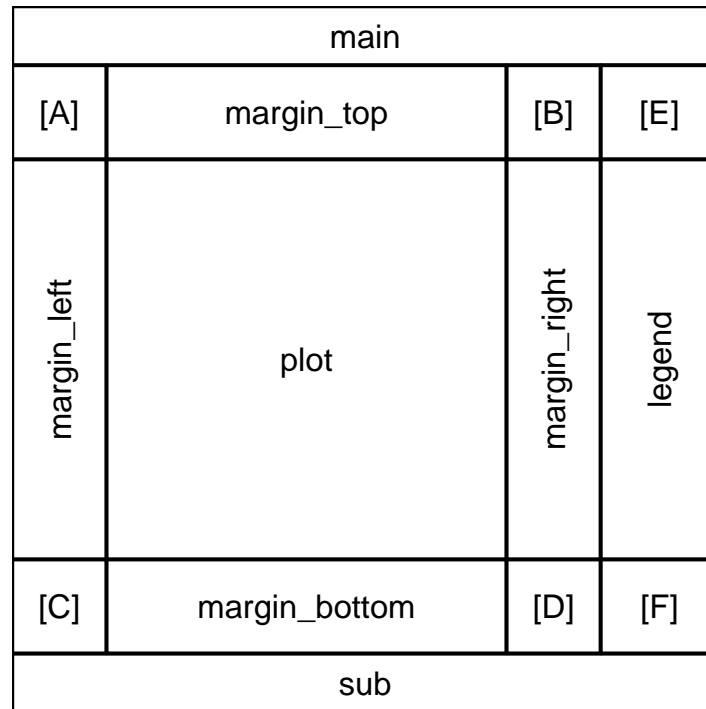


Figure 6: Viewport layout for strucplot displays with their names. [A] = “corner\_top\_left”, [B] = “corner\_top\_right”, [C] = “corner\_bottom\_left”, [D] = “corner\_bottom\_right”, [E] = “legend\_top”, [F] = “legend\_sub”.

```
> mosaic(HEC, type = "expected")
```

In order to compare observed and expected values, a sieve plot ([Riedwyl and Schüpbach 1994](#)) could be used (see [Figure 9](#)):

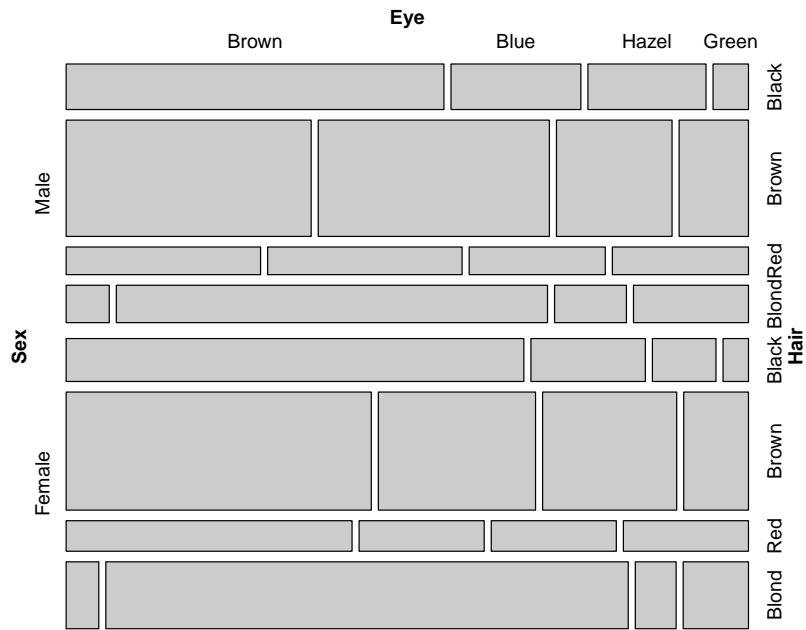
```
> sieve(~Sex + Eye + Hair, data = HEC, spacing = spacing_dimequal(c(2,
+ 0, 0)))
```

where `spacing_dimequal` is used to set the spacing of the second and third dimension to zero. Alternatively, we can directly inspect the residuals. The Pearson residuals (standardized deviations of observed from expected values) are conveniently visualized using association plots ([Cohen 1980](#)). In contrast to `assocplot()` in base R, `vcd`’s `assoc()` function scales to more than two variables (see [Figure 10](#)):

```
> assoc(HEC, compress = FALSE)
```

where the `compress` argument keeps distances between tiles equal.

For both mosaic plots and association plots, the splitting of the tiles can be controlled using the `split_vertical` argument. The default is to alternate splits starting with a horizontal one (see [Figure 11](#)):

Figure 7: Mosaic plot for the `HairEyeColor` data.Figure 8: Mosaic plot for the `HairEyeColor` data (expected values).

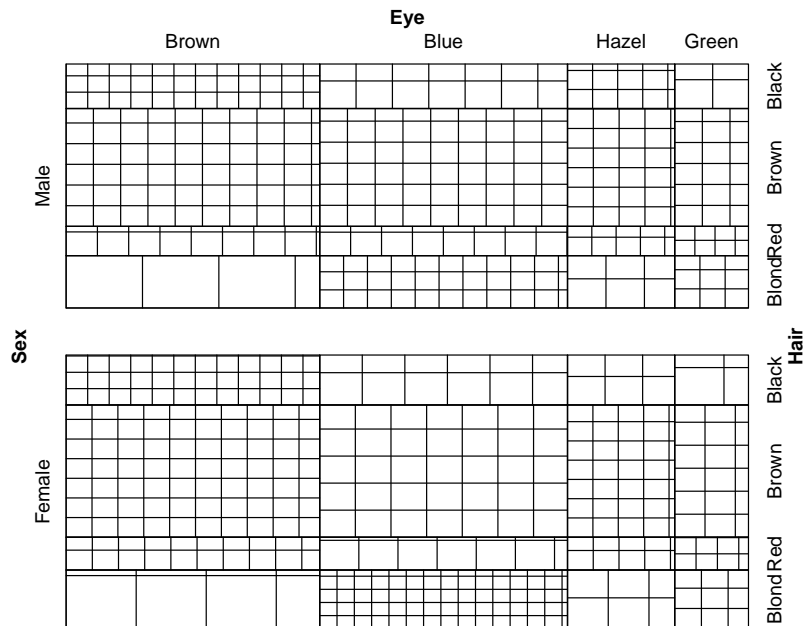


Figure 9: Sieve plot for the `HairEyeColor` data visualizing simultaneously observed and expected values.

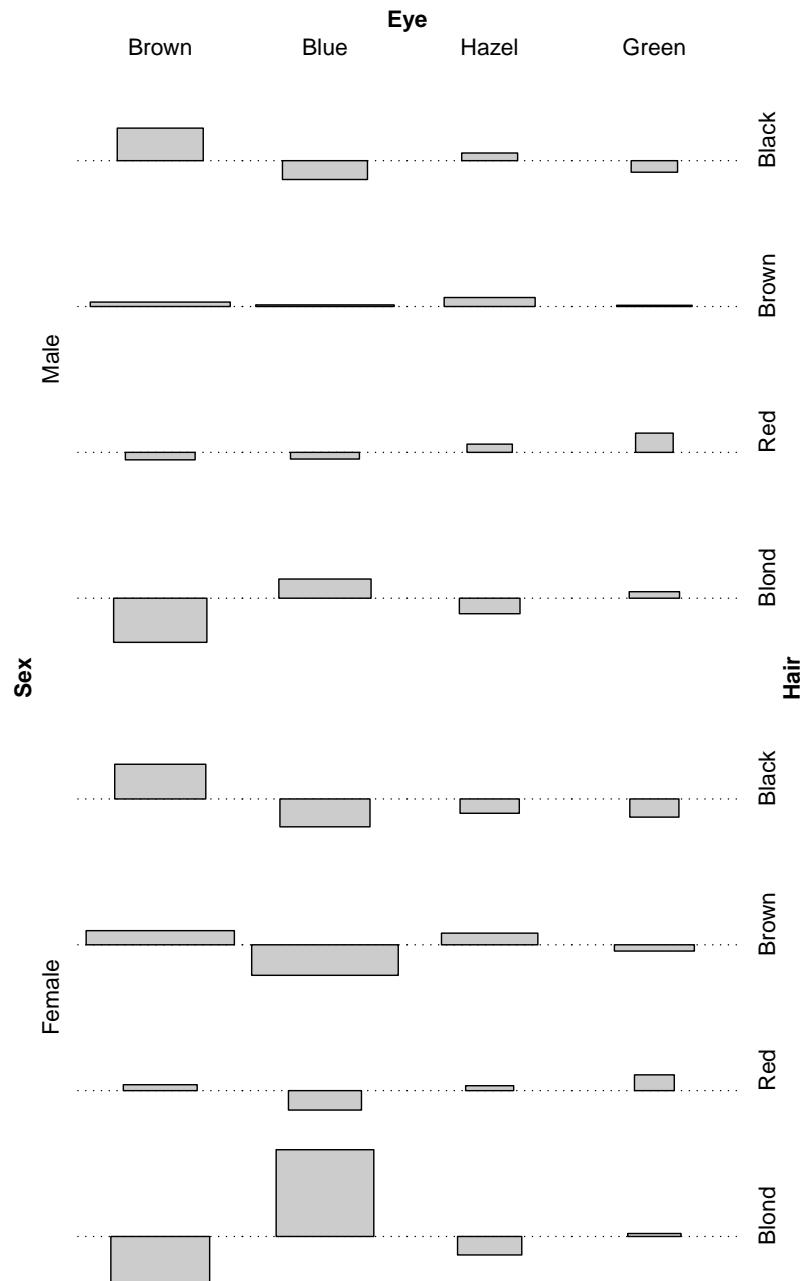
```
> mosaic(HEC, split_vertical = c(TRUE, FALSE, TRUE),
+       labeling_args = list(abbreviate = c(Eye = 3)))
```

(Note that `HEC`, a `struc`table object, already includes a splitting information which simply gets overloaded in this example.) For compatibility with `mosaicplot()` in base R, the `mosaic()` function also allows the use of a `direction` argument taking a vector of "h" and "v" characters:

```
> mosaic(HEC, direction = c("v", "h", "v"))
```

By a suitable combination of splitting, spacing, and labeling settings, the functions provided by the `strucplot` framework can be customized in a quite flexible way. For example, the default method for `doubledecker()` is simply a wrapper for `strucplot()`, setting the right defaults. Most default settings such as colors, spacing, and labeling are specified via the parameters and passed through to `strucplot()`. The additional code just handles the dependent variable information, and in particular permutes the table to have the dependent variable as the last dimension as required for the `doubledecker` plot. Figure 4 shows a `doubledecker` plot of the `Titanic` data, explaining the probability of survival ("survived") by age, given sex, given class. It is created by:

```
> doubledecker(Titanic)
```

Figure 10: Association plot for the `HairEyeColor` data.

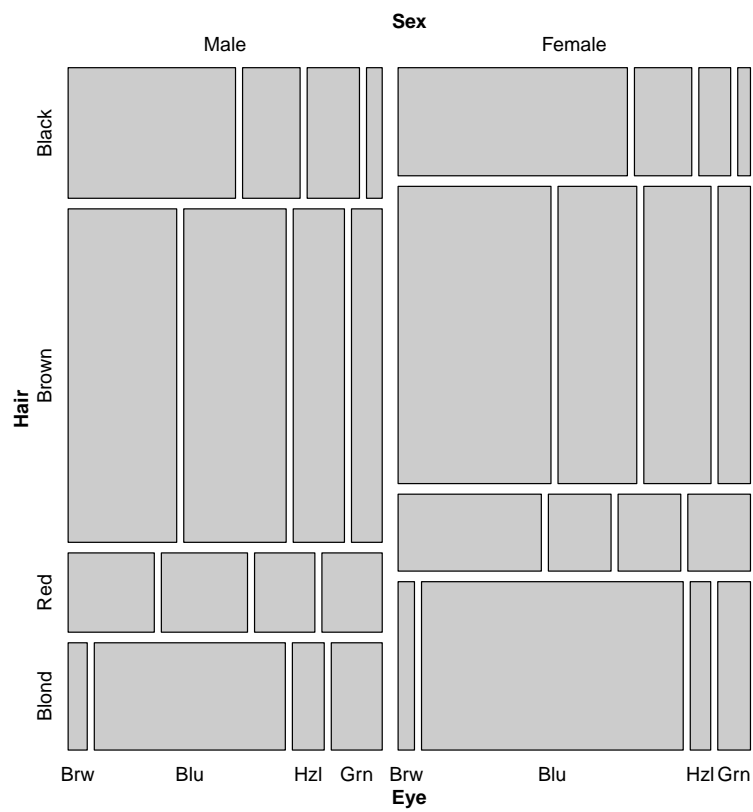


Figure 11: Mosaic plot for the `HairEyeColor` data—alternative splitting.

equivalent to:

```
> doubledecker(Survived ~ Class + Sex + Age, data = Titanic)
```

## 2.2. Conditional and partial views

So far, we have visualized either full or collapsed tables, as suggested by the analysis task at hand. Subtables can be selected in a similar way as for objects of class `table` using indexing. Note, however, that subsetting of `structable` objects is more restrictive because of their inherent conditional structure. Since the variables on both the row and the columns side are nested, subsetting is only possible “outside-in”, that is, indexing operates on blocks defined by the variable levels. In the following, we use the Titanic data again, this time collapsed over `Survived` to investigate the structure of crew and passengers (and having the `Child` and `Age` labels of the `Age` variable swapped for optical clarity):

```
> (STD <- structable(~Sex + Class + Age, data = Titanic[, ,
+      2:1, ]))
```

		Class	1st	2nd	3rd	Crew
Sex	Age					
Male	Adult		175	168	462	862
	Child		5	11	48	0
Female	Adult		144	93	165	23
	Child		1	13	31	0

```
> STD["Male", ]
```

		Class	1st	2nd	3rd	Crew
Sex	Age					
Male	Adult		175	168	462	862
	Child		5	11	48	0

```
> STD["Male", c("1st", "2nd", "3rd")]
```

		Class	1st	2nd	3rd
Sex	Age				
Male	Adult		175	168	462
	Child		5	11	48

*Conditioning* on levels (i.e., choosing a table subset for fixed levels of the conditioning variable(s)) is done using the `[[` operator. Here again, the sequence of conditioning levels is restricted by the hierarchical structure of the `structable` object. In the following examples, note that compared to subsetting, the first dimension(s) are dropped:

```
> STD[["Male", ]]
```

```

      Class 1st 2nd 3rd Crew
Age
Adult      175 168 462  862
Child       5  11  48   0

```

```
> STD[[c("Male", "Adult"), ]]
```

```

Class 1st 2nd 3rd Crew

      175 168 462  862

```

```
> STD[["Male", "1st"]]
```

```

Age
Adult 175
Child  5

```

Now, there are several ways for visualizing conditional independence structures. The “brute force” method is to draw separate plots for the strata. The following example compares the association between hair and eye color, given gender, by using subsetting on the flat table and **grid**’s viewport framework to visualize the two groups besides each other:

```

> pushViewport(viewport(layout = grid.layout(ncol = 2)))

> pushViewport(viewport(layout.pos.col = 1))
> mosaic(STD[["Male"]], margins = c(left = 2.5, top = 2.5,
+   0), sub = "Male", newpage = FALSE)
> popViewport()

> pushViewport(viewport(layout.pos.col = 2))
> mosaic(STD[["Female"]], margins = c(top = 2.5, 0), sub = "Female",
+   newpage = FALSE)
> popViewport(2)

```

Note the use of the **margins** argument: it takes a vector with up to four values whose unnamed components are recycled, but “overruled” by the named arguments. Thus, in the second example, only the top margin is set to 2.5 lines, and all other to 0. This idea applies to almost all vectorized arguments in the **strucplot** framework (with **split\_vertical** as a prominent exception).

The **cotabplot()** function does a much better job on this task: it arranges stratified **strucplot** displays in a lattice-like layout, conditioning on variable *levels*. The plot in Figure 13 shows hair and eye color, given sex:

```
> cotabplot(~Class + Age | Sex, data = STD, split_vertical = TRUE)
```

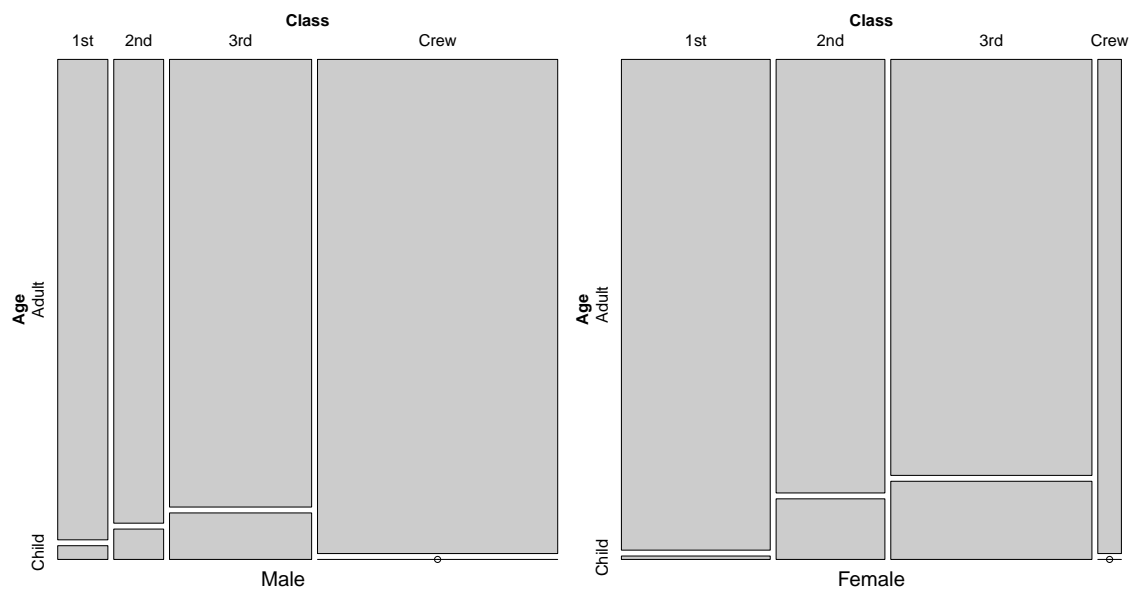


Figure 12: Two mosaic displays put side-by-side, visualizing the distribution of class and age, given gender. The marginal distribution of gender cannot be seen.

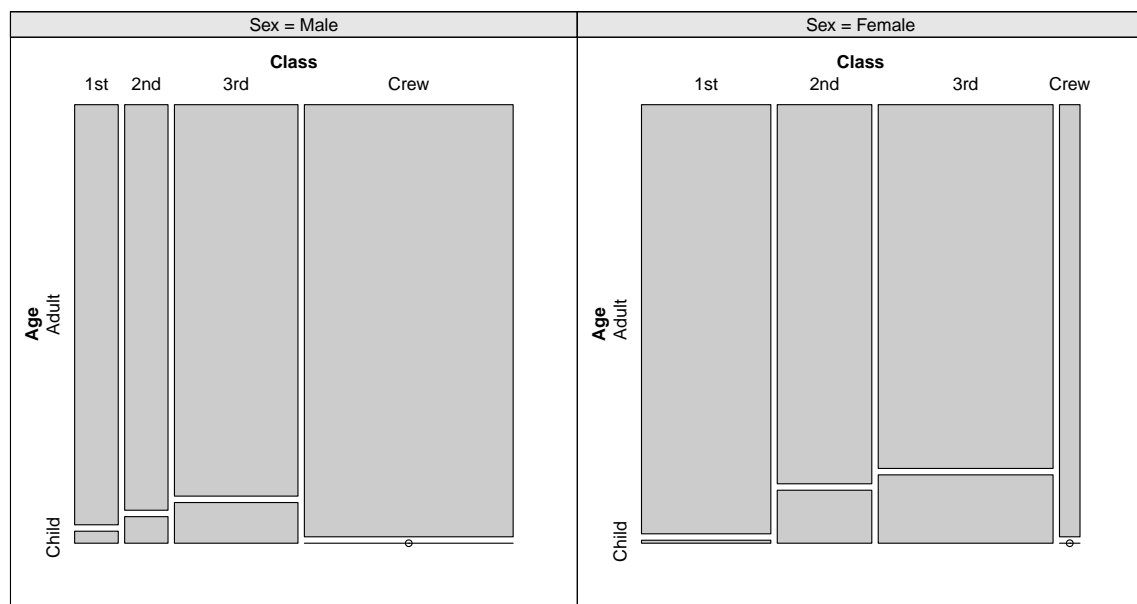


Figure 13: Conditional table plot for the `Titanic` data, again visualizing the distribution of age and class, given gender, using separate mosaic displays like the “manual” plot in Figure 12.



Visualizing the strata separately “hides” the distribution of the conditioning variable(s) which may or may not be appropriate or sensible in a particular analysis step. If we wish to keep the information on the marginal distribution(s), we can use one single mosaic for the stratified plot since mosaic displays are “conditional plots” by definition. We just need to make sure that conditioning variables are used first for splitting. Both the default and the formula interface of `mosaic()` allow the specification of conditioning variables (see Figure 14):

```
> mosaic(STD, condvars = "Sex", split_vertical = c(TRUE,
+      TRUE, FALSE))

> mosaic(~Class + Age | Sex, data = STD, split_vertical = c(TRUE,
+      TRUE, FALSE))
```

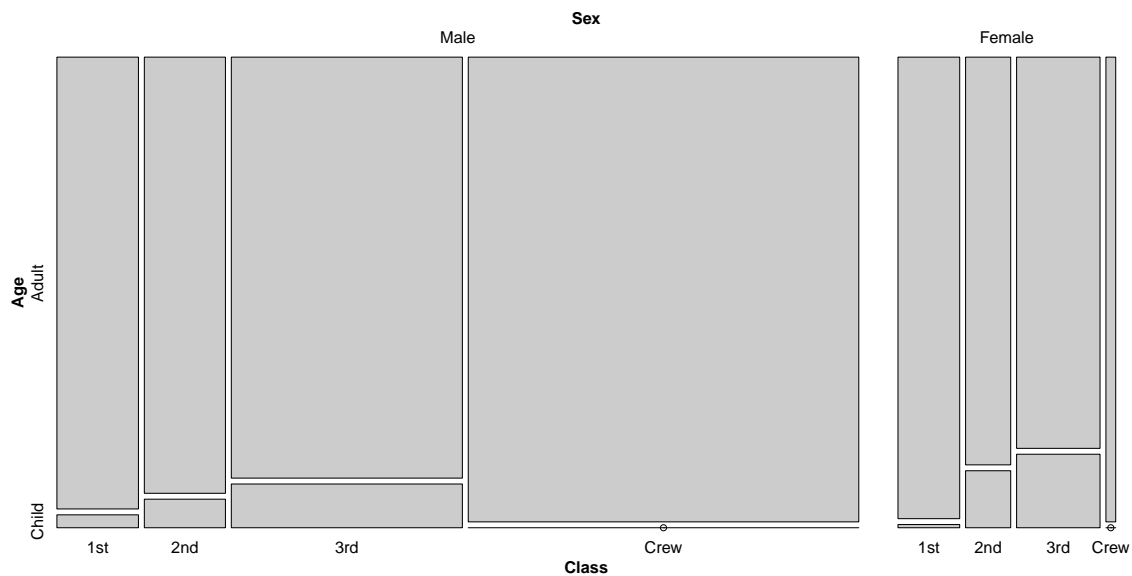


Figure 14: Mosaic plot again visualizing the distribution of class and age, given gender, this time using a single mosaic plot. In contrast to Figures 12 and 13, this plot also visualizes the marginal distribution of gender.

The effect of using this is that conditioning variables are permuted ahead of the the conditioned variables in the table, and that `spacing_conditional()` is used as default to better distinguish conditioning from conditioned dimensions. This spacing uses equal space between tiles of conditioned variables, and increasing space between tiles of conditioning variables (See Section 5).

Another set of high-level functions for visualizing conditional independence models are the `pairs()` methods for `table` and `strucTable` objects. In contrast to `cotabplot()` which conditions on variables, the `pairs()` methods create pairwise views of the table. They produce, by default, a plot matrix having `strucplot` displays in the off-diagonal panels, and the variable names (optionally, with univariate displays) in the diagonal cells. Figure 15 shows a `pairs`

display for the **Titanic** data with univariate mosaics in the diagonal, and mosaic plots visualizing the corresponding bivariate mosaics in the upper and lower triangles. Due to the inherent asymmetry of mosaic displays, the corresponding plots in the upper and lower triangle differ depending on which variable is used first for splitting—inspecting both views might help detecting patterns in a data set. Additionally, we are using a special spacing and shading normally used to ‘highlight’ the second variable in the first (as will be discussed in Section 5): here, the intention of the spacing is to emphasize the conditional distributions of the second variable, given the first one, and the shading helps identifying the factor levels in the second variable.

```
> pairs(STD, highlighting = 2, diag_panel = pairs_diagonal_mosaic,
+       diag_panel_args = list(fill = grey.colors))
```

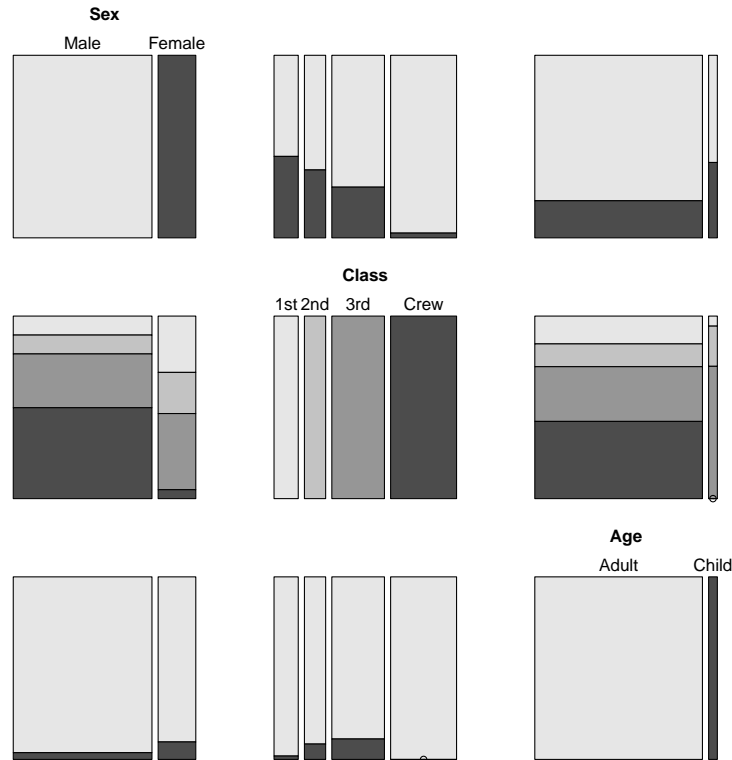


Figure 15: Pairs plot for the **Titanic** data.

The labels of the variables are to be read from left to right and from top to bottom. In addition, the levels can be matched by position within the columns and by shading within the rows. In plots produced by `pairs()`, each panel’s row and column define two variables  $X$  and  $Y$  used for the specification of four different types of independence: pairwise, total, conditional, and joint. The pairwise mosaic matrix shows bivariate marginal relations between  $X$  and  $Y$ , collapsed over all other variables. The total independence mosaic matrix shows mosaic plots for mutual independence, i.e., for marginal and conditional independence among

all pairs of variables. The conditional independence mosaic matrix shows mosaic plots for marginal independence of  $X$  and  $Y$ , given all other variables. The joint independence mosaic matrix shows mosaic plots for joint independence of all pairs  $(X, Y)$  of variables from the others.

Upper and lower parts can independently be used to display different types of independence models, or different strucplot displays (mosaic, association, or sieve plots). The available panel functions (`pairs_assoc()`, `pairs_mosaic()`, and `pairs_sieve()`) are simple wrappers to `assoc()`, `mosaic()`, and `sieve()`, respectively. Obviously, seeing patterns in strucplot matrices becomes increasingly difficult with higher dimensionality. Therefore, this plot is typically used with a suitable residual-based shading (see Section 3).

### 2.3. Interactive plot modifications

All strucplot core functions are supposed to produce conditional hierarchical plots by the means of nested viewports, corresponding to the provided splitting information. Thus, at the end of the plotting, each tile is associated with a particular viewport. Each of those viewports has to be conventionally named, enabling other strucplot modules, in particular the labeling functions, to access specific tiles after they have been plotted. The naming convention for the viewports is:

*[Optional prefix] cell:Variable1=Level1,Variable2=Level2 ...*

Clearly, these names depend on the splitting. The following example shows how to access parts of the plot after it has been drawn (see Figure 16):

```
> mosaic(~Hair + Eye, data = HEC, pop = FALSE)
> seekViewport("cell:Hair=Blond")
> grid.rect(gp = gpar(col = "red", lwd = 4))
> seekViewport("cell:Hair=Blond, Eye=Blue")
> grid.circle(r = 0.2, gp = gpar(fill = "cyan"))
```

Note that the viewport tree is removed by default. Therefore, the `pop` argument has to be set to `FALSE` when viewports shall be accessed.

In addition to the viewports, the main graphical elements get names following a similar construction method. This allows to change graphical parameters of plot elements *after* the plotting (see Figure 17):

```
> assoc(Eye ~ Hair, data = HEC, pop = FALSE)
> getNames()[1:6]

[1] "GRID.lines.2661"      "rect:Hair=Black, Eye=Brown"
[3] "GRID.lines.2662"      "rect:Hair=Black, Eye=Blue"
[5] "GRID.lines.2663"      "rect:Hair=Black, Eye=Hazel"

> grid.edit("rect:Hair=Blond, Eye=Blue", gp = gpar(fill = "red"))
```

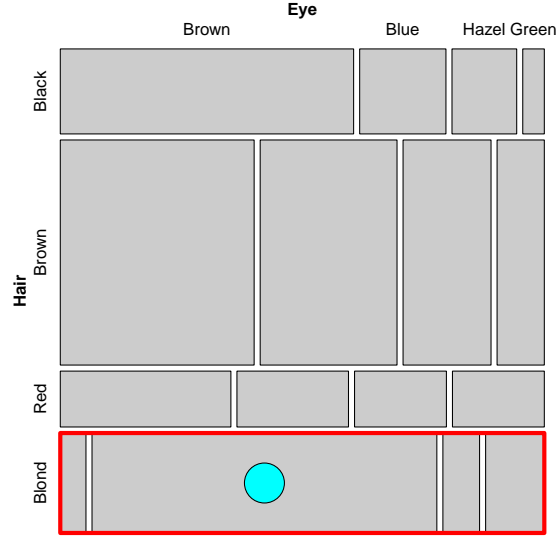


Figure 16: Adding elements to a mosaic plot after drawing.

## 2.4. Performance issues

As stated above, the implementation of strucplot displays is based on creating and nesting **grid** viewports. The main time-consuming steps performed by the core functions are the following:

1. recursively, split the table until the individual cells are reached
2. during the splits, add viewports to the plot
3. for the individual cells, add plot-specific content (rectangles for mosaics, bars for association plots, etc.)

All these operations scale linearly with the amount of created viewports. For a  $d$ -dimensional table with  $k_i$  levels,  $i = 1 \dots d$ , the total number of needed viewports  $T_d$  can roughly be estimated as

$$T_d = k_1 + k_1 k_2 + \dots + k_1 \dots k_d = \sum_{i=1}^d \prod_{j \leq i} k_j \quad (1)$$

since we first push the  $k_1$  viewports for the levels of the first dimension, then, for *each* of these, the  $k_2$  levels of the second dimension, etc. If the number of levels is equal ( $k$ ) for all dimensions,  $T_d$  simplifies to

$$T_d = \sum_{i=1}^d k^i = \frac{k(k^d - 1)}{k - 1} \quad (2)$$

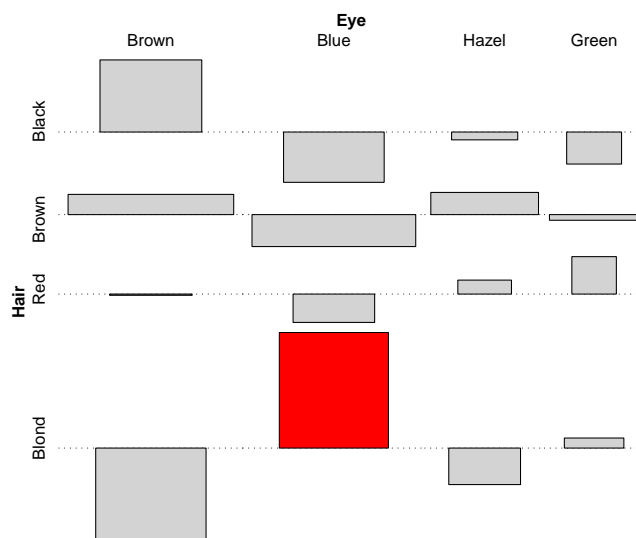


Figure 17: Changing graphical parameters of elements after drawing.

and so the time complexity for drawing a strucplot display is of order  $k^d$ .

### 3. Shadings

Unlike other graphics functions in base R, the strucplot framework allows almost full control over the graphical parameters of all plot elements. In particular, in association plots, mosaic plots, and sieve plots, the user can modify the graphical appearance of each tile individually. Built on top of this functionality, the framework supplies a set of shading functions choosing colors appropriate for the visualization of log-linear models. The tiles' graphical parameters are set using the `gp` argument of the functions of the strucplot framework. This argument basically expects an object of class `gpar` whose components are arrays of the same shape (length and dimensionality) as the data table (see Section 3.1). For convenience, however, the user can also supply a `grapcon` function that computes such an object given a vector of residuals, or, alternatively, a generating function that takes certain arguments and returns such a `grapcon` function (see Section 3.2). We provide several shading functions, including support for both HSV and HCL colors, and the visualization of significance tests (see Section 3.3).

#### 3.1. Specifying graphical parameters of strucplot displays

As an example, consider the `UCBAdmissions` data. In the table aggregated over departments, we would like to highlight the (incidentally wrong) impression that there were too many male students accepted compared to the presumably discriminated female students (see Figure 18):

```
> (ucb <- margin.table(UCBAdmissions, 1:2))
```

```

      Gender
Admit   Male Female
Admitted 1198   557
Rejected 1493  1278

> (fill_colors <- matrix(c("dark cyan", "gray", "gray",
+   "dark magenta"), ncol = 2))

      [,1]      [,2]
[1,] "dark cyan" "gray"
[2,] "gray"      "dark magenta"

> mosaic(ucb, gp = gpar(fill = fill_colors, col = 0))

```

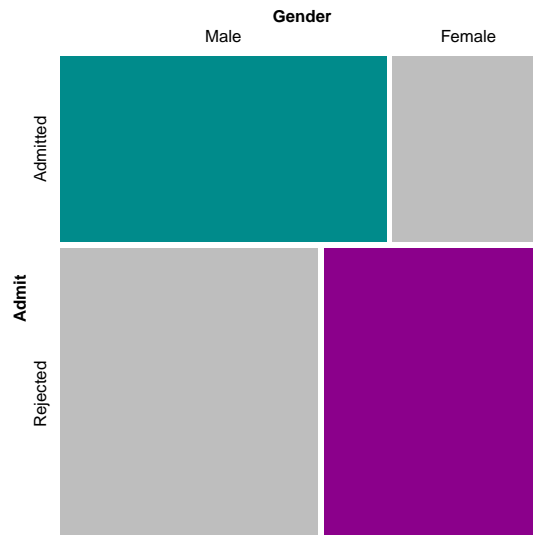


Figure 18: Mosaic plot for the UCBA admissions data with highlighted cells.

As the example shows, we create a fourfold table with appropriate colors (dark cyan for admitted male students and dark magenta for rejected female students) and supply them to the `fill` component of the `gpar` object passed to the `gp` argument of `mosaic()`. For visual clarity, we additionally hide the tiles' borders by setting the `col` component to 0 (transparent). If the parameters specified in the `gpar` object are “incomplete”, they will be recycled along the last splitting dimension. In the following example based on the `Titanic` data, we will highlight all cells corresponding to survived passengers (see Figure 19):

```

> mosaic(Titanic, gp = gpar(fill = c("gray", "dark magenta")),
+   spacing = spacing_highlighting, labeling_args = list(abbreviate = c(Age = 3),
+   rep = c(Survived = FALSE)))

```

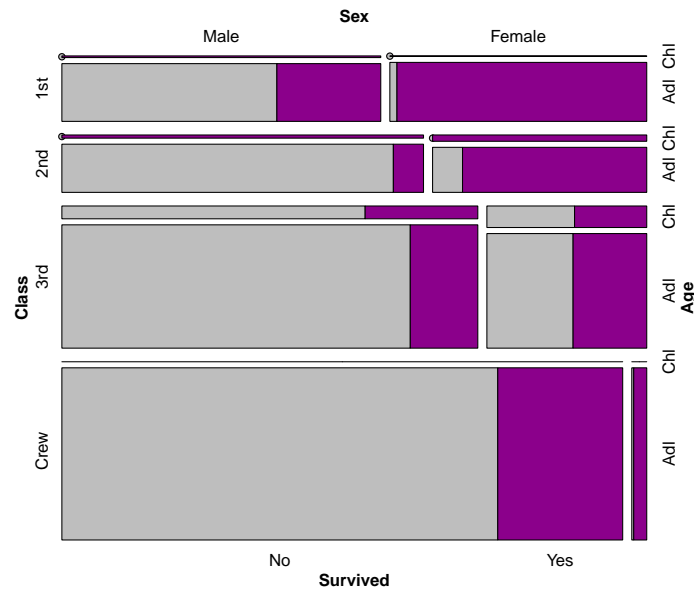


Figure 19: Recycling of parameters, used for highlighting the survived passengers in the `Titanic` data.

Note that `spacing_highlighting()` sets the spaces between tiles in the last dimension to 0. The `labeling_args` argument ensures that labels do not overlap (see Section 4).

### 3.2. Customizing residual-based shadings

This flexible way of specifying graphical parameters is the basis for a suite of shading functions that modify the tiles' appearance with respect to a vector of residuals, resulting from deviations of observed from expected frequencies under a given log-linear model. The idea is to visualize at least sign and absolute size of the residuals, but some shadings, additionally, indicate overall significance. One particular shading, the maximum shading (Meyer *et al.* 2003; Zeileis *et al.* 2005), even allows to identify the cells that cause the rejection of the null hypothesis.

Conceptually, the `strucplot` framework offers three alternatives to add residual-based shading to plots:

1. Precomputing the graphical parameters (e.g., fill colors), encapsulating them into an object of class `gpar` as demonstrated in the previous section, and passing this object to the `gp` argument.
2. Providing a `grapcon` function to the `gp` argument that takes residuals as input and returns an object as described in alternative 1.
3. Providing a `grapcon` generator taking parameters and returning a function as described in alternative 2.

For each of these approaches, we will demonstrate the necessary steps to obtain a binary

shading that visualizes the sign of the residuals by a corresponding fill color (for simplicity, we will treat 0 as positive).

*Alternative 1: Precomputed gpar object*

The first method is precomputing the graphical parameters “by hand”. We will use `royalblue4` color for positive and `mediumorchid4` color for negative residuals (see Figure 20):

```
> expected <- independence_table(ucb)
> (x <- (ucb - expected)/sqrt(expected))
```

	Gender	
Admit	Male	Female
Admitted	4.784093	-5.793466
Rejected	-3.807325	4.610614

```
> (shading1_obj <- ifelse(x > 0, "royalblue4", "mediumorchid4"))
```

	Gender	
Admit	Male	Female
Admitted	"royalblue4"	"mediumorchid4"
Rejected	"mediumorchid4"	"royalblue4"

```
> mosaic(ucb, gp = gpar(fill = shading1_obj))
```

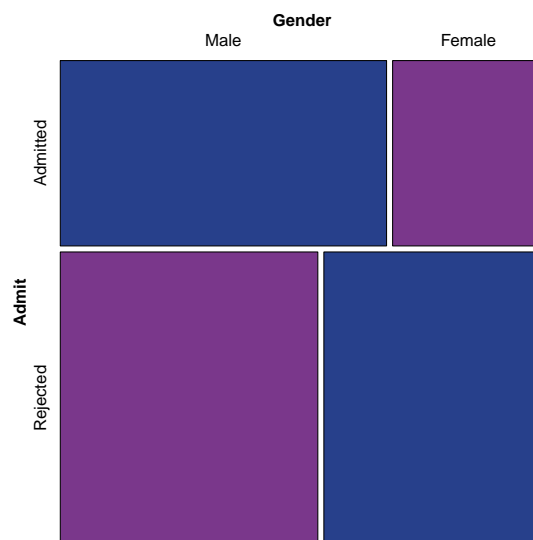


Figure 20: Binary shading visualizing the sign of the residuals.



*Alternative 2: Grapcon function*

For implementing alternative 2, we need to create a “shading function” that computes `gpar` objects from residuals. For that, we can just reuse the code from the previous step:

```
> shading2_fun <- function(x) gpar(fill = ifelse(x > 0,
+       "royalblue4", "mediumorchid4"))
```

To create a mosaic display with binary shading, it now suffices to specify the data table along with `shading2_fun()`:

```
> mosaic(ucb, gp = shading2_fun)
```

`mosaic()` internally calls `strucplot()` which computes the residuals from the specified independence model (total independence by default), passes them to `shading2_fun()`, and uses the `gpar` object returned to finally create the plot.

Our `shading2_fun()` function might be useful, but can still be improved: the hard-wired colors should be customizable. We cannot simply extend the argument list to include, e.g., a `fill = c("royalblue4", "mediumorchid4")` argument because `strucplot()` will neither know how to handle it, nor let us change the defaults. In fact, the interface of shading functions is fixed, they are expected to take exactly one argument: a table of residuals. This is where generating functions (alternative 3) come into play.

*Alternative 3: Grapcon generator*

We simply wrap our `grapcon` shading function in another function that takes all additional arguments it needs to use, possibly preprocesses them, and returns the actual shading function. This returned function will have access to the parameters since in R, nested functions are lexically scoped. Thus, the `grapcon` generator returns (“creates”) a “parameterized” shading function with the minimal standard interface `strucplot()` requires. The following example shows the necessary extensions for our running example:

```
> shading3a_fun <- function(col = c("royalblue4", "mediumorchid4")) {
+   col <- rep(col, length.out = 2)
+   function(x) gpar(fill = ifelse(x > 0, col[1], col[2]))
+ }
```

The first statement just makes sure that exactly two colors are specified. In the call to `mosaic()`, using the new `shading3a_fun()` function, we can now simply change the colors:

```
> mosaic(ucb, gp = shading3a_fun(c("royalblue4", "mediumorchid4")))
```

(figure not shown). The procedure described so far is a rather general concept, applicable to a wide family of user-level **grid** graphics. Indeed, the customization of other components of the `strucplot` framework (labeling, spacing, legend, and core functions) follows the same idea. Now for the shading functions, more customization is needed. Note that `shading3a_fun()` needs to be evaluated by the user, even if the defaults are to be used. It is a better idea

to let `strucplot()` call the generating function, which, in particular, allows the passing of arguments that are computed by `strucplot()`. Since shading functions can be used for visualizing significance (see Section 3.3), it makes sense for generating functions to have access to the model, i.e., observed and expected values, residuals, and degrees of freedom. For example, the `shading_max()` generating function computes a permutation distribution of the maximum statistic and  $p$  values for specified significance levels based on the observed table to create data-driven cut-off points. If this was done in the shading function itself, the permutation statistic would be recomputed every time the shading function is called, resulting in possibly severe performance loss and numerical inconsistencies. Therefore, generating functions for shadings are required to take at least the parameters `observed`, `expected`, `residuals`, and `df` (these are provided by the strucplot framework), followed by other parameters controlling the shading appearance (to be specified by the user):

```
> shading3b_fun <- function(observed = NULL, residuals = NULL,
+   expected = NULL, df = NULL, col = c("royalblue4",
+   "mediumorchid4")) {
+   col <- rep(col, length.out = 2)
+   function(x) gpar(fill = ifelse(x > 0, col[1], col[2]))
+ }
> class(shading3b_fun) <- "grapcon_generator"
```

Note that in this simple binary shading example, the first four parameters are not used. In some sense, generating functions for shadings are parameterized both by the user and the strucplot framework. For shading functions that require model information, the user-specified parameters are to be passed to the `gp_args` argument instead, and for this to work, the generating function needs a class attribute to be distinguishable from the “normal” shading functions. For others (like our simple `shading3b_fun()`) this is optional, but recommended for consistency:

```
> mosaic(ucb, gp = shading3b_fun, gp_args = list(col = c("red",
+   "blue")))
```

The final `shading3b_fun()` pretty much resembles `shading_binary()`, one of the standard shading functions provided by the `vcd` package.

### 3.3. An overview of the shading functions in vcd

Friendly (1994) suggested a residual-based shading for the mosaic tiles that can also be applied to the rectangles in association plots (Meyer *et al.* 2003). Apart from `shading_binary()`, there are currently two basic shadings available in `vcd`: `shading_hcl()` and `shading_hsv()`, as well as two derived functions: `shading_Friendly()` building upon `shading_hsv()`, and `shading_max()` building upon `shading_hcl()`. `shading_hsv()` and `shading_hcl()` provide the same conceptual tools, but use different color spaces: the Hue-Saturation-Value (HSV) and the Hue-Chroma-Luminance (HCL) scheme, respectively. We will first expose the basic concept of these shading functions using HSV space, and then briefly explain the differences to HCL space (a detailed discussion can be found in Zeileis *et al.* 2005). Color palettes in

HCL space are preferable to palettes derived from HSV space from a perceptual point of view. Functions for creating palettes (see, e.g., `diverge_hcl()`) are provided with the **vcd** package. In HSV space, colors are specified in three dimensions: Hue, Saturation (“colorfulness”), and Value (“lightness”, amount of gray). These three dimensions are used by `shading_hsv()` to visualize information about the residuals and the underlying independence model. The hue indicates the residuals’ sign: by default, blue for positive, and red for negative residuals. The saturation of a residual is set according to its size: high saturation for large, and low saturation for small residuals. Finally, the overall lightness is used to indicate the significance of a test statistic: light colors for significant, and dark colors for non-significant results.

As an example, we will visualize the association of hair and eye color in the **HairEyeColor** data set (see Figure 21, top):

```
> haireye <- margin.table(HairEyeColor, 1:2)
> mosaic(haireye, gp = shading_hsv)
```

As introduced before, the default shading scheme is not `shading_hsv()` but `shading_hcl()` due to the better perceptual characteristics of HCL color space. The following example again illustrates the **HairEyeColor** data, this time with HCL colors:

```
> mosaic(haireye, gp = shading_hcl)

> mosaic(haireye, gp = shading_hcl, gp_args = list(h = c(130,
+      43), c = 100, l = c(90, 70)))
```

In Figure 21, the plot in the middle depicts the default palette, and the bottom plot an alternative setting for Hue (**h**), Chroma (**c**), and Luminance (**l**).

Large positive residuals (greater than 4) can be found for brown eyes/black hair and blue eyes/blond hair, and are colored in deep blue. On the other hand, there is a large negative residual (less than  $-4$ ) for brown eyes/blond hair, colored deep red. There are also three medium-sized positive (negative) residuals between 2 and 4 ( $-2$  and  $-4$ ): the colors for them are less saturated. Residuals between  $-2$  and 2 are shaded in white (gray for HCL-shading). The heuristic for choosing the cut-off points 2 and 4 is that the Pearson residuals are approximately standard normal which implies that the highlighted cells are those with residuals *individually* significant at approximately the  $\alpha = 0.05$  and  $\alpha = 0.0001$  levels, respectively. These default cut-off points can be changed to alternative values using the `interpolate` argument (see Figure 22):

```
> mosaic(haireye, shade = TRUE, gp_args = list(interpolate = 1:4))
```

The elements of the numeric vector passed to `interpolate` define the knots of an interpolating step function used to map the absolute residuals to saturation levels. The `interpolate` argument also accepts a user-defined function, which then is called with the absolute residuals to get a vector of cut-off points. Thus, it is possible to automatically choose the cut-off points in a data-driven way. For example, one might think that the extension from four cut-off points to a continuous shading—visualizing the whole range of residuals—could be useful. We simply need a one-to-one mapping from the residuals to the saturation values:

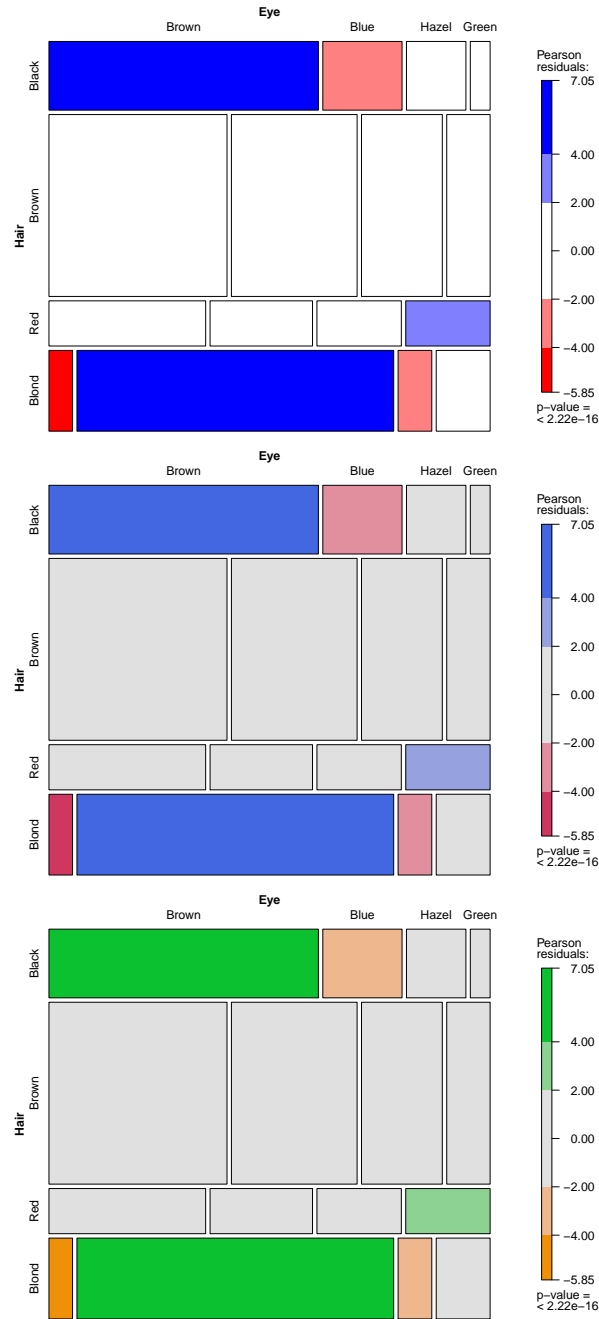


Figure 21: Three mosaic plots for the `HairEyeColor` data using different color palettes. Top: default HSV color palette. Middle: default HCL color palette. Bottom: a custom HCL color palette.

```
> ipol <- function(x) pmin(x/4, 1)
```

Note that this `ipol()` function maps residuals greater than 4 to a saturation level of 1. However, the resulting plot (Figure 22, right) is deceiving:

```
> mosaic(haireye, shade = TRUE, gp_args = list(interpolate = ipol),
+        labeling_args = list(abbreviate = c(Sex = TRUE)))
```

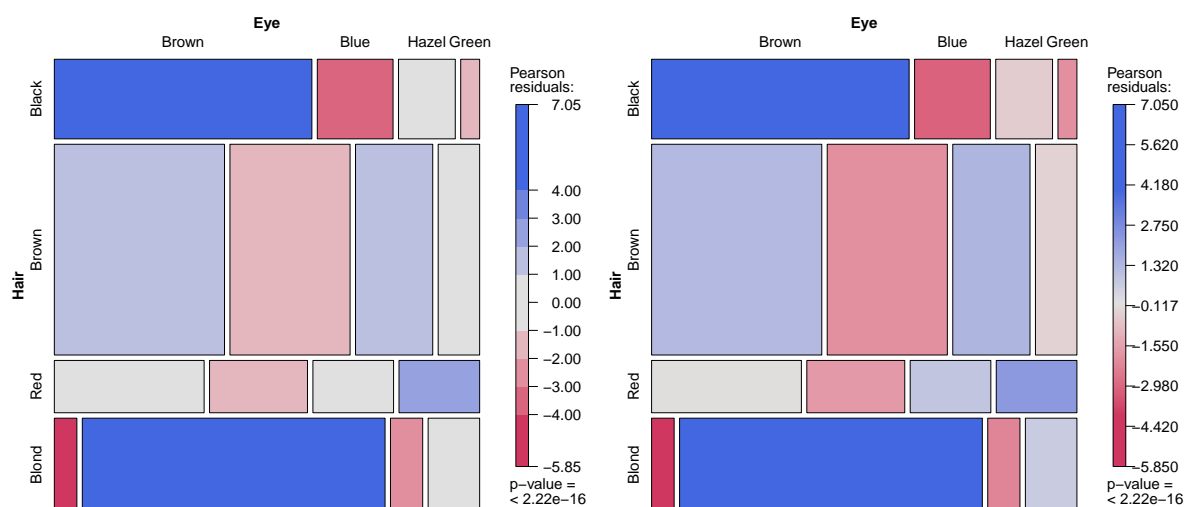


Figure 22: The `HairEyeColor` data. Left: shading with 4 cut-off points. Right: continuous shading.

Too much color makes it difficult to interpret the image, and the subtle color differences are hard to catch. Therefore, we only included shadings with discrete cut-off points.

The third remaining dimension, the value, is used for visualizing the significance of a test statistic. The user can either directly specify the  $p$  value, or, alternatively, a function that computes it, to the `p.value` argument. Such a function must take observed and expected values, residuals, and degrees of freedom (used by the independence model) as arguments. If nothing is specified, the  $p$  value is computed from a  $\chi^2$  distribution with `df` degrees of freedom. The `level` argument is used to specify the confidence level: if `p.value` is smaller than  $1 - \text{level}$ , light colors are used, otherwise dark colors are employed. The following example using the `Bundesliga` data shows the relationship of home goals and away goals of Germany's premier soccer league in 1995: although there are two "larger" residuals (one greater than 2, one less than  $-2$ ), the  $\chi^2$  test does not reject the null hypothesis of independence. Consequently, the colors appear dark (see Figure 23, left):

```
> BL <- xtabs(~HomeGoals + AwayGoals, data = Bundesliga,
+            subset = Year == 1995)
> mosaic(BL, shade = TRUE)
```

Note that in extended mosaic plots, bullets drawn for zero cells are shaded, too, bringing out non-zero residuals, if any.

A shading function building upon `shading_hsv()` is `shading_Friendly()`, implementing the shading introduced by Friendly (1994). In addition to the defaults of the HSV shading, it uses the border color and line type to redundantly code the residuals' sign. The following example again uses the Bundesliga data from above, this time using the Friendly scheme and, in addition, an alternative legend (see Figure 23, right):

```
> mosaic(BL, gp = shading_Friendly, legend = legend_fixed,
+        zero_size = 0)
```

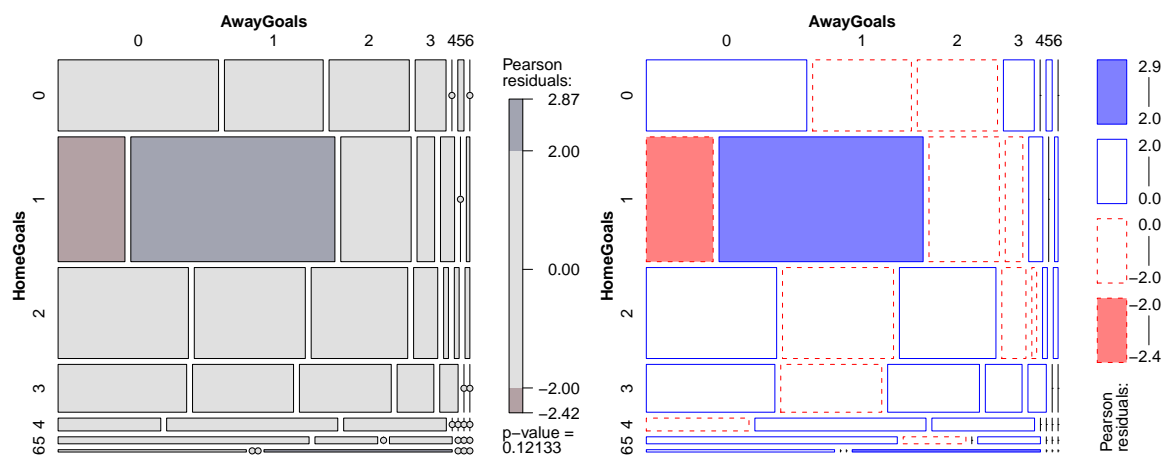


Figure 23: The Bundesliga data for 1995. Left: Non-significant  $\chi^2$  test. Right: using the Friendly shading and a legend with fixed bins.

(The `zero_size = 0` argument removes the bullets indicating zero observed values. This feature is not provided in the original SAS implementation of the Friendly mosaic plots.)

A more “advanced” function building upon `shading_hcl()` is `shading_max()`, using the maximum statistic both to conduct the independence test and to visualize significant *cells* causing the rejection of the independence hypothesis (Meyer *et al.* 2003; Zeileis *et al.* 2005). The `level` argument of `shading_max()` then can be used to specify several confidence levels from which the corresponding cut-off points are computed. By default, two cut-off points are computed corresponding to confidence levels of 90% and 99%, respectively. In the following example, we investigate the effect of a new treatment for rheumatoid arthritis on a group of female patients using the maximum shading (see Figure 24):

```
> set.seed(4711)
> mosaic(~Treatment + Improved, data = Arthritis, subset = Sex ==
+        "Female", gp = shading_max)
```

The maximum test is significant although the residuals are all in the  $[-2, 2]$  interval. The `shading_hcl()` function with default cut-off points would not have shown any color. In

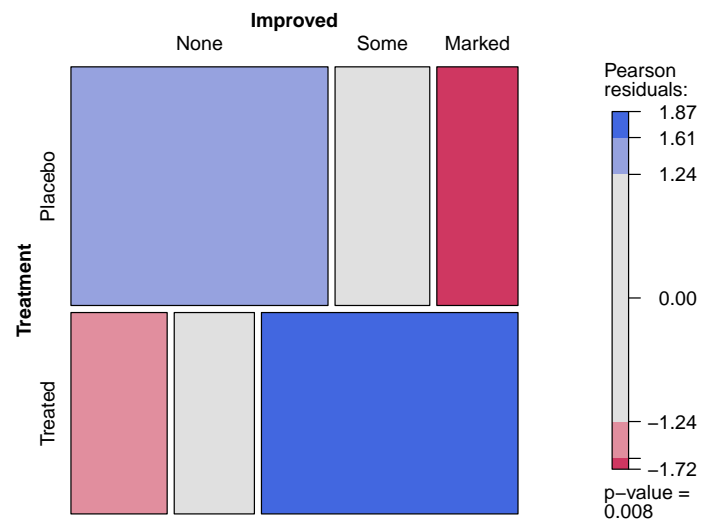


Figure 24: The **Arthritis** data (female patients) with significant maximum test.

addition, since the test statistic is the maximum of the absolute Pearson residuals, *each* colored residual violates the null hypotheses of independence, and thus, the “culprits” can immediately be identified.

## 4. Labeling

One of the major enhancements in package **vcd** compared to `mosaicplot()` and `assocplot()` in base R is the labeling in the strucplot framework which offers more features and greater flexibility. Like shading, spacing, and drawing of legend and core plot, labeling is now carried out by grapcon functions, rendering labeling completely modular. The user supplies either a labeling function, or, alternatively, a generating function that parameterizes a labeling function, to `strucplot()` which then draws the labels. Labeling is well-separated from the actual plotting that occurs in the low-level core functions. It only relies on the viewport tree produced by them, and the `dimnames` attribute of the visualized table. Labeling functions are grapcons that “add ink to the canvas”: the drawing of the labels happens after the actual plot has been drawn by the core function. Thus, it is possible to supply one’s own labeling function, or to combine some of the basic functions to produce a more complex labeling. In the following, we describe the three basic modules (`labeling_text()`, `labeling_list()`, and `labeling_cells()`) and derived functions that build upon them.

### 4.1. Labels in the borders: `labeling_text()`

`labeling_text()` is the default for all strucplot displays. It plots labels in the borders similar to the `mosaicplot()` function in base R, but is much more flexible: it is not limited to 4 dimensions, and the positioning and graphical parameters of levels and variable names are customizable. In addition, the problem of overlapping labels can be handled in several ways. As an example, again consider the **Titanic** data: by default, the variable names and levels are plotted “around” the plot in a counter-clockwise way (see Figure 25, top left):

```
> mosaic(Titanic)
```

Note that the last two levels of the **survived** variable do overlap, as well as some adult and child labels of the **age** Variable. This issue can be addressed in several ways. The “brute force” method is to enable clipping for these dimensions (see Figure 25, top right):

```
> mosaic(Titanic, labeling_args = list(clip = c(Survived = TRUE,
+      Age = TRUE)))
```

The `clip` parameter is passed to the labeling function via the `labeling_args` argument which takes a list of parameters. `clip` itself takes a vector of logicals (one for each dimension). Almost all vectorized arguments in the strucplot framework can be abbreviated in the following way: unnamed components (or the defaults, if there are none) are recycled as needed, but overridden by the named components. Here, the default is **FALSE**, and therefore clipping is enabled only for the **survived** and **age** variables. A more sensible solution to the overlap problem is to abbreviate the levels (see Figure 25, middle left):

```
> mosaic(Titanic, labeling_args = list(abbreviate = c(Survived = TRUE,
+      Age = 3)))
```

The `abbreviate` argument takes a vector of integers indicating the number of significant characters the levels should be abbreviated to (**TRUE** is interpreted as 1, obviously). Abbreviation



is performed using the `abbreviate()` function in base R. Another possibility is to rotate the levels (see Figure 25, bottom):

```
> mosaic(Titanic, labeling_args = list(rot_labels = c(bottom = 90,
+   right = 0), offset_varnames = c(right = 1), offset_labels = c(right = 0.3)),
+   margins = c(right = 4, bottom = 3))
```

Finally, we could also inhibit the output of repeated levels (see Figure 25, middle right):

```
> mosaic(Titanic, labeling_args = list(rep = c(Survived = FALSE,
+   Age = FALSE)))
```

We now proceed with a few more “cosmetic” features (which do not all produce satisfactory results for our sample data). A first simple, but effective modification is to position all labels and variables left-aligned (see Figure 26, top left):

```
> mosaic(Titanic, labeling_args = list(pos_varnames = "left",
+   pos_labels = "left", just_labels = "left", rep = FALSE))
```

Note that obviously we need to change the justification to "left" as well. We can achieve the same effect by using the convenience function `labeling_left()`:

```
> mosaic(Titanic, labeling = labeling_left)
```

Next, we show how to put all levels to the bottom and right margins, and all variable names to the top and left margins (see Figure 26, top right):

```
> mosaic(Titanic, labeling_args = list(tl_labels = FALSE,
+   tl_varnames = TRUE, abbreviate = c(Survived = 1,
+   Age = 3)))
```

The `tl_`foo (“top left”) arguments are TRUE by default. Now, we will add boxes to the labels and additionally enable clipping (see Figure 26, bottom left):

```
> mosaic(Titanic, labeling_args = list(tl_labels = FALSE,
+   tl_varnames = TRUE, boxes = TRUE, clip = TRUE))
```

The values to `boxes` and `clip` are recycled for all dimensions. The result is pretty close to what calling `mosaic()` with the `labeling_cboxed()` wrapper does, except that variables and levels, by default, are put to the top and to the left of the plot:

```
> mosaic(Titanic, labeling = labeling_cboxed)
```

Another variant is to put the variable names into the same line as the levels (see Figure 26, bottom right—clipping for `Survived` and `Age` is, additionally, disabled, and `Age` abbreviated):

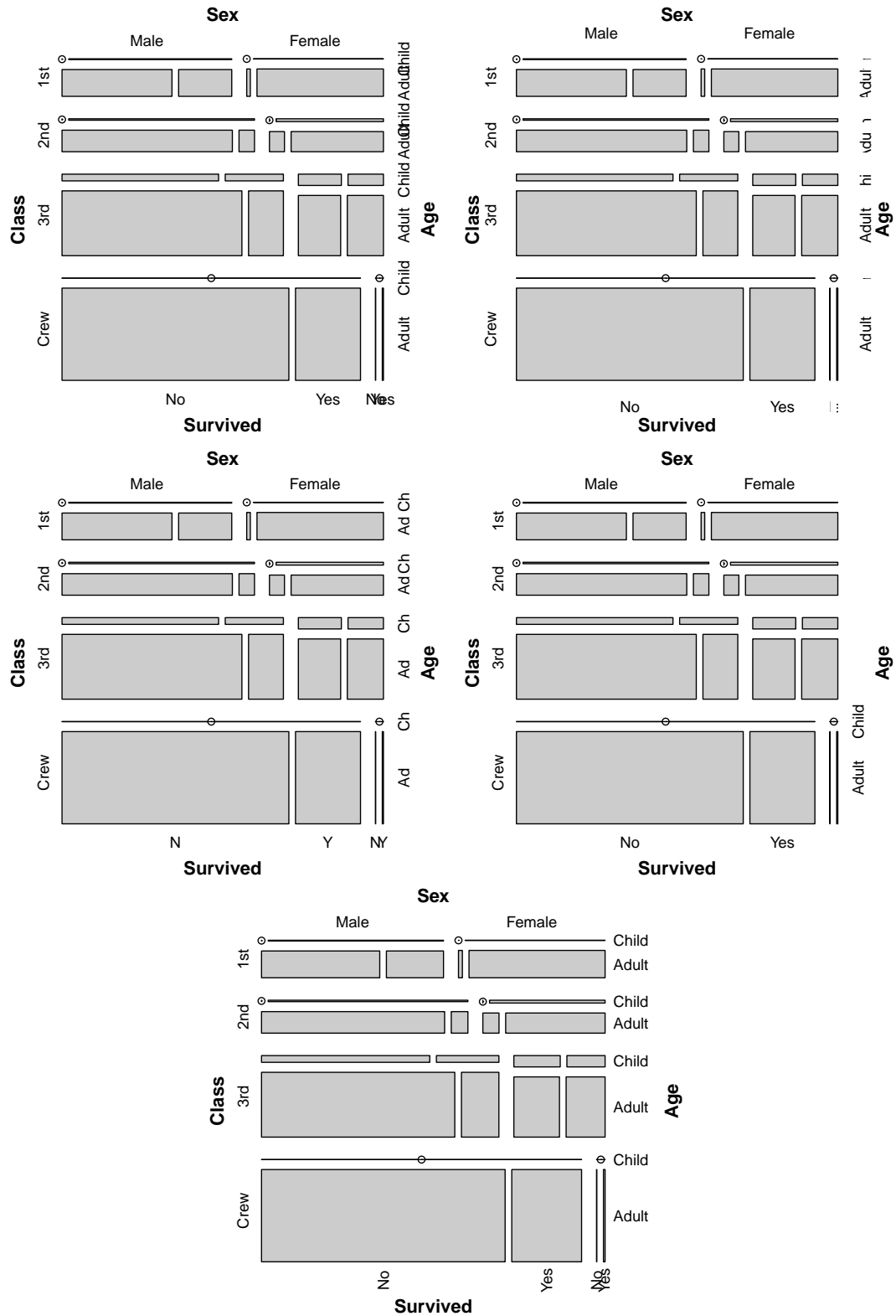


Figure 25: Examples for possible labeling strategies for the Titanic data mosaic. Top left: default labeling (many labels overlap). Top right: with clipping turned on. Middle left: **Age** and **Survived** labels abbreviated. Middle right: **Age** labels not repeated. Bottom: **Age** and **Survived** labels rotated.

```
> mosaic(Titanic, labeling_args = list(tl_labels = TRUE,
+   boxes = TRUE, clip = c(Survived = FALSE, Age = FALSE,
+   TRUE), abbreviate = c(Age = 4), labbl_varnames = TRUE),
+   margins = c(left = 4, right = 1, 3))
```

`labbl_varnames` (“variable names to the bottom/left of the labels”) is a vector of logicals indicating the side for the variable names. The resulting layout is close to what `labeling_lboxed()` produces, except that variables and levels, by default, are left-aligned and put to the bottom and to the right of the plot:

```
> mosaic(Titanic, labeling = labeling_lboxed, margins = c(right = 4,
+   left = 1, 3))
```

A similar design is used by the `doubledecker()` function.

#### 4.2. Labels in the cells: `labeling_cells()`

This labeling draws both variable names and levels in the cells. As an example, we use the `PreSex` data on pre- and extramarital sex and divorce (see Figure 27, top left):

```
> mosaic(~MaritalStatus + Gender, data = PreSex, labeling = labeling_cells)
```

In the case of narrow cells, it might be useful to abbreviate labels and/or variable names and turn off clipping (see Figure 27, top right):

```
> mosaic(~PremaritalSex + ExtramaritalSex, data = PreSex,
+   labeling = labeling_cells(abbreviate_labels = TRUE,
+   abbreviate_varnames = TRUE, clip = FALSE))
```

For some data, it might be convenient to combine cell labeling with border labeling as done by `labels_conditional()` (see Figure 27, bottom left):

```
> mosaic(~PremaritalSex + ExtramaritalSex | MaritalStatus +
+   Gender, data = PreSex, labeling = labeling_conditional(abbreviate_varnames = TRUE,
+   abbreviate_labels = TRUE, clip = FALSE, gp_text = gpar(col = "red")))
```

Additionally, the cell labeling allows the user to add arbitrary text to the cells by supplying a character array in the same shape as the data array to the `text` argument (cells with missing values are ignored). In the following example using the `Titanic` data, this is used to add all observed values greater than 5 to the cells after the mosaic has been plotted (see Figure 27, bottom right):

```
> mosaic(Titanic, labeling_args = list(abbreviate = c(Survived = 1,
+   Age = 4)), pop = FALSE)
> tab <- ifelse(Titanic < 6, NA, Titanic)
> labeling_cells(text = tab, clip = FALSE)(Titanic)
```

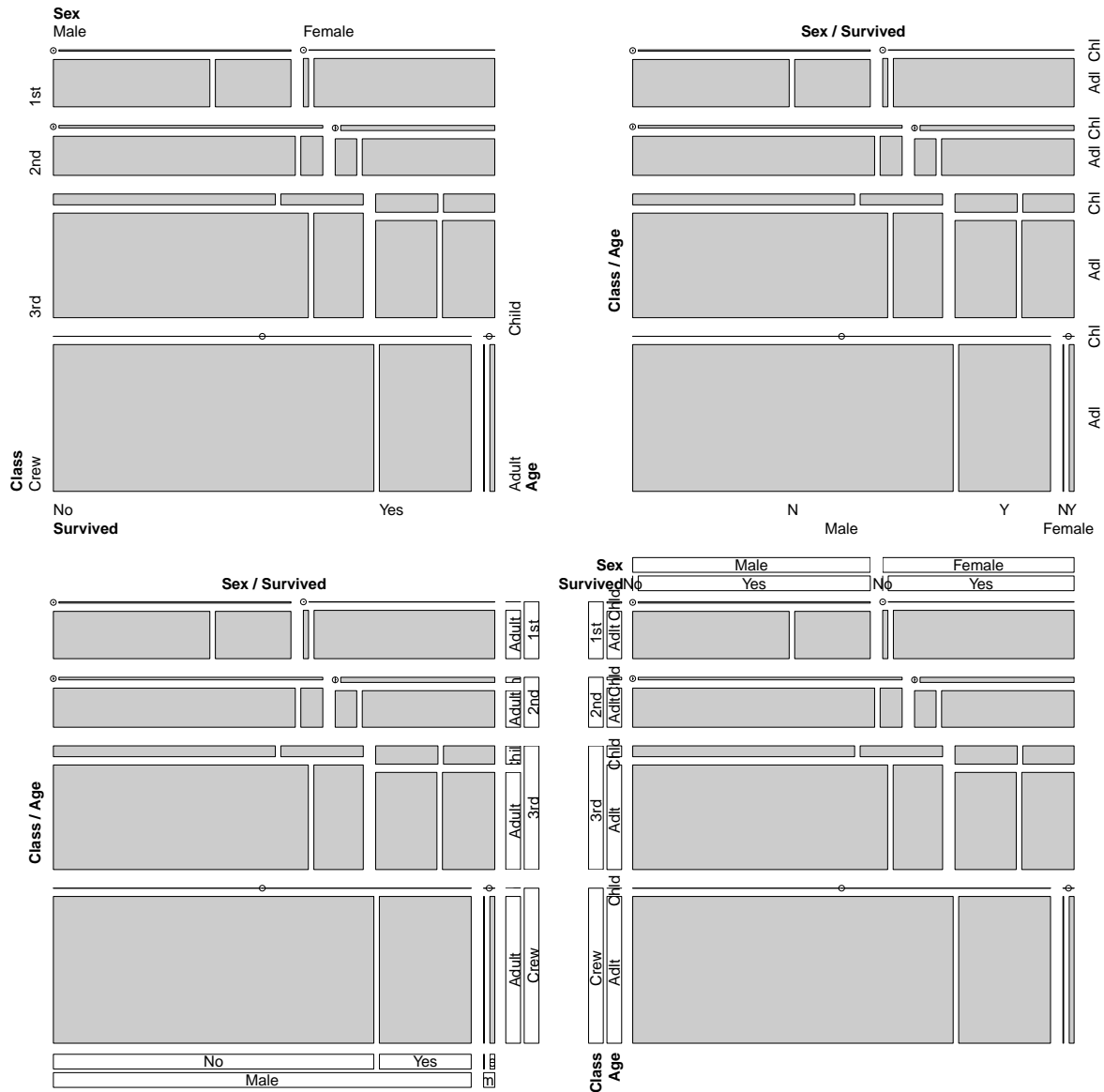


Figure 26: Advanced strategies for labeling of the Titanic data. Top left: left aligning of both variable names and labels. Top right: changes in the margins (all variable names are in the top and left margins, and all labels in the bottom and right margins). Bottom left: clipping turned on, and boxes used. Bottom right: variable names beneath levels, clipping disabled for the survival and age variables, and **Age** abbreviated.

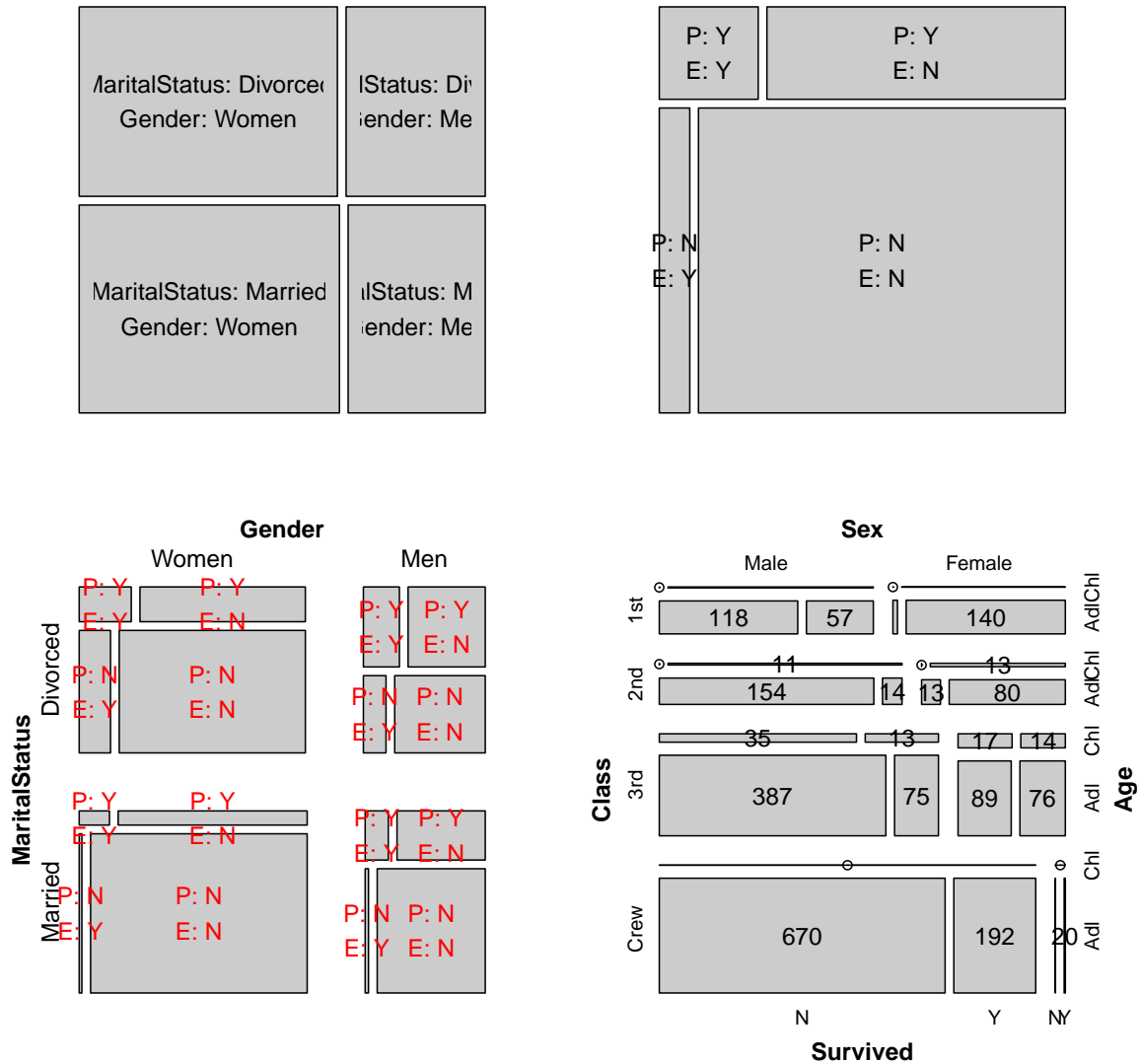


Figure 27: Cell labeling. Top left: default labeling using the `PreSex` data. Top right: abbreviated labels. Bottom left: conditional labeling (labels abbreviated and in red for clarity). Bottom right: user-supplied text (observed frequencies exceeding 5) added to a mosaic display of the `Titanic` data. Note that clipping is on by default (top left), and has explicitly been turned off for the three other plots.

### 4.3. A simple list of labels: `labeling_list()`

If problems with overlapping labels cannot satisfactorily resolved, the last remedy could be to simply list the levels below the plot (see Figure 28):

```
> mosaic(Titanic, labeling = labeling_list, margins = c(bottom = 5))
```

The number of columns can be specified.

## 5. Spacing

Spacing of strucplot displays is customizable in a similar way than shading. The `spacing` argument of the `strucplot()` function takes a list of unit vectors, one for each dimension, specifying the space between the tiles corresponding to the levels. Consider again the introductory example of the *Arthritis* data (Figure 1). Since we are interested in the effect of the medicament in the placebo and treatment groups, a mosaic plot is certainly appropriate to visualize the three levels of **Improved** in the two **Treatment** strata. Another conceptual approach is to use spine plots with highlighting (Hummel 1996). A spine plot is a variation of a bar plot where the heights of the bars are held constant, whereas the widths are used to represent the number of cases in each category. This is equivalent to a mosaic plot for a one-way table. If a second (indicator) variable is highlighted in a spine plot, we obtain a display equivalent to a simple mosaic display for a two-way table, except that no space between the levels of the highlighted variable is used. In the *Arthritis* example, we will highlight patients with **Marked** improvement in both groups. To obtain such a display within the strucplot framework, it suffices to set the space between the **Improved** tiles to 0 (see Figure 29):

```
> (art <- structable(~Treatment + Improved, data = Arthritis,
+   split_vertical = TRUE))
```

	Treatment Placebo	Treated
Improved		
None	29	13
Some	7	7
Marked	7	21

```
> (my_spacing <- list(unit(0.5, "lines"), unit(c(0, 0),
+   "lines")))
```

```
[[1]]
[1] 0.5lines
```

```
[[2]]
[1] 0lines 0lines
```

```
> my_colors <- c("lightgray", "lightgray", "black")
> mosaic(art, spacing = my_spacing, gp = gpar(fill = my_colors,
+   col = my_colors))
```

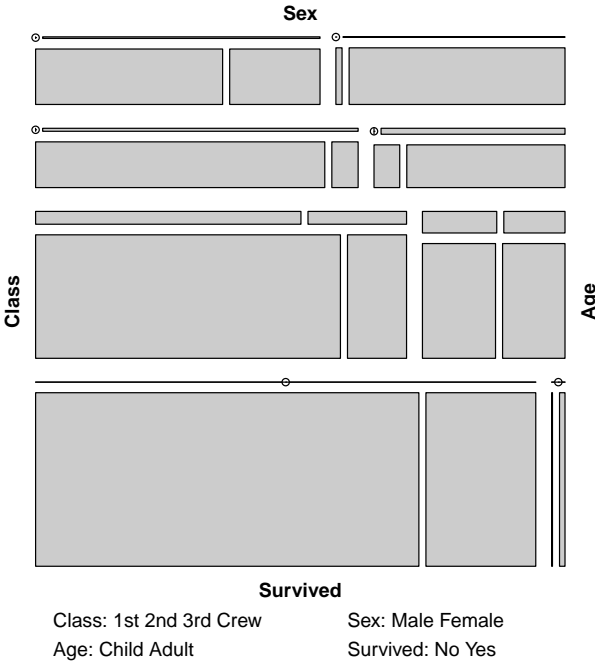


Figure 28: Labels indicated below the plot.

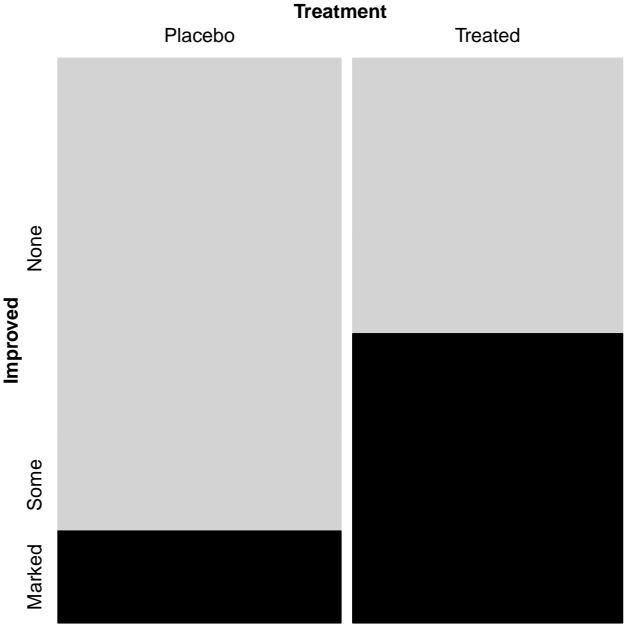


Figure 29: Spine plot for the `Arthritis` data using the `strucplot` framework.

Note that the default and formula methods for `mosaic()` provide a convenience interface for highlighting. A similar plot (with slightly different shading) than the previous one can be obtained using:

```
> mosaic(Improved ~ Treatment, data = Arthritis, split_vertical = TRUE)
```

The strucplot framework also provides a set of spacing grapcon generators which compute suitable spacing objects for typical applications. The simplest spacing is `spacing_equal()` that uses the same space between all tiles (see Figure 30, top left):

```
> mosaic(art, spacing = spacing_equal(unit(2, "lines")))
```

`spacing_equal()` is the default grapcon generator for two-dimensional tables. Slightly more flexible is `spacing_dimequal()` that allows an individual setting for each dimension (see Figure 30, top right):

```
> mosaic(art, spacing = spacing_dimequal(unit(1:2, "lines")))
```

The default for multi-way contingency tables is `spacing_increase()` which uses increasing spaces for the dimensions. The user can specify a start value and the increase factor (see Figure 30, bottom left):

```
> mosaic(art, spacing = spacing_increase(start = unit(0.5,
+      "lines"), rate = 1.5))
```

For the arthritis example above, we could as well have used `spacing_highlighting()` which is similar to `spacing_increase()` but sets the spacing in the last splitting dimension to 0 (see Figure 30, bottom right):

```
> mosaic(art, spacing = spacing_highlighting, gp = my_colors)
```

Finally, `spacing_conditional()` can be used for visualizing conditional independence: it combines `spacing_equal()` (for the conditioned dimensions) and `spacing_increase()` (for the conditioning dimensions). As an example, consider Figure 3: the spacing clearly allows to better distinguish the conditioning variables (`Gender` and `MaritalStatus`) from the conditioned variables (`PremaritalSex` and `ExtramaritalSex`). This spacing is the default when conditional variables are specified for a strucplot display (see Section 2).

## 6. Example: Ovarian cancer survival

In the following, we demonstrate some of the described techniques in analyzing a data set originating from (Obel 1975) (taken from Andersen 1991) about a retrospective study of ovary cancer carried out in 1973. Information was obtained from 299 women, who were operated for ovary cancer 10 years before. The data consists of four binary variables: the `stage` of the cancer at the time of operation (levels: `early`, `advanced`), the type of `operation` performed (`radical`, `limited`), the `survival` status after 10 years (`yes`, `no`), and `xray` indicating whether X-ray treatment was received (`yes`, `no`).

The dataset in `vcd` comes pretabulated in a data frame, so we first create the four-way table:



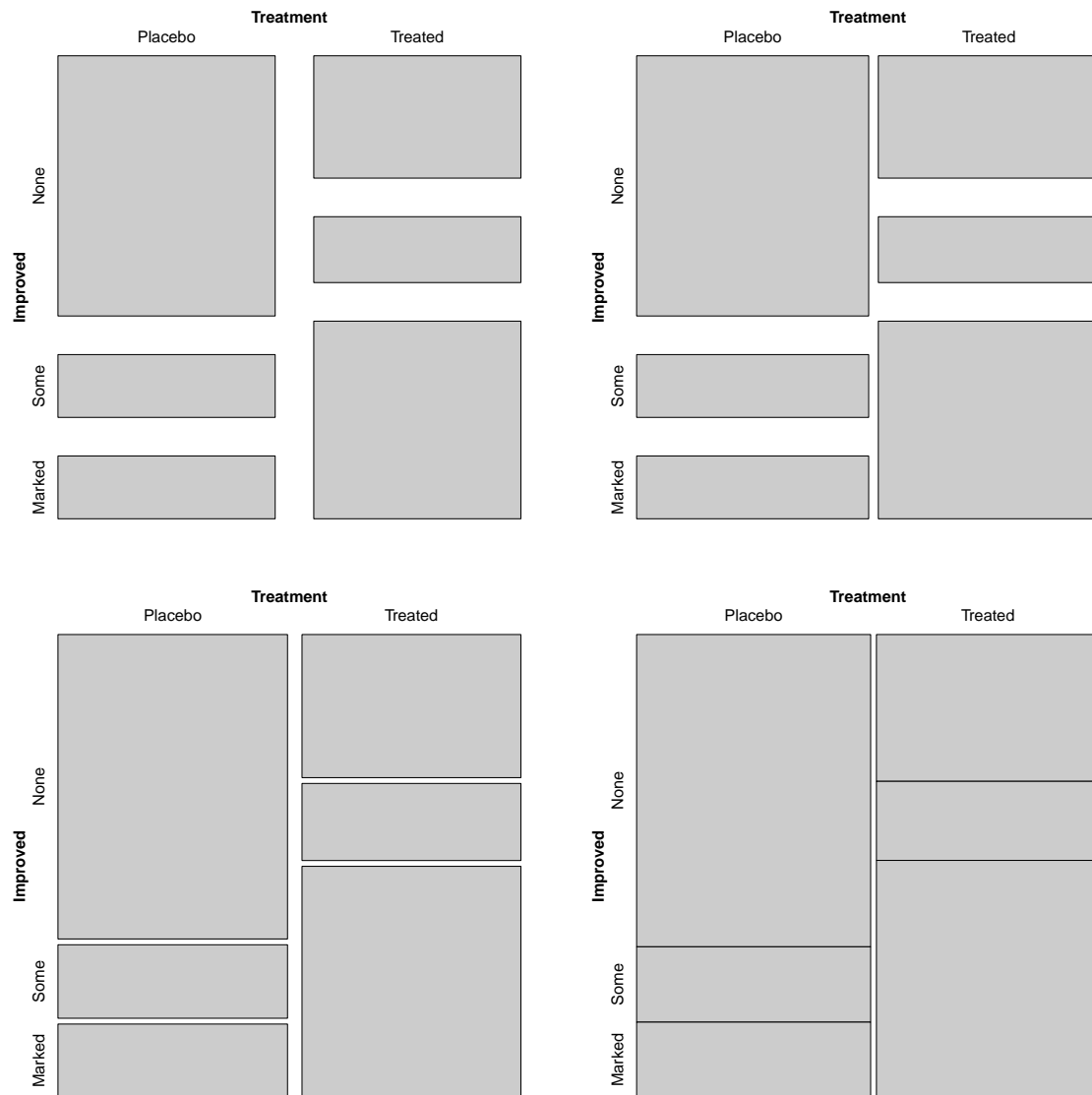


Figure 30: Varying spacing for the Arthritis data. Top left: equal spacing for all dimensions. Top right: different spacings for individual dimensions. Bottom left: increasing spacing. Bottom right: spacing used for highlighting.

```
> tab <- xtabs(Freq ~ stage + operation + xray + survival,
+             data = OvaryCancer)
```

A “flattened” textual representation can be obtained using `structable()`:

```
> structable(survival ~ ., data = tab)
```

			survival no yes	
stage	operation	xray		
early	radical	no	10	41
		yes	17	64
	limited	no	1	13
		yes	3	9
advanced	radical	no	38	6
		yes	64	11
	limited	no	3	1
		yes	13	5

A first overview can be obtained using a pairs plot (Figure 31):

```
> dpa <- list(var_offset = 1.2, rot = -30, just_leveltext = "left")
> pairs(tab, diag_panel_args = dpa)
```

The pairs plot, by default, creates mosaic displays for all pairwise variable combinations, and bar plots in the diagonal to visualize the absolute frequencies of the variables. The `var_offset` argument modifies the offset of the (centered) variable names to avoid overlap with the bars. Additionally, we use the `rot` and the `just_leveltext` arguments to rotate the level names, again to avoid their overlap. First, we consider the marginal distributions. The study design involved (nearly) the same number of survived (150) and deceased (149) patients. Similarly balanced, 158 cases were in an advanced and 141 in an early stage. Most patients (251, 84%) were treated with a radical operation, and 186 (62%) were submitted to X-ray treatment. Next, we inspect the two-way interaction of the influencing factors (`stage`, `operation`, and `xray`): the corresponding mosaics exhibit symmetric, regular shapes with aligned tiles, which indicate no marginal interaction between these variables. The same is true for the interactions of `survival` with `operation` and `xray`, respectively. Only the stage seems to influence survival: here, the tiles are “shifted”.

A different view on the data, focused on the influence of the explanatory variables on `Survival`, can be obtained using a doubledacker plot (Figure 32):

```
> doubledacker(survival ~ stage + operation + xray, data = tab)
```

From a technical point of view, the display is constructed as a mosaic plot showing the conditional distribution of `survival`, given `xray`, given `operation`, given `stage`, with vertical splits for the conditioning variables and horizontal ones for `survival`. Additionally, there is zero space between the tiles of the last dimension and a binary shading is used for survived and deceased patients. Conceptually, this plot is interpreted as a mosaic plot of just the

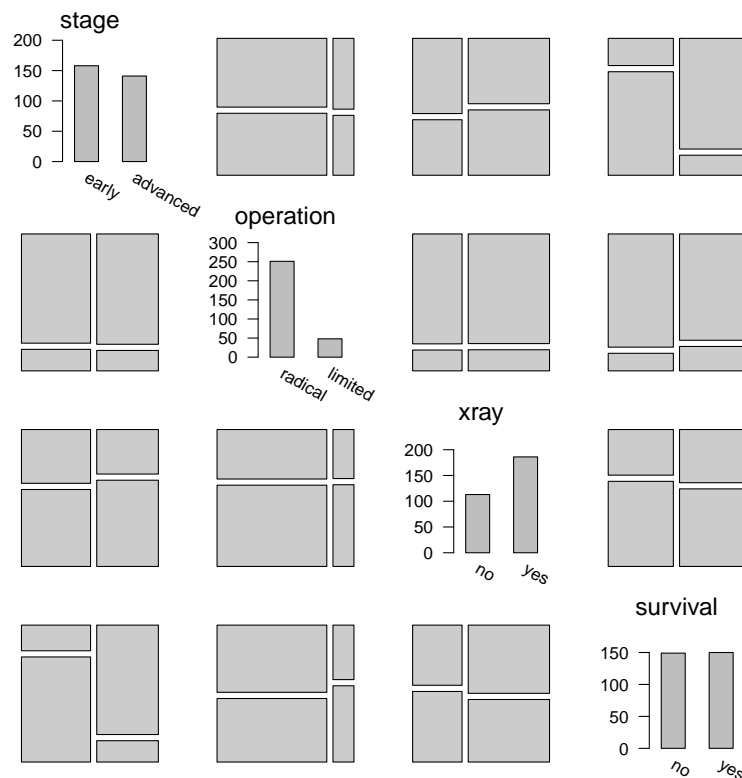


Figure 31: Pairs plot for the `OvaryCancer` data showing mosaic displays for all pairwise distributions and bar plots for all marginal distributions.

influencing variables, with `survival` highlighted in the tiles. Thus, the plot really shows the influence of the explanatory variables on `survival`. Clearly, the survival rate is higher among patients in an early stage, but neither radical operation nor X-ray treatment seem to improve the situation. From this exploratory phase, the survival rate seems to be slightly higher for patients who received a limited operation only, whereas the effect for X-ray treatment is less marked.

To visualize inference results, we can make use of residual-based shadings, investigating log-linear models for the four-way table. Figure 33 visualizes the null model, where survival is independent from the combined effect of operation, X-ray treatment, and stage:

```
> split <- c(TRUE, TRUE, TRUE, FALSE)
> mosaic(tab, expected = ~survival + operation * xray *
+       stage, split_vertical = split)
```

The model is clearly rejected ( $p$ -value: 0.000). From the exploratory phase of our analysis, we (only) suspect `stage` to be influential on the survival rate. A corresponding hypothesis is that `survival` be independent of `xray` and `operation`, given `stage`. The model is specified using the `expected` argument, either using the `loglin()` interface or the `loglm()` formula interface (the resulting mosaic plot is shown in Figure 34):

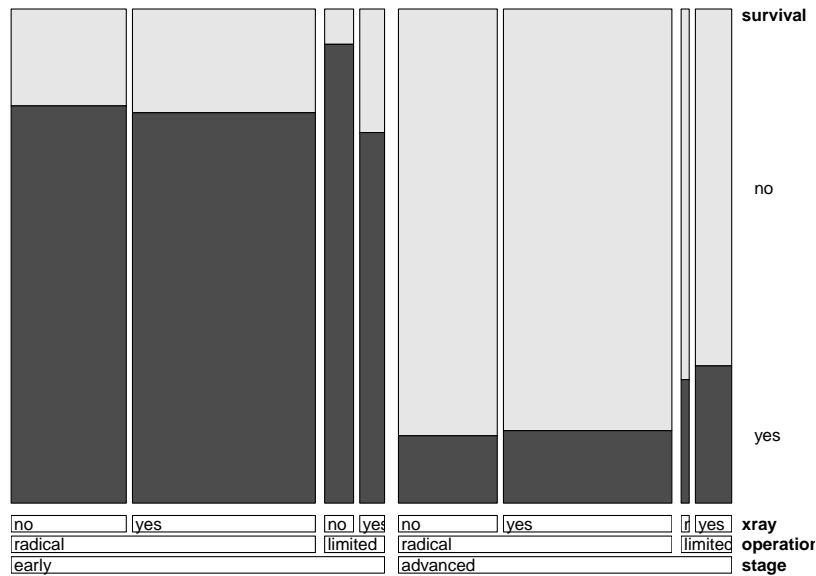


Figure 32: Doubledecker plot for the `OvaryCancer` data showing the conditional distribution of X-ray, given operation, given stage, and with survival highlighted.

```
> mosaic(tab, expected = ~(survival + operation * xray) *
+       stage, split_vertical = split)
```

Thus, based on this data, only pre-diagnosis seems to matter in ovarian cancer therapy.

## 7. Conclusion

In this paper, we describe the “strucplot” framework for the visualization of multi-way contingency tables. Strucplot displays include popular basic plots such as mosaic, association, and sieve plots, integrated in a unified framework: all can be seen as visualizations of hierarchical conditional flat tables. Additionally, these core strucplot displays can be combined into more complex, specialized plots, such as pairs and trellis-like displays for visualizing conditional independence. Residual-based shadings permit the visualization of log-linear models and the results of independence tests. The framework’s modular design allows flexible customization of the plots’ graphical appearance, including shading, labeling, spacing, and legend, by means of graphical appearance control (“grapcon”) functions. These “graphical hyperparameters” are customized and created by generating functions. Our work includes a set of predefined grapcon generators for typical analysis tasks, and user-level extensions can easily be added.

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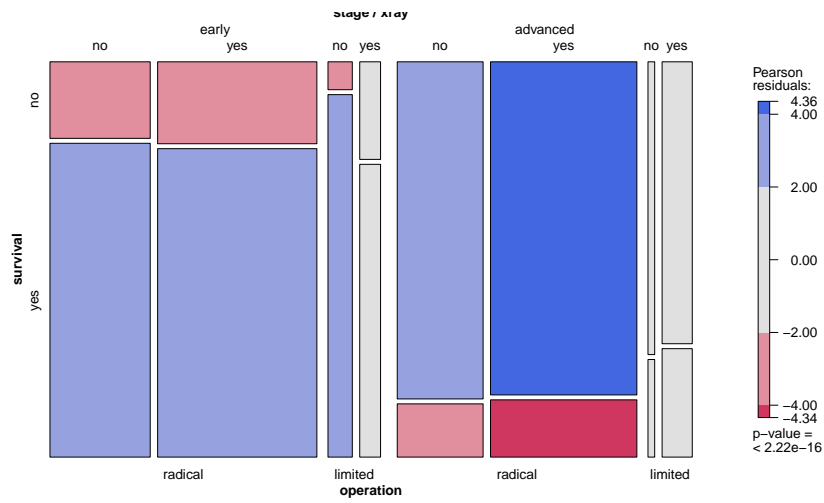


Figure 33: Mosaic plot for the `OvaryCancer` data, with residual-based shading for the (clearly rejected) null model  $(\text{survival})|(\text{operation}, \text{X-ray}, \text{stage})$ .

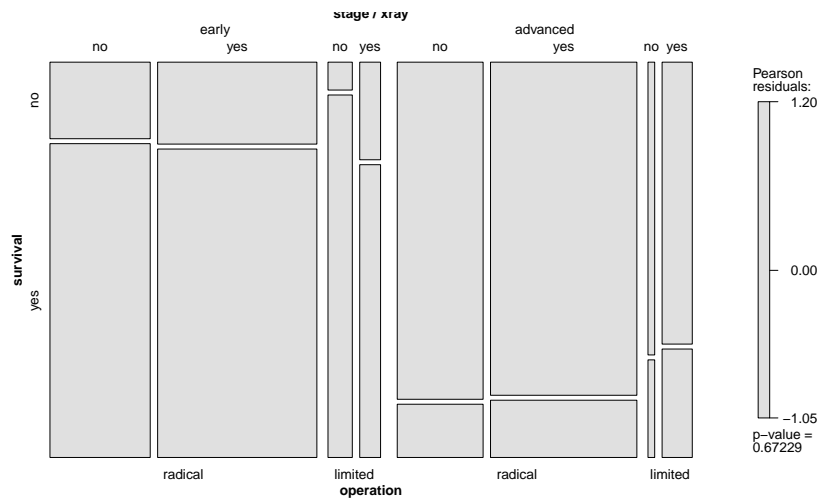


Figure 34: Mosaic plot for the `OvaryCancer` data, with residual-based shading for the hypothesis of survival being independent of X-ray and operation, given stage. The hypothesis is not rejected.

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## A. Data sets

The data set names in the paper are those from the R system. In the following, we give a short description of each data set.

**Arthritis** Data from a double-blind clinical trial investigating a new treatment for rheumatoid arthritis. Source: Koch and Edwards (1988). Taken from: Friendly (2000). Package: **vcd**.

**Bundesliga** Results from the first German soccer league in the years 1995/6 (Knorr-Held 1999) and 2001/2 (Collected by: Achim Zeileis). Package: **vcd**.

**HairEyeColor** Distribution of hair and eye color and gender in 592 statistics students. The gender information is artificial. Source: [Snee \(1974\)](#). Taken from: [Friendly \(2000\)](#). Package: **datasets** (included in base R).

**OvaryCancer** Data about a retrospective study of ovary cancer carried out in 1973. Information was obtained from 299 women, who were operated for ovary cancer 10 years before. Source: [Obel \(1975\)](#). Taken from: [Andersen \(1991\)](#). Package: **vcd**.

**PreSex** Data on pre- and extra-marital sex and divorce. Source: [Thornes and Collard \(1979\)](#). Taken from [Gilbert \(1981\)](#). Package: **vcd**.

**Titanic** Information on the fate of passengers on the fatal maiden voyage of the ocean liner “Titanic”, summarized according to economic status (class), gender (**Sex**), age and survival. Data originally collected by the British Board of Trade in their investigation of the sinking. Taken from: [Dawson \(1995\)](#). Package: **datasets** (included in base R).

**UCBAdmissions** Aggregate data on applicants to graduate school at Berkeley for the six largest departments in 1973 classified by admission and gender. Source: [Bickel, Hammel, and O’Connell \(1975\)](#). Taken from: [Friendly \(2000\)](#). Package: **datasets** (included in base R).

### Affiliation:

Firstname Lastname

Affiliation

Address, Country

E-mail: **name@address**

URL: **http://link/to/webpage/**