DECISION TREE CLASSIFICATION BASIC ALGORITHM

Classification Learning ALGORITHMS Different Classifiers

- DESCRIPTIVE:
- Decision Trees (ID3, C4.5)
- Rough Sets
- Genetic Algorithms
- Classification by Association
- STATISTICAL:
- Neural Networks
- Bayesian Networks

Classification Data

Data format: a data table with key attribute removed.
 Special attribute- class attribute must be distinguished

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

Classification (Training) Data with objects

rec	Age	Income	Student	Credit_rating	Buys_computer (CLASS)
r1	<=30	High	No	Fair	No
r2	<=30	High	No	Excellent	No
r3	3140	High	No	Fair	Yes
r4	>40	Medium	No	Fair	Yes
r5	>40	Low	Yes	Fair	Yes
r6	>40	Low	Yes	Excellent	No
r7	3140	Low	Yes	Excellent	Yes
r8	<=30	Medium	No	Fair	No
r9	<=30	Low	Yes	Fair	Yes
r10	>40	Medium	Yes	Fair	Yes
r11	<=30	Medium	Yes	Excellent	Yes
r12	3140	Medium	No	Excellent	Yes
r13	3140	High	Yes	Fair	Yes
r14	>40	Medium	No	Excellent	No

Classification by Decision Tree Induction

Decision tree is

A flow-chart-like tree structure;

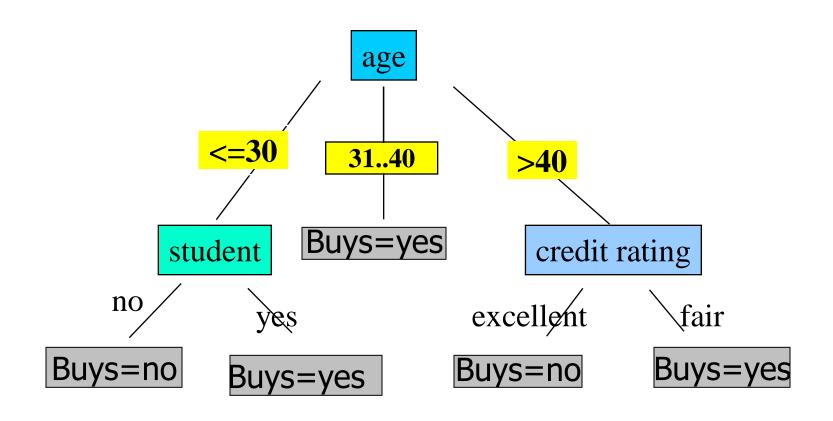
Internal node denotes an attribute;

Branch represents the values of the node attribute;

Leaf nodes represent class labels or class distribution

DECISION TREE

An Example



Classification by Decision Tree Induction Basic Algorithm

- The basic algorithm for decision tree construction
 is a greedy algorithm that constructs decision trees in a
 top-down recursive divide-and-conquer manner
- Given a training set D of classification data, i.e.
- a data table with a distinguished class attribute
- This training set is recursively partitioned into smaller subsets (data tables) as the tree is being built

Classification by Decision Tree Induction Basic Algorithm

- Tree STARTS as a single node (root) representing all training dataset D (samples)
- We choose a root attribute from D
- It is called a SPLIT attribute
- A branch is created for each value as defined in D of the node attribute and is labeled by its values and the samples (it means the data table) are partitioned accordingly
- The algorithm uses the same process recursively to form a decision tree at each partition
- Once an attribute has occurred at a node, it need not be considered in any other of the node's descendants

Classification by Decision Tree Induction Basic Algorithm

- The recursive partitioning STOPS only when any one of the following conditions is true
 - 1. All the samples (records) in the partition are of the same class, then the node becomes the leaf labeled with that class
- 2. There is no remaining attributes on which the data may be further partitioned, i.e. we have only class attribute left. In this case we apply MAJORITY VOTING to classify the node.

MAJORITY VOTING involves converting the node into a leaf and labeling it with the most common class in the training data set

3. There is no records (samples) left — a LEAF is created with majority vote for training data set

Classification by Decision Tree Induction

Crucial point

Good choice of the root attribute and internal nodes attributes is a crucial point

Bad choice may result, in the worst case in a just another knowledge representation:

a relational table re-written as a tree with class attributes (decision attributes) as the leaves.

 Decision Tree Algorithms differ on methods of evaluating and choosing the root and internal nodes attributes

Decision Tree Construction Example 1

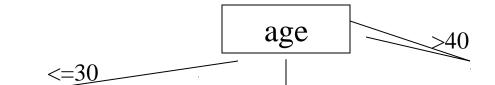
Consider our TRAING Dataset (next slide)

We START building the Decision Tree by choosing the attribute age as the root of the tree

Training Data with objects

rec	Age	Income	Student	Credit_rating	Buys_computer(CLASS)
r1	<=30	High	No	Fair	No
r2	<=30	High	No	Excellent	No
r3	3140	High	No	Fair	Yes
r4	>40	Medium	No	Fair	Yes
r5	>40	Low	Yes	Fair	Yes
r6	>40	Low	Yes	Excellent	No
r7	3140	Low	Yes	Excellent	Yes
r8	<=30	Medium	No	Fair	No
r9	<=30	Low	Yes	Fair	Yes
r10	>40	Medium	Yes	Fair	Yes
r11	<=30	Medium	Yes	Excellent	Yes
r12	3140	Medium	No	Excellent	Yes
r13	3140	High	Yes	Fair	Yes
r14	>40	Medium	No	Excellent	No

Building The Tree: we choose "age" as a root



income	student	credit	class
high	no	fair	no
high	no	excellent	no
medium	no	fair	no
low	yes	fair	yes
medium	yes	excellent	yes

income	student	credit	class
medium	no	fair	yes
low	yes	fair	yes
low	yes	excellent	no
medium	yes	fair	yes
medium	no	excellent	no

31...40

income	student	credit	class
high	no	fair	yes
low	yes	excellent	yes
medium	no	excellent	yes
high	yes	fair	yes

Building The Tree: "age" as the root



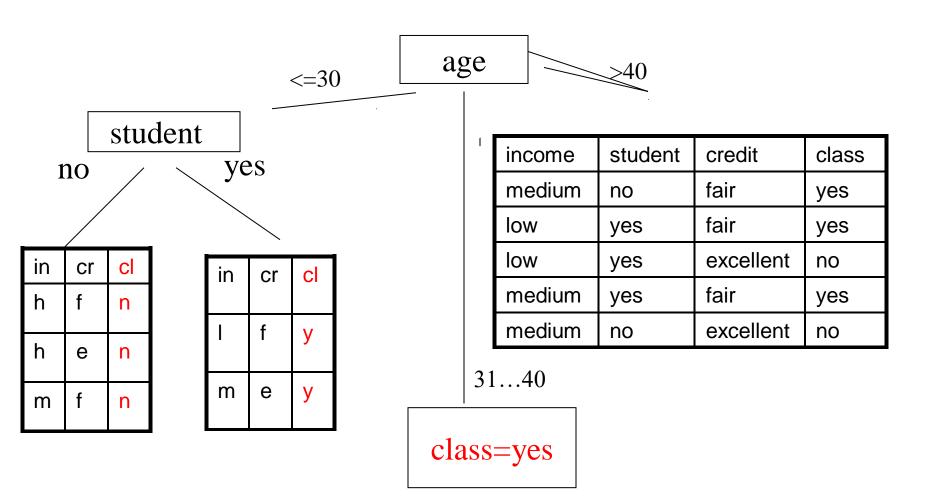
income	student	credit	class
high	no	fair	no
high	no	excellent	no
medium	no	fair	no
low	yes	fair	yes
medium	yes	excellent	yes

income	student	credit	class
medium	no	fair	yes
low	yes	fair	yes
low	yes	excellent	no
medium	yes	fair	yes
medium	no	excellent	no

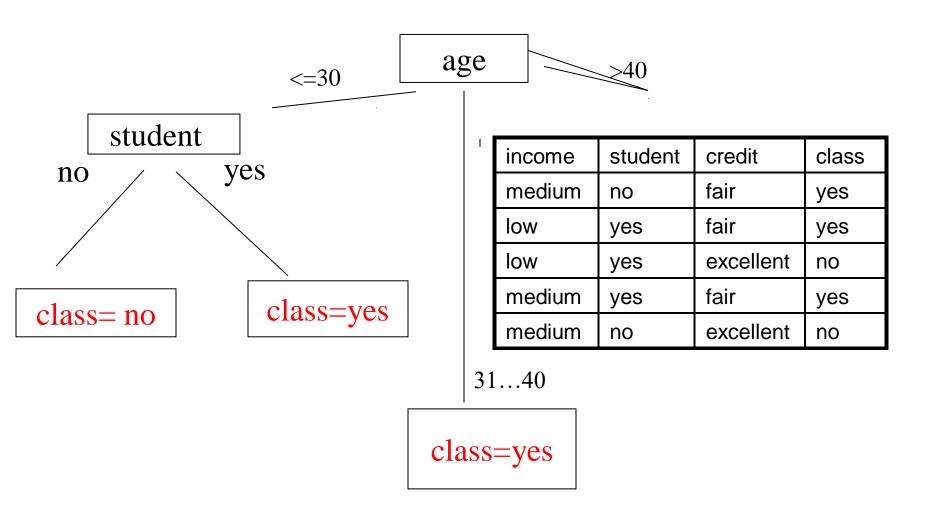
31...40

class=yes

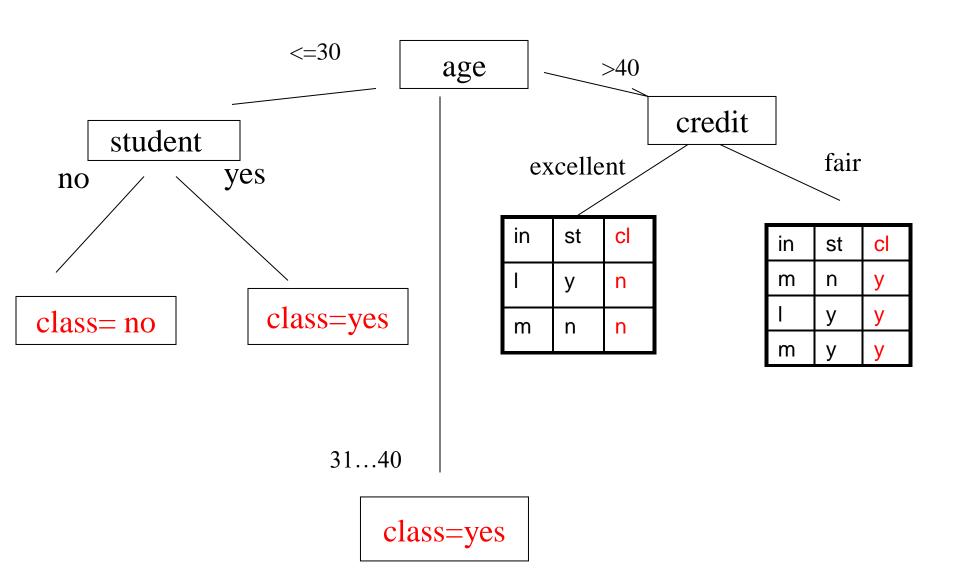
Building The Tree: we chose "student" on <=30 branch



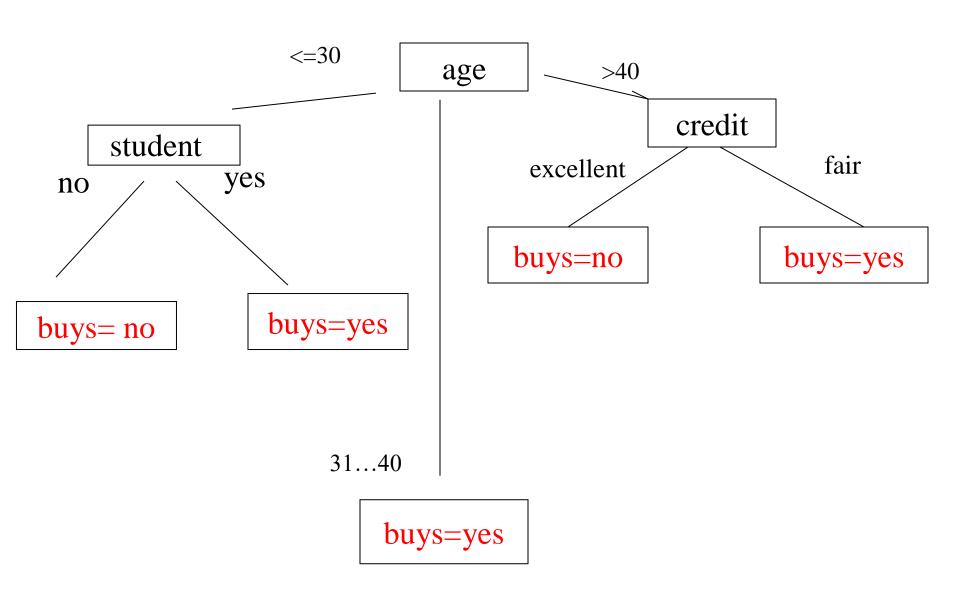
Building The Tree: we chose "student" on <=30 branch



Building The Tree: we chose "credit" on >40 branch



Finished Tree for class="buys"



Extracting Classification Rules from Trees

- Goal: Represent the knowledge in the form of
- IF-THEN determinant rules
- One rule is created for each path from the root to a leaf;
- Each attribute-value pair along a path forms a conjunction;
- The leaf node holds the class prediction
- Rules are easier to understand

Discriminant RULES extracted from our TREE

The rules are:

```
IF age = "<=30" AND student = "no" THEN
  buys_computer = "no"
IF age = "<=30" AND student = "yes" THEN
  buys_computer = "yes"
IF age = "31...40"
                                     THEN
  buys_computer = "yes"
IF age = ">40" AND credit_rating = "excellent" THEN
  buys_computer = "no"
IF age = ">40" AND credit_rating = "fair" THEN
  buys_computer = "yes"
```

Rules format for testing and applications

 In order to use rules for testing, and later when testing is done and predictive accuracy is acceptable we write rules in a predicate form:

```
IF age( x, <=30) AND student(x, no) THEN
buys_computer (x, no)
IF age(x, <=30) AND student (x, yes) THEN
buys_computer (x, yes)</pre>
```

• Attributes and their values of the new record x are matched with the IF part of the rule and the record x is classified accordingly to the THEN part of the rule

Exercise

Calculate the predictive accuracy of our set of rules with respect of the TEST data given by the next slide

```
R1: IF age = "<=30" AND student = "no" THEN
  buys_computer = "no"
R2: IF age = "<=30" AND student = "yes" THEN
  buys_computer = "yes"
R3: IF age = "31...40"
                                     THEN
  buys_computer = "yes"
R4: IF age = ">40" AND credit_rating = "excellent"
  THEN buys_computer = "no"
R5: IF age = ">40" AND credit_rating = "fair" THEN
  buys_computer = "yes"
```

TEST Data for predictive accuracy evaluation

rec	Age	Income	Student	Credit_rating	Buys_computer(CLASS)
r1	<=30	Low	No	Fair	yes
r2	<=30	High	yes	Excellent	No
r3	<=30	High	No	Fair	Yes
r4	3140	Medium	yes	Fair	Yes
r5	>40	Low	Yes	Fair	Yes
r6	>40	Low	Yes	Excellent	yes
r7	3140	High	Yes	Excellent	Yes
r8	<=30	Medium	No	Fair	No
r9	3140	Low	no	Excellent	Yes
r10	>40	Medium	Yes	Fair	Yes

Basic Idea of ID3/C4.5 Algorithm

- The basic algorithm for decision tree induction is a greedy algorithm that constructs decision trees in a top-down recursive divide-and – conquer manner.
- The basic strategy is as follows.
- Tree STARTS as a single node representing all training dataset (data table with records called samples)
- IF the samples (records in the data table) are all in the same class, THEN the node becomes a leaf and is labeled with that class

Basic Idea of ID3/C4.5 Algorithm

- OTHERWISE
- the algorithm uses an entropy-based measure known as information gain as a heuristic for selecting the attribute that will best separate the samples: split the data table into individual classes
- This attribute becomes the node-name:
 test, or tree split decision attribute
- A branch is created for each value of the node-attribute (as defined by the training data)
 and is labeled by this value
 and the samples (data table at the node) are partitioned
 accordingly

Basic Idea of ID3/C4.5 Algorithm Revisisted

- The algorithm uses the same process recursively
- to form a decision tree at each partition
- Once an attribute has occurred at a node, it need not be considered in any other of the node's descendants

 The recursive partitioning STOPS only when any one of the following conditions is TRUE

Basic Idea of ID3/C4.5 Algorithm

Termination conditions:

1. All records (samples) for the given node belong to the same class

OR

2. There are no remaining attributes left on which the samples (records in the data table) may be further partitioned

In this case we **convert** the given node into a **LEAF** and **label** it with the **class** in **majority** among **original training samples**

- This is called a majority voting
- •OR
- 3. There is no records (samples) left a LEAF is created with majority vote for training sample

Heuristics: Attribute Selection Measures

- Construction of the tree depends on the order in which root attributes are selected
- Different choices produce different trees;
 some better, some worse
- Shallower trees are better;
 they are the ones in which classification is reached in fewer levels
- These trees are said to be more efficient and hence termination is reached quickly

Attribute Selection Measures

- Given a training data set (set of training samples)
 there are many ways to choose the root and nodes
 attributes while constructing the decision tree
- Some possible choices:
- Random
- Attribute with smallest/largest number of values
- Following certain order of attributes
- We present here a special order: information gain as a measure of goodness of the split
- The attribute with the highest information gain is always chosen as the split decision attribute for the current node while building the tree.

Information Gain Computation (ID3/C4.5): Case of Two Classes

Assume there are two classes, P (positive) and N (negative)

Let S be a training data set consisting of s examples (records):

$$|S|=s$$

And S contains p elements of class P and n elements of class N

The amount of information, needed to **decide** if an arbitrary example in S belongs to P or N is defined as

$$I(p,n) = -\frac{p}{p+n}\log_2\frac{p}{p+n} - \frac{n}{p+n}\log_2\frac{n}{p+n}$$

We use log_2 because the information is encoded in bits

Information Gain Measure

• Assume that using **attribute** A a set S will be partitioned into sets S_1 , S_2 , ..., S_v (v is number of values of the attribute A)

If S_i contains p_i examples of P and n_i examples of N

the entropy E(A), or the expected information needed to classify objects in all sub-trees S_i is

$$E(A) = \sum_{i=1}^{\nu} \frac{p_i + n_i}{p+n} I(p, n)$$

• The encoding information that would be gained by branching on A Gain(A) = I(p,n) - E(A)

Attribute Selection: Information Gain

Data Mining Book slide

$$Info(D) = I(9,5) = -\frac{9}{14} \log_{2}(\frac{9}{14}) - \frac{5}{14} \log_{2}(\frac{5}{14}) = 0.940$$

age	рi	ni	I(p _i , n _i)
<=30	2	3	0.971
3140	4	0	0
>40	3	2	0.971

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

"yes"

Class N: buys_computer = "no"

$$Info_{age}(D) = \frac{5}{14}I(2,3) + \frac{4}{14}I(4,0)$$
 $Info(D) = I(9,5) = -\frac{9}{14}\log_{\frac{9}{14}}(\frac{9}{14}) - \frac{5}{14}\log_{\frac{9}{2}}(\frac{5}{14}) = 0.940$
 $+\frac{5}{14}I(3,2) = 0.694$

$$\frac{5}{14}I(2,3)$$
 means "age <=30" has 5 out of 14 samples, with 2 yes' es and 3 no's. Hence

$$Gain(age) = Info(D) - Info_{age}(D) = 0.246$$

Similarly,

$$Gain(income) = 0.029$$

 $Gain(student) = 0.151$
 $Gain(credit_rating) = 0.048$

Attribute Selection by Information Gain Computation

- Class P: buys_computer = "yes"
- Class N: buys_computer = "no"
- \blacksquare I(p, n) = I(9, 5) = 0.940
- Compute the entropy for

age	рi	ni	I(p _i , n _i)
<=30	2	3	0.971
3140	4	0	0
>40	3	2	0.971

$$E(age) = \frac{5}{14}I(2,3) + \frac{4}{14}I(4,0) + \frac{5}{14}I(3,2) = 0.694$$

Hence

$$Gain(age) = I(p, n) - E(age)$$

Gain(age)=0.246

Similarly

Gain(income) = 0.029

Gain(student) = 0.151

 $Gain(credit_rating) = 0.048$

The attribute "age" becomes the root.

Decision Tree Induction, Predictive Accuracy and Information Gain

EXAMPLES

Decision Tree Construction Example 2

TASK: Use Decision Tree Induction algorithm and use different choices of the root and nodes attributes to FIND discriminant rules that determine whether a person buys a computer or not

Compute **Information gain** for all nodes of the tree.

- We choose attribute buys_computer as the class attribute
- 2. We perform DT algorithm "by hand" using different choices of the root attribute, and different "by hand" choices of the following nodes
- We build two trees with attributes: Income and Credit Rating respectively, as the root attribute to derive rules

Training Data

age	income	student	credit_rating	buys_computer
<=30	high	no	fair	no
<=30	high	no	excellent	no
3140	high	no	fair	yes
>40	medium	no	fair	yes
>40	low	yes	fair	yes
>40	low	yes	excellent	no
3140	low	yes	excellent	yes
<=30	medium	no	fair	no
<=30	low	yes	fair	yes
>40	medium	yes	fair	yes
<=30	medium	yes	excellent	yes
3140	medium	no	excellent	yes
3140	high	yes	fair	yes
>40	medium	no	excellent	no

Training Data with objects

rec	Age	Income	Student	Credit_rating	Buys_computer
r1	<=30	High	No	Fair	No
r2	<=30	High	No	Excellent	No
r3	3140	High	No	Fair	Yes
r4	>40	Medium	No	Fair	Yes
r5	>40	Low	Yes	Fair	Yes
r6	>40	Low	Yes	Excellent	No
r7	3140	Low	Yes	Excellent	Yes
r8	<=30	Medium	No	Fair	No
r9	<=30	Low	Yes	Fair	Yes
r10	>40	Medium	Yes	Fair	Yes
r11	<=30	Medium	Yes	Excellent	Yes
r12	3140	Medium	No	Excellent	Yes
r13	3140	High	Yes	Fair	Yes
r14	>40	Medium	No	Excellent	No

EXAMPLE 2 Incorrect Solutions

- BOTH TREES of the following Example 2 Solutions
 ARE NOT CORRECT !!!
- FIND STEPS where the construction didn't follow the ALGORITHM and CORRECT THEM
- Write the CORRECT Solutions for the EXAMPLE 2
- Perform Exercises 1 and 2 for the corrected trees



Low



Gain=0.027

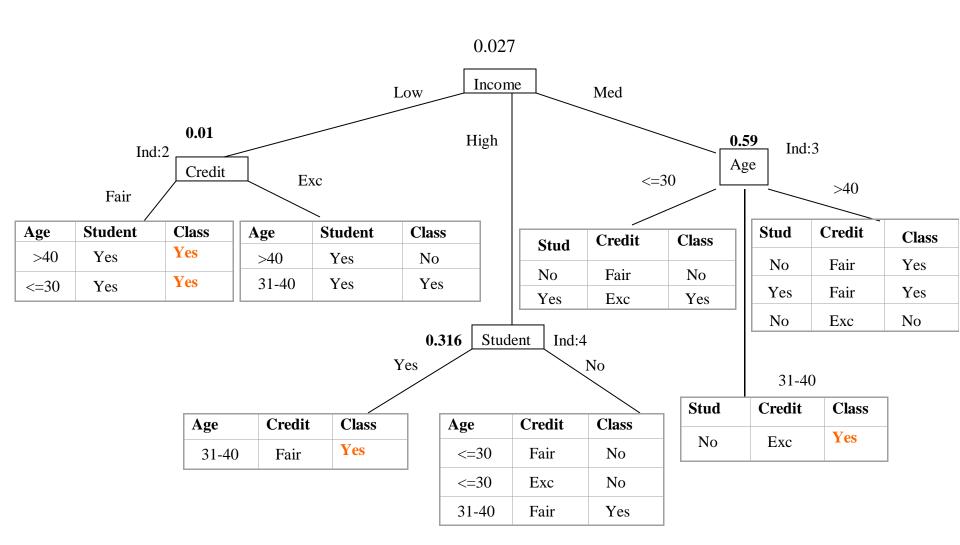
Med

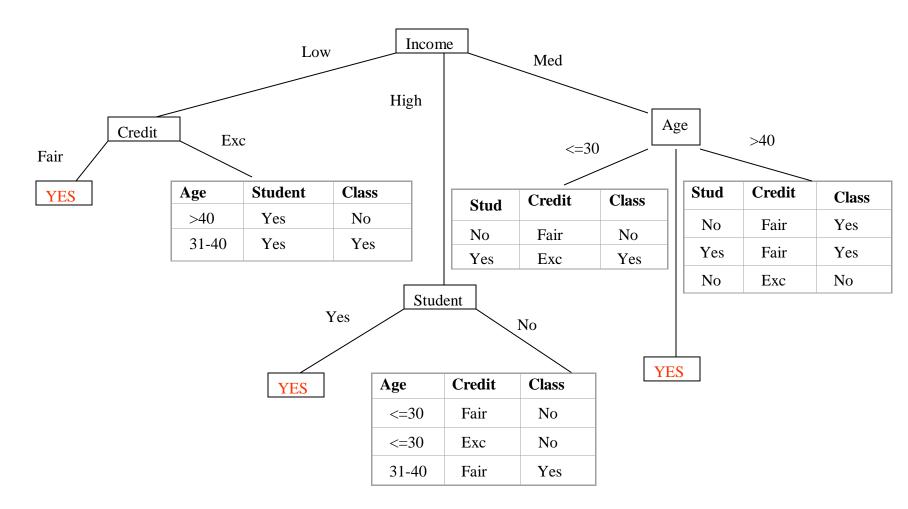
High

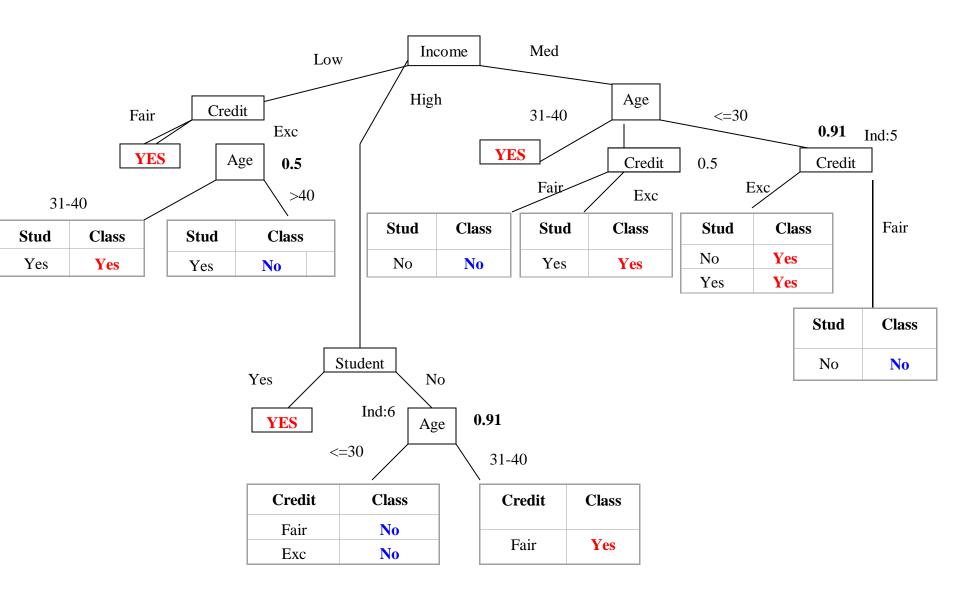
Age	Student	Credit	Class
>40	Yes	Fair	Yes
>40	Yes	Exc	No
31-40	Yes	Exc	Yes
<=30	Yes	Fair	Yes

Age	Student	Credit	Class
>40	No	Fair	Yes
<=30	No	Fair	No
>40	Yes	Fair	Yes
<=30	Yes	Exc	Yes
31-40	No	Exc	Yes
>40	No	Exc	No

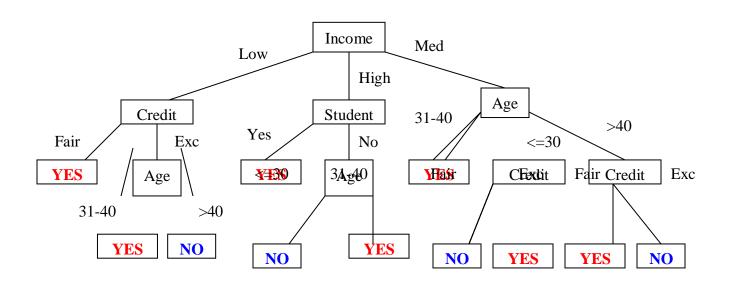
Age	Student	Credit	Class
<=30	No	Fair	No
<=30	No	Exc	No
31-40	No	Fair	Yes
31-40	Yes	Fair	Yes







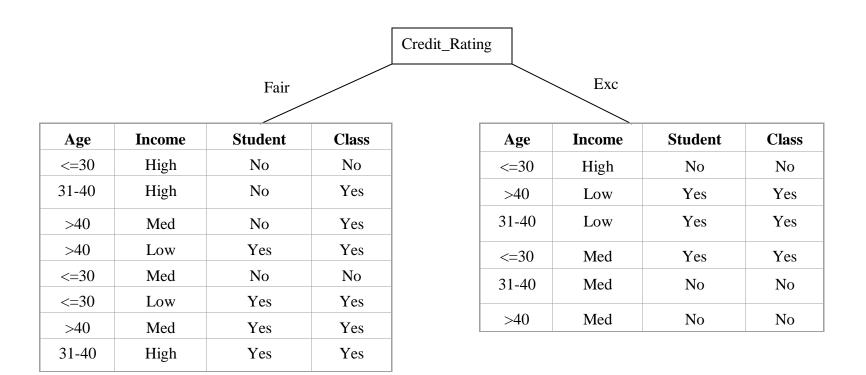
Tree 1 with root attribute Income

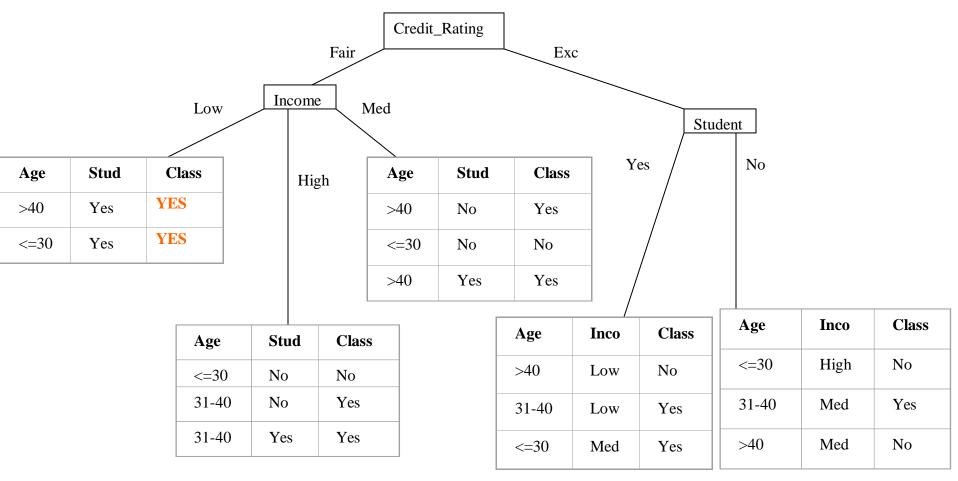


Rules derived from tree 1 (predicate form for testing)

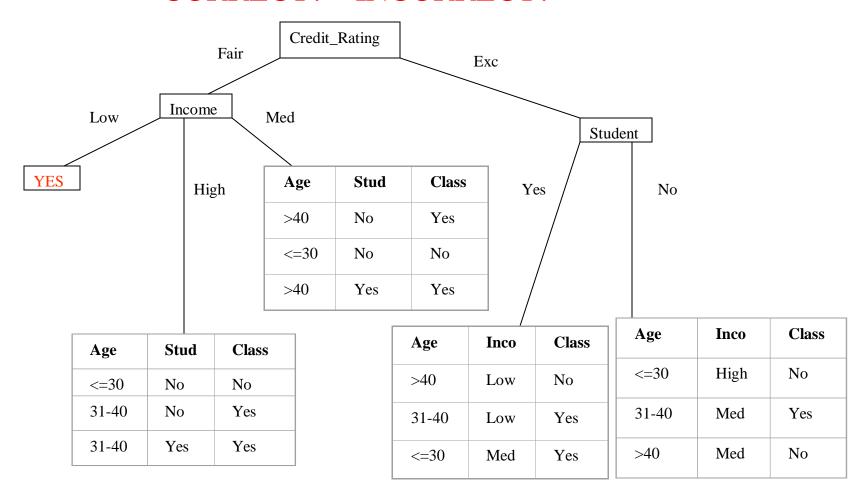
- 1. Income(x, Low) ^ Credit(x, Fair) -> buysComputer(x, Yes).
- 2. Income(x, Low) $^{\land}$ Credit(x, Exc) $^{\land}$ Age(x, 31-40) -> buysComputer(x, Yes).
- 3. Income(x, Low) $^{\land}$ Credit(x, Exc) $^{\land}$ Age(>40) -> buysComputer(x, No).
- 4. Incomex, (High) $^{\land}$ Student(x, Yes) -> buysComputer(x, Yes).
- 5. Income(x, High) $^{\land}$ Student(x, No) $^{\land}$ Agex(x, <=30) -> buysComputer(x, No).
- 6. Income(x, High) $^{\land}$ Student(x, No) $^{\land}$ Age(x, 31-40) -> buysComputer(x, Yes).
- 7. Income(x, Medium) A Age(x, 31-40) -> buysComputer(x, Yes).
- 8. Income(x, Medium) A Age(x, <=30) C Credit(x, Fair) -> buysComputer(x, No).
- 9. Income(x, Medium) A Age(x, <=30) C Credit(x, Exc) -> buysComputer(x, Yes).
- 10. Income(x, Medium) A Age(x, >40) A Credit(x, Fair) -> buysComputer(x, Yes).
- 11. Income(x, Medium) A Age(x, >40) A Credit(x, Exc) -> buysComputer(x, No).

Tree 2 with root attribute Credit Rating

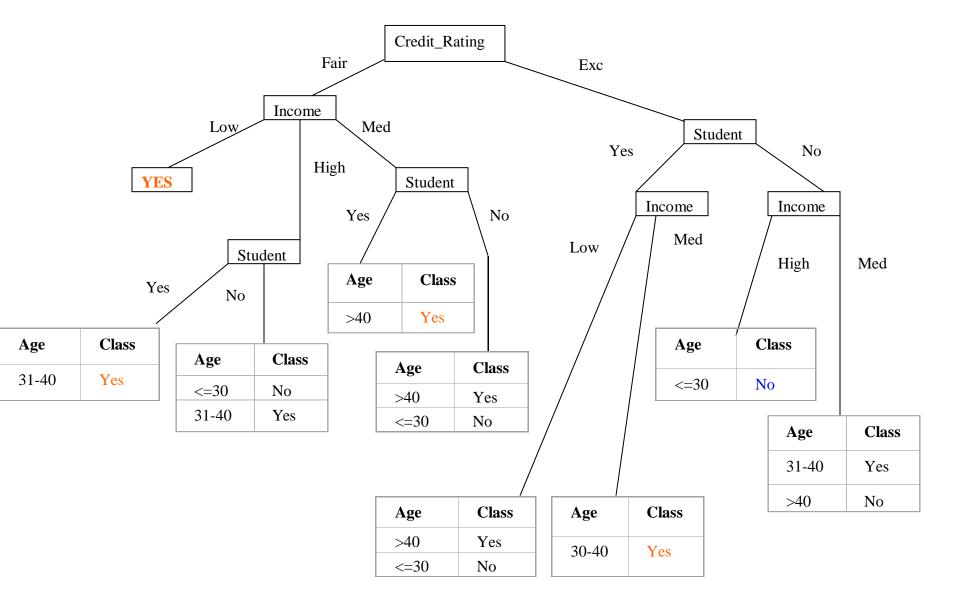




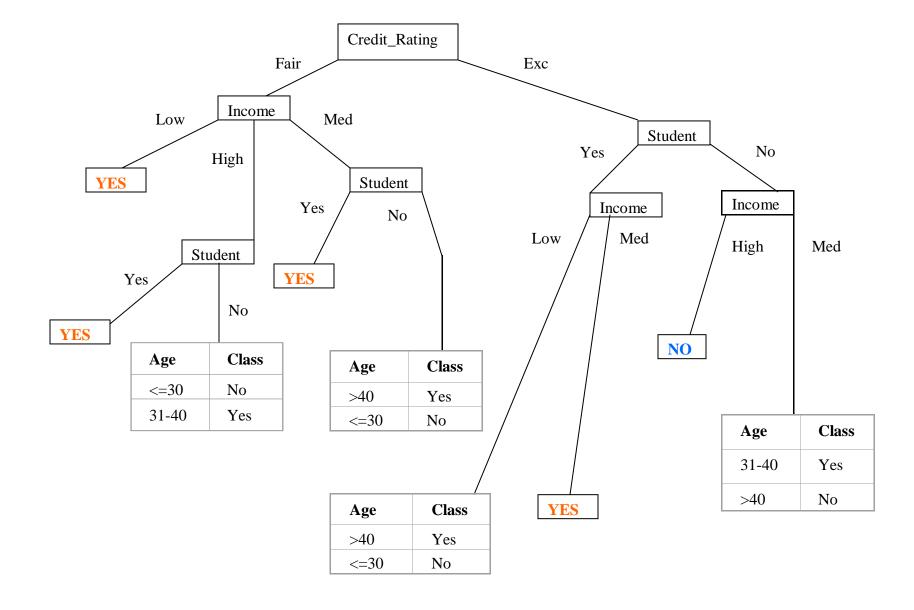
Tree 2 with next level attributes Income and Student

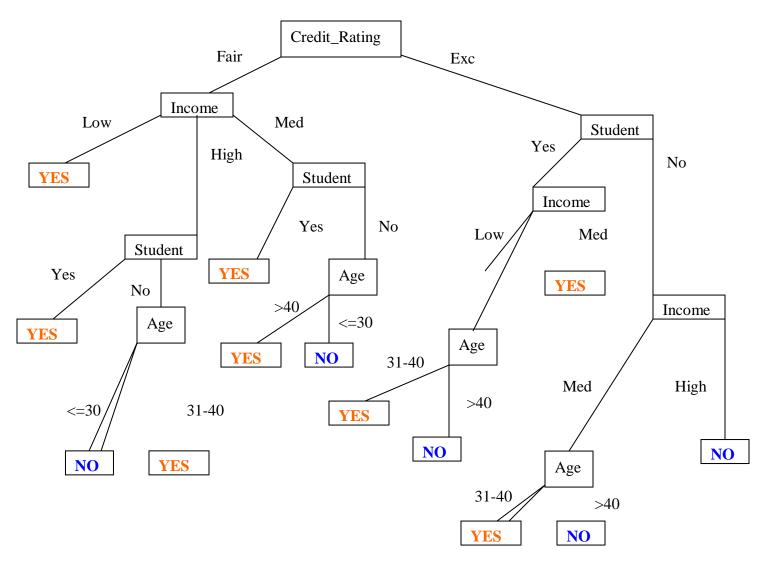


Tree 2 with root attribute Credit Rating



CORRECT? – INCORRECT?





Final Tree 2 with root attribute Credit Rating

The Decision tree with root attribute *Credit_Rating* has produced 13 rules, two more than with root attribute *Income*

- 1. Credit(x, Fair) $^{\land}$ Income(x,Low) -> buysComp(x,Yes).
- 2. Credit(x,Fair) $^{\land}$ Income(x, High) $^{\land}$ Student(x,Yes) -> buysComp(x, Yes).
- 3. Credit(x,Fair) $^{\land}$ Income(x, High) $^{\land}$ Student(x, No) $^{\land}$ Age(<=30) -> buysComp(x, No).
- 4. Credit(x,Fair) $^{\land}$ Income(x, High) $^{\land}$ Student(x, No) $^{\land}$ Age(31-40) -> buysComp(x, Yes).
- 5. Credit(x, Fair) $^{\land}$ Income(x, Med) $^{\land}$ Student(x, Yes) -> buysComp(x, Yes).
- 6. Credit(x, Fair) $^{\land}$ Income(x, Med) $^{\land}$ Student(x, No) $^{\land}$ Age(>40) -> buysComp(x, Yes).
- 7. Credit(x, Fair) $^{\land}$ Income(x, Med) $^{\land}$ Student(x, No) $^{\land}$ Age(<=30) -> buysComp(x, No).
- 8. Credit(x, Exc) $^{\land}$ Student(x, Yes) $^{\land}$ Income(x, Low) $^{\land}$ Age(31-40) -> buysComp(x, Yes).
- 9. Credit(x, Exc) $^{\land}$ Student(x, Yes) $^{\land}$ Income(x, Low) $^{\land}$ Age(>40) -> buysComp(x, No).
- 10. Credit(x, Exc) $^{\land}$ Student(x, Yes) $^{\land}$ Income(x, Med) -> buysComp(x, Yes).
- 11. Credit(x, Exc) $^{\land}$ Student(x, No) $^{\land}$ Income(x, Med) $^{\land}$ Age(x, 31-40) $^{\rightarrow}$ buysComp(x, Yes).
- 12. Credit(x, Exc) $^{\land}$ Student(x, No) $^{\land}$ Income(x, Med) $^{\land}$ Age(x, >40) -> buysComp(x, No).
- 13. Credit(x, Exc) $^{\land}$ Student(x, No) $^{\land}$ Income(x, High) -> buysComp(x, No).

EXERCISE 1

 We use some random records (tuples) to calculate the Predictive Accuracy of the set of rules from the Example 2

Predictive Accuracy is the % of well classified records not from training set for which the class attribute is known

Random Tuples to Check Predictive Accuracy based on three sets of rules

Obj	Age	Income	Student	Credit_R	Class
1	<=30	High	Yes	Fair	Yes
2	31-40	Low	No	Fair	Yes
3	31-40	High	Yes	Exc	No
4	>40	Low	Yes	Fair	Yes
5	>40	Low	Yes	Exc	No
6	<=30	Low	No	Fair	No

Predictive accuracy:

- 1. Against Lecture Notes: 4/6 = 66.66%
- 2. Against Tree 1 rules with root att. *Income*: 3/6 = 50%
- 3. Against Tree 2 rules with root att. *Credit*: 5/6 = 83.33%

EXERCISE 2

- Predictive accuracy depends heavily on a choice of the test and training data.
- Find a small set of TEST records such that they would give a predictive accuracy 100% for rules From the Lecture Tree and Trees 1 and 2 from Example 1

1. <u>TEST DATA applied against rules in Lecture Notes</u> that gives predictive accuracy 100%

No	Age	Income	Student	Credit_R	Class
1	<=30	Med	No	Exc	No
2	<=30	High	Yes	Fair	Yes
3	31-40	Low	No	Exc	Yes
4	>40	High	Yes	Exc	No
5	<=30	Low	No	Fair	Yes
6	31-40	High	Yes	Fair	Yes

2. TEST DATA that applied against the rules with root attribute *Income* give predictive accuracy 100%

No	Age	Income	Student	Credit_R	Class
1	31-40	Low	Yes	Fair	Yes
2	>40	Low	No	Exc	No
3	<=30	High	Yes	Fair	Yes
4	31-40	High	No	Exc	Yes
5	31-40	Med	No	Fair	Yes
6	>40	Med	Yes	Exc	No

3.TEST DATA that applied against the rules with root attribute *Credit Rating* **gives predictive accuracy 100%**

No	Age	Income	Student	Credit_R	Class
1	31-40	Low	No	Fair	Yes
2	<=30	High	Yes	Fair	Yes
3	<=30	Med	No	Fair	No
4	31-40	High	Yes	Exc	Yes
5	>40	Med	Yes	Exc	No
6	>40	Med	No	Exc	No

Exercise 2 Corrections

We **FIXED** the following two points of the **Tree construction:**

- We choose recursively internal nodes (attributes)
 with all of their values in TRAINING set as branches
 Mistake: NOT ALL attributes values were always
 used
- 2. there is no more samples (records) left In this case we apply Majority Voting to classify the node, where the

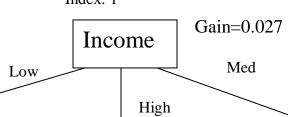
Majority Voting involves converting the node into a leaf and labeling it with the most common class in the training set

3. There is no more attributes (non-class) leftapply Majority Voting

Mistake: NO MAJORITY Voting was used

CORRECT



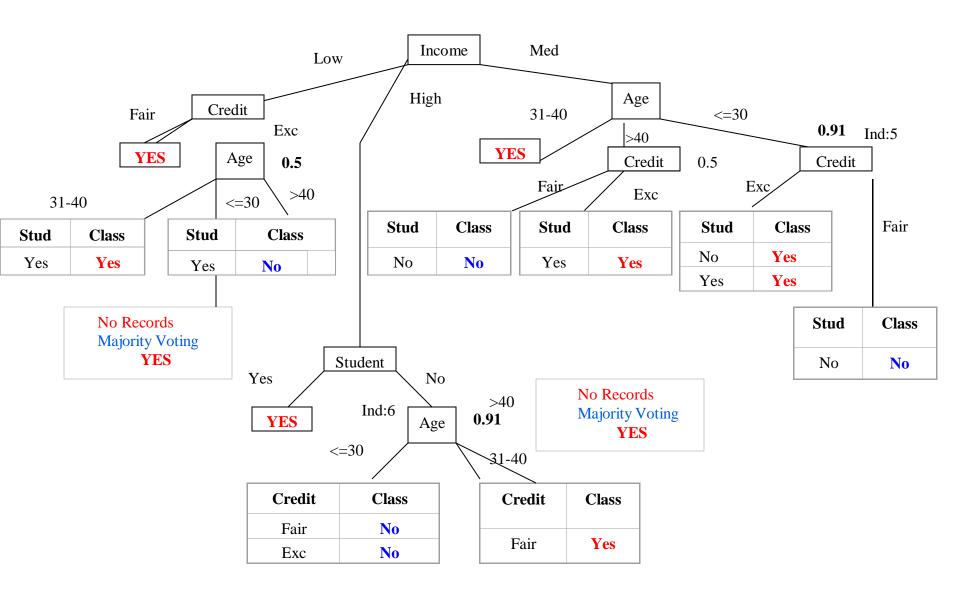


Age	Student	Credit	Class
>40	Yes	Fair	Yes
>40	Yes	Exc	No
31-40	Yes	Exc	Yes
<=30	Yes	Fair	Yes

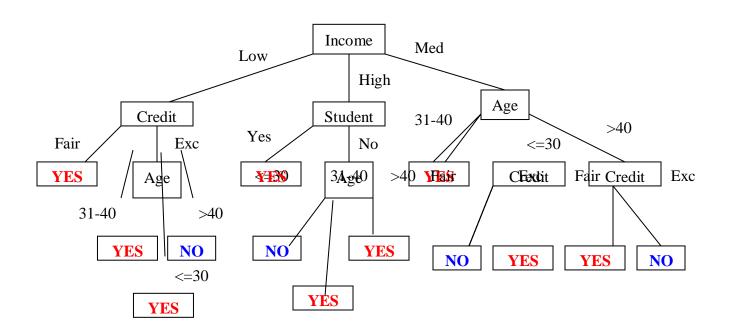
Age	Student	Credit	Class			
>40	No	Fair	Yes			
<=30	No	Fair	No			
>40	Yes	Fair	Yes			
<=30	Yes	Exc	Yes			
31-40	No	Exc	Yes			
>40	No	Exc	No			

Age	Student	Credit	Class
<=30	No	Fair	No
<=30	No	Exc	No
31-40	No	Fair	Yes
31-40	Yes	Fair	Yes

CORRECTED



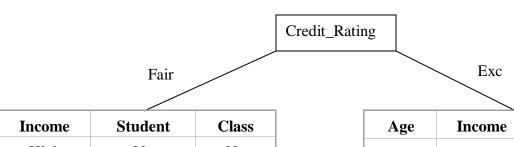
CORRECT Tree 1 with root attribute Income



Rules derived from Tree 1 (predicate form for testing)

- 1. Income(x, Low) ^ Credit(x, Fair) -> buysComputer(x, Yes).
- 2. Income(x, Low) $^{\land}$ Credit(x, Exc) $^{\land}$ Age(x, 31-40) -> buysComputer(x, Yes).
- 3. Income(x, Low) $^{\land}$ Credit(x, Exc) $^{\land}$ Age(>40) -> buysComputer(x, No).
- 4. Incomex, (High) $^{\land}$ Student(x, Yes) -> buysComputer(x, Yes).
- 5. Income(x, High) $^{\land}$ Student(x, No) $^{\land}$ Age(x, <=30) -> buysComputer(x, No).
- 6. Income(x, High) $^{\land}$ Student(x, No) $^{\land}$ Age(x, 31-40) -> buysComputer(x, Yes).
- 7. Income(x, Medium) A Age(x, 31-40) -> buysComputer(x, Yes).
- 8. Income(x, Medium) A Age(x, <=30) C Credit(x, Fair) -> buysComputer(x, No).
- 9. Income(x, Medium) A Age(x, <=30) C Credit(x, Exc) -> buysComputer(x, Yes).
- 10. Income(x, Medium) A Age(x, >40) A Credit(x, Fair) -> buysComputer(x, Yes).
- 11. Income(x, Medium) A Age(x, >40) A Credit(x, Exc) -> buysComputer(x, No).
- 12. Income(x, Low) A Age(x, <=30) C Credit(x, Exc) -> buysComputer(x, Yes). Majority Voting
- 13. Income(x, High) ^ Student(x, No) ^ Age(x>40) -> buysComputer(x, Yes). Majority Voting

Tree 2 with root attribute Credit Rating



Age	Income	Student	Class
<=30	High	No	No
31-40	High	No	Yes
>40	Med	No	Yes
>40	Low	Yes	Yes
<=30	Med	No	No
<=30	Low	Yes	Yes
>40	Med	Yes	Yes
31-40	High	Yes	Yes

Age	Income	Student	Class
<=30	High	No	No
>40	Low	Yes	Yes
31-40	Low	Yes	Yes
<=30	Med	Yes	Yes
31-40	Med	No	No
>40	Med	No	No

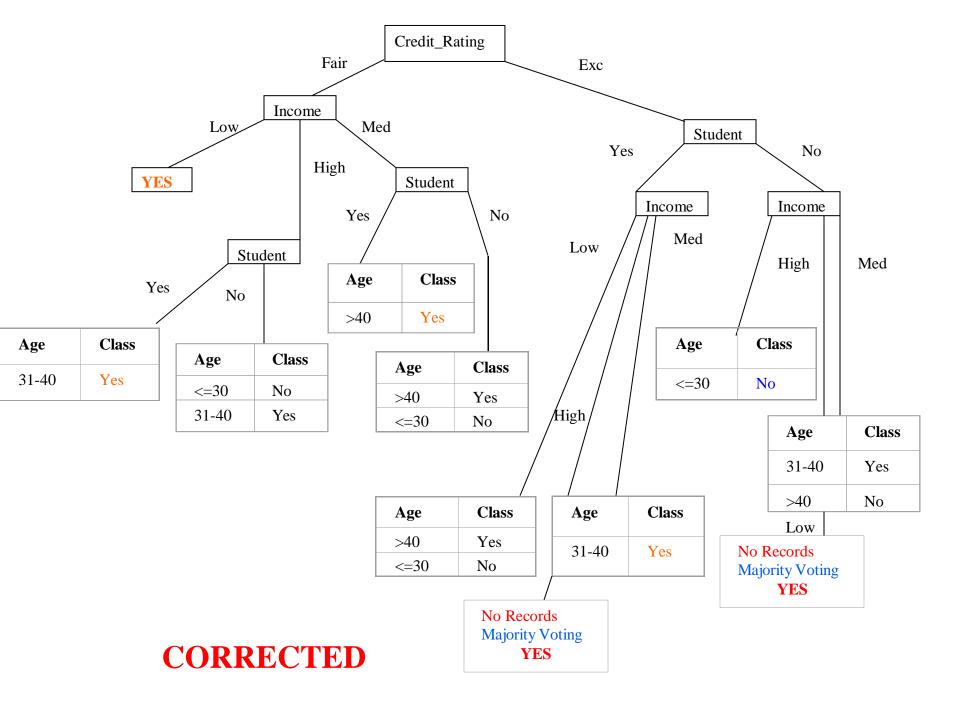
CORRECT

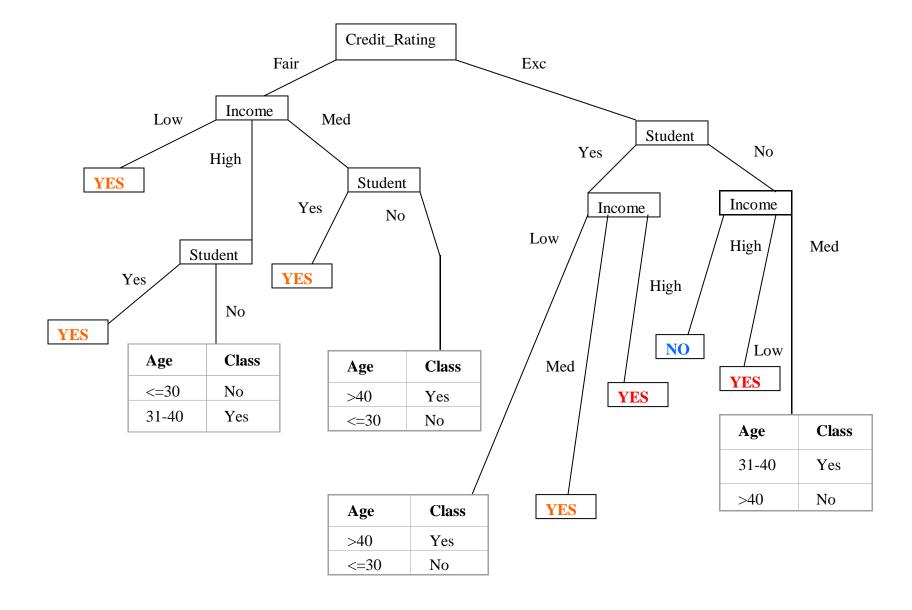
CORRECT Credit_Rating Fair Exc Income Med Low Student Yes No Class Stud Class Age Stud Age High **YES** >40 Yes >40 Yes No **YES** <=30 Yes <=30 No No >40 Yes Yes Class Age Inco Inco Class Age Class Stud Age <=30 High No >40 Low No <=30 No No 31-40 No Yes 31-40 Med Yes 31-40 Low Yes 31-40 Yes Yes >40 Med No <=30 Med Yes

Tree 2 with next level attributes Income and Student

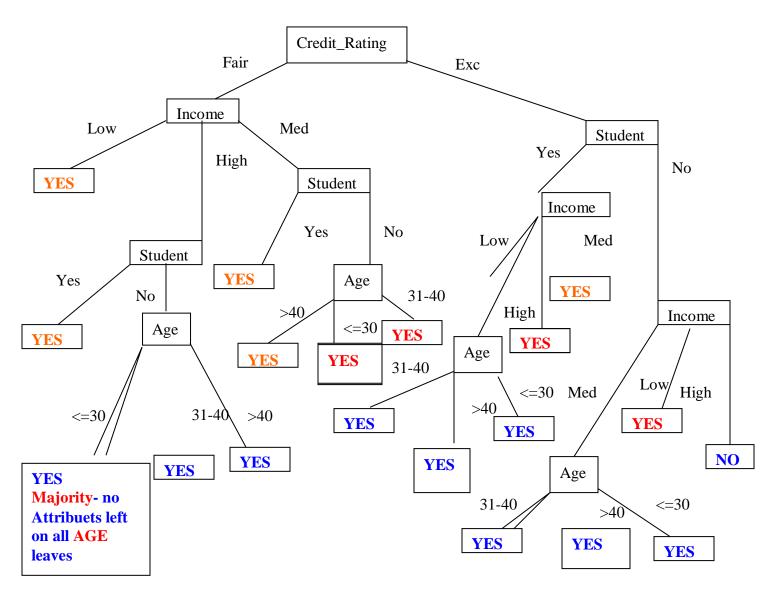
CORRECT Credit_Rating Fair Exc Income Med Low Student YES Stud Class Age High Yes No >40 No Yes <=30 No No >40 Yes Yes Inco Class Age Inco Class Age Stud Class Age <=30 No High >40 Low No No <=30 No 31-40 No Yes 31-40 Med Yes 31-40 Low Yes 31-40 Yes Yes >40 Med No <=30 Med Yes

Tree 2 with root attribute Credit Rating





CORRECTED



CORRECTED Tree 2 – IS IT CORRECT???

Random Tuples to Check Predictive Accuracy based on three sets of rules

Obj	Age	Income	Student	Credit_R	Class
1	<=30	High	Yes	Fair	Yes
2	31-40	Low	No	Fair	Yes
3	31-40	High	Yes	Exc	No
4	>40	Low	Yes	Fair	Yes
5	>40	Low	Yes	Exc	No
6	<=30	Low	No	Fair	No

Predictive accuracy:

- 1. Against Lecture Notes: 4/6 = 66.66%
- 2. Against **Tree 1** rules with root att. *Income*: 3/6 = 50%
- 3. Against **Tree 2** rules with root att. *Credit*: 4/6 = 66.66%
- 4. Against OLD Tree 2 rules with root att. Credit: 5/6 = 83.33%

Calculation of Information gain at each level of tree with root attribute *Income*

1. Original Table:

Class P: buys_computer = yes; Class N: buys_computer = No

$$I(P,N) = -P/P + N \log_2 (P/P+N) - N/P + N \log_2 N/P + N - - - - (equation 1)$$

$$I(P,N) = I(9,5) = (-9/9+5) \log_2 (9/9+5) - (5/9+5) \log_2 (5/9+5)$$

$$= 0.940$$

2. <u>Index:1</u>

Income	Pi	Ni	I(Pi,Ni)
Low	3	1	0.8111
Med	4	2	0.9234
High	2	2	1

E(Income) =
$$4/14$$
 I(3,1) + $6/14$ I(4,2) + $4/14$ I(2,2) ------(eq.2)
I(3,1) = 0.8111 (Using equation 1)
I(4,2) = 0.9234 (Using equation 1)
I(2,2) = 1 Contd.....

Information gain calculation for Index 1 contd:

Substituting the values in eq.2 we get, E(Income) = 0.2317 + 0.3957 + 0.2857 = 0.9131 Gain (Income) = I(P,N) - E(Income)= 0.940 - 0.9131 = 0.027

2. Index 2

Credit	Pi	Ni	I(Pi,Ni)
Fair	2	1	0.913
Exc	2	1	0.913

$$I(P,N) = I(4,2) = 0.9234$$
 (Using equation 1)
 $E(Credit) = 3/6 I(2,1) + 3/6 I(2,1)$ ----- (3)
 $I(2,1) = 0.913$ (Using equation 1)
 $E(Credit) = 0.913$ (Substituting value of $I(2,1)$ in (3)
 $Gain(Credit) = I(P,N) - E(Credit) = 0.9234 - 0.913$
 $= 0.01$

Similarly we can calculate Information gain of tables at each stage.