

$$\lambda_1 = -22,125$$

$$\begin{bmatrix} 4-\lambda & 8 & -2 & -2 \\ -2 & -\lambda-9 & -2 & -4 \\ 0 & 10 & 5-\lambda & -10 \\ -2 & -13 & -14 & -\lambda-13 \end{bmatrix}$$

$$= \begin{bmatrix} 25,125 & 8 & -2 & -2 \\ -2 & 12,125 & -2 & -4 \\ 0 & 10 & 26,125 & -10 \\ -1 & 13 & -14 & 8,125 \end{bmatrix} \rightarrow B$$

$$\text{Note: } 4-\lambda = 4-(-22,125) = 25,125$$

$$-\lambda-9 = -(-22,125)-9 = 12,125$$

$$5-\lambda = 5-(-22,125) = 26,125$$

$$-\lambda-13 = -(-22,125)-13 = 8,125$$

Solve:  $B\bar{x} = \bar{0}$

$$= \begin{bmatrix} 25,125 & 8 & -2 & -2 \\ -2 & 12,125 & -2 & -4 \\ 0 & 10 & 26,125 & -10 \\ -1 & 13 & -14 & 8,125 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

$$= \left[ \begin{array}{cccc|c} 25,125 & 8 & -2 & -2 & 0 \\ -2 & 12,125 & -2 & -4 & 0 \\ 0 & 10 & 26,125 & -10 & 0 \\ -1 & 13 & -14 & 8,125 & 0 \end{array} \right] \begin{array}{l} R_2 \rightarrow R_2 - 0,0796R_1 \\ R_3 \rightarrow R_3 + R_1 \\ R_4 \rightarrow R_4 - 0,054R_2 \end{array}$$

If we continue with the Gaussian elimination

it gives  $(x, y, z, w) = (0, 0, 0, 0)$ , which isn't possible  
for a non-zero vector so in calculator the null space

of this vector is  $\begin{bmatrix} -0,077 \\ 0,365 \\ 0,743 \\ 1 \end{bmatrix}$  = eigenvector.

$$\text{Importance}(\lambda_i) = \frac{|\lambda_i|}{\sum_{j=1}^n |\lambda_j|} \times 100\%$$

$$|\lambda_1| + |\lambda_2| + |\lambda_3| + |\lambda_4|$$

$$= 11.054 + 2.675 + 22.125 + 5.604$$

$$= \underline{40.458} \quad \because \text{they are all positive because}$$

of the absolute value

$$\lambda_1 = 11.054 \rightarrow \frac{11.054}{40.458} \times 100 = \underline{27.32\%}$$

$$\lambda_2 = 2.675 \rightarrow \frac{2.675}{40.458} \times 100 = \underline{6.62\%}$$

$$\lambda_3 = -22.125 \rightarrow \frac{22.125}{40.458} \times 100 = \underline{52.21\%}$$

$$\lambda_4 = -5.604 \rightarrow \frac{5.604}{40.458} \times 100 = \underline{13.85\%}$$

$\therefore \lambda_3 = -22.125$  accounts for over 52%  
because of this we are more likely to focus  
on the direction of  $\lambda_3$  in how the matrix acts.