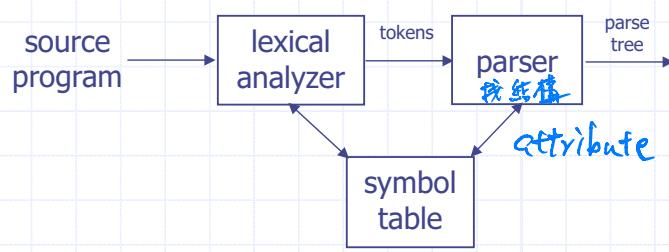


編譯器設計

Chapter 3: Lexical Analysis

Lexical Analysis

- ◆ The role of the lexical analyzer
 - To read the input characters
 - To produce a sequence of tokens



- ◆ Reasons to separate lexical analysis

- Simpler design is the most import consideration
- Compiler efficiency is improved
- Compiler portability is enhanced

$a = b + c$
↓
lexical
 $id = id + id$
↓
 $\langle \text{statement} \rangle$
↓
 $\langle \text{if} \rangle = \langle \text{expr} \rangle$
↓
 $\langle \text{expr} \rangle + \langle \text{expr} \rangle$
↓
 $\langle \text{id} \rangle$
↓
 $\langle \text{id} \rangle$

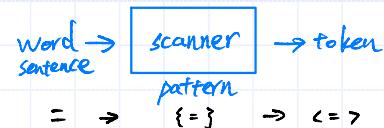
parser recognize tokens
⇒ too complicate

pascal, C++
parser 都一樣

Tokens, Patterns, and Lexemes

◆ Tokens 如果 input 符合 token 的 pattern

- The terminal symbols in the grammar



◆ Patterns describe patterns with regular language

- Rule describing the set of strings that correspond to the same token 長的樣子

◆ Lexeme 如果 input 符合 token 的 pattern → lexeme

“不等合” “ → not lexeme

- A sequence of characters matched by a pattern

Token	Sample Lexemes	Informal Description of Pattern
const	const	const
if	if	if
relop	<, <=, =, >, >=	< or <= or = or > or >=
id	pi, count, D2	letter followed by letters and digits
num	0, 3.14, 6.02E23	any number constant

) regular language

Operations on Languages

$$L_1 = \{a, b\}$$

$$L_2 = \{o, l\}$$

◆ Union of L and M , written as $L \cup M$

$$L \cup M = \{s \mid s \in L \vee s \in M\} \quad L_1 \cup L_2 = \{a, b, o, l\}$$

◆ Concatenation of L and M , written as LM

$$LM = \{st \mid s \in L \wedge t \in M\} \quad \text{順序不可換} \quad L_1 L_2 = \{ao, al, bo, bl\}$$

$$L_1 L_1 = \{aa, ab, ba, bb\}$$

$$L_1^2, L_1^3, L_1^4, \dots$$

◆ Kleene closure of L , written as L^*

- denotes “zero or more concatenations of L

$$L^* = \bigcup_{i=0}^{\infty} L^i = L^0 \cup L^1 \cup L^2 \cup L^3 \cup \dots$$

◆ Positive closure of L , written as L^+

$$L^+ = \bigcup_{i=1}^{\infty} L^i$$

Positive & Kleene
差異在有沒有 $L^0(\emptyset)$

Positive starts from L^1
但 Positive 也可能有 \emptyset
依 L 決定

Operations on Languages

◆ Example

Let $L = \{A, B, \dots, Z, a, b, \dots, z\}$ and $D = \{0, 1, 2, \dots, 9\}$

■ $L \cup D$ A~Z, 0~9

- the set of letters and digits

■ LD {A1, A2, ..., Z9}

- the set of strings consists of a letter followed by a digit

■ L^4

- the set of all four-letter strings

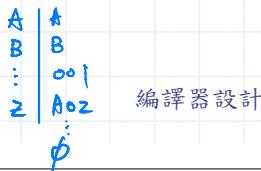
■ L^*

- the set of all strings of letters, including ϵ

■ $L(L \cup D)^*$ pattern of id

- the set of all strings of letters and digits beginning with a letter

Lexical Analysis



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Regular Expressions

Regular grammar \rightarrow Regular language
expression

regular grammar 較難
expression 較簡單

◆ Each regular expression r denotes a language $L(r)$

◆ Rules to define the regular expressions over Σ

■ ϵ is regular expression that denotes $\{\epsilon\}$

■ If a is a symbol in Σ , then a is a regular expression that denote $\{a\}$

$\Sigma = \{0, 1\}$

■ Suppose r and s are regular expressions, then

• $(r)|(s)$ is a regular expression denoting $L(r) \cup L(s)$ 為了怕順序出錯
才加 |

• $(r)(s)$ is a regular expression denoting $L(r)L(s)$

r	$L(r)$
ϵ	$\{\epsilon\}$
0	$\{0\}$
1	$\{1\}$
$r s$	$L(r) \cup L(s)$
rs	$L(r)L(s)$
r^*	$L(r)^*$
r^+	$L(r)^+$

• $(r)^*$ is a regular expression denoting $(L(r))^*$

• $(r)^+$ is a regular expression denoting $(L(r))^+$

■ If two regular expressions r and s denote the same language, we say r and s are equivalent and write

$$r = s \quad r = \{aa, ab, ba, bb\}, \quad s = (a|b)(a|b), \quad r = s$$

Lexical Analysis

編譯器設計

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Regular Expressions

◆ Example: let $\Sigma = \{a, b\}$

- The regular expression $a | b$ denotes $\{a, b\}$
- $(a|b)(a|b)$ denotes $\{aa, ab, ba, bb\}$
 - i.e. the set of all 2-letter strings of a's and b's
 - Another form is $aa | ab | ba | bb$
- a^* denotes the set of all strings of a's
 - i.e. $\{\epsilon, a, aa, aaa, \dots\}$
- $(a | b)^*$ denotes the set of all strings of a's and b's
 - Another form is $(a^*b^*)^*$
- $a | a^*b$ denotes the set containing the string a and all strings consisting of zero or more a's and followed by b's

if → parser → yes if
→ no

Angular grammar
 $A \rightarrow aB$ $S \rightarrow A$
 $A \rightarrow a$ $A \rightarrow f$

if → {if} → cf>
↑ {is}
f {f}
if = {if} (concat)

Precedence

- ## ◆ Unnecessary parentheses can be avoided in regular expressions if
- The unary operator * has the highest precedence and is left associative ^
 - Concatenation has the second highest precedence and is left associative x
 - | has the lowest precedence and is left associative +
 - Example
 - $(a)|((b)^*(c)) \equiv a | b^*c$

Algebraic Properties of Regular Expressions

- ◆ Some algebraic laws that hold for regular expressions r , s , and t

Axiom	Description
$r s = s r$	is commutative 交換的
$r (s t) = (r s) t$	is associative 組合的
$(rs)t = r(st)$	concatenation is associative
$r(s t) = rs rt$ $(s t)r = sr tr$	concatenation distributes over
$\epsilon r = r$ $r\epsilon = r$	ϵ is the identity element of concatenation /like 0
$r^* = (r \epsilon)^*$	relationship between * and ϵ
$r^{**} = r^*$	* is idempotent

Lexical Analysis

編譯器設計

Idempotent 邏輯等價的 9

Regular Definitions

$\{A, B, \dots, Z\}$ language
letter $\rightarrow A|B|\dots|Z$ expression
digit $\rightarrow 0|1|\dots|9$
 $(\text{digit})^+$ \rightarrow 所有整數(並不空) $(\text{digit})^+.$ $(\text{digit})^+ \rightarrow (0|1|\dots|9)^+.$ $(0|1|\dots|9)^+$

- ◆ For notational convenience, we may wish to give names to regular expressions

- To define regular expressions using these names as if they were symbols
- If Σ is an alphabet, then a regular definition is a sequence of definitions of the form

$$d_1 \rightarrow r_1 \quad d(\text{digit})$$

$$d_2 \rightarrow r_2$$

...

$$d_n \rightarrow r_n$$

where each r_i is a regular expression over the symbols in $\Sigma \cup \{r_1, r_2, \dots, r_{i-1}\}$

Lexical Analysis

編譯器設計

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Regular Definitions

◆ Notational Shorthands

- +: one or more instance 1次 or more digit⁺ | digit⁺. digit⁺
- ?: zero or one instance 0次 or 1次 = digit⁺(. digit⁺)?
- [abc]: character classes, i.e. $\equiv a|b|c$ 不用“|”

◆ Example

Tokens

1. keywords

2. operators

3. number

4. strings " "

5. id

digit $\rightarrow 0 | 1 | \dots | 9$

letter $\rightarrow [A-Za-z]$ Why not [A-z]? In ASCII code, there are other symbols between Z-a

id $\rightarrow \text{letter} (\text{letter} | \text{digit})^*$

digits $\rightarrow \text{digit}^+$

optional_fraction $\rightarrow (. \text{ digits})?$

optional_exp $\rightarrow (\text{E} (+ | -)?) \text{ digits}?)$ $1.0 \text{ E} (-10) = 1.0 \times 10^{-10}$ ($\text{E} (+|-)?(\text{digit})^+)?$

num $\rightarrow \text{digits optional_fraction optional_exp}$

Recognition of Tokens

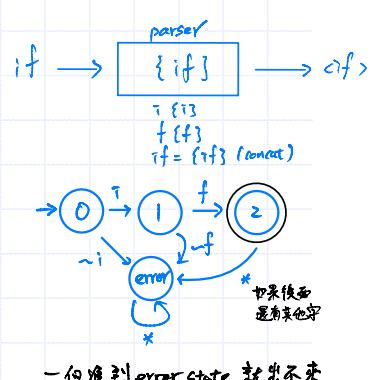
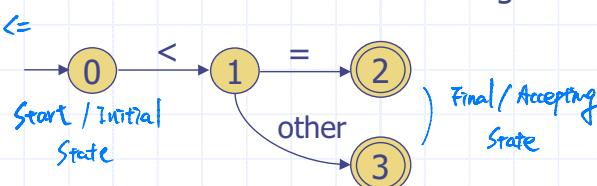
◆ State transition diagrams

- depicts the actions that take place when a lexical analyzer is called by the parser to get the next token

■ States

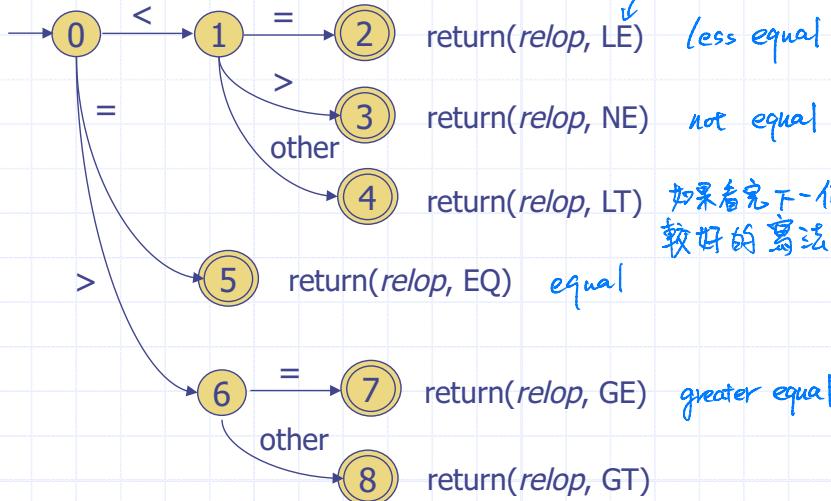
- Positions in a transition diagram
 - drawn as circles
- States are connected by arrows, call edges
- Start state

- the initial state of the transition diagram



Recognition of Tokens

- ◆ Example: $relop \rightarrow < | \leq | = | \geq | >$



Pascal 等於
因為 Pascal 的 “=” 是 “:=”

attribute

return(relop, LE) less equal

return(relop, NE) not equal

return(relop, LT)

如果看不完下一個字是錯的，要還回去
較好的寫法是①

return(relop, EQ) equal

return(relop, GE) greater equal

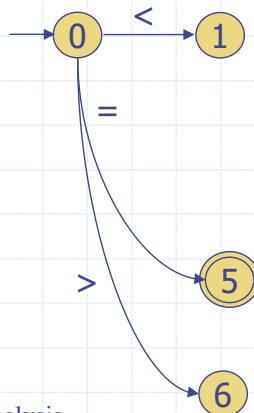
只要最終是⑧，就可以說是 Yes

if
→ 會被 keyword to string 跳過
會自動選最長的

Implementing a Transition Diagram

- ◆ A transition diagram can be converted into a program

- Each state gets a segment of code
 - If there are edges leaving a state, then its code reads a character and selects an edge to follow
 - If there is an edge labeled by the character read, then control is transferred
 - If there is no such edge, then fail



```
token nexttoken( ) {
    switch(state) {
        case 0: /* state 0 */
            c = nextchar();
            if (c == '<') state = 1;
            else if (c == '=') state = 5;
            else if (c == '>') state = 6;
            else state = fail;
            break;
    }
}
```

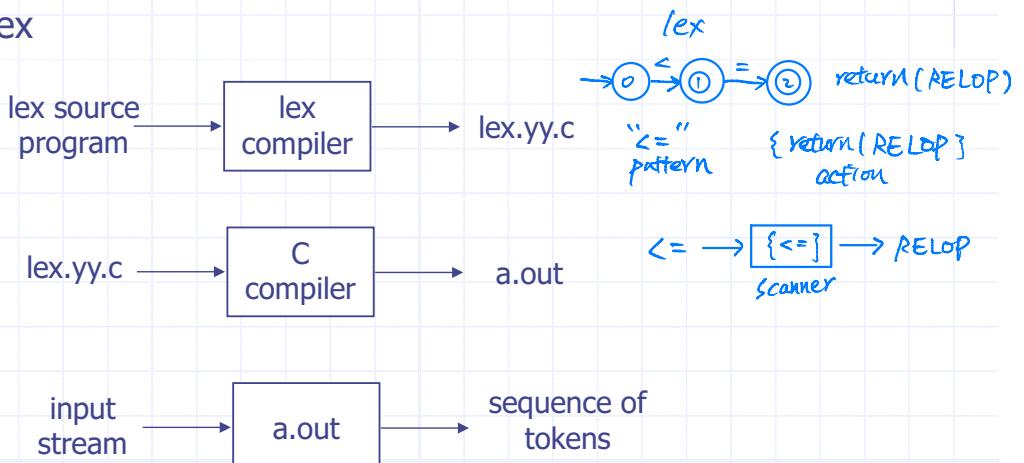
simple and intuitive,
but complex

⇒ use tools to
generate the code

Implementing a Transition Diagram

- ◆ Several tools have built for constructing lexical analyzer from regular expressions

- e.g. lex



Lexical Analysis

編譯器設計

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Finite Automata

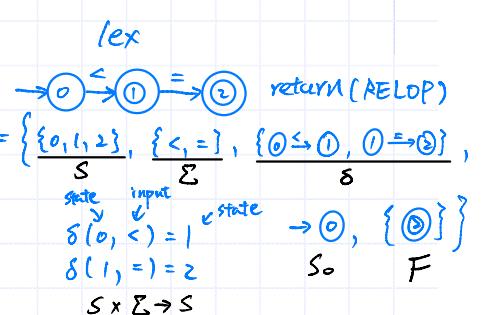
數學名詞 = state transition diagram



- ◆ We compile a regular expression into a lexical analyzer by constructing a generalized transition diagram called a *finite automaton*

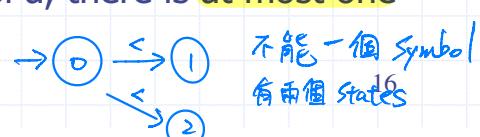
- $M = \{S, \Sigma, \delta, s_0, F\}$

- S : a finite, nonempty set of *states*
- Σ : an *alphabet*
- δ : mapping $S \times \Sigma \rightarrow S$ *delta*
- s_0 : start state
- F : the set of accepting (or final) states



- A finite automaton is called a deterministic finite automaton (DFA) if

- No state has an ϵ -transition, and $\rightarrow \circ \xrightarrow{\epsilon} \circ$ 不確定是在 State 0 還是 1
- For each state s and input symbol a , there is at most one edge labeled a leaving s



Lexical Analysis

編譯器設計

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Simulating a DFA

◆ Input

- An input string x terminated by an eof
- A DFA $D = \{S, \Sigma, \delta, s_0, F\}$

◆ Output

- "yes" if D accepts x ; "no" otherwise

◆ Method

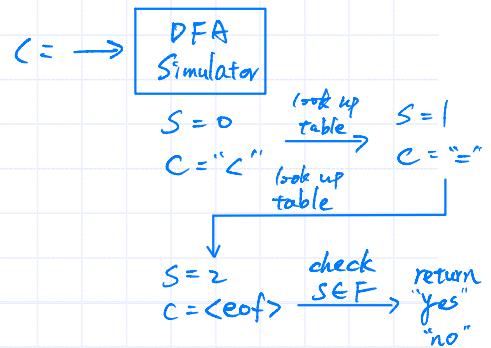
```

 $s = s_0$ 
 $c = \text{nextchar}();$ 
while  $c \neq \text{eof}$  do
     $s = \text{move}(s, c);$ 
     $c = \text{nextchar}();$ 
end
if  $s$  is in  $F$  then return "yes"
 $s \in F$  else return "no"

```

Σ		
$<$	$=$	
0	1	.
1	.	2
2	.	.

empty spots are error states

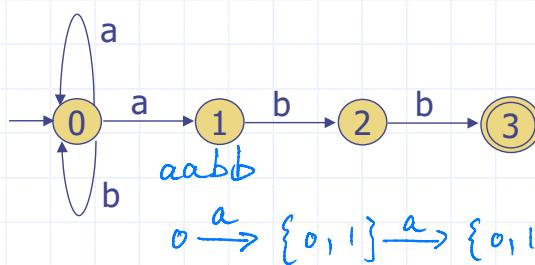


Nondeterministic Finite Automata (NFA)

◆ $M = \{S, \Sigma, \delta, s_0, F\}$

- S : a finite, nonempty set of *states*
- Σ : an *alphabet*
- δ : mapping $S \times \Sigma \rightarrow 2^S$
- s_0 : start state
- F : the set of accepting (or final) states

只要有一條路
抵達 F 就 return yes



$$\begin{aligned}\delta(0, a) &= \{0, 1\} \\ \delta(0, b) &= \{0\} \\ \delta(1, b) &= \{2\} \\ \delta(2, b) &= \{3\}\end{aligned}$$

$$0 \xrightarrow{a} \{0, 1\} \xrightarrow{a} \{0, 1\} \xrightarrow{b} \{0, 2\} \xrightarrow{b} \{0, 3\}$$

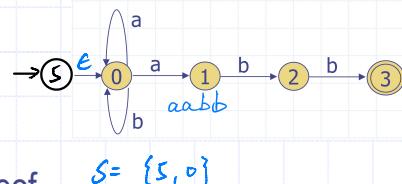
有可能有多種 F

編譯器設計如果抵達多種 F , 依照 priority 裁斷

Simulating an NFA

◆ Input

- An input string x terminated by an eof
- A NFA N



$$S = \{S, \emptyset\}$$

◆ Output

- "yes" if N accepts x ; "no" otherwise

◆ Method

```

 $S = \epsilon\text{-closure}(s_0)$ 
c = nextchar;
while c ≠ eof do
     $S = \epsilon\text{-closure}(\text{move}(S, c))$ ;
    c = nextchar();
end
if  $S \cap F \neq \emptyset$  then return "yes"
else return "no"

```

Operations on NFA States

◆ ϵ -closure(s)

- Set of NFA states reachable from state s on ϵ -transitions only

Regular Expression DFA \in NFA
 ϵ -closure NFA \in DFA
 ϵ -closure DFA = DFA

在寫 compiler 的時候會寫
NFA 而非 DFA (原因後面)
algorithm
From regular expression to NFA
too difficult to
from DFA

◆ ϵ -closure(T)

- Set of NFA states reachable from some state s in T on ϵ -transitions only

push all states in T onto stack

initialize ϵ -closure(T) to T

while stack is not empty do

pop t , the top element, off the stack

for each state u with an edge from t to u labeled ϵ do

if u is not in ϵ -closure(T) then

add u to ϵ -closure(T)

push u onto stack

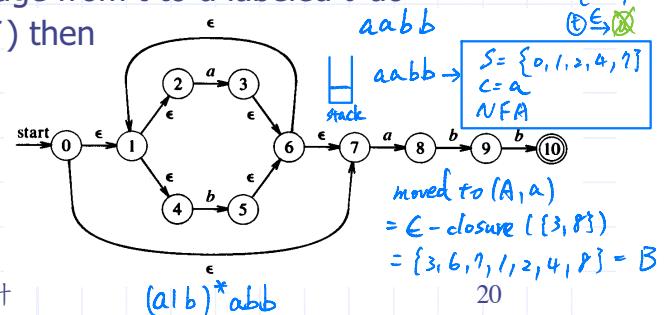
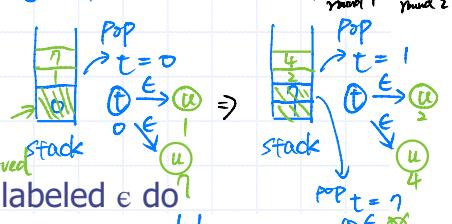
end if

end

end

Regular Expression DFA \in NFA
 ϵ -closure NFA \in DFA
 ϵ -closure DFA = DFA

$$\epsilon\text{-closure } \{0\} = \{0, 1, 2, 4\}$$



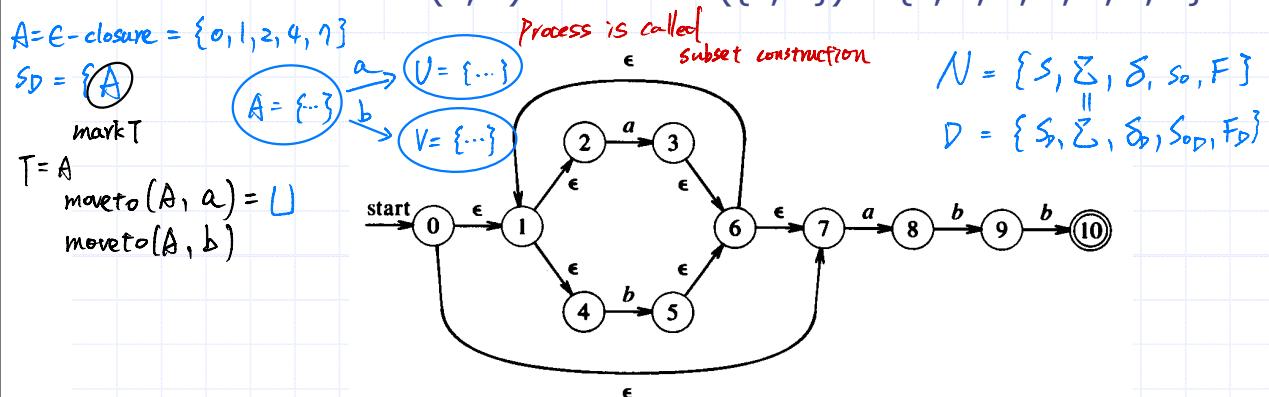
Operations on NFA States

◆ $\text{moveto}(T, a)$

- Set of NFA states to which there is a transition on input symbol a from some NFA state s in T

◆ Example: NFA for $(a|b)^*abb$

- $\epsilon\text{-closure}(0) = \{0, 1, 2, 4, 7\} \equiv A$
- $\text{moveto}(A, a) = \epsilon\text{-closure}(\{3, 8\}) = \{1, 2, 3, 4, 6, 7, 8\} \equiv B$



Constructing a DFA from an NFA

◆ Algorithm (Subset construction)

- Input. An NFA N
- Output. A DFA D accepting the same language
- Method. Constructs a transition table D_{tran} for D

initially, $\epsilon\text{-closure}(S_0)$ is the only state in D_{states} and unmarked
while there is an unmarked state T in D_{states} do

 mark T

 for each input symbol a do

$U = \epsilon\text{-closure}(\text{moveto}(T, a))$

 if U is not in D_{states} then

 add U to as an unmarked state to D_{states}

$D_{\text{tran}}[T, a] = U$

 end

 end

Constructing a DFA from an NFA

◆ Example: NFA for $(a|b)^*abb$

- $\epsilon\text{-closure}(0) = \{0, 1, 2, 4, 7\} \equiv A$
- $\text{moveto}(A, a) = \epsilon\text{-closure}(\{3, 8\}) = \{1, 2, 3, 4, 6, 7, 8\} \equiv B$
- $\text{moveto}(A, b) = \epsilon\text{-closure}(\{5\}) = \{1, 2, 4, 5, 6, 7\} \equiv C$
- $\text{moveto}(B, a) = \epsilon\text{-closure}(\{3, 8\}) = B$
- $\text{moveto}(B, b) = \epsilon\text{-closure}(\{5, 9\}) = \{1, 2, 4, 5, 6, 7, 9\} \equiv D$
- $\text{moveto}(C, a) = \epsilon\text{-closure}(\{3, 8\}) = B$
- $\text{moveto}(C, b) = \epsilon\text{-closure}(\{5\}) = C$
- $\text{moveto}(D, a) = \epsilon\text{-closure}(\{3, 8\}) = B$
- $\text{moveto}(D, b) = \epsilon\text{-closure}(\{5, 10\}) = \{1, 2, 4, 5, 6, 7, 10\} \equiv E$
- $\text{moveto}(E, a) = \epsilon\text{-closure}(\{3, 8\}) = B$
- $\text{moveto}(E, b) = \epsilon\text{-closure}(\{5\}) = C$

$$S_0 = \{A, B, C, D\}$$

fix A mark

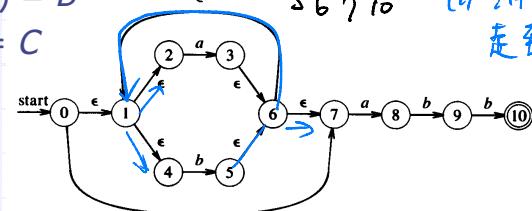
		a	b
S ₀	A	B	C
B	B	B	D
C	B	B	C
D	B	B	E
E	B	B	C

ex. $B \rightarrow$ 空集

看能不能走到，能走到就加入
 $\epsilon\text{-closure}$

(不消耗就可以
走到的)

$$\begin{aligned}\epsilon\text{-closure}(\{S\}) \\ = \{1, 2, 4, 5, 6, 7\}\end{aligned}$$

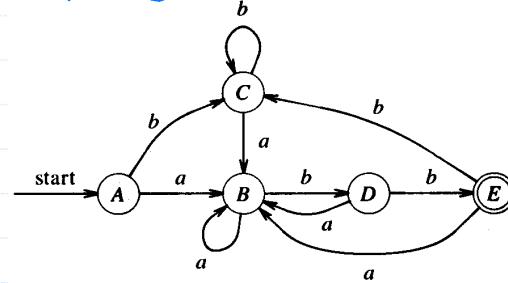


Constructing a DFA from an NFA

◆ Example: NFA for $(a|b)^*abb$

原本的 final state 是 10
只要有包含 10 的 state
就是 final state

State	Input Symbol	
	a	b
A	B	C
B	B	D
C	B	C
D	B	E
E	B	C



$$A = \{0, 1, 2, 4, 7\}$$

E 为 final state

$$B = \{1, 2, 3, 4, 6, 7, 8\}$$

$$C = \{1, 2, 3, 4, 5, 6, 7\}$$

$$D = \{1, 2, 4, 5, 6, 7, 9\}$$

$$E = \{1, 2, 4, 5, 6, 7, \underline{10}\}$$

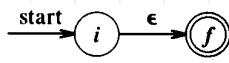
Constructing NFA from Regular Expression

- ◆ Algorithm (Thompson's construction)
 - Input. A regular expression r over Σ
 - Output. An NFA N accepting $L(r)$
 - Method.

$$\Sigma = \{a, b\}$$

r	$L(r)$
ϵ	$\{\epsilon\}$
a	$\{a\}$
b	$\{b\}$
$r_1 s$	$L(r_1) \cup L(s)$
$r s$	$L(r)L(s)$
r^*	$L(r)^*$

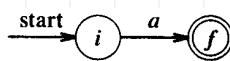
- For ϵ , construct the NFA



$a \rightarrow \boxed{\{a\} \{ε\}}$ → Yes

- This NFA recognizes $\{\epsilon\}$

- For a in Σ , construct the NFA



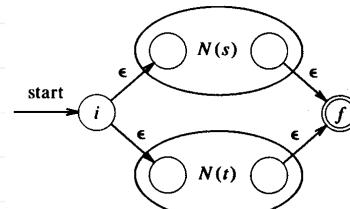
- This NFA recognizes $\{a\}$

Constructing NFA from Regular Expression

- Suppose $N(s)$ and $N(t)$ are NFA's for regular expressions s and t

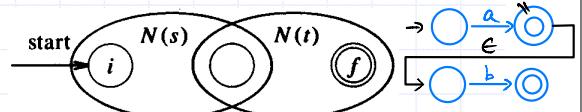
- For the regular expression $s \mid t$

- This NFA recognizes $L(s) \cup L(t)$



- For the regular expression st

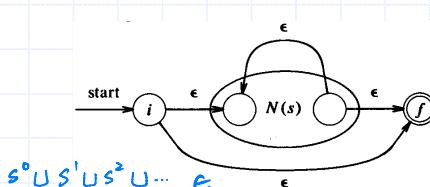
- This NFA recognizes $L(s)L(t)$



- For the regular expression s^*

- This NFA recognizes $L(s)^*$

$$s^* = s^0 \cup s^1 \cup s^2 \cup \dots$$



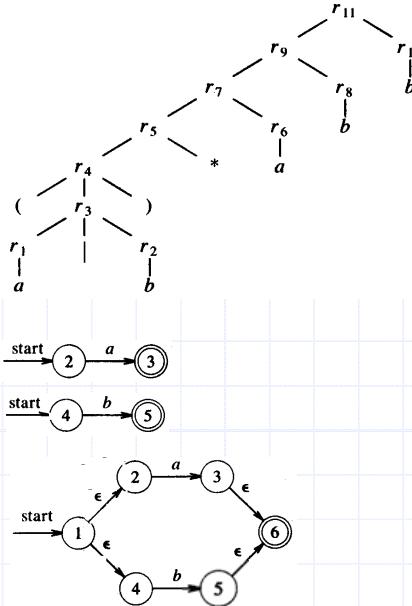
如果 positive 則沒有這條

Constructing NFA from Regular Expression

◆ Example: $r = (a|b)^*abb$

- Parse r into its constituent subexpressions

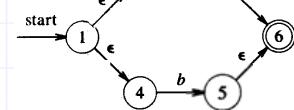
R.E. \Rightarrow N.F.A \Rightarrow D.F.A.



start \rightarrow 2

start \rightarrow 4

start \rightarrow 1



start \rightarrow 2

start \rightarrow 4

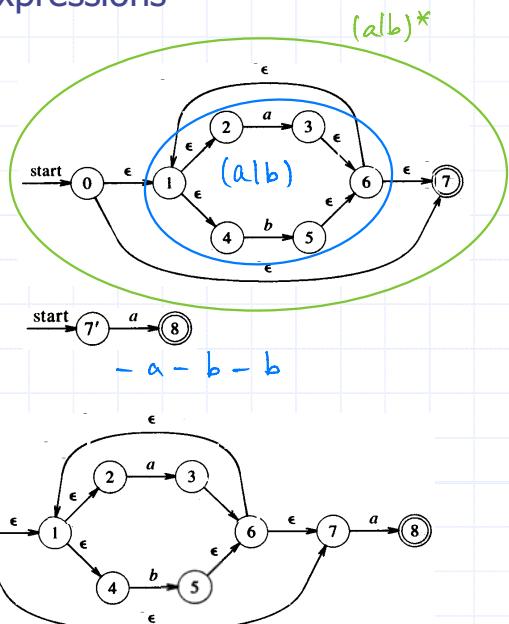
start \rightarrow 1



Lexical Analysis

編譯器設計

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Constructing NFA from Regular Expression

◆ The construction produces an NFA $N(r)$ with the following properties



- $N(r)$ has at most twice as many states as the number of symbols and operators in r
 - Each step creates at most two new states
- $N(r)$ has exactly one start state and one accepting state
 - The accepting state has no outgoing transitions
- Each state of $N(r)$ has either one outgoing transition on a symbol in Σ or at most two outgoing ϵ -transitions

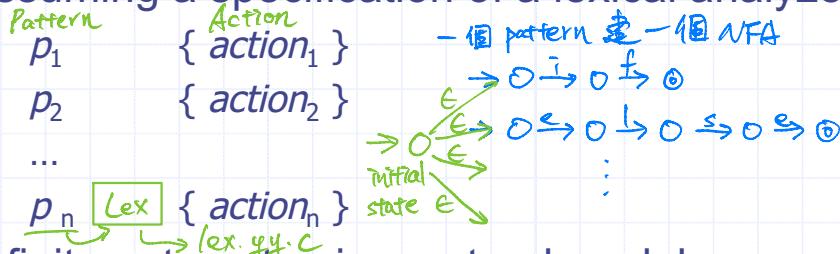
Lexical Analysis

編譯器設計

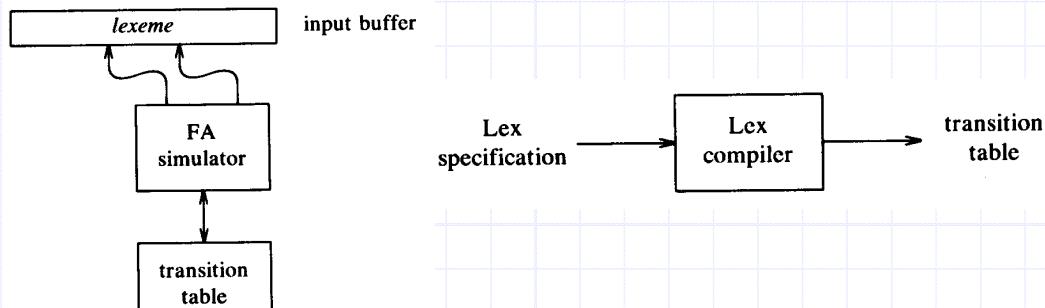
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Design of a Lexical Analyzer Generator

- ◆ Assuming a specification of a lexical analyzer



- ◆ A finite automaton is a natural model



Lexical Analysis

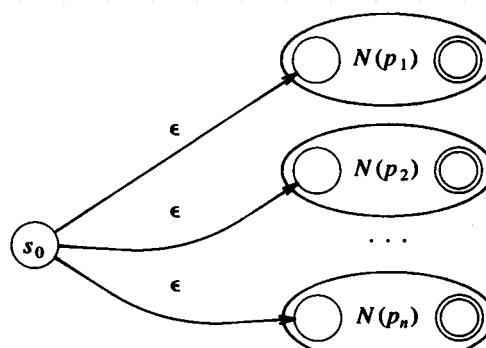
編譯器設計

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Design of a Lexical Analyzer Generator

- ◆ Pattern matching based on NFA's

- To construct the transition table of a NFA N for the pattern $p_1 | p_2 | \dots | p_n$



對應到某個 final state
就執行其 action

若 match 兩個 pattern
依優先順序決定

DFA 只是數學家簡化用
來太多實際用途

DFA 最多是 NFA 的兩倍
但在 compiler 中花最多時間
的是 optimization, 這部份幾乎
不花時間

Lexical Analysis

編譯器設計

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Minimizing the Number of States

$RE \Rightarrow NFA \Rightarrow DFA \Rightarrow mDFA$

◆ An important theoretical result

- Every regular set is recognized by a minimum-state DFA that is unique up to state names 名字不同而已, pattern 一樣是 equivalent.

◆ String w distinguishes state s from state t if

- By starting with the DFA M in state s and feeding it input w , we end up in an accepting state, but
- By starting in state t and feeding it input w , we end up in a nonaccepting state, or vice versa
- e.g. ϵ distinguishes any accepting state from any nonaccepting state
 $\textcircled{S} \rightarrow$ 因為 DFA 不吃 ϵ
 $\textcircled{N} \rightarrow$ 會停在原地

$\textcircled{S} \xrightarrow{w} \textcircled{A}$
 $\textcircled{N} \xrightarrow{w} \textcircled{N}$

If one of s/w compose string w
⇒ distinguish
or
⇒ not distinguish

◆ DFA states can be minimized by finding all groups of states that can be distinguished by some input string

- Each group of states that cannot be distinguished by some input string starting is then merged into single state

Minimizing the Number of States

◆ Algorithm

- Construct an initial partition $\Pi = \{F, S - F\}$
- Construct a new partition:
 - for each group $G \in \Pi$ do
 - partition G into subgroups such that
 - two states s and $t \in G$ are in the same subgroup iff
 - for all input symbol a ,
 - s and t have transitions on a to states in the same group in Π
 - replace G in Π_{new} by the set of subgroups formed
 - end
 - If $\Pi_{\text{new}} \neq \Pi$, then let $\Pi = \Pi_{\text{new}}$. Repeat.
 - Choose one state in each group as the representative
 - Update the transitions



Minimizing the Number of States

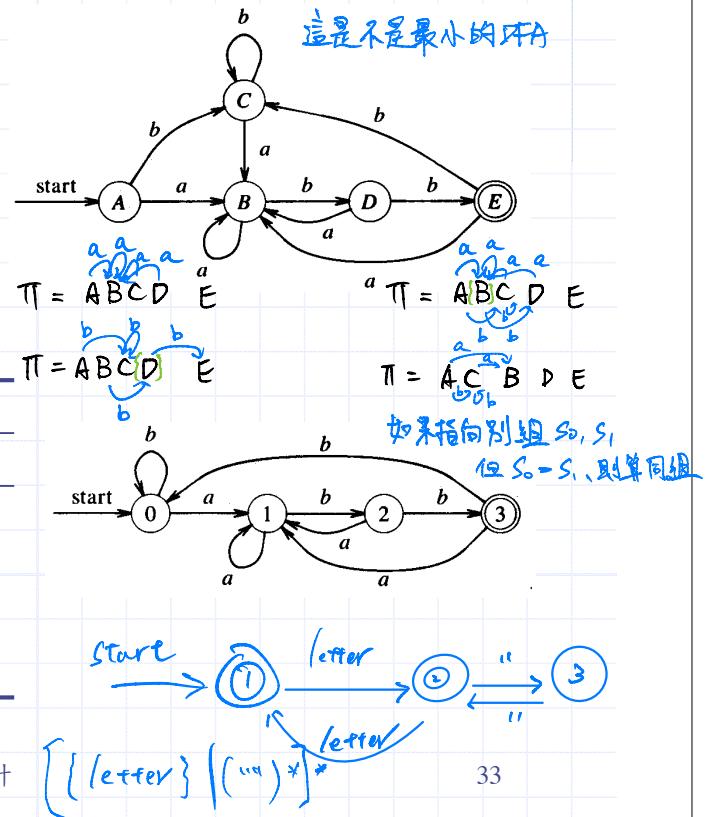
◆ Example

- Initially, $\Pi = \{(ABCD), (E)\}$
 - $(ABCD) \Rightarrow (ABC)(D)$ 又有一個不用切
- $\Pi = \{(ABC), (D), (E)\}$
 - $(ABC) \Rightarrow (AC)(B)$
- $\Pi = \{(AC), (B), (D), (E)\}$

State	Input Symbol	
	a	b
A (0)	B	A
B (1)	B	D
D (2)	B	E
E (3)	B	A

Lexical Analysis

編譯器設計



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Building Regular Grammar from NFA

◆ Input. An NFA N

$RE \Rightarrow NFA$

◆ Output. A regular grammar r . N accepts $L(r)$

$RG \Leftrightarrow$

◆ Method

- For each state i of N , create a nonterminal symbol A_i
- If state i goes to state j on symbol a , introduce the production $A_i \rightarrow aA_j$
- If state i goes to state j on symbol ϵ , introduce the production $A_i \rightarrow A_j$
- If state i is a final state, introduce the production $A_i \rightarrow \epsilon$
- If state i is the start state, make A_i be the start symbol

$$G = \{N, \Sigma, P, S\}_{\text{nonterminal}}$$

Lexical Analysis

編譯器設計

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Building Regular Grammar from NFA

◆ Example

- Nonterminal symbol:

A_0, A_1, A_2, A_3

- Productions

$A_0 \rightarrow aA_0$

$A_0 \rightarrow bA_0$

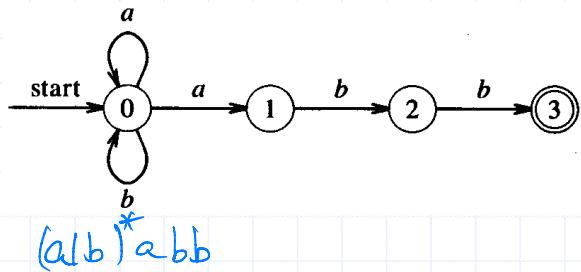
$A_0 \rightarrow aA_1$

$A_1 \rightarrow bA_2$

$A_2 \rightarrow bA_3$

$A_3 \rightarrow \epsilon$

- Start symbol: A_0



$$M = \{\{0, 1, 2, 3\}, \{a, b\}, \delta, 0, \{3\}\}$$

$$V_N = \{A_0, A_1, A_2, A_3\}$$

$$\begin{matrix} 0 \xrightarrow{a} 0 \\ 0 \xrightarrow{b} 0 \end{matrix} \quad \begin{matrix} 0 \xrightarrow{\epsilon} 0 \\ A_i \rightarrow aA_j \\ A_i \rightarrow A_j \end{matrix}$$

$$P = \{ A_0 \rightarrow aA_0 \quad \text{match Regular Grammar} \\ A_0 \rightarrow bA_0 \\ A_0 \rightarrow aA_1 \\ A_1 \rightarrow bA_2 \\ A_2 \rightarrow bA_3 \\ A_3 \rightarrow \epsilon \}$$

Building NFA from Regular Grammar

- Input. A regular grammar $G = (V_N, V_T, P, S)$

- Output. An NFA $N = (K, V_T, \delta, s_0, F)$ that accepts $L(G)$

◆ Method

- $K = V_N \cup \{A\}$ $V_N = \{A_0, A_1, A_2\}$, $K = \{A_0, A_1, A_2, A\}$

- If $S \rightarrow \epsilon \in P$, $F = \{S, A\}$ 因為上面例子沒有 ϵ , $F = \{A\}$

$A_0 \xrightarrow{\epsilon} A$
Otherwise, $F = \{A\}$

- If $B \rightarrow a \in P$ then

$A \in \delta(B, a)$

- If $B \rightarrow aC \in P$ then

$C \in \delta(B, a)$

- For every $a \in V_T$

$\delta(A, a) = \emptyset$

