KAN Kolmogorov Arnold Network Note

研究任務

- 1. 閱讀 KAN Kolmogorov-Arnold Network 論文
- 2. 設計 KAN 網路系統階層式架構 IDEFO
- 3. 設計 KAN 網路系統每個功能模組離散事件建模 Grafcet
- 4. 以 MIAT 方法論合成每個 Grafcet 控制器電路
- 5. 以 ChatGPT 合成每個 Grafcet Datapath 電路
- 6. FPGA 整合驗證

A Attention

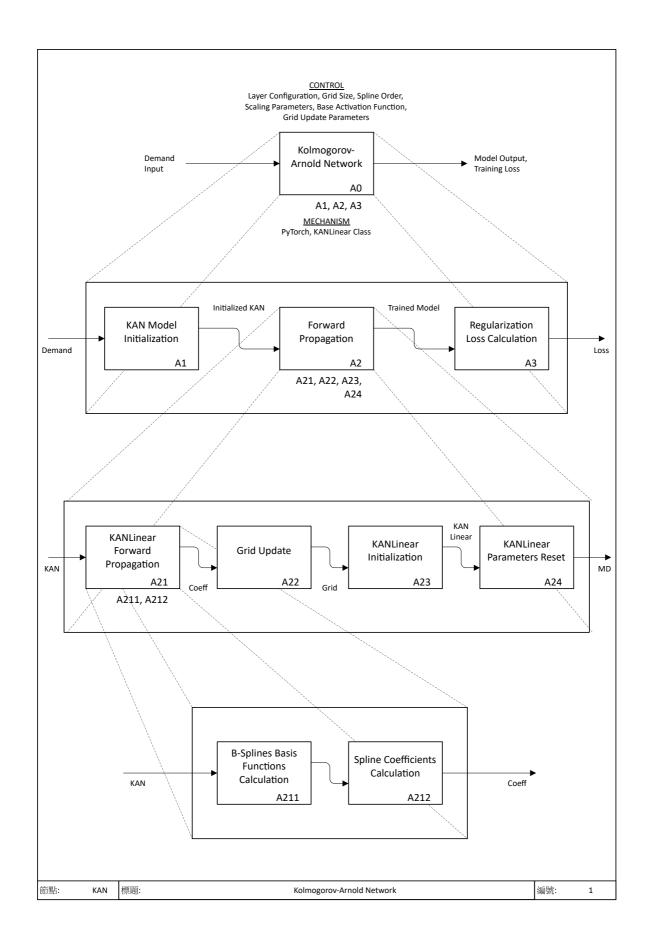
KAN 之研究任務須於六月底完成,作為實習機會的前置條件。

開放原始碼

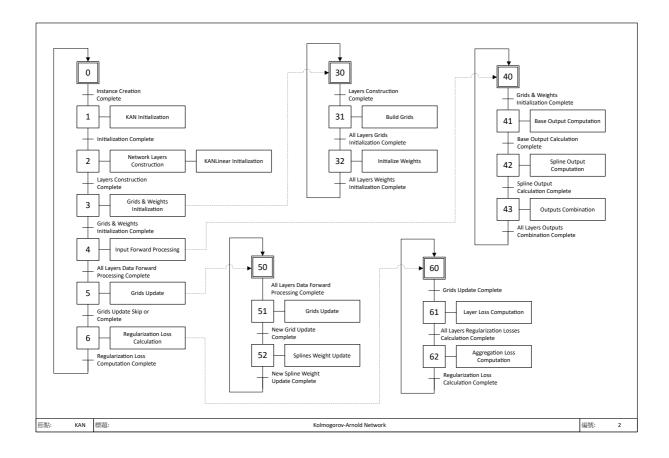
• Code: https://github.com/KindXiaoming/pykan

• Reference: https://arxiv.org/abs/2404.19756

設計階層式架構 IDEF0



設計功能模組離散事件建模 Grafcet



Python 模擬驗證

• 重構後之 Kolmogorov-Arnold Network

```
import math

import torch
import torch.nn.functional as F

class KANLinear(torch.nn.Module):
    def __init__(
        self,
        in_features,
        out_features,
        grid_size=5,
        spline_order=3,
        scale_base=1.0,
```

```
scale_spline=1.0,
            enable_standalone_scale_spline=True,
            base_activation=torch.nn.SiLU,
            qrid_eps=0.02,
            qrid_range=[-1, 1],
    ):
        super(KANLinear, self).__init__()
        self.in_features = in_features
        self.out_features = out_features
        self.grid_size = grid_size
        self.spline_order = spline_order
        # 構建網格點
        self.grid = self.build_grid(grid_range, grid_size,
spline_order)
        # 初始化基礎權重和樣條權重
        self.base_weight, self.spline_weight,
self.spline_scaler = self.initialize_weights(
            out_features, in_features, grid_size,
spline_order, scale_base, scale_spline,
enable_standalone_scale_spline
        )
        self.scale_base = scale_base
        self.scale_spline = scale_spline
        self.enable_standalone_scale_spline =
enable_standalone_scale_spline
        self.base_activation = base_activation()
        self.grid_eps = grid_eps
    def build_grid(self, grid_range, grid_size,
spline_order):
        h = (grid_range[1] - grid_range[0]) / grid_size
        grid = (
            (
                    torch.arange(-spline_order, grid_size +
spline_order + 1) * h
                    + grid_range[0]
```

```
.expand(self.in_features, -1)
            .contiquous()
        )
        return grid
    def initialize_weights(self, out_features, in_features,
grid_size, spline_order, scale_base, scale_spline,
                           enable_standalone_scale_spline):
        base_weight =
torch.nn.Parameter(torch.Tensor(out_features, in_features))
        spline_weight = torch.nn.Parameter(
            torch.Tensor(out_features, in_features,
grid_size + spline_order)
        if enable_standalone_scale_spline:
            spline_scaler = torch.nn.Parameter(
                torch.Tensor(out_features, in_features)
            )
        else:
            spline_scaler = None
        torch.nn.init.kaiming_uniform_(base_weight,
a=math.sqrt(5) * scale_base)
        torch.nn.init.kaiming_uniform_(spline_weight,
a=math.sqrt(5) * scale_spline)
        if enable_standalone_scale_spline:
            torch.nn.init.kaiming_uniform_(spline_scaler,
a=math.sqrt(5) * scale_spline)
        return base_weight, spline_weight, spline_scaler
    def b_splines(self, x: torch.Tensor):
        bases = self.calculate_b_spline_bases(x)
        return bases.contiquous()
    def calculate_b_spline_bases(self, x: torch.Tensor):
        grid: torch.Tensor = (
            self.grid
        ) # (in_features, grid_size + 2 * spline_order +
1)
```

```
x = x.unsqueeze(-1)
        bases = ((x \ge grid[:, :-1]) \& (x < grid[:,
1:])).to(x.dtype)
        for k in range(1, self.spline_order + 1):
            bases = (
                            (x - qrid[:, : -(k + 1)])
                            / (grid[:, k:-1] - grid[:, : -
(k + 1))
                            * bases[:, :, :-1]
                    ) + (
                            (qrid[:, k + 1:] - x)
                            / (grid[:, k + 1:] - grid[:, 1:
(-k)])
                            * bases[:, :, 1:]
                    )
        return bases
    def curve2coeff(self, x: torch.Tensor, y:
torch.Tensor):
        A = self.b_splines(x).transpose(
            0, 1
        ) # (in_features, batch_size, grid_size +
spline_order)
        B = y.transpose(0, 1) # (in_features, batch_size,
out_features)
        solution = torch.linalq.lstsq(
            A, B
        ).solution # (in_features, grid_size +
spline_order, out_features)
        result = solution.permute(
            2, 0, 1
        ) # (out_features, in_features, grid_size +
spline_order)
        return result.contiquous()
    @property
    def scaled_spline_weight(self):
        if self.enable_standalone_scale_spline:
            return self.spline_weight *
```

```
self.spline_scaler.unsqueeze(-1)
        else:
            return self.spline_weight
    def forward(self, x: torch.Tensor):
        base_output = self.compute_base_output(x)
        spline_output = self.compute_spline_output(x)
        return base_output + spline_output
    def compute_base_output(self, x: torch.Tensor):
        return F.linear(self.base_activation(x),
self.base_weight)
    def compute_spline_output(self, x: torch.Tensor):
        return F.linear(
            self.b_splines(x).view(x.size(0), -1),
self.scaled_spline_weight.view(self.out_features, -1),
        )
   @torch.no_grad()
   def update_grid(self, x: torch.Tensor, margin=0.01):
        batch = x.size(0)
        splines = self.b_splines(x) # (batch, in, coeff)
        splines = splines.permute(1, 0, 2) # (in, batch,
coeff)
        orig_coeff = self.scaled_spline_weight # (out, in,
coeff)
        oriq_coeff = oriq_coeff.permute(1, 2, 0) # (in,
coeff, out)
        unreduced_spline_output = torch.bmm(splines,
oriq_coeff) # (in, batch, out)
        unreduced_spline_output =
unreduced_spline_output.permute(
           1, 0, 2
        ) # (batch, in, out)
        x_sorted = torch.sort(x, dim=0)[0]
```

```
grid_adaptive = x_sorted[
            torch.linspace(
                0, batch - 1, self.grid_size + 1,
dtype=torch.int64, device=x.device
        ]
        uniform_step = (x_sorted[-1] - x_sorted[0] + 2 *
marqin) / self.qrid_size
        grid_uniform = (
                torch.arange(
                    self.grid_size + 1,
dtype=torch.float32, device=x.device
                ).unsqueeze(1)
                * uniform_step
                + x_sorted[0]
                - margin
        )
        qrid = self.qrid_eps * grid_uniform + (1 -
self.grid_eps) * grid_adaptive
        grid = torch.concatenate(
            qrid[:1]
                - uniform_step
                * torch.arange(self.spline_order, 0, -1,
device=x.device).unsqueeze(1),
                grid,
                grid[-1:]
                + uniform_step
                * torch.arange(1, self.spline_order + 1,
device=x.device).unsqueeze(1),
            ],
            dim=0,
        )
        self.grid.copy_(grid.T)
        self.spline_weight.data.copy_(self.curve2coeff(x,
unreduced_spline_output))
```

```
def regularization_loss(self,
regularize_activation=1.0, regularize_entropy=1.0):
        l1_fake = self.spline_weight.abs().mean(-1)
        regularization_loss_activation = l1_fake.sum()
        p = l1_fake / regularization_loss_activation
        regularization_loss_entropy = -torch.sum(p *
p.loq())
        return (
                regularize_activation *
regularization_loss_activation
                + regularize_entropy *
regularization_loss_entropy
        )
class KAN(torch.nn.Module):
    def __init__(
            self,
            layers_hidden,
            grid_size=5,
            spline_order=3,
            scale_base=1.0,
            scale_spline=1.0,
            base_activation=torch.nn.SiLU,
            qrid_eps=0.02,
            grid_range=[-1, 1],
    ):
        super(KAN, self).__init__()
        self.grid_size = grid_size
        self.spline_order = spline_order
        # 構建 KAN 的層
        self.layers = self.build_layers(
            layers_hidden, grid_size, spline_order,
scale_base, scale_spline, base_activation, grid_eps,
grid_range
```

```
def build_layers(self, layers_hidden, grid_size,
spline_order, scale_base, scale_spline, base_activation,
grid_eps,
                     grid_range):
        layers = torch.nn.ModuleList()
        for in_features, out_features in zip(layers_hidden,
layers_hidden[1:]):
            layers.append(
                KANLinear(
                    in_features,
                    out_features,
                    grid_size=grid_size,
                    spline_order=spline_order,
                    scale_base=scale_base,
                    scale_spline=scale_spline,
                    base_activation=base_activation,
                    qrid_eps=qrid_eps,
                    grid_range=grid_range,
                )
            )
        return layers
    def forward(self, x: torch.Tensor, update_grid=False):
        for layer in self.layers:
            if update_grid:
                layer.update_grid(x)
            x = layer(x)
        return x
    def regularization_loss(self,
regularize_activation=1.0, regularize_entropy=1.0):
        return sum(
layer.regularization_loss(regularize_activation,
reqularize_entropy)
            for layer in self.layers
        )
```

```
from EfficientKAN import KAN
# Train on MNIST
import torch
import torch.nn as nn
import torch.optim as optim
import torchvision
import torchvision.transforms as transforms
from torch.utils.data import DataLoader
from tqdm import tqdm
# Load MNIST
transform = transforms.Compose(
    [transforms.ToTensor(), transforms.Normalize((0.5,),
(0.5,))
)
trainset = torchvision.datasets.MNIST(
    root="./data", train=True, download=True,
transform=transform
valset = torchvision.datasets.MNIST(
    root="./data", train=False, download=True,
transform=transform
)
trainloader = DataLoader(trainset, batch_size=64,
shuffle=True)
valloader = DataLoader(valset, batch_size=64,
shuffle=False)
# Define model
model = KAN([28 * 28, 64, 10])
device = torch.device("cuda" if torch.cuda.is_available()
else "cpu")
model.to(device)
# Define optimizer
optimizer = optim.AdamW(model.parameters(), lr=1e-3,
weight_decay=1e-4)
# Define learning rate scheduler
scheduler = optim.lr_scheduler.ExponentialLR(optimizer,
```

```
qamma=0.8)
# Define loss
criterion = nn.CrossEntropyLoss()
for epoch in range(10):
    # Train
    model.train()
    with tqdm(trainloader) as pbar:
        for i, (images, labels) in enumerate(pbar):
            images = images.view(-1, 28 * 28).to(device)
            optimizer.zero_grad()
            output = model(images)
            loss = criterion(output, labels.to(device))
            loss.backward()
            optimizer.step()
            accuracy = (output.argmax(dim=1) =
labels.to(device)).float().mean()
            pbar.set_postfix(loss=loss.item(),
accuracy=accuracy.item(), lr=optimizer.param_groups[0]
['lr'])
    # Validation
    model.eval()
    val_loss = 0
    val_accuracy = 0
    with torch.no_grad():
        for images, labels in valloader:
            images = images.view(-1, 28 * 28).to(device)
            output = model(images)
            val_loss += criterion(output,
labels.to(device)).item()
            val_accuracy += (
                (output.argmax(dim=1) =
labels.to(device)).float().mean().item()
    val_loss ⊨ len(valloader)
    val_accuracy ⊨ len(valloader)
    # Update learning rate
```

```
scheduler.step()
    print(
        f"Epoch {epoch + 1}, Val Loss: {val_loss}, Val
Accuracy: {val_accuracy}"
    )
# Print model weights
print("Trained Model Weights:")
for i, layer in enumerate(model.layers):
    print(f"Layer {i + 1}:")
    print("Spline Weights:")
    print(layer.spline_weight)
    print("Base Weights:")
    print(layer.base_weight)
    print()
# Save model weights (need to create KAN instance then
"torch.load")
torch.save(model.state_dict(), "kan_mnist_weights.pth")
# Save the entire model (just get with "torch.load")
torch.save(model, "kan_mnist_model.pth")
```

Model 訓練結果(MNIST)

```
100%| 938/938 [00:40<00:00, 23.07it/s, accuracy=1, loss=0.031, lr=0.000134] Epoch 10, Val Loss: 0.08577567627701677, Val Accuracy: 0.9750199044585988
```

有達到預期的準確度,單輪訓練也有訓練出 Accuracy = 1 的終極情況,總的來說代表調整後的代碼是正確工作的

• KAN 測試 (x * y)

```
import torch
import torch.nn as nn
from tqdm import tqdm

from EfficientKAN import KAN
```

```
def test_mul():
    kan = KAN([2, 3, 3, 1], base_activation=nn.Identity)
    optimizer = torch.optim.LBFGS(kan.parameters(),
lr=0.001)
    with tqdm(range(200)) as pbar:
        for i in pbar:
            loss, req_loss = None, None
            def closure():
                optimizer.zero_grad()
                x = torch.rand(1024, 2)
                y = kan(x, update_qrid=(i \% 20 = 0))
                assert y.shape = (1024, 1)
                nonlocal loss, reg_loss
                U = X[:, 0]
                v = x[:, 1]
                loss =
nn.functional.mse_loss(y.squeeze(-1), u * v)
                reg_loss = kan.regularization_loss(1, 0)
                (loss + 1e-5 * req_loss).backward()
                return loss + req_loss
            optimizer.step(closure)
            pbar.set_postfix(mse_loss=loss.item(),
req_loss=req_loss.item())
    for layer in kan.layers:
        print(layer.spline_weight)
    torch.save(kan, 'model/kan_multiple_model.pth')
    torch.save(kan.state_dict(),
"model/kan_multiple_weights.pth")
    # Test the trained model
    test_model(kan)
```

```
def test_model(model):
    model.eval()
    with torch.no_grad():
        test_x = torch.rand(1024, 2)
        test_y = model(test_x)
        u = test_x[:, 0]
        v = test_x[:, 1]
        expected_y = u * v
        test_loss =
nn.functional.mse_loss(test_y.squeeze(-1), expected_y)
        print(f"Test Loss: {test_loss.item():.4f}")
```

Model 訓練結果(x * y)

方法論合成 Grafcet 控制器電路

• 模型量化與權重輸出(輸出符合 Quartus 的 Weights · 並動態進行 Scaling 以避免 Quantize 完變成零)

```
import torch
import numpy as np

# Load the trained model
model = torch.load('model/kan_multiple_model.pth')
model.eval()

# Quantize the weights to fixed-point format with dynamic scaling
def quantize_weight(weight, scale):
    return (weight * scale).round().int().numpy()
```

```
# Convert to 16-bit signed hex
def to_hex_str(arr):
    return [format(x & 0xFFFF, '04X') for x in arr]
# Function to find dynamic scale
def find_dynamic_scale(weight, target_range=32767):
    max_val = torch.max(torch.abs(weight)).item()
    if max_val = 0:
        return 1
    return target_range / max_val
# Extract and quantize weights
layer_base_weights = []
layer_spline_weights = []
for i, layer in enumerate(model.layers):
    # Print statistics of weights before quantization
    print(f"Layer {i} base_weight min:
{layer.base_weight.min()}, max: {layer.base_weight.max()}")
    print(f"Layer {i} spline_weight min:
{layer.spline_weight.min()}, max:
{layer.spline_weight.max()}")
    # Determine dynamic scales
    base_scale = find_dynamic_scale(layer.base_weight)
    spline_scale = find_dynamic_scale(layer.spline_weight)
    print(f"Layer {i} base_scale: {base_scale}")
    print(f"Layer {i} spline_scale: {spline_scale}")
    # Quantize weights with dynamic scales
    base_weight = quantize_weight(layer.base_weight,
scale=base_scale).flatten()
    spline_weight = quantize_weight(layer.spline_weight,
scale=spline_scale).flatten()
    # Check if spline weights are being quantized to zero
    if np.all(spline_weight = 0):
        print(f"Warning: All spline weights in layer {i}
are quantized to zero.")
```

```
# Save weights to files
with open(f'weight2/base_weight_layer_{i}.txt', 'w') as
f:
    f.write('\n'.join(to_hex_str(base_weight)))
    with open(f'weight2/spline_weight_layer_{i}.txt', 'w')
as f:
    f.write('\n'.join(to_hex_str(spline_weight)))
```

A Warning

我 Quartus Prime 是選擇用實驗室的板子來進行預設的 FPGA 規格,下列的設計是可以用的(經過其他的驗證程式確認),但因為使用了大量的 PIN 腳,而 MAX10 預設的 PIN 腳不夠用,所以沒有辦法編譯成 MAX10 可用的電路規格,可能會需要優化,或是更換為比較簡易的測試資料(當前模型採用 MNIST Dataset 進行測試)。

• 方法論重構後之 KANLayer 實現 (KANLayer.v)

```
module KANLayer #(
    parameter IN_FEATURES = 784,
    parameter OUT_FEATURES = 64,
   parameter SCALE = 256, // Quantization scale factor
   parameter BASE_WEIGHT_FILE =
"C:/intelFPGA_lite/18.1/KAN/base_weight_layer_0.txt",
    parameter SPLINE_WEIGHT_FILE =
"C:/intelFPGA_lite/18.1/KAN/spline_weight_layer_0.txt"
)(
   input wire clk,
   input wire reset,
   input wire [7:0] in_data [0:IN_FEATURES-1], // Input
data
   output req [7:0] out_data [0:0UT_FEATURES-1] // Output
data
);
   // Weights stored in on-chip memory (BRAM)
```

```
reg signed [15:0] base_weights
[0:OUT_FEATURES*IN_FEATURES-1];
    reg signed [15:0] spline_weights
[0:OUT_FEATURES*IN_FEATURES-1];
    // Load weights from memory (initialization)
    initial begin
        $readmemh(BASE_WEIGHT_FILE, base_weights);
        $readmemh(SPLINE_WEIGHT_FILE, spline_weights);
    end
    // Output registers
    req signed [31:0] base_output [0:0UT_FEATURES-1];
   reg signed [31:0] spline_output [0:0UT_FEATURES-1];
   reg signed [31:0] total_output [0:0UT_FEATURES-1];
    integer i, j;
    // Forward pass
   always @(posedge clk or posedge reset) begin
        if (reset) begin
            for (i = 0; i < OUT\_FEATURES; i = i + 1) begin
                base_output[i] ≤ 0;
                spline_output[i] ≤ 0;
                total_output[i] ≤ 0;
            end
        end else begin
            for (i = 0; i < OUT_FEATURES; i = i + 1) begin
                base_output[i] \leq 0;
                spline_output[i] ≤ 0;
                for (j = 0; j < IN\_FEATURES; j = j + 1)
begin
                    base_output[i] ≤ base_output[i] +
in_data[j] * base_weights[i*IN_FEATURES + j];
                    spline_output[i] ≤ spline_output[i] +
in_data[j] * spline_weights[i*IN_FEATURES + j];
                end
                total_output[i] ≤ (base_output[i] +
spline_output[i]) / SCALE; // Combine and scale the
```

Success

更換測試資料以求可以將電路設計容納進去(學習 mulitplication:x * y)

• 方法論重構後之 KANLayer 實現(KANLayer.v)

```
module KANLinear #(parameter IN_FEATURES = 2, OUT_FEATURES
= 3, integer LAYER_NUM = 0) (
    input clk,
    input reset,
    input [15:0] data_in [IN_FEATURES-1:0],
    output reg [15:0] data_out [OUT_FEATURES-1:0]
);
    req [15:0] base_weight [OUT_FEATURES*IN_FEATURES-1:0];
    reg [15:0] spline_weight [OUT_FEATURES*IN_FEATURES-
1:0];
    reg [15:0] base_weight_2d [OUT_FEATURES-1:0]
[IN_FEATURES-1:0];
    req [15:0] spline_weight_2d [OUT_FEATURES-1:0]
[IN_FEATURES-1:0];
    integer i, j;
    initial begin
        if (LAYER_NUM = 0) begin
```

```
$readmemh("C:/intelFPGA_lite/18.1/KAN2/base_weight_layer_0.
txt", base_weight);
$readmemh("C:/intelFPGA_lite/18.1/KAN2/spline_weight_layer_
0.txt", spline_weight);
        end else if (LAYER_NUM = 1) begin
$readmemh("C:/intelFPGA_lite/18.1/KAN2/base_weight_layer_1.
txt", base_weight);
$readmemh("C:/intelFPGA_lite/18.1/KAN2/spline_weight_layer_
1.txt", spline_weight);
        end else if (LAYER_NUM = 2) begin
$readmemh("C:/intelFPGA_lite/18.1/KAN2/base_weight_layer_2.
txt", base_weight);
$readmemh("C:/intelFPGA_lite/18.1/KAN2/spline_weight_layer_
2.txt", spline_weight);
        end
        for (i = 0; i < OUT_FEATURES; i = i + 1) begin
            for (j = 0; j < IN\_FEATURES; j = j + 1) begin
                base_weight_2d[i][j] = base_weight[i *
IN_FEATURES + j];
                spline_weight_2d[i][j] = spline_weight[i *
IN_FEATURES + j];
            end
        end
    end
    always @(posedge clk or posedge reset) begin
        if (reset) begin
            for (i = 0; i < OUT\_FEATURES; i = i + 1) begin
                data_out[i] \leq 16'd0;
            end
        end else begin
            for (i = 0; i < OUT\_FEATURES; i = i + 1) begin
                data_out[i] \leq 16'd0;
```

ChatGPT 合成 Grafcet Datapath 電路

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• 方法論重構後之完整 Network 實現 (KAN.v)

```
module KAN (
    input wire clk,
    input wire reset,
    input wire [7:0] in_data [0:783], // 28x28 = 784
pixels, 8-bit each
    output wire [7:0] out_data [0:9] // 10 classes, 8-bit
each
```

```
);
    // Internal signals for each layer
    wire [7:0] layer1_out [0:63];
    wire [7:0] layer2_out [0:9];
    // Instantiate layers
    KANLayer #(
        .IN_FEATURES(784),
        .OUT_FEATURES(64),
.BASE_WEIGHT_FILE("C:/intelFPGA_lite/18.1/KAN/base_weight_l
ayer_0.txt"),
.SPLINE_WEIGHT_FILE("C:/intelFPGA_lite/18.1/KAN/spline_weig
ht_layer_0.txt")
    ) layer1 (
        .clk(clk),
        .reset(reset),
        .in_data(in_data),
        .out_data(layer1_out)
    );
    KANLayer #(
        .IN_FEATURES(64),
        .OUT_FEATURES(10),
.BASE_WEIGHT_FILE("C:/intelFPGA_lite/18.1/KAN/base_weight_l
ayer_1.txt"),
.SPLINE_WEIGHT_FILE("C:/intelFPGA_lite/18.1/KAN/spline_weig
ht_layer_1.txt")
    ) layer2 (
        .clk(clk),
        .reset(reset),
        .in_data(layer1_out),
        .out_data(layer2_out)
    );
    // Connect the final output
```

```
assign out_data = layer2_out;
endmodule
```

Success

更換測試資料以求可以將電路設計容納進去(學習 mulitplication:x * y)

• 方法論重構後之完整 Network 實現(KAN.v)

```
module KAN #(parameter IN_FEATURES = 2, L1_FEATURES = 3,
L2_FEATURES = 3, OUT_FEATURES = 1) (
    input clk,
    input reset,
    input [15:0] input_data [IN_FEATURES-1:0],
    output [15:0] output_data
);
    wire [15:0] layer1_out [L1_FEATURES-1:0];
    wire [15:0] layer2_out [L2_FEATURES-1:0];
    wire [15:0] layer3_out [OUT_FEATURES-1:0];
    KANLinear #(.IN_FEATURES(IN_FEATURES),
.OUT_FEATURES(L1_FEATURES), .LAYER_NUM(0)) layer1 (
        .clk(clk),
        .reset(reset),
        .data_in(input_data),
        .data_out(layer1_out)
    );
    KANLinear #(.IN_FEATURES(L1_FEATURES),
.OUT_FEATURES(L2_FEATURES), .LAYER_NUM(1)) layer2 (
        .clk(clk),
        .reset(reset),
        .data_in(layer1_out),
        .data_out(layer2_out)
    );
```

FPGA 整合驗證

```
♥Success

更換測試資料以求可以將電路設計容納進去(學習
mulitplication:x * y)
```

• Testbench 實現 (Testbench.v)

```
initial begin
    clk = 0;
    reset = 1;
    input_data[0] = 16'd0;
    input_data[1] = 16'd0;
   #10 reset = 0;
    // test data 1
    input_data[0] = 16'd50;
    input_data[1] = 16'd30;
    #10;
    $display("Output (Test 1): %d", output_data);
    // test data 2
    input_data[0] = 16'd100;
    input_data[1] = 16'd200;
    #10;
    $display("Output (Test 2): %d", output_data);
    // test data 3
    input_data[0] = 16'd150;
    input_data[1] = 16'd250;
    #10;
    $display("Output (Test 3): %d", output_data);
    // test data 4
    input_data[0] = 16'd75;
    input_data[1] = 16'd125;
    #10;
    $display("Output (Test 4): %d", output_data);
    // test data 5
    input_data[0] = 16'd175;
    input_data[1] = 16'd225;
    #10;
    $display("Output (Test 5): %d", output_data);
end
```

always #5 clk = ~clk;

endmodule

A Warning

硬體設計完仿真的結果如下,誤差老實說非常大,進行排查之後確認是權重的問題,因為 PyTorch 讀取 Quantize 後的權重結果一樣糟糕,可能會需要考慮導入可以計算小數的硬體來解決問題。

• ModelSim 仿真結果

