

# Compiling hierarchical block diagrams into CompCert

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These slides summarise the results of an ongoing research collaboration with Léo Brun, Pierre-Évariste Dagand, Xavier Leroy, Marc Pouzet, and Lionel Rieg.

7 February 2019, Coq Meetup, Paris

## The Lustre synchronous language

Vélus: A Lustre compiler verified in Coq

Translation: from NLustre to Obc

Optimization: control structure fusion

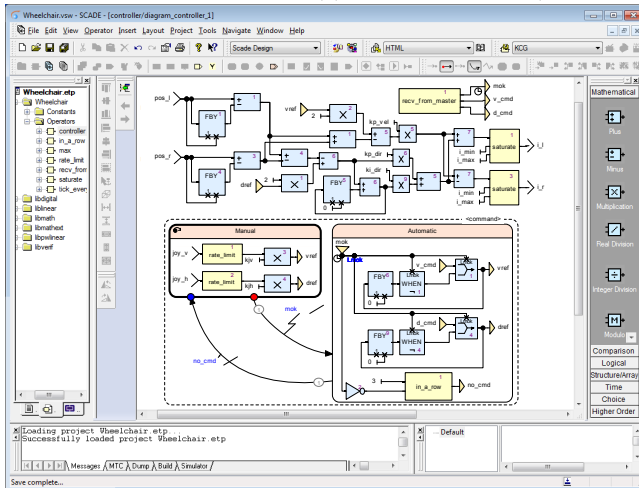
Generation: from Obc to Clight

Main theorem and experimental results

Conclusion

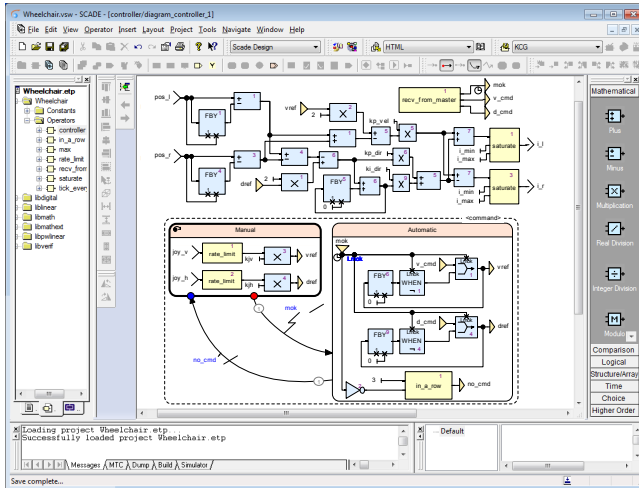
# Executable block-diagrams = “Model-Based Development”

Scade Suite — <http://www.ansys.com/...>



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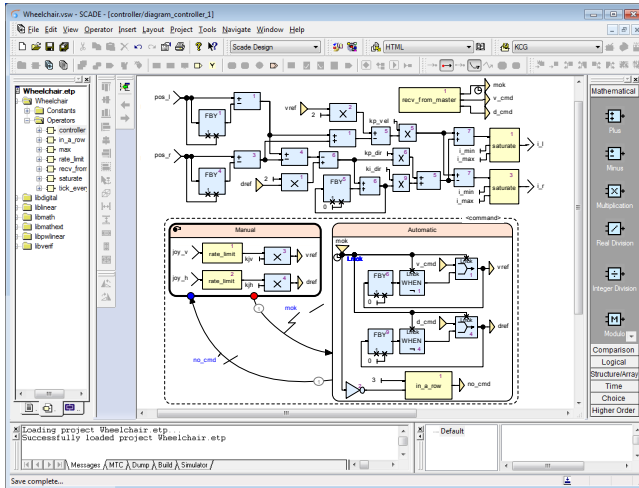
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block/node = system  
line = signal

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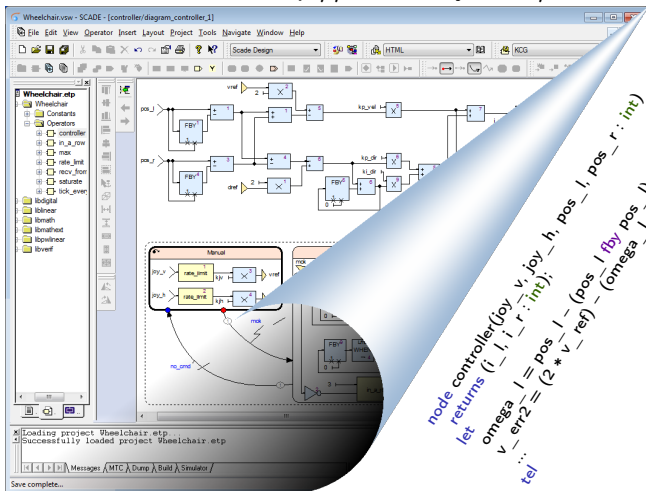
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block/node = system = stream function  
line = signal = flow of values

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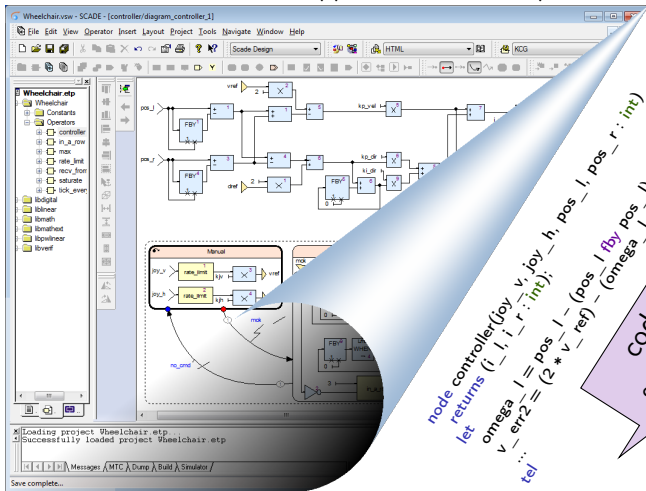
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block/node = system = stream function  
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# Executable block-diagrams = “Model-Based Development”

Scade Suite — <http://www.ansys.com/...>



```
node controller(joy_v, joy_h, pos_l, pos_r : int)
let
  omega_l = pos_l - (pos_l - ref) - (omega_l + omega_r);
  v - err2 = (2 * v - ref) - (omega_l + omega_r);
tel
```

code  
generator

sequential program  
(C, Ada, assembly)

block/node = system = stream function  
line = signal = flow of values

# What is Lustre?

- A language for programming cyclic control software.

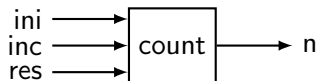
```
every trigger {  
    read inputs;  
    calculate; // and update internal state  
    write outputs;  
}
```

- A language for *programming* transition systems

- » ...+ functional abstraction
- » ...+ conditional activations
- » ...+ efficient (modular) compilation

- A restriction of Kahn process networks [Kahn (1974): The Semantics of a Simple Language for Parallel Programming],  
guaranteed to execute in bounded time and space.





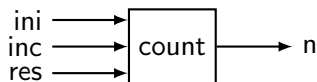
```
node count (ini, inc: int; res: bool)
returns (n: int)
let
  n = if (true fby false) or res then ini
      else (0 fby n) + inc;
tel
```



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```



ini	0	0	0	0	0	0	0	...
inc	0	1	2	1	2	3	0	...
res	F	F	F	F	T	F	F	...
true fby false	T	F	F	F	F	F	F	...
0 fby n	0	0	1	3	4	0	3	...
n	0	1	3	4	0	3	3	...

- Node: set of causal equations (variables at left).
- Semantic model: synchronized streams of values.
- A node defines a function between input and output streams.

# Lustre: instantiation and sampling

```
node avgvelocity(delta: int; sec: bool) returns (r, v: int)
  var t : int;
let
  r = count(0, delta, false);
  t = count((1, 1, false) when sec);
  v = merge sec ((r when sec) / t) ((0 fby v) when not sec);
tel
```

# Lustre: instantiation and sampling

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delta	0	1	2	1	2	3	0	3	...
sec	F	F	F	T	F	T	T	F	...

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tel
```

delta	0	1	2	1	2	3	0	3	...
sec	F	F	F	T	F	T	T	F	...
r	0	1	3	4	6	9	9	12	...
(c <sub>1</sub> )	0	0	1	3	4	6	9	9	...

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(c <sub>1</sub> )	0	0	1	3	4	6	9	9	...
r when sec				4		9	9		...
t				1		2	3		...
(c <sub>2</sub> )				0		1	2		...



# Lustre: instantiation and sampling

```

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```

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t				1		2	3		...
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(c <sub>1</sub> )	0	0	1	3	4	6	9	9	...
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(0 fby v) when not sec	0	0	0		4			3	...
v	0	0	0	4	4	4	3	3	...

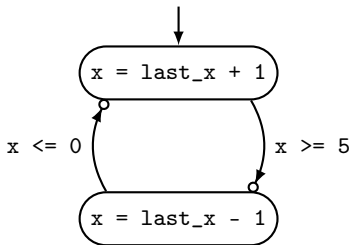
# Sampling and merging: what for?

- Provides a means of conditional activation,
- and a target for sophisticated structures [ Colaço, Pagano, and Pouzet (2005): A Conservative Extension of Synchronous Data-flow with State Machines ].

```
node main (go : bool)
  returns (x : int)
  var last_x : int;
let
  last_x = 0 fby x;

  automaton
  state Up
    do x = last_x + 1
    until x >= 5 then Down

  state Down
    do x = last_x - 1
    until x <= 0 then Up
  end;
tel
```



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```
  var last_x : int;
```

```
let
```

```
  last_x = 0 fby x;
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```
  automaton
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    state Up
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```
      do x = last_x + 1
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```
      until x >= 5 then Down
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```
    state Down
```

```
      do x = last_x - 1
```

```
      until x <= 0 then Up
```

```
  end;
```

```
tel
```

```
type st = St_Up | St_Down
```

```
(* ... *)
```

```
last_x = 0 fby x
```

```
x_St_Down = (last_x when St_Down(ck)) - 1
```

```
x_St_Up = (last_x when St_Up(ck)) + 1
```

```
x = merge ck (St_Down: x_St_Down)  
              (St_Up: x_St_Up);
```

```
ck = St_Up fby ns
```

```
ns = ...
```

# Lustre-N: langage flots de données

## Expressions

$e ::=$	$x$	variables
	$k$	constants
	$\diamond e$	unary operators
	$e \oplus e$	binary operators
	$e \text{ when } (x = k)$	sampling
$ce ::=$	$\text{merge } x \text{ } ce_t \text{ } ce_f$	binary merge
	$\text{if } e \text{ then } ce_t \text{ else } ce_f$	multiplexors
	$e$	simple expressions

## Equations

$eq ::=$	$x =^{ck} ce$
	$x =^{ck} k_0 \text{ fby } e$
	$x =^{ck} f(e, \dots, e)$

## Nodes

**node**  $f (x : \tau)$  **returns**  $(x : \tau)$   
**var**  $x : \tau, \dots, x : \tau$   
**let**  $eq; \dots; eq$  **tel**

## Clocks

$ck ::= \text{base} \mid ck \text{ on } (x = k)$

# Lustre: syntax and semantics

```

node count (ini, inc: int; res: bool)
returns (n: int)
let
  n = if (true fby false) or res then ini
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```

ini	0	0	0	0	0	0	0	...
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```
Inductive clock : Set :=
| Cbase : clock
| Con   : clock → ident → bool → clock.
```

```
Inductive lexp : Type :=
| Econst : const → lexp
| Evar   : ident → type → lexp
| Ewhen  : lexp → ident → bool → lexp
| Eunop  : unop → lexp → type → lexp
| Ebinop : binop → lexp → lexp → type → lexp.
```

```
Inductive cexp : Type :=
| Emerge : ident → cexp → cexp → cexp
| Eite    : lexp → cexp → cexp → cexp
| Eexp    : lexp → cexp.
```

```
Inductive equation : Type :=
| EqDef : ident → clock → cexp → equation
| EqApp : idsents → clock → ident → lexs → equation
| EqFby : ident → clock → const → lexp → equation.
```

```
Record node : Type := mk_node {
  n_name : ident;
  n_in   : list (ident * (type * clock));
  n_out  : list (ident * (type * clock));
  n_vars : list (ident * (type * clock));
  n_eqs  : list equation;

  n_defd : Permutation (vars_defined n_eqs)
    (map fst (n_vars ++ n_out));
  n_nodup : NoDupMembers (n_in ++ n_vars ++ n_out);
  ... }.

```

ini	0	0	0	0	0	0	0	...
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Inductive equation : Type :=
| EqDef : ident → clock → cexp → equation
| EqApp : ident → clock → ident → lexp → equation
| EqFby : ident → clock → const → lexp → equation.
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  n_eqs  : list equation;

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    (map fst (n_vars ++ n_out));
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```

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0 fby n	0	0	1	3	4	0	3	...
n	0	1	3	4	0	3	3	...

```
Inductive sem_node (G: global) :
  ident → stream (list value) → stream (list value) → Prop :=
| SNode:
  find_node f G = Some n →
  clock_of xss bk →
  sem_vars bk H (map fst n.(n_in)) xss →
  sem_vars bk H (map fst n.(n_out)) yss →
  sem_clocked_vars bk H (idck n.(n_in)) →
  Forall (sem_equation G bk H) n.(n_eqs) →
  sem_node G f xss yss.
```



# Lustre: syntax and semantics

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```

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Inductive equation : Type :=
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  sem_clocked_vars bk H (idck n.(n_in)) →
  Forall (sem_equation G bk H) n.(n_eqs) →
  sem_node G f xss yss.
```

$\text{sem\_node } G \ f \ xss \ yss$



$f : \text{stream}(T^+) \rightarrow \text{stream}(T^+)$

## The Lustre synchronous language

### Vélus: A Lustre compiler verified in Coq

- Translation: from NLustre to Obc

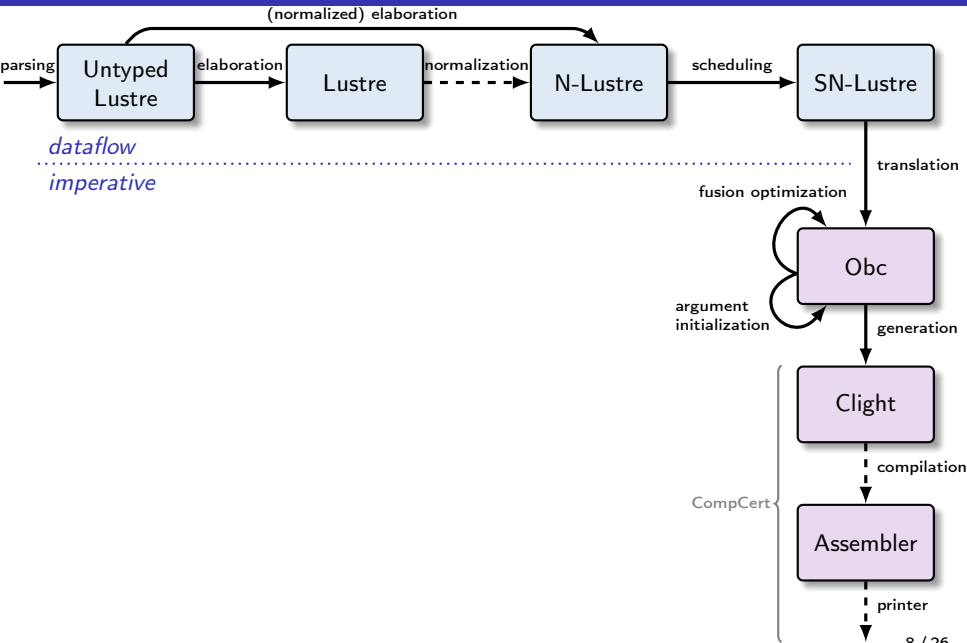
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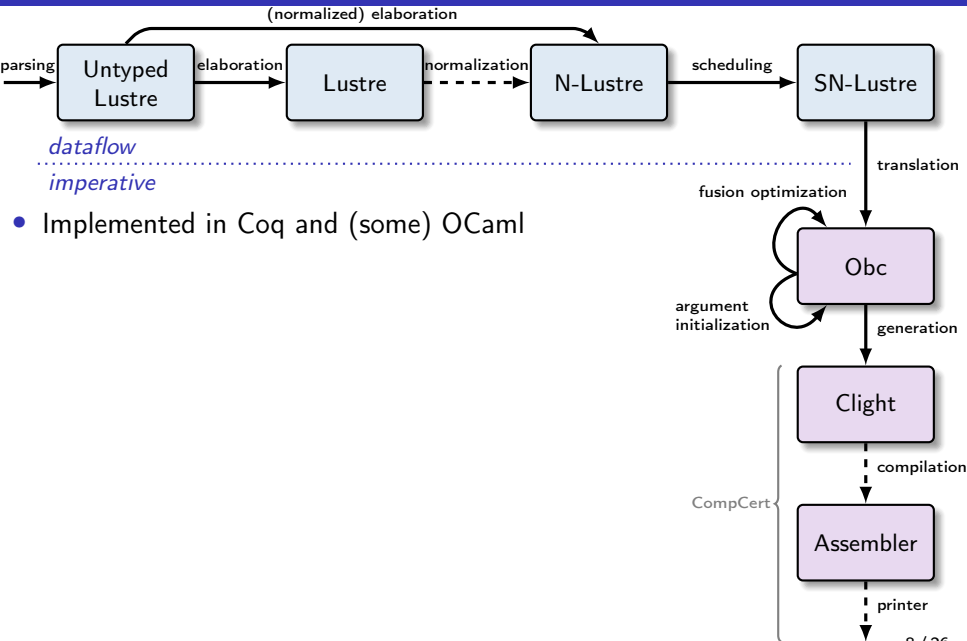
- Main theorem and experimental results

## Conclusion

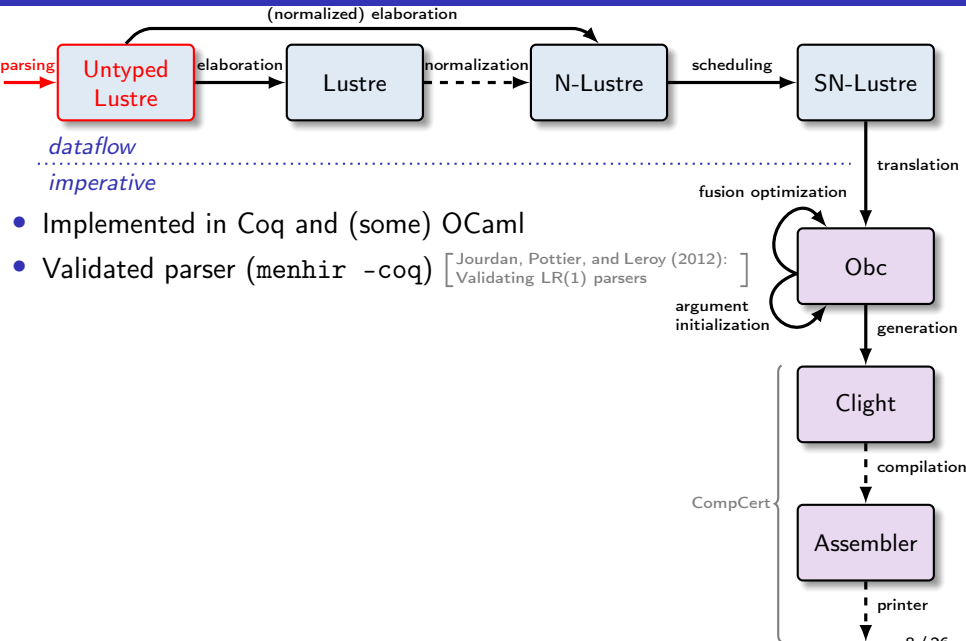
# The Vélus Lustre Compiler



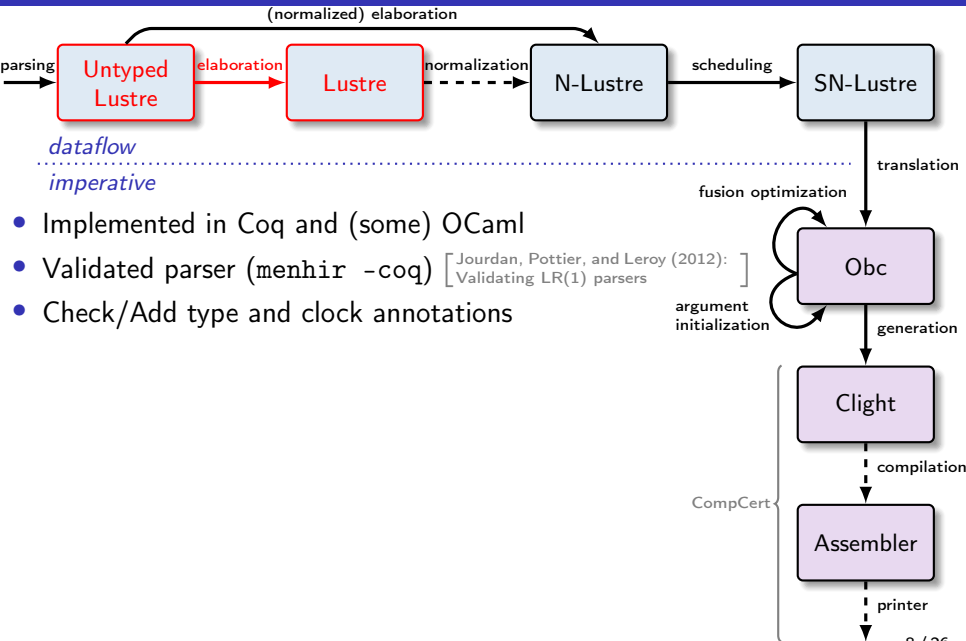
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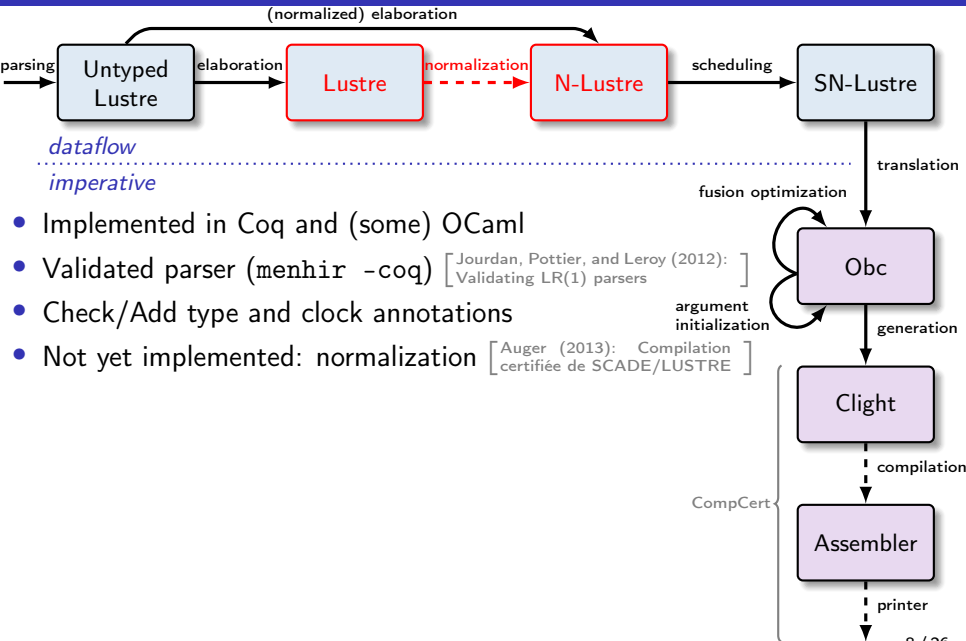
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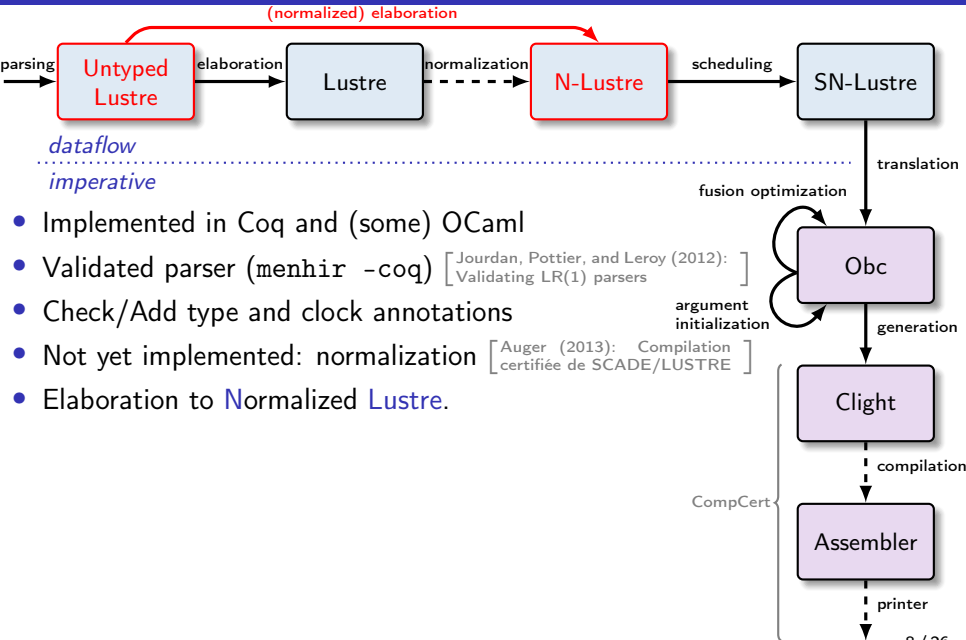
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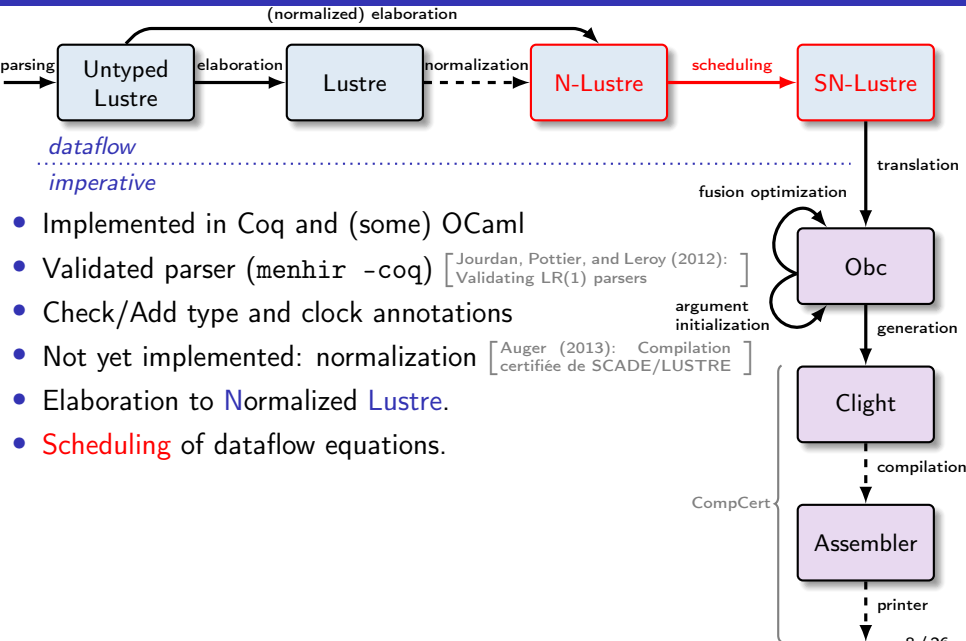


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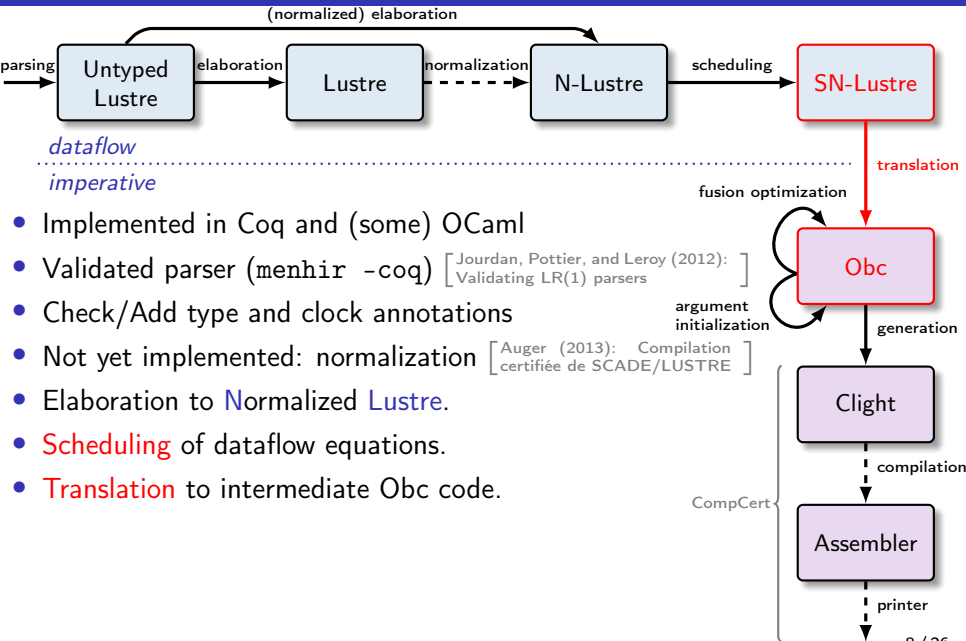




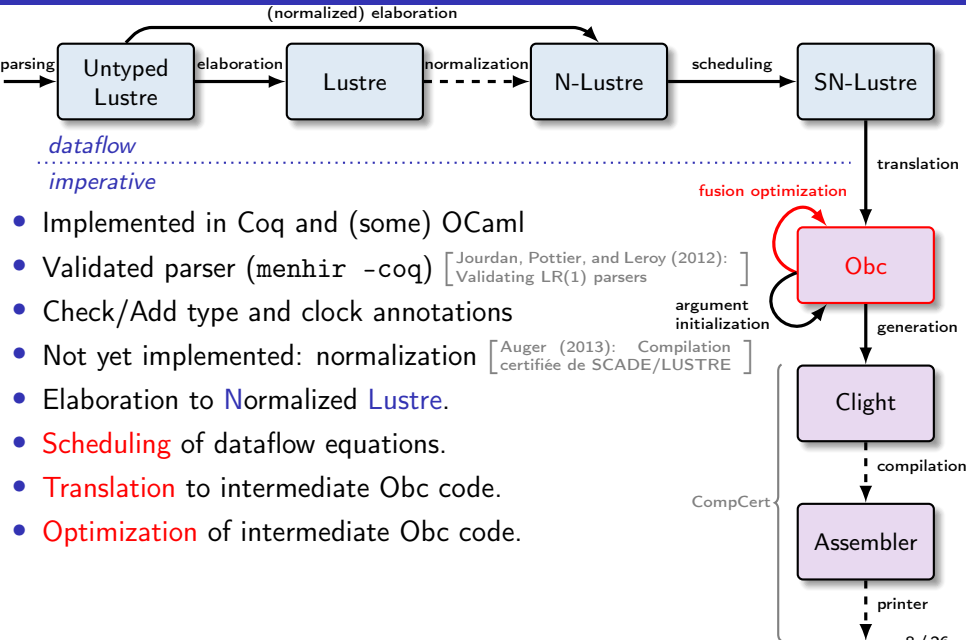
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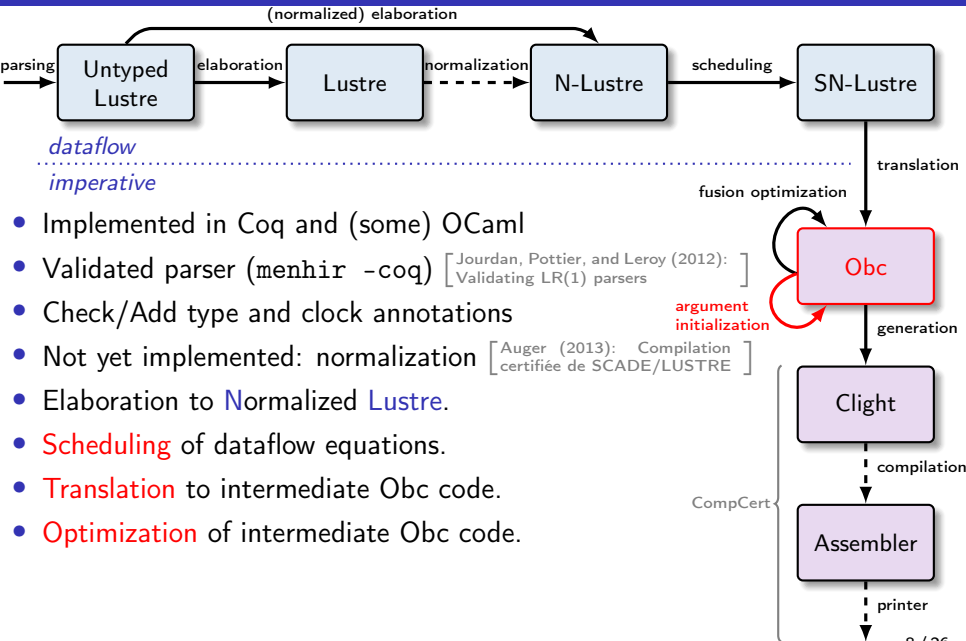
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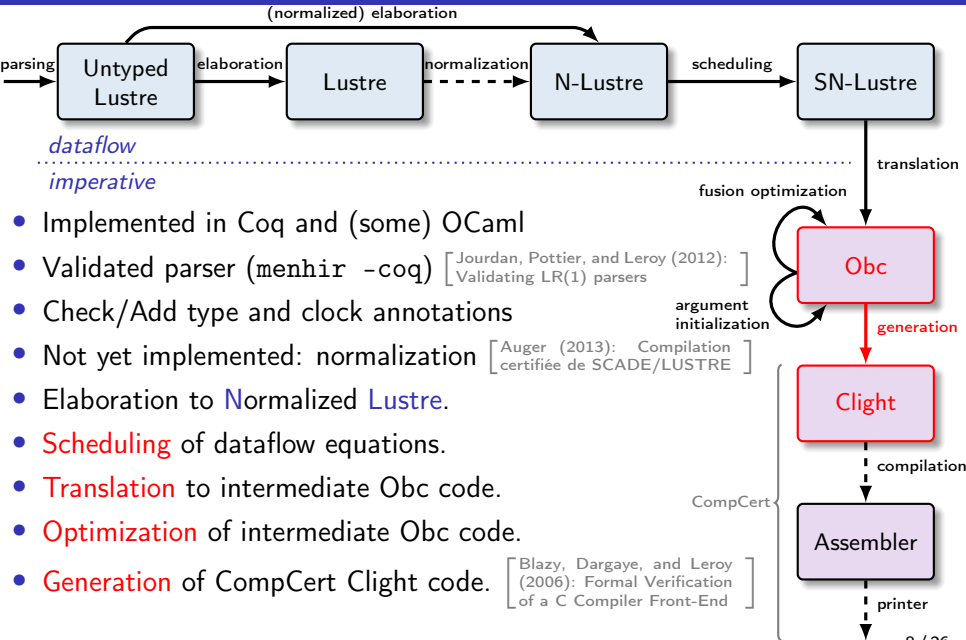
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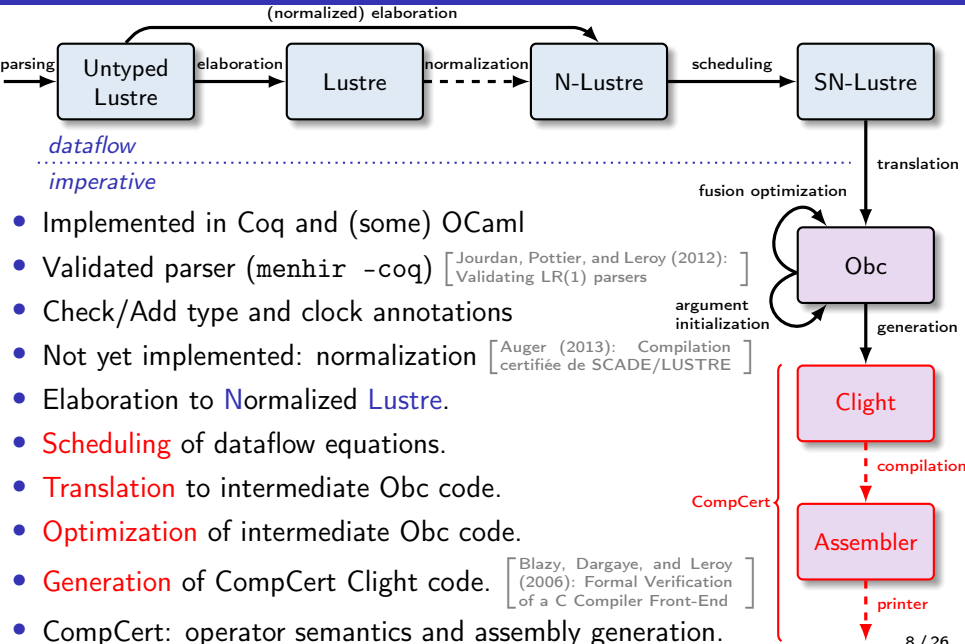
# The Vélus Lustre Compiler



# The Vélus Lustre Compiler



# The Vélus Lustre Compiler



# Lustre Compilation: normalization and scheduling

```
node count (ini, inc: int; res: bool)
returns (n: int)
let
  n = if (true fby false) or res then ini
       else (0 fby n) + inc;
tel
```

# Lustre Compilation: normalization and scheduling

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node count (ini, inc: int; res: bool)
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tel
```

normalization



```
node count (ini, inc: int; res: bool)
returns (n: int)
var f : bool; c : int;
let
  f = true fby false;
  c = 0 fby n;
  n = if f or res then ini else c + inc;
tel
```

## Normalization

- Rewrite to put each **fby** in its own equation.
- Introduce fresh variables using the substitution principle.



# Lustre Compilation: normalization and scheduling

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normalization

```
node count (ini, inc: int; res: bool)
returns (n: int)
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let
  f = true fby false;
  c = 0 fby n;
  n = if f or res then ini else c + inc;
tel
```

## Scheduling

- The semantics is independent of equation ordering; but not the correctness of imperative code translation.
- Reorder so that
  - » 'Normals' variables are written before being read, ... and
  - » 'fby' variables are read before being written.

scheduling

```
node count (ini, inc: int; res: bool)
returns (n: int)
var f : bool; c : int;
let
  n = if f or res then ini else c + inc;
  f = true fby false;
  c = 0 fby n;
tel
```

# Compiling Lustre: Translation to imperative code

```
node avgvelocity(delta: int; sec: bool)
returns (r, v: int)
var t, w: int;
let
  r = count(0, delta, false);
  t = count((1, 1, false) when sec);
  v = merge sec ((r when sec) / t)
              (w when not sec);
  w = 0 fby v;
tel
```

[Biernacki, Colaço, Hamon, and Pouzet  
(2008): Clock-directed modular code generation for synchronous data-flow languages]

```
class avgvelocity {
  memory w : int;
  class count o1, o2;
```

```
  reset() {
    count.reset o1;
    count.reset o2;
    state(w) := 0
  }
```

```
  step(delta: int, sec: bool) returns (r, v: int)
  { var t : int;
```

```
    r := count.step o1 (0, delta, false);
    if sec
      then t := count.step o2 (1, 1, false);
    if sec
      then v := r / t else v := state(w);
    state(w) := v
  }
```

# Compiling Lustre: Translation to imperative code

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node avgvelocity(delta: int; sec: bool)
returns (r, v: int)
var t, w: int;
let
  r = count(0, delta, false);
  t = count((1, 1, false) when sec);
  v = merge sec ((r when sec) / t)
              (w when not sec);
  w = 0 fby v;
tel
```

[Biernacki, Colaço, Hamon, and Pouzet  
(2008): Clock-directed modular code generation for synchronous data-flow languages]

```
class avgvelocity {
  memory w : int;
  class count o1, o2;
```

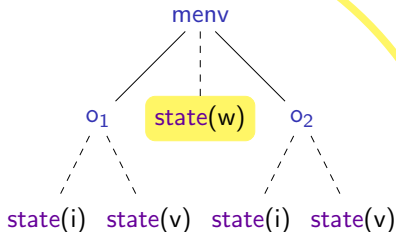
```
  reset() {
    count.reset o1;
    count.reset o2;
    state(w) := 0
  }
```

```
  step(delta: int, sec: bool) returns (r, v: int)
  { var t : int;

    r := count.step o1 (0, delta, false);
    if sec
      then t := count.step o2 (1, 1, false);
    if sec
      then v := r / t else v := state(w);
    state(w) := v
  }
```

# Compiling Lustre: Translation to imperative code

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node avgvelocity(delta: int; sec: bool)
returns (r, v: int)
var t, w: int;
let
  r = count(0, delta, false);
  t = count((1, 1, false) when sec);
  v = merge sec ((r when sec) / t)
              (w when not sec);
  w = 0 fby v;
tel
```



```
class avgvelocity {
  memory w : int;
  class count o1, o2;

  reset() {
    count.reset o1;
    count.reset o2;
    state(w) := 0
  }
}
```

```
step(delta: int, sec: bool) returns (r, v: int)
{ var t : int;

  r := count.step o1 (0, delta, false);
  if sec
    then t := count.step o2 (1, 1, false);
  if sec
    then v := r / t else v := state(w);
  state(w) := v
}
```

# Compiling Lustre: Translation to imperative code

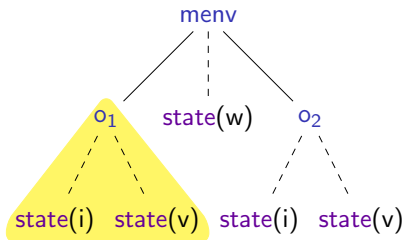
```
node avgvelocity(delta: int; sec: bool)
returns (r, v: int)
var t, w: int;
let
  r = count(0, delta, false);
  t = count((1, 1, false) when sec);
  v = merge sec ((r when sec) / t)
              (w when not sec);
  w = 0 fby v;
tel
```

```
class avgvelocity {
  memory w : int;
  class count o1, o2;
```

```
  reset() {
    count.reset o1;
    count.reset o2;
    state(w) := 0
  }
```

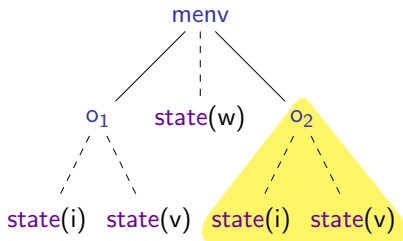
```
  step(delta: int, sec: bool) returns (r, v: int)
  { var t : int;
```

```
    r := count.step o1 (0, delta, false);
    if sec
      then t := count.step o2 (1, 1, false);
    if sec
      then v := r / t else v := state(w);
    state(w) := v
  }
```



# Compiling Lustre: Translation to imperative code

```
node avgvelocity(delta: int; sec: bool)
returns (r, v: int)
var t, w: int;
let
  r = count(0, delta, false);
  t = count((1, 1, false) when sec);
  v = merge sec ((r when sec) / t)
            (w when not sec);
  w = 0 fby v;
tel
```



```
class avgvelocity {
  memory w : int;
  class count o1, o2;
```

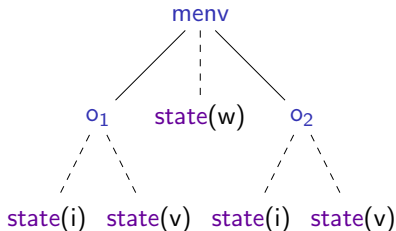
```
  reset() {
    count.reset o1;
    count.reset o2;
    state(w) := 0
  }
```

```
  step(delta: int, sec: bool) returns (r, v: int)
  { var t : int;
```

```
    r := count.step o1 (0, delta, false);
    if sec
      then t := count.step o2 (1, 1, false);
    if sec
      then v := r / t else v := state(w);
    state(w) := v
  }
```

# Compiling Lustre: Translation to imperative code

```
node avgvelocity(delta: int; sec: bool)
returns (r, v: int)
var t, w: int;
let
  r = count(0, delta, false);
  t = count((1, 1, false) when sec);
  v = merge sec ((r when sec) / t)
              (w when not sec);
  w = 0 fby v;
tel
```



```
class avgvelocity {
  memory w : int;
  class count o1, o2;
```

```
  reset() {
    count.reset o1;
    count.reset o2;
    state(w) := 0
  }
```

```
  step(delta: int, sec: bool) returns (r, v: int)
  { var t : int;
```

```
    r := count.step o1 (0, delta, false);
    if sec
    then t := count.step o2 (1, 1, false);
    if sec
    then v := r / t else v := state(w);
    state(w) := v
  }
```

# Compiling Lustre: Translation to imperative code

```
node avgvelocity(delta: int; sec: bool)
returns (r, v: int)
var t, w: int;
let
  r = count(0, delta, false);
  t = count((1, 1, false) when sec);
  v = merge sec ((r when sec) / t)
              (w when not sec);
  w = 0 fby v;
tel
```

```
Inductive memory (A: Type): Type :=
mk_memory {
  mm_values : PM.t A;
  mm_instances : PM.t (memory A)
}.

```

```
Definition obc_memory :=
memory (const).
```

```
class avgvelocity {
  memory w : int;
  class count o1, o2;
```

```
  reset() {
    count.reset o1;
    count.reset o2;
    state(w) := 0
  }
```

```
  step(delta: int, sec: bool) returns (r, v: int)
  { var t : int;
```

```
    r := count.step o1 (0, delta, false);
    if sec
      then t := count.step o2 (1, 1, false);
    if sec
      then v := r / t else v := state(w);
    state(w) := v
  }
```

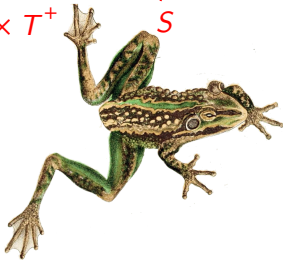


# Compiling Lustre: Translation to imperative code

```
node avgvelocity(delta: int; sec: bool)
returns (r, v: int)
var t, w: int;
let
  r = count(0, delta, false);
  t = count((1, 1, false) when sec);
  v = merge sec ((r when sec) / t)
              (w when not sec);
  w = 0 fby v;
tel
```

$(f_t, s_0)$

$S \times T^+ \rightarrow S \times T^+ \quad S$



```
class avgvelocity {
  memory w : int;
  class count o1, o2;
```

```
  reset() {
    count.reset o1;
    count.reset o2;
    state(w) := 0
  }
```

```
  step(delta: int, sec: bool) returns (r, v: int)
  { var t : int;
```

```
    r := count.step o1 (0, delta, false);
    if sec
      then t := count.step o2 (1, 1, false);
    if sec
      then v := r / t else v := state(w);
    state(w) := v
  }
```

# Obc: simple imperative language

$e ::=$	$x$	variables
	$\text{st}(x)$	memories
	$c$	constants
	$\diamond e$	unary operators
	$e \oplus e$	binary operators
	$\langle e \rangle$	validity assertions
$s ::=$	$x := e$	variable assignments
	$\text{st}(x) := e$	memory assignments
	$\text{if } e \{s\} \text{ else } \{s\}$	conditional branchings
	$s ; s$	sequential compositions
	$x, \dots, x := \text{cl.m } i \ (e, \dots, e)$	method calls
	$\text{skip}$	nop

$p, me, ve \vdash s \Downarrow (me', ve')$

$me : \text{memory}$

$ve : \text{ident} \rightarrow \text{option val}$

**Inductive** memory (A: Type): Type :=  
mk\_memory {  
  mm\_values : PM.t A;  
  mm\_instances : PM.t (memory A)  
}.

# Implementation of translation

- Translation pass: small set of functions on abstract syntax.
- Challenge: going from one semantic model to another.

```
Definition tovar (x: ident) : exp :=  
  if PS.mem x memories then State x else Var x.
```

```
Fixpoint Control (ck: clock) (s: stmt) : stmt :=  
  match ck with  
  | Cbase => s  
  | Con ck x true => Control ck (Ifte (tovar x) s Skip)  
  | Con ck x false => Control ck (Ifte (tovar x) Skip s)  
end.
```

```
Fixpoint translate_lexp (e : lexp) : exp :=  
  match e with  
  | Econst c => Const c  
  | Evar x => tovar x  
  | Ewhen e c x => translate_lexp e  
  | Eop op es => Op op (map translate_lexp es)  
end.
```

```
Fixpoint translate_cexp (x: ident) (e: cexp) : stmt :=  
  match e with  
  | Emerge y t f => Ifte (tovar y) (translate_cexp x t)  
    (translate_cexp x f)  
  | Eexp l => Assign x (translate_lexp l)  
end.
```

```
Definition translate_eqn (eqn: equation) : stmt :=  
  match eqn with  
  | EqDef x ck ce => Control ck (translate_cexp x ce)  
  | EqApp x ck f les => Control ck (Step_ap x f x (map translate_lexp les))  
  | EqFby x ck v le => Control ck (AssignSt x (translate_lexp le))  
end.
```

```
Definition translate_eqns (eqns: list equation) : stmt :=  
  fold_left (fun i eq => Comp (translate_eqn eq) i) eqns Skip.
```

```
Definition translate_reset_eqn (s: stmt) (eqn: equation) : stmt :=  
  match eqn with  
  | EqDef _ _ => s  
  | EqFby x _ v0 _ => Comp (AssignSt x (Const v0)) s  
  | EqApp x _ f _ => Comp (Reset_ap f x) s  
end.
```

```
Definition translate_reset_eqns (eqns: list equation): stmt :=  
  fold_left translate_reset_eqn eqns Skip.
```

```
Definition ps_from_list (l: list ident) : PS.t :=  
  fold_left (fun s i => PS.add i s) l PS.empty.
```

```
Definition translate_node (n: node): class :=  
  let names := gather_eqs n.(n_eqs) in  
  let mems := ps_from_list (fst names) in  
  mk_class n.(n_name) n.(n_input) n.(n_output)  
    (fst names) (snd names)  
    (translate_eqns mems n.(n_eqs))  
    (translate_reset_eqns n.(n_eqs)).
```

```
Definition translate (G: global) : program := map translate_node G.
```

# Translation: definition

**Variable** mems : PS.t.

**Definition** tovar (x: ident) : exp := if PS.mem x mems then State x else Var x.

**Fixpoint** Control (ck: clock) (s: stmt) : stmt :=

  match ck with

  | Cbase  $\Rightarrow$  s

  | Con ck x true  $\Rightarrow$  Control ck (Ifte (tovar x) s Skip)

  | Con ck x false  $\Rightarrow$  Control ck (Ifte (tovar x) Skip s)

end.

**Fixpoint** translate\_cexp (x: ident) (e : cexp) {struct e} : stmt :=

  match e with

  | Emerge y t f  $\Rightarrow$  Ifte (tovar y) (translate\_cexp x t) (translate\_cexp x f)

  | Eexp l  $\Rightarrow$  Assign x (translate\_lexp l)

end.

**Definition** translate\_eqn (eqn: equation) : stmt :=

  match eqn with

  | EqDef x (CAexp ck ce)  $\Rightarrow$  Control ck (translate\_cexp x ce)

  | EqApp x f (LAexp ck le)  $\Rightarrow$  Control ck (Step\_ap x f x (translate\_lexp le))

  | EqFby x v (LAexp ck le)  $\Rightarrow$  Control ck (AssignSt x (translate\_lexp le))

end.

# Translation: definition

**Variable** mems : PS.t.

**Definition** tovar (x: ident) : exp := if PS.mem x mems then State x else Var x.

**Fixpoint** Control (ck: clock) (s: stmt) : stmt :=

  match ck with

  | Cbase  $\Rightarrow$  s

  | Con ck x true  $\Rightarrow$  Control ck (Ifte (tovar x) s Skip)

  | Con ck x false  $\Rightarrow$  Control ck (Ifte (tovar x) Skip s)

end.

**Fixpoint** translate\_cexp (x: ident)(e : cexp) {struct e} : stmt := ...

**Definition** translate\_eqn (eqn: equation) : stmt :=

  match eqn with

  | EqDef x (CAexp ck ce)  $\Rightarrow$  Control ck (translate\_cexp x ce)

  | EqApp x f (LAexp ck le)  $\Rightarrow$  Control ck (Step\_ap x f x (translate\_lexp le))

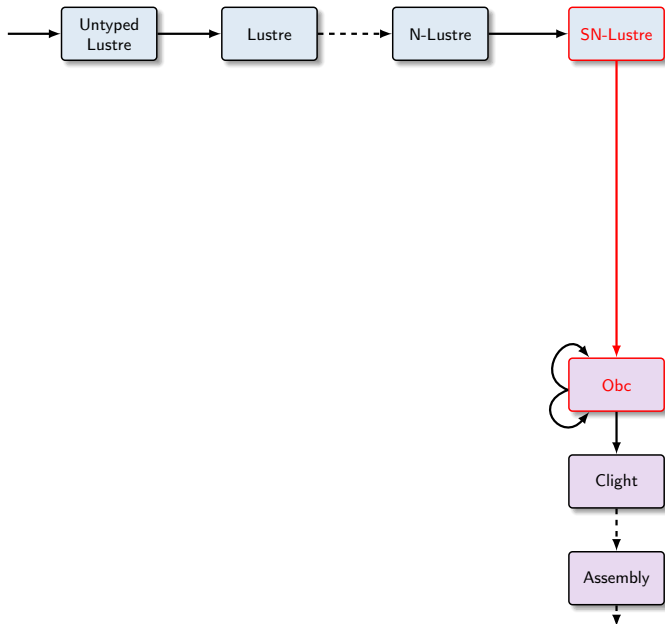
  | EqFby x v (LAexp ck le)  $\Rightarrow$  Control ck (AssignSt x (translate\_lexp le))

end.

**Definition** translate\_eqns (eqns: list equation): stmt :=

  List.fold\_left (fun i eq  $\Rightarrow$  Comp (translate\_eqn eq) i) eqns Skip.

# Correctness of the translation to Obc



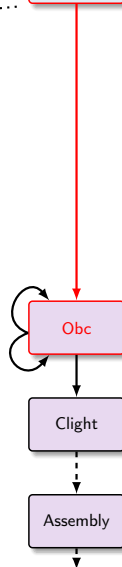
# Correctness of the translation to Obc



`sem_node G f xss yss`

$\text{stream}(T_i) \rightarrow \text{stream}(T_o)$

x	$x_0$	$x_1$	$x_2$	$x_3$	...
y	$y_0$	$y_1$	$y_2$	$y_3$	...
pre x	nil	$x_0$	$x_1$	$x_2$	...
$x + y$	$x_0 + y_0$	$x_1 + y_1$	$x_2 + y_2$	$x_3 + y_3$	...



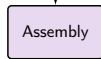
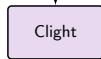
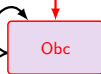
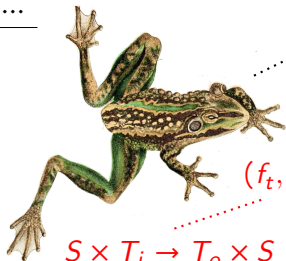
# Correctness of the translation to Obc



$\text{sem\_node } G \text{ f xss yss}$

$\text{stream}(T_i) \rightarrow \text{stream}(T_o)$

x	$x_0$	$x_1$	$x_2$	$x_3$	...
y	$y_0$	$y_1$	$y_2$	$y_3$	...
pre x	nil	$x_0$	$x_1$	$x_2$	...
$x + y$	$x_0 + y_0$	$x_1 + y_1$	$x_2 + y_2$	$x_3 + y_3$	...



$(f_t, s_0)$   
 $S \times T_i \rightarrow T_o \times S$



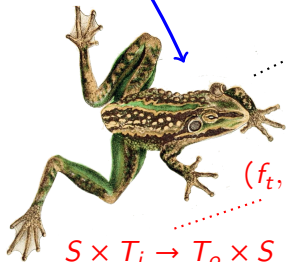
# Correctness of the translation to Obc



$\text{sem\_node } G \text{ f xss yss}$

$\text{stream}(T_i) \rightarrow \text{stream}(T_o)$

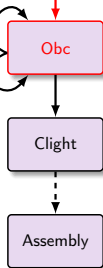
too weak for a direct proof by  
induction  $\times$



$(f_t, s_0)$

$S \times T_i \rightarrow T_o \times S$

$S$



# Correctness of the translation to Obc



$\text{sem\_node } G \text{ f xss yss}$

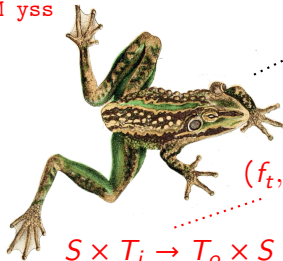
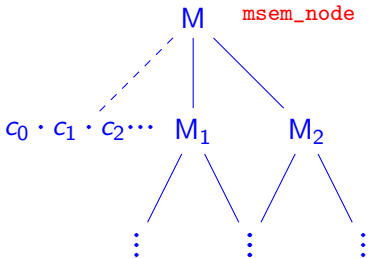
$\text{stream}(T_i) \rightarrow \text{stream}(T_o)$

Inductive memory (A: Type): Type := mk memory {  
 mm\_values : PM.t A;  
 mm\_instances : PM.t (memory A)  
 }.

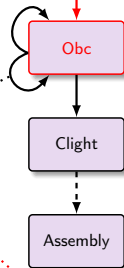
Definition memory := memory (stream const).



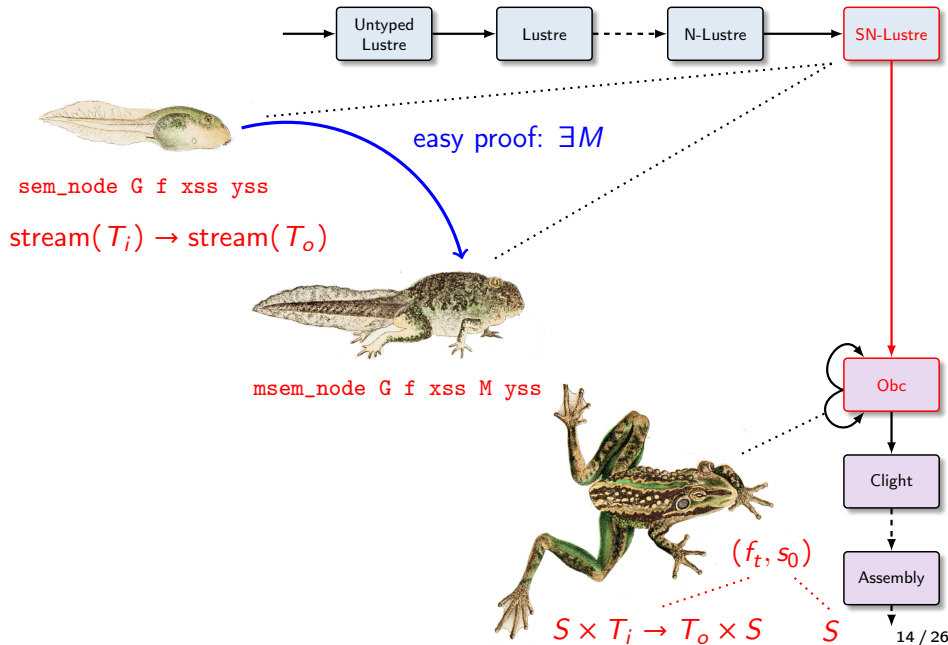
$\text{msem\_node } G \text{ f xss M yss}$



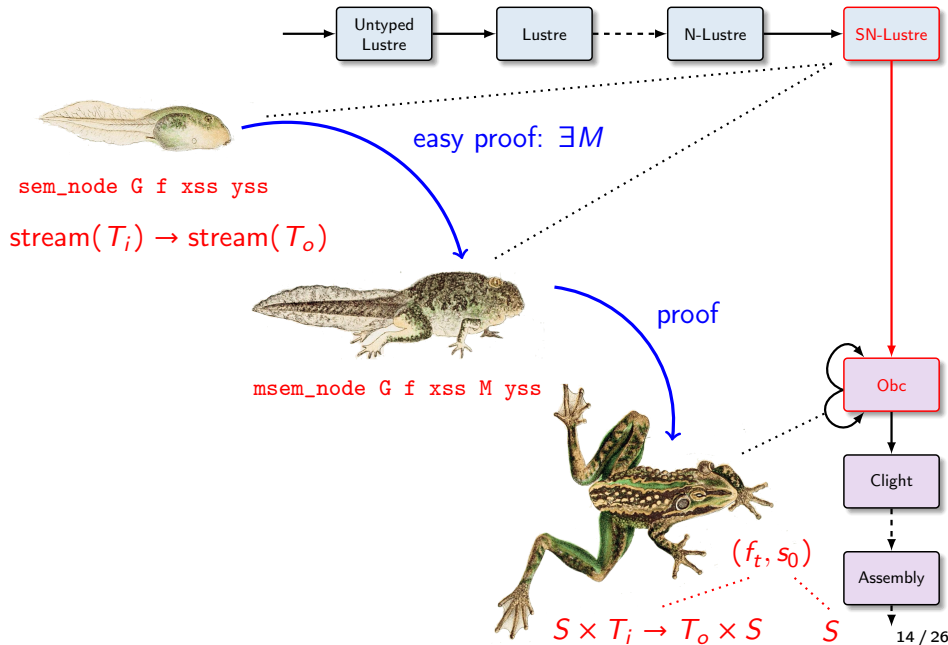
$(f_t, s_0)$   
 $S \times T_i \rightarrow T_o \times S$



# Correctness of the translation to Obc



# Correctness of the translation to Obc



# Correctness of the translation to Obc

induction n



└ induction G

└ induction eqs

└ case:  $x = (ce)^{ck}$

└└ case: present

└└ case: absent

└ case:  $x = (f\ e)^{ck}$

└└ case: present

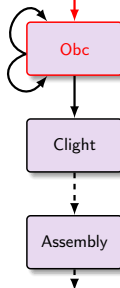
└└ case: absent

└ case:  $x = (k\ fby\ e)^{ck}$

└└ case: present

└└ case: absent

- Tricky proof, many technicalities.
- $\approx 100$  lemmas
- Several iterations to find the right definitions.
- The intermediate model is central.



# Correctness of the translation to Obc

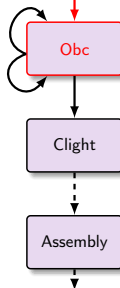
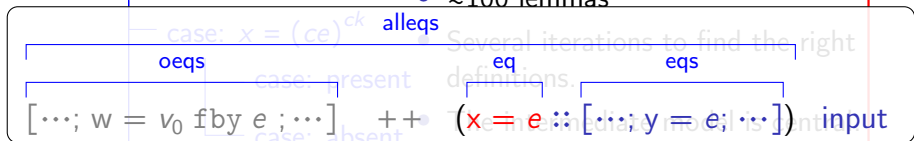
induction n

└ induction G

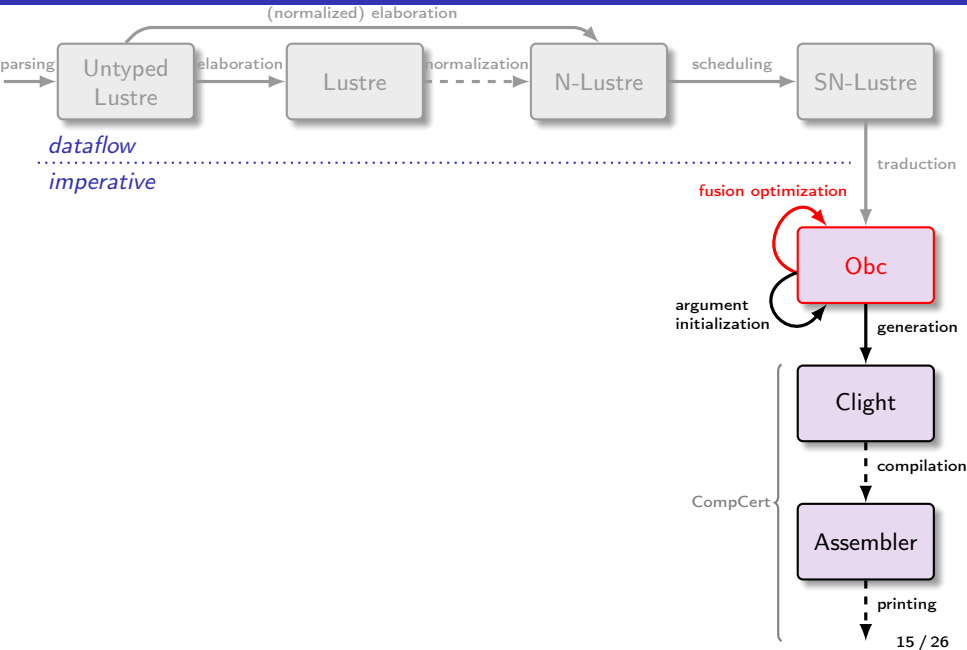
└ induction eqs



- Tricky proof, many technicalities.
- $\approx 100$  lemmas



# Fusion optimization: Obc to Obc



# Control structure fusion

[Biernacki, Colaço, Hamon, and Pouzet (2008): Clock-directed modular code generation for synchronous data-flow languages]

```
step(delta: int, sec: bool)
```

```
  returns (v: int) {
```

```
    var r, t : int;
```

```
    r := count.step o1 (0, delta, false);
```

```
    if sec then {
```

```
      t := count.step o2 (1, 1, false)
```

```
    };
```

```
    if sec then {
```

```
      v := r / t
```

```
    } else {
```

```
      v := state(w)
```

```
    };
```

```
    state(w) := v
```

```
  }
```

```
step(delta: int, sec: bool)
```

```
  returns (v: int) {
```

```
    var r, t : int;
```

```
    r := count.step o1 (0, delta, false);
```

```
    if sec then {
```

```
      t := count.step o2 (1, 1, false);
```

```
      v := r / t
```

```
    } else {
```

```
      v := state(w)
```

```
    };
```

```
    state(w) := v
```

```
  }
```

- Generate control for each equation; splits proof obligation in two.
- Fuse afterward: scheduler places similarly clocked equations together.
- Use whole framework to justify required invariant.
- Easier to reason in intermediate language than in Clight.



We also define the function  $Join(.,.)$  which merges two control structures gathered by the same guards:

$$\begin{aligned} Join( \text{case } (x) \{ C_1 : S_1; \dots; C_n : S_n \}, \\ \text{case } (x) \{ C_1 : S'_1; \dots; C_n : S'_n \} ) \\ = \text{case } (x) \{ C_1 : Join(S_1, S'_1); \dots; C_n : Join(S_n, S'_n) \} \\ Join(S_1, S_2) = S_1; S_2 \end{aligned}$$

$$\begin{aligned} JoinList(S) &= S \\ JoinList(S_1, \dots, S_n) &= Join(S_1, JoinList(S_2, \dots, S_n)) \end{aligned}$$

[ Biernacki, Colaço, Hamon, and Pouzet (2008): Clock-directed modular code generation for synchronous data-flow languages ]

We also define the function  $Join(.,.)$  which merges two control structures gathered by the same guards:

$$\begin{aligned} &Join(\text{case } (x) \{C_1 : S_1; \dots; C_n : S_n\}, \\ &\quad \text{case } (x) \{C'_1 : S'_1; \dots; C'_n : S'_n\}) \\ &= \text{case } (x) \{C_1 : Join(S_1, S'_1); \dots; C_n : Join(S_n, S'_n)\} \\ Join(S_1, S_2) &= S_1; S_2 \end{aligned}$$

$$\begin{aligned} JoinList(S) &= S \\ JoinList(S_1, \dots, S_n) &= Join(S_1, JoinList(S_2, \dots, S_n)) \end{aligned}$$

```
Fixpoint zip s1 s2 : stmt :=
  match s1, s2 with
  | Ifte e1 t1 f1, Ifte e2 t2 f2 =>
    if equiv_decb e1 e2
    then Ifte e1 (zip t1 t2) (zip f1 f2)
    else Comp s1 s2
  | Skip, s => s
  | s, Skip => s
  | Comp s1' s2', _ => Comp s1' (zip s2' s2)
  | s1, s2 => Comp s1 s2
  end.
```

```
Fixpoint fuse' s1 s2 : stmt :=
  match s1, s2 with
  | s1, Comp s2 s3 => fuse' (zip s1 s2) s3
  | s1, s2 => zip s1 s2
  end.
```

```
Definition fuse s : stmt :=
  match s with
  | Comp s1 s2 => fuse' s1 s2
  | _ => s
  end.
```

**C program**

```

1 int fixpoint(int s1, int s2) {
2   if (s1 == s2) return s1;
3   if (s1 < s2) return fixpoint(s1, s2 + 1);
4   if (s1 > s2) return fixpoint(s1 - 1, s2);
5 }

```

**Fixpoint program**

```

1 Fixpoint fixpoint (s1 : int, s2 : int) : int :=
2   if s1 == s2 then s1
3   else if s1 < s2 then fixpoint s1 (s2 + 1)
4   else if s1 > s2 then fixpoint (s1 - 1) s2
5 end

```

**Definition**

```

1 Definition fixpoint (s1 : int, s2 : int) : int :=
2   if s1 == s2 then s1
3   else if s1 < s2 then fixpoint s1 (s2 + 1)
4   else if s1 > s2 then fixpoint (s1 - 1) s2
5 end

```

**Fixpoint zip s1 s2 : stmt :=**

```

1 match s1, s2 with
2 | Ifte e1 t1 f1, Ifte e2 t2 f2 =>
3   if equiv_dec e1 e2
4   then Ifte e1 (zip t1 t2) (zip f1 f2)
5   else Comp s1 s2
6 | Skip, s => s
7 | s, Skip => s
8 | Comp s1' s2', _ => Comp s1' (zip s2' s2)
9 | s1, s2 => Comp s1 s2
10 end.

```

**Fixpoint fuse' s1 s2 : stmt :=**

```

1 match s1, s2 with
2 | s1, Comp s2 s3 => fuse' (zip s1 s2) s3
3 | s1, s2 => zip s1 s2
4 end.

```

**Definition fuse s : stmt :=**

```

1 match s with
2 | s1, s2 => zip s1 s2
3 end.

```


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## Fusion of control structures: requires invariant

`if e then {s1} else {s2};`  
`if e then {t1} else {t2}`     `if e then {s1; t1} else {s2; t2};`


## Fusion of control structures: requires invariant

`if e then {s1} else {s2};`  
`if e then {t1} else {t2}`  `if e then {s1; t1} else {s2; t2};`

`if x then {x := false} else {x := true};`  
`if x then {t1} else {t2}` 

# Fusion of control structures: requires invariant

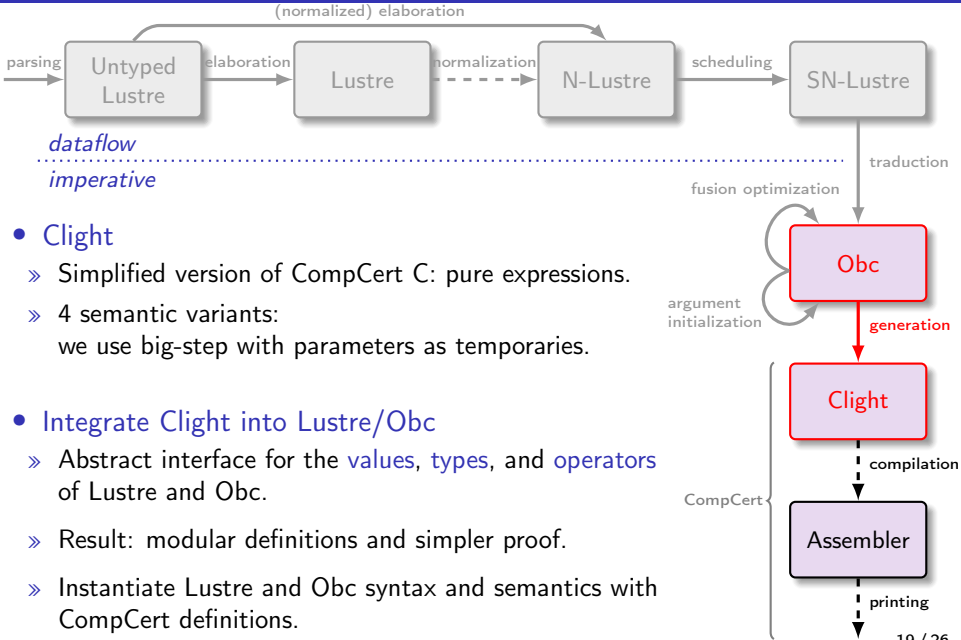
$\text{if } e \text{ then } \{s_1\} \text{ else } \{s_2\};$   
 $\text{if } e \text{ then } \{t_1\} \text{ else } \{t_2\}$    $\text{if } e \text{ then } \{s_1; t_1\} \text{ else } \{s_2; t_2\};$

$\text{if } x \text{ then } \{x := \text{false}\} \text{ else } \{x := \text{true}\};$   
 $\text{if } x \text{ then } \{t_1\} \text{ else } \{t_2\}$  

$$\frac{\text{fusible}(s_1) \quad \text{fusible}(s_2) \quad \forall x \in \text{free}(e), \neg \text{maywrite } x \ s_1 \wedge \neg \text{maywrite } x \ s_2}{\text{fusible}(\text{if } e \text{ then } \{s_1\} \text{ else } \{s_2\})}$$

$$\frac{\text{fusible}(s_1) \quad \text{fusible}(s_2)}{\text{fusible}(s_1; s_2)} \quad \dots$$

# Generation: Obc to Clight





- Introduce an abstract interface for values, types, and operators.
  - » Define N-Lustre and Obc syntax and semantics against this interface.
  - » Likewise for the N-Lustre to Obc translation and proof.
- Instantiate with definitions for the Obc to Clight translation and proof.

Module Type OPERATORS.

Parameter val : Type.

Parameter type : Type.

Parameter const : Type.

- Introduce an abstract interface for values, types, and operators.
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Module Type OPERATORS.

```
Parameter val    : Type.  
Parameter type  : Type.  
Parameter const : Type.
```

```
(* Boolean values *)  
Parameter bool_type : type.
```

```
Parameter true_val  : val.  
Parameter false_val : val.  
Axiom true_not_false_val :  
  true_val <> false_val.
```

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```

```
(* Constants *)  
Parameter type_const : const → type.  
Parameter sem_const  : const → val.
```

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```

```
(* Constants *)  
Parameter type_const : const → type.  
Parameter sem_const  : const → val.
```

```
(* Operators *)  
Parameter unop  : Type.  
Parameter binop : Type.
```

```
Parameter sem_unop :  
  unop → val → type → option val.
```

```
Parameter sem_binop :  
  binop → val → type → val → type  
  → option val.
```

```
Parameter type_unop :  
  unop → type → option type.
```

```
Parameter type_binop :  
  binop → type → type → option type.
```

```
(* ... *)
```

End OPERATORS.

- Introduce an abstract interface for values, types, and operators.
  - » Define N-Lustre and Obc syntax and semantics against this interface.
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Axiom true\_not\_false\_val :

  true\_val <> false\_val.

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Parameter type\_const : const → type.

Parameter sem\_const : const → val.

(\* Operators \*)

Parameter unop : Type.

Parameter binop : Type.

Parameter sem\_unop :

  unop → val → type → option val.

Parameter sem\_binop :

  binop → val → type → val → type  
  → option val.

Parameter type\_unop :

  unop → type → option type.

Parameter type\_binop :

  binop → type → type → option type.

(\* ... \*)

End OPERATORS.

Module Export Op <: OPERATORS.

Definition val: Type := Values.val.

Inductive val: Type :=

| Vundef : val

| Vint : int → val

| Vlong : int64 → val

| Vfloat : float → val

| Vsingle : float32 → val

| Vptr : block → int → val.

Module Type OPERATORS.

Parameter val : Type.  
Parameter type : Type.  
Parameter const : Type.

(\* Boolean values \*)  
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Parameter true\_val : val.  
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  binop → val → type → val → type  
  → option val.

Parameter type\_unop :  
  unop → type → option type.

Parameter type\_binop :  
  binop → type → type → option type.

(\* ... \*)

End OPERATORS.

Module Export Op <: OPERATORS.

Definition val: Type := Values.val.

Inductive type : Type :=  
| Tint : intsize → signedness → type  
| Tlong : signedness → type  
| Tfloat : floatsize → type.

Inductive signedness : Type :=  
| Signed : signedness  
| Unsigned : signedness.

Inductive intsize : Type :=  
| I8 : intsize (\* char \*)  
| I16 : intsize (\* short \*)  
| I32 : intsize (\* int \*)  
| IBool : intsize. (\* bool \*)

Inductive floatsize : Type :=  
| F32 : floatsize (\* float \*)  
| F64 : floatsize. (\* double \*)

Module Type OPERATORS.

Parameter val : Type.  
Parameter type : Type.  
Parameter const : Type.

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Parameter bool\_type : type.

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Parameter type\_unop :  
  unop → type → option type.

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(\* ... \*)

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Inductive type : Type :=  
| Tint : intsize → signedness → type  
| Tlong : signedness → type  
| Tfloat : floatsize → type.

Inductive const : Type :=  
| Cint : int → intsize → signedness → const  
| Clong : int64 → signedness → const  
| Cfloat : float → const  
| Csingle : float32 → const.



Module Type OPERATORS.

Parameter val : Type.  
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  → option val.

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Parameter type\_binop :  
  binop → type → type → option type.

(\* ... \*)

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| Cint : int → intsize → signedness → const  
| Clong : int64 → signedness → const  
| Cfloat : float → const  
| Csingle : float32 → const.

Definition true\_val := Vtrue. (\* Vint Int.one \*)  
Definition false\_val := Vfalse. (\* Vint Int.zero \*)

Lemma true\_not\_false\_val: true\_val <> false\_val.  
Proof. discriminate. Qed.

Definition bool\_type : type := Tint IBool Signed.

Module Type OPERATORS.

Parameter val : Type.  
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(\* Boolean values \*)  
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Parameter type\_unop :  
  unop → type → option type.

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(\* ... \*)  
End OPERATORS.

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Lemma true\_not\_false\_val: true\_val <> false\_val.  
Proof. discriminate. Qed.

Definition bool\_type : type := Tint IBool Signed.

Inductive unop : Type :=  
| UnaryOp: Cop.unary\_operation → unop  
| CastOp: type → unop.

Definition binop := Cop.binary\_operation.

Definition sem\_unop (uop: unop) (v: val) (ty: type) : option val  
:= match uop with  
| UnaryOp op ⇒ sem\_unary\_operation op v (cltype ty) Mem.empty  
| CastOp ty' ⇒ sem\_cast v (cltype ty) (cltype ty') Mem.empty  
end.

(\* ... \*)  
End Op.

```
class count { ... }
```

```
class avgvelocity {
  memory w : int;
  class count o1, o2;
```

```
  reset() {
    count.reset o1;
    count.reset o2;
    state(w) := 0
  }
```

```
  step(delta: int, sec: bool) returns (r, v: int)
  {
    var t : int;

    r := count.step o1 (0, delta, false);
    if sec
      then (t := count.step o2 (1, 1, false);
            v := r / t)
      else v := state(w);
    state(w) := v
  }
}
```

- Standard technique for encapsulating state.
- Each detail entails complications in the proof.

```
struct count { _Bool f; int c; };
void count$reset(struct count *self) { ... }
int count$step(struct count *self, int ini, int inc, _Bool res) { ... }
```

```
struct avgvelocity {
  int w;
  struct count o1;
  struct count o2;
};
```

```
struct avgvelocity$step {
  int r;
  int v;
};
```

```
void avgvelocity$reset(struct avgvelocity *self)
{
  count$reset(&(self→o1));
  count$reset(&(self→o2));
  self→w = 0;
}
```

```
void avgvelocity$step(struct avgvelocity *self,
  struct avgvelocity$step *out, int delta, _Bool sec)
{
  register int t, step$N;
```

```
  step$N = count$step(&(self→o1), 0, delta, 0);
  out→r = step$N;
  if (sec) {
    step$N = count$step(&(self→o2), 1, 1, 0);
    t = step$N;
    out→v = out→r / t;
  } else {
    out→v = self→w;
  }
  self→w = out→v;
```

```
}
```

```
class count { ... }
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```
class avgvelocity {
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  out→r = step$N;
  if (sec) {
    step$N = count$step(&(self→o2), 1, 1, 0);
    t = step$N;
    out→v = out→r / t;
  } else {
    out→v = self→w;
  }
  self→w = out→v;
}
```

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```

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  } else {
    out→v = self→w;
  }
  self→w = out→v;
```

```
}
```

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  }
```

```
  step(delta: int, sec: bool) returns (r, v: int)
  {
    var t : int;
```

```
    r := count.step o1 (0, delta, false);
    if sec
      then (t := count.step o2 (1, 1, false);
           v := r / t)
      else v := state(w);
    state(w) := v
  }
}
```

- Standard technique for encapsulating state.
- Each detail entails complications in the proof.

```
struct count { _Bool f; int c; };
void count$reset(struct count *self) { ... }
int count$step(struct count *self, int ini, int inc, _Bool res) { ... }
```

```
struct avgvelocity {
  int w;
  struct count o1;
  struct count o2;
};
```

```
struct avgvelocity$step {
  int r;
  int v;
};
```

```
void avgvelocity$reset(struct avgvelocity *self)
{
  count$reset(&(self→o1));
  count$reset(&(self→o2));
  self→w = 0;
}
```

```
void avgvelocity$step(struct avgvelocity *self,
  struct avgvelocity$step *out, int delta, _Bool sec)
{
  register int t, step$N;
```

```
  step$N = count$step(&(self→o1), 0, delta, 0);
  out→r = step$N;
  if (sec) {
    step$N = count$step(&(self→o2), 1, 1, 0);
    t = step$N;
    out→v = out→r / t;
  } else {
    out→v = self→w;
  }
  self→w = out→v;
}
```



```
class count { ... }
```

```
class avgvelocity {
  memory w : int;
  class count o1, o2;
```

```
  reset() {
    count.reset o1;
    count.reset o2;
    state(w) := 0
  }
```

```
  step(delta: int, sec: bool) returns (r, v: int)
```

```
{
  var t : int;

  r := count.step o1 (0, delta, false);
  if sec
    then (t := count.step o2 (1, 1, false);
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  int v;
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  self→w = 0;
}
```

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  out→r = step$N;
  if (sec) {
    step$N = count$step(&(self→o2), 1, 1, 0);
    t = step$N;
    out→v = out→r / t;
  } else {
    out→v = self→w;
  }
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```

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- Standard technique for encapsulating state.
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struct avgvelocity {
  int w;
  struct count o1;
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```

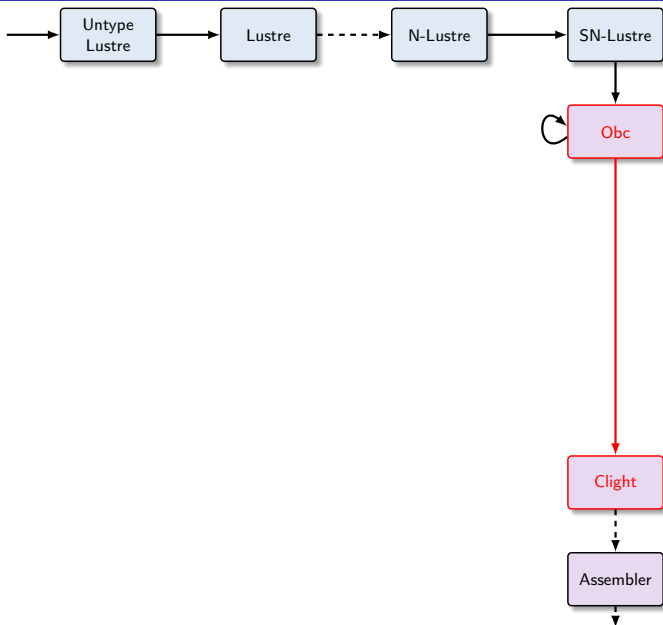
```
struct avgvelocity$step {
  int r;
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};
```

```
void avgvelocity$reset(struct avgvelocity *self)
{
  count$reset(&(self→o1));
  count$reset(&(self→o2));
  self→w = 0;
}
```

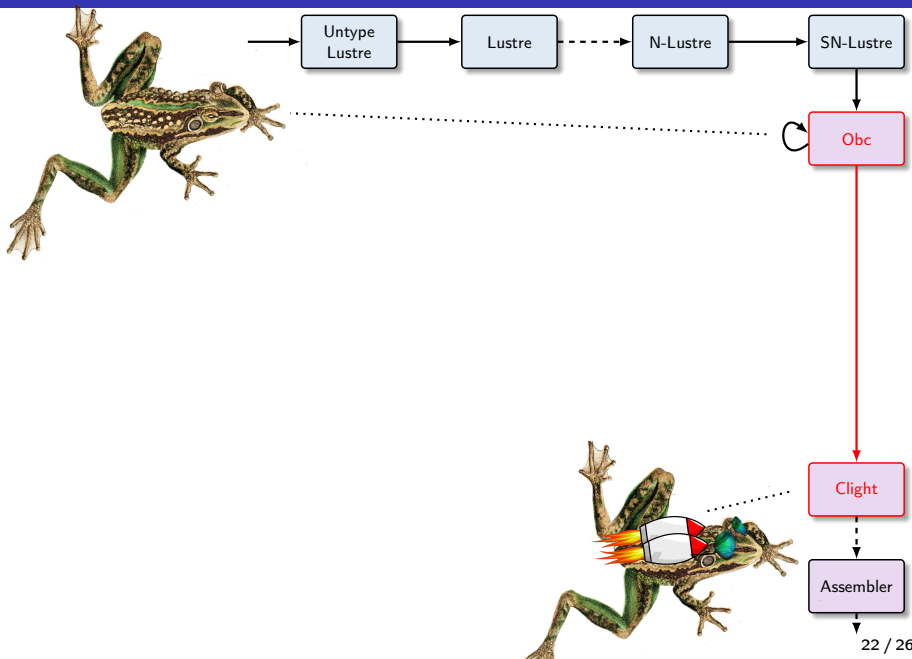
```
void avgvelocity$step(struct avgvelocity *self,
  struct avgvelocity$step *out, int delta, _Bool sec)
{
  register int t, step$n;

  step$n = count$step(&(self→o1), 0, delta, 0);
  out→r = step$n;
  if (sec) {
    step$n = count$step(&(self→o2), 1, 1, 0);
    t = step$n;
    out→v = out→r / t;
  } else {
    out→v = self→w;
  }
  self→w = out→v;
}
```

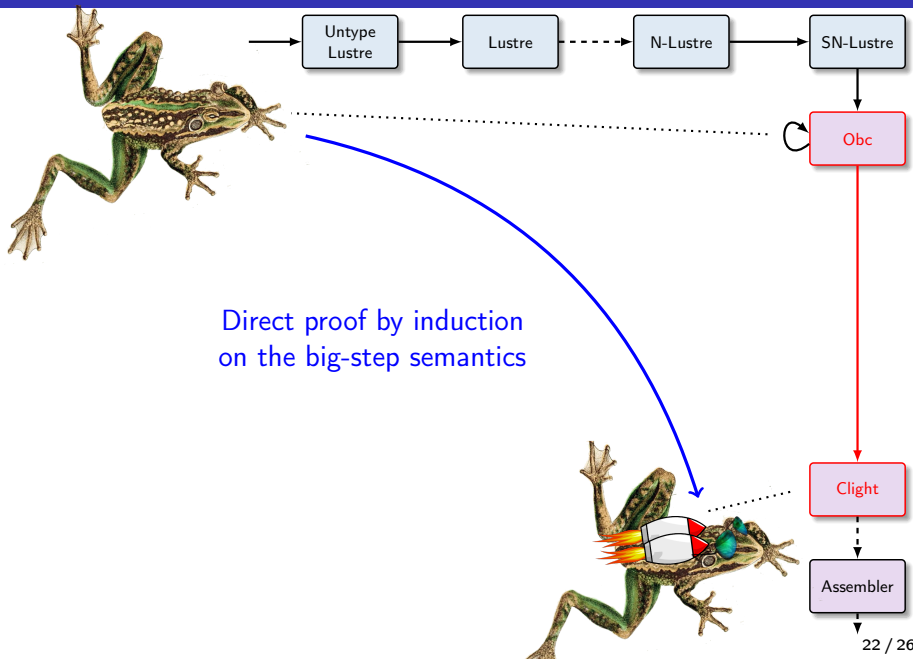
# Correctness of Clight generation



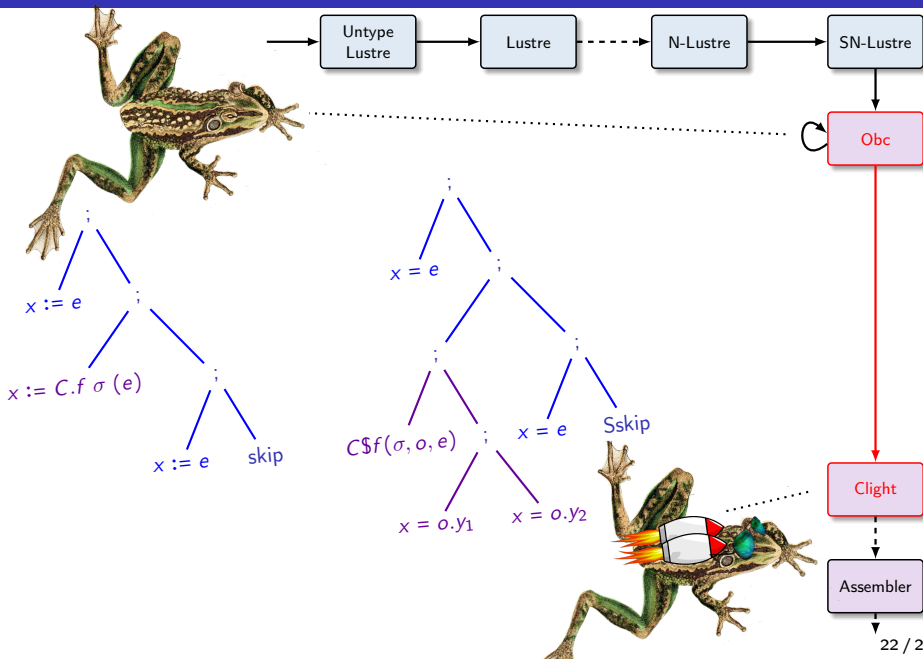
# Correctness of Clight generation



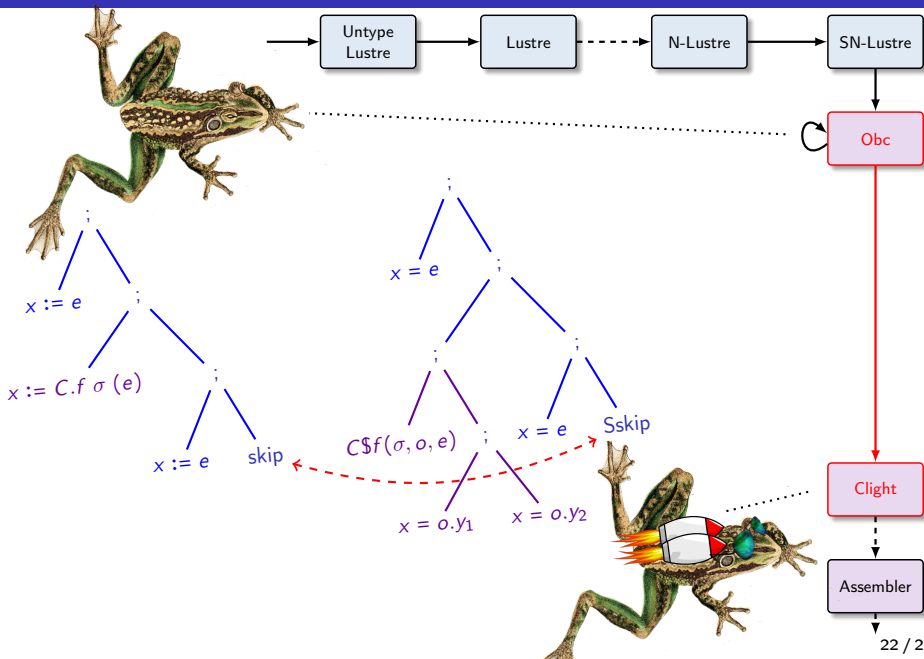
# Correctness of Clight generation



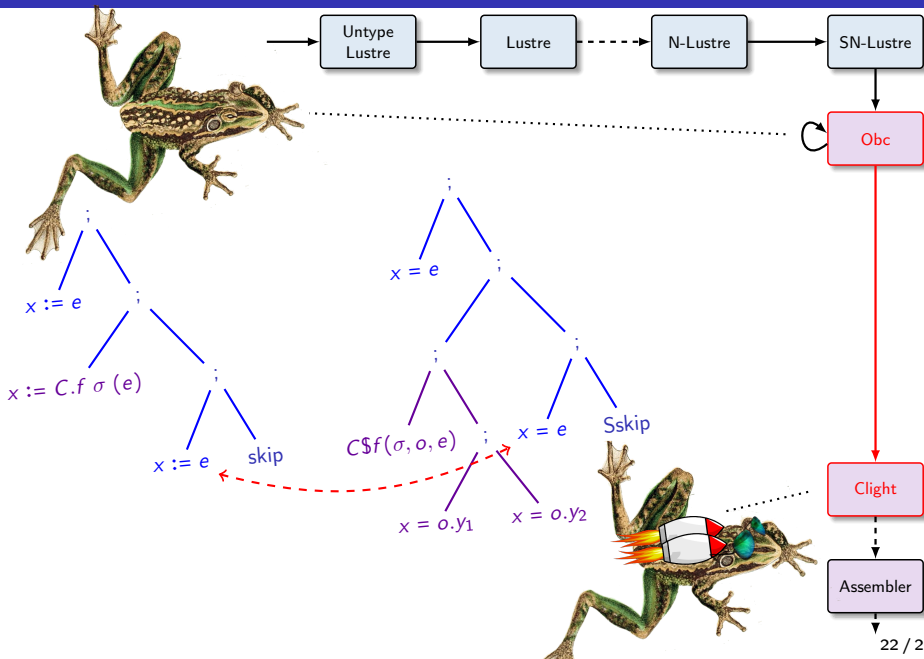
# Correctness of Clight generation



# Correctness of Clight generation

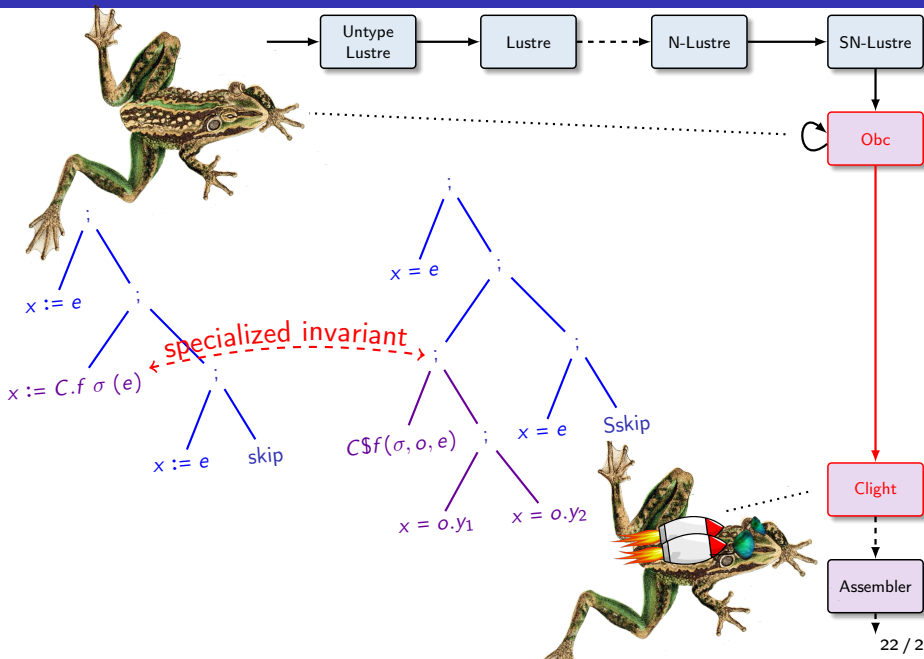


# Correctness of Clight generation

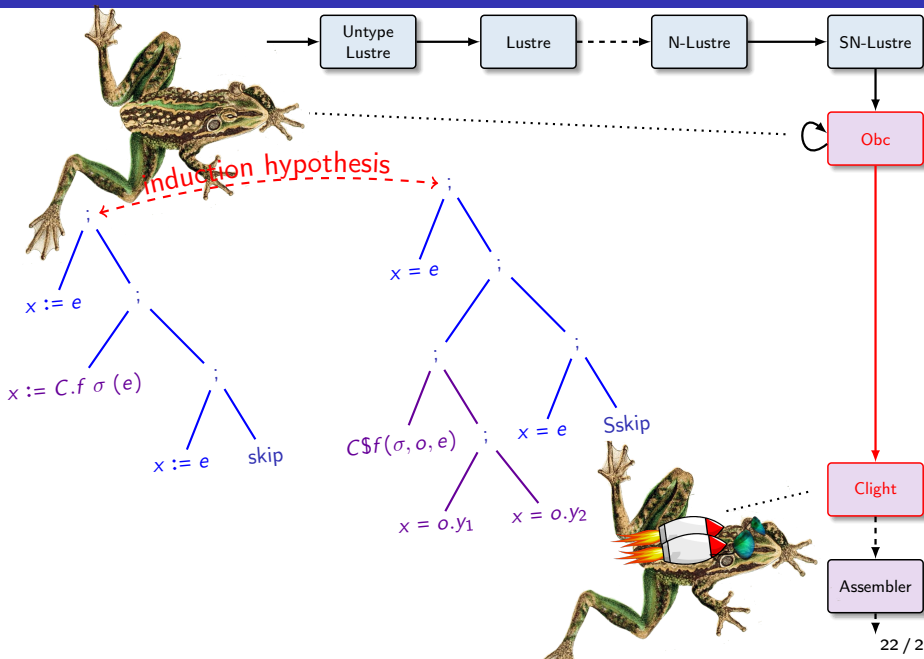




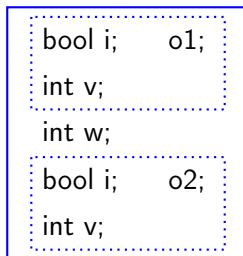
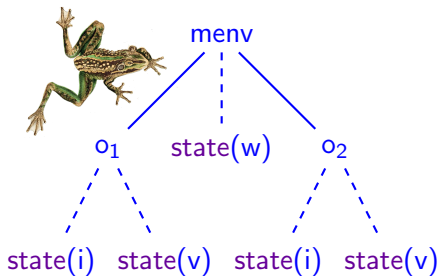
# Correctness of Clight generation



# Correctness of Clight generation

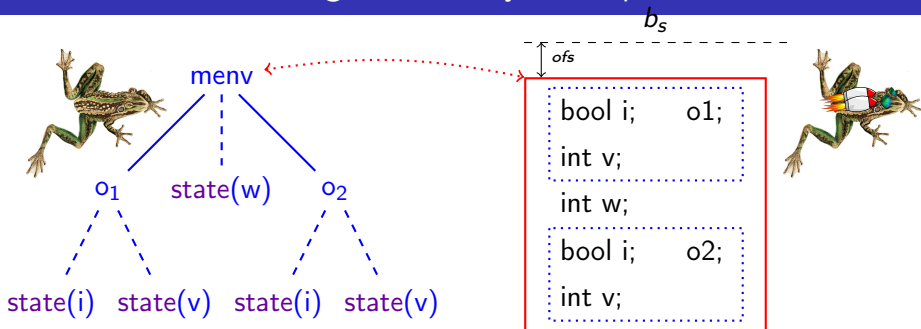


# Obc to Clight: memory correspondence



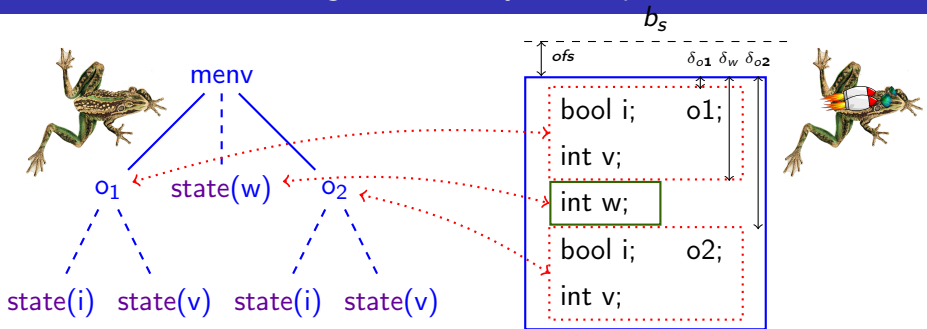
- This time the semantic models are similar (Clight: very detailed)
- The real challenge is to relate the memory models.
  - » Obc: tree structure, variable separation is manifest.
  - » Clight: block-based, must treat **aliasing**, **alignment**, and **sizes**.
- Extend CompCert's lightweight library of separating assertions:  
<https://github.com/AbsInt/CompCert/common/Separation.v>.
- Encode simplicity of source model in richer memory model.
- General (and very useful) technique for interfacing with CompCert.

# Obc to Clight: memory correspondence



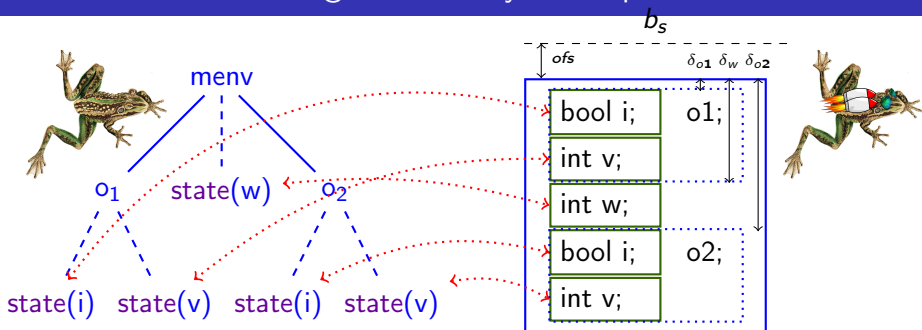
$$m \models \text{staterep avgvelocity } me \ (b_s, ofs)$$

# Obc to Clight: memory correspondence



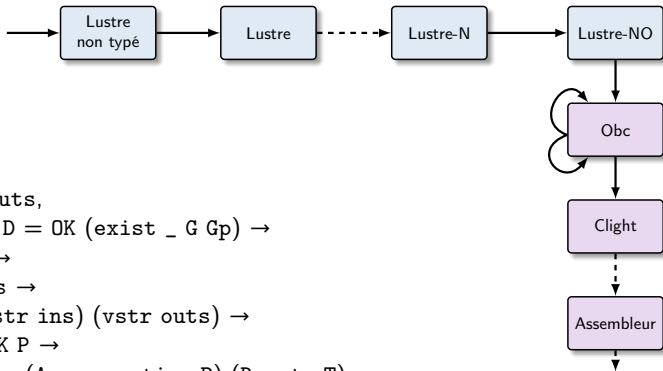
$m \models$     `staterep count`  $me(o1)$   $(b_s, ofs + \delta_{o1})$   
           \* `contains`  $tyint32s$   $(b_s, ofs + \delta_w)$   $[me.state(w)]$   
           \* `staterep count`  $me(o2)$   $(b_s, ofs + \delta_{o2})$

# Obc to Clight: memory correspondence



$m \models$  contains *tybool* ( $b_s, ofs + \delta_{o1} + \delta_i$ ) [ $me.o1.state(i)$ ]  
 $m \models$  \* contains *tyint32s* ( $b_s, ofs + \delta_{o1} + \delta_v$ ) [ $me.o1.state(v)$ ]  
 $m \models$  \* contains *tyint32s* ( $b_s, ofs + \delta_w$ ) [ $me.state(w)$ ]  
 $m \models$  \* contains *tybool* ( $b_s, ofs + \delta_{o2} + \delta_i$ ) [ $me.o2.state(i)$ ]  
 $m \models$  \* contains *tyint32s* ( $b_s, ofs + \delta_{o2} + \delta_v$ ) [ $me.o2.state(v)$ ]

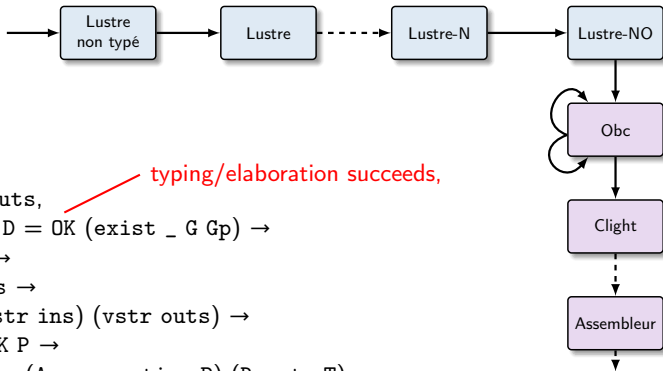
# Main theorem



**Theorem** behavior\_asm:

$$\begin{aligned} &\forall D \ G \ Gp \ P \ \text{main} \ \text{ins} \ \text{outs}, \\ &\quad \text{elab\_declarations } D = \text{OK} \ (\text{exist } \_ \ G \ Gp) \rightarrow \\ &\quad \text{wt\_ins } G \ \text{main} \ \text{ins} \rightarrow \\ &\quad \text{wt\_outs } G \ \text{main} \ \text{outs} \rightarrow \\ &\quad \text{sem\_node } G \ \text{main} \ (\text{vstr } \text{ins}) \ (\text{vstr } \text{outs}) \rightarrow \\ &\quad \text{compile } D \ \text{main} = \text{OK} \ P \rightarrow \\ &\quad \exists T, \text{program\_behaves} \ (\text{Asm.semantics } P) \ (\text{Reacts } T) \\ &\quad \wedge \text{bisim\_io } G \ \text{main} \ \text{ins} \ \text{outs} \ T. \end{aligned}$$

# Main theorem



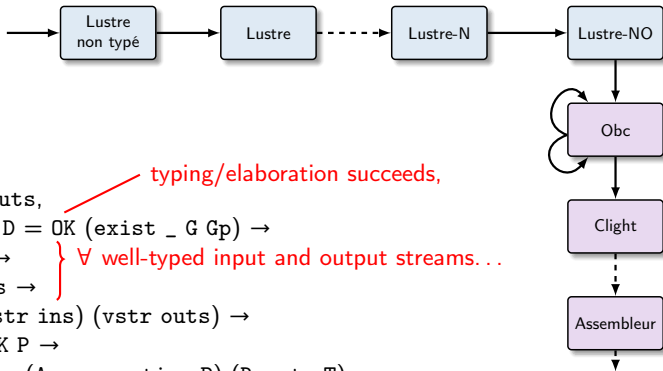
**Theorem** behavior\_asm:

$\forall D G Gp P \text{ main ins outs,}$   
elab\_declarations  $D = \text{OK}$  (exist \_  $G Gp$ )  $\rightarrow$   
wt\_ins  $G \text{ main ins} \rightarrow$   
wt\_outs  $G \text{ main outs} \rightarrow$   
sem\_node  $G \text{ main (vstr ins) (vstr outs)} \rightarrow$   
compile  $D \text{ main} = \text{OK}$   $P \rightarrow$   
 $\exists T, \text{program\_behaves (Asm.semantics } P) (\text{Reacts } T)$   
 $\wedge \text{bisim\_io } G \text{ main ins outs } T.$

typing/elaboration succeeds,



# Main theorem

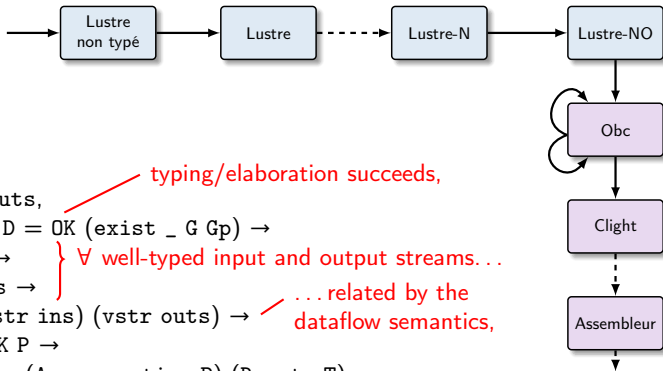


**Theorem** behavior\_asm:

$\forall D \ G \ Gp \ P \ \text{main} \ \text{ins} \ \text{outs},$   
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 $\text{wt\_ins} \ G \ \text{main} \ \text{ins} \rightarrow$   
 $\text{wt\_outs} \ G \ \text{main} \ \text{outs} \rightarrow$   
 $\text{sem\_node} \ G \ \text{main} \ (\text{vstr} \ \text{ins}) \ (\text{vstr} \ \text{outs}) \rightarrow$   
 $\text{compile} \ D \ \text{main} = \text{OK} \ P \rightarrow$   
 $\exists T, \text{program\_behaves} \ (\text{Asm.semantics} \ P) \ (\text{Reacts} \ T)$   
 $\wedge \text{bisim\_io} \ G \ \text{main} \ \text{ins} \ \text{outs} \ T.$

*typing/elaboration succeeds,*  
 *$\forall$  well-typed input and output streams...*

# Main theorem

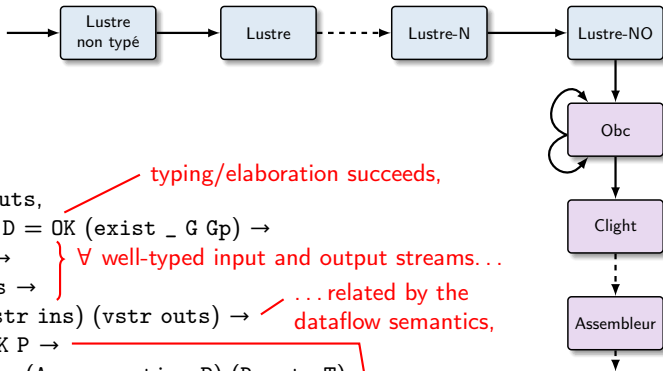


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 $\text{wt\_ins } G \text{ main ins} \rightarrow$   
 $\text{wt\_outs } G \text{ main outs} \rightarrow$   
 $\text{sem\_node } G \text{ main (vstr ins) (vstr outs)} \rightarrow$   
 $\text{compile } D \text{ main} = \text{OK } P \rightarrow$   
 $\exists T, \text{program\_behaves (Asm.semantics } P) (\text{Reacts } T)$   
 $\wedge \text{bisim\_io } G \text{ main ins outs } T.$

typing/elaboration succeeds,  
 }  $\forall$  well-typed input and output streams...  
 ...related by the  
 dataflow semantics,

# Main theorem

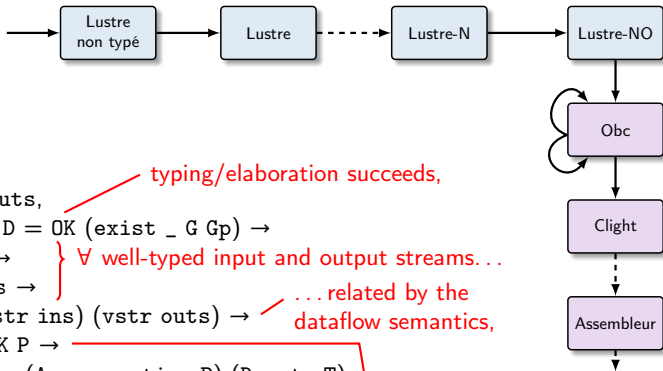


**Theorem** behavior\_asm:

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 &\forall D \ G \ Gp \ P \ \text{main} \ \text{ins} \ \text{outs}, \\
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 &\quad \text{wt\_ins } G \ \text{main} \ \text{ins} \rightarrow \\
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 &\quad \text{sem\_node } G \ \text{main} \ (\text{vstr} \ \text{ins}) \ (\text{vstr} \ \text{outs}) \rightarrow \\
 &\quad \text{compile } D \ \text{main} = \text{OK} \ P \rightarrow \\
 &\quad \exists T, \text{program\_behaves} \ (\text{Asm.semantics } P) \ (\text{Reacts } T) \\
 &\quad \wedge \text{bisim\_io } G \ \text{main} \ \text{ins} \ \text{outs} \ T.
 \end{aligned}$$

typing/elaboration succeeds,  
 }  $\forall$  well-typed input and output streams...  
 ...related by the  
 dataflow semantics,  
 if compilation  
 succeeds,

# Main theorem

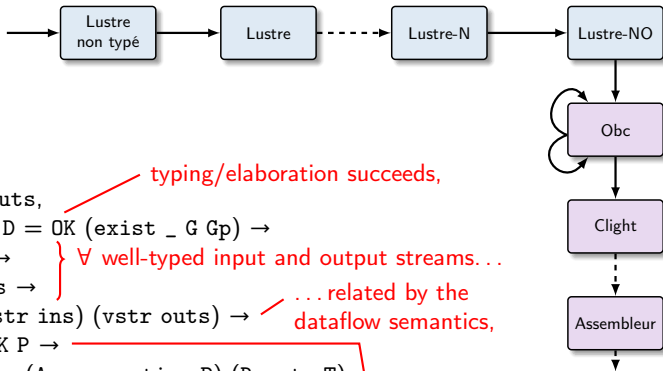


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 $wt\_outs \ G \ main \ outs \rightarrow$   
 $sem\_node \ G \ main \ (vstr \ ins) \ (vstr \ outs) \rightarrow$   
 $compile \ D \ main = OK \ P \rightarrow$   
 $\exists T, program\_behaves \ (Asm.semantics \ P) \ (Reacts \ T)$   
 $\wedge bisim\_io \ G \ main \ ins \ outs \ T.$

typing/elaboration succeeds,  
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 ...related by the dataflow semantics,  
 if compilation succeeds,  
 then, the generated assembly produces an infinite trace...

# Main theorem



**Theorem** behavior\_asm:

$\forall D G G_p P \text{ main ins outs,}$   
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 $\text{wt\_outs } G \text{ main outs} \rightarrow$   
 $\text{sem\_node } G \text{ main (vstr ins) (vstr outs)} \rightarrow$   
 $\text{compile } D \text{ main} = \text{OK } P \rightarrow$   
 $\exists T, \text{program\_behaves (Asm.semantics } P) (\text{Reacts } T)$   
 $\wedge \text{bisim\_io } G \text{ main ins outs } T.$

typing/elaboration succeeds,  
 }  $\forall$  well-typed input and output streams...  
 ...related by the  
 dataflow semantics,  
 if compilation  
 succeeds,  
 then, the generated assembly  
 produces an infinite trace...  
 ... that corresponds to the dataflow model.

## Industrial application

- $\approx 6\,000$  nodes
- $\approx 162\,000$  equations
- $\approx 12$  MB source file  
(minus comments)
- Modifications:
  - » Remove constant lookup tables.
  - » Replace calls to assembly code.
- Vélus compilation:  $\approx 1\text{ min }40\text{ s}$

# Experimental results

## Industrial application

- $\approx 6\,000$  nodes
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- $\approx 12$  MB source file (minus comments)
- Modifications:
  - » Remove constant lookup tables.
  - » Replace calls to assembly code.
- Vélus compilation:  $\approx 1\text{ min }40\text{ s}$

	Vélus	Hept+CC	Hept+gcc	Hept+gcc	Lustre+CC	Lustre+gcc	Lustre+gcc
avgvelocity	315	385 (22%)	265 (-15%)	70 (-77%)	1150 (268%)	625 (98%)	350 (11%)
count	55	55 (0%)	25 (-54%)	25 (-54%)	300 (445%)	160 (100%)	50 (-9%)
tracker	680	790 (16%)	530 (-22%)	500 (-26%)	2610 (283%)	1515 (122%)	735 (8%)
pip_ex	4415	4065 (-7%)	2565 (-41%)	2040 (-53%)	10845 (147%)	6245 (41%)	2905 (-34%)
mp_longitudinal [16]	5525	6465 (17%)	3465 (-37%)	2835 (-48%)	11675 (111%)	6785 (22%)	3135 (-43%)
cruise [54]	1760	1875 (6%)	1230 (-30%)	1230 (-30%)	5855 (232%)	3595 (104%)	1965 (11%)
risingedgegenerator [19]	285	300 (5%)	190 (-33%)	190 (-33%)	1440 (402%)	820 (187%)	335 (17%)
chromo [20]	410	425 (3%)	305 (-25%)	305 (-25%)	2490 (507%)	1500 (265%)	670 (63%)
watchdog3 [26]	610	575 (-5%)	355 (-41%)	310 (-49%)	2015 (230%)	1135 (86%)	530 (-13%)
functionalchain [17]	11550	13535 (17%)	8545 (-26%)	7525 (-34%)	23085 (99%)	14280 (23%)	8240 (-28%)
landing_gear [11]	9660	8475 (-12%)	5880 (-39%)	5810 (-39%)	25470 (163%)	15055 (59%)	8025 (-16%)
minus [57]	890	900 (1%)	580 (-34%)	580 (-34%)	2825 (216%)	1620 (82%)	800 (-10%)
predcell [32]	1020	990 (-3%)	620 (-39%)	410 (-59%)	3615 (256%)	2090 (105%)	1070 (-4%)
ums_verif [57]	2590	2285 (-11%)	1380 (-46%)	920 (-64%)	11725 (352%)	6730 (159%)	3420 (32%)

Figure 12. WCET estimates in cycles [4] for step functions compiled for an armv7-a/vfpv3-d16 target with CompCert 2.6 (CC) and GCC 4.4.8-04 without inlining (gcc) and with inlining (gcc). Percentages indicate the difference relative to the first column.

It performs loads and stores of volatile variables to model, respectively, input consumption and output production. The inductive predicate presented in Section 1 is introduced to relate the trace of these events to input and output streams.

Finally, we exploit an existing CompCert lemma to transfer our results from the big-step model to the small-step one, from whence they can be extended to the generated assembly code to give the property stated at the beginning of the paper. The transfer lemma requires showing that a program does not diverge. This is possible because the body of the main loop always produces observable events.

### 5. Experimental Results

Our prototype compiler, Vélus, generates code for the platforms supported by CompCert (PowerPC, ARM, and x86). The code can be executed in a 'test mode' that scans inputs and prints outputs using an alternative (unverified) entry point. The verified integration of generated code into a complete system where it would be triggered by interrupts and interact with hardware is the subject of ongoing work.

As there is no standard benchmark suite for Lustre, we adapted examples from the literature and the Lustre v4 distribution [57]. The resulting test suite comprises 14 programs, totaling about 160 nodes and 960 equations. We compared the code generated by Vélus with that produced by the Heptagon 1.03 [23] and Lustre v6 [35, 57] academic compilers. For the example with the deepest nesting of clocks (3 levels), both Heptagon and our prototype found the same optimal schedule. Otherwise, we follow the approach of [23, §6.2] and estimate the Worst-Case Execution Time (WCET) of the generated code using the open-source ODTAWA v5 framework [4] with the 'trivial' script and default parameters.<sup>16</sup> For the targeted domain, an over-approximation to the WCET is

usually more valuable than raw performance numbers. We compiled with CompCert 2.6 and GCC 4.4.8 (-O1) for the arm-no-neon target (armv7-a) with a hardware floating-point unit (vfpv3-d16).

The results of our experiments are presented in Figure 12. The first column shows the worst-case estimates in cycles for the step functions produced by Vélus. These estimates compare favorably with those for generation with either Heptagon or Lustre v6 and then compilation with CompCert. Both Heptagon and Lustre (automatically) re-normalize the code to have one operator per equation, which can be costly for nested conditional statements, whereas our prototype simply maintains the (manually) normalized form. This re-normalization is unsurprising: both compilers must treat a richer input language, including arrays and automata, and both expect the generated code to be post-optimized by a C compiler. Compiling the generated code with GCC but still without any inlining greatly reduces the estimated WCETs, and the Heptagon code then outperforms the Vélus code. GCC applies 'if-conversions' to exploit predicated ARM instructions which avoids branching and thereby improves WCET estimates. The estimated WCETs for the Lustre v6 generated code only become competitive when inlining is enabled because Lustre v6 implements operators, like `pw` and `+`, using separate functions. CompCert can perform inlining, but the default heuristic has not yet been adapted for this particular case. We note also that we use the modular compilation scheme of Lustre v6, while the code generator also provides more aggressive schemes like clock enumeration and automaton minimization [29, 56].

Finally, we tested our prototype on a large industrial application ( $\approx 60\,000$  nodes,  $\approx 162\,000$  equations,  $\approx 12$  MB source file without comments). The source code was already normalized since it was generated with a graphical interface,

<sup>16</sup>This configuration is quite pessimistic but suffices for the present analysis.

# Experimental results

## Industrial application

- $\approx 6\,000$  nodes
- $\approx 162\,000$  equations
- $\approx 12$  MB source file (minus comments)
- Modifications:
  - » Remove constant lookup tables.
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- Vélus compilation:  $\approx 1\text{ min }40\text{ s}$

	Vélus	HepC+CC	HepC+gcc	HepC+gcc	Laue+CC	Laue+gcc	Laue+gcc
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risingedgegenerator [19]	285	300 (5%)	190 (-33%)	190 (-33%)	1440 (403%)	820 (187%)	335 (17%)
chromo [20]	410	425 (3%)	305 (-25%)	305 (-25%)	2490 (507%)	1500 (265%)	670 (63%)
watchdog3 [26]	610	575 (-5%)	355 (-41%)	310 (-49%)	2015 (230%)	1135 (86%)	530 (-13%)
functionalchain [17]	11550	13535 (17%)	8545 (-26%)	7525 (-34%)	23085 (99%)	14280 (23%)	8240 (-28%)
landing_gear [11]	9660	8475 (-12%)	5880 (-39%)	5810 (-39%)	25470 (163%)	15055 (55%)	8025 (-16%)
minus [57]	890	900 (1%)	580 (-35%)	580 (-35%)	2825 (216%)	1620 (82%)	800 (-10%)
prodcell [32]	1020	990 (-3%)	620 (-39%)	410 (-59%)	3615 (256%)	2090 (105%)	1070 (4%)
ums_verif [57]	2590	2285 (-11%)	1380 (-46%)	920 (-64%)	11725 (352%)	6730 (159%)	3420 (32%)

Figure 12. WCET estimates in cycles [4] for step functions compiled for an armv7-avfp3-416 target with CompCen 2.6 (CC) and GCC 4.4.8-04 without inlining (gcc) and with inlining (gcc). Percentages indicate the difference relative to the first column.

It performs loads and stores of volatile variables to model, directly, input consumption and output generation. This is a more accurate model than the one used by the academic compilers. The transfer lemma requires showing that a program does not modify volatile variables. This is done by the user, using the transfer lemma. The transfer lemma requires showing that a program does not modify volatile variables. This is done by the user, using the transfer lemma.

Usually, we return an existing CompCen lemma to the user. For our code, we return a lemma to the user. The transfer lemma requires showing that a program does not modify volatile variables. This is done by the user, using the transfer lemma. The transfer lemma requires showing that a program does not modify volatile variables. This is done by the user, using the transfer lemma.

5. Ballabriga, Cassé, Rochange, and Sainrat (2010): OTAWA: An Open Toolbox for Adaptive WCET Analysis.

Results depend on C compiler:

» CompCen: Vélus code same/better

» gcc -O1 no-inlining: Vélus code slower

» gcc -O1: Vélus code much slower

[TODO]: 12

adjust CompCen inlining heuristic.



## The Lustre synchronous language

### Vélus: A Lustre compiler verified in Coq

Translation: from NLustre to Obc

Optimization: control structure fusion

Generation: from Obc to Clight

Main theorem and experimental results

## Conclusion

# Conclusion

## First results

- Working compiler from Lustre to assembler in Coq.

[Bourke, Dagand, Pouzet, and Rieg (2017): Vérification de la génération modulaire du code impératif pour Lustre]

[Bourke, Brun, Dagand, Leroy, Pouzet, and Rieg (2017): A Formally Verified Compiler for Lustre]

- Formally relate dataflow model to imperative code.
- Generate Clight for CompCert; change to richer memory model.
- Intermediate language and separation predicates were decisive.

## Ongoing work

- Add resets, finish normalization pass, add automata. . .
- Prove that a well-typed program has a semantics.
- Combine interactive and automatic proof to verify Lustre programs.

» Can verify reactive models in Isabelle. [Bourke, Glabbeek, and Höfner (2016): Mechanizing a Process Algebra for Network Protocols]

» Can compile reactive programs in Coq.

» What's the best way to do both at the same time?

- Treat side-effects in dataflow model and integrate C code.

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## Indexed or coinductive: fby

```
CoFixpoint fby (c: val) (xs: Stream value) : Stream value :=  
  match xs with  
  | absent ::: xs  $\Rightarrow$  absent ::: fby c xs  
  | present x ::: xs  $\Rightarrow$  present c ::: fby x xs  
end.
```

# Indexed or coinductive: fby

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CoFixpoint fby (c: val) (xs: Stream value) : Stream value :=  
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  | present x ::: xs  $\Rightarrow$  present c ::: fby x xs  
  end.
```

```
Fixpoint hold (v0: val) (xs: stream value) (n: nat) : val :=  
  match n with  
  | 0  $\Rightarrow$  v0  
  | S m  $\Rightarrow$  match xs m with  
    | absent  $\Rightarrow$  hold v0 xs m  
    | present hv  $\Rightarrow$  hv  
  end  
end.
```

```
Definition fby (v0: val) (xs: stream value) : nat  $\rightarrow$  value :=  
  fun n  $\Rightarrow$   
    match xs n with  
    | absent  $\Rightarrow$  absent  
    | _  $\Rightarrow$  present (hold v0 xs n)  
  end.
```



# Indexed or coinductive (NLustre)

Indexed streams ( $\text{nat} \mapsto \text{value}$ )

Coinductive streams

`fun`  $n \Rightarrow n$

`(cofix`  $f\ n := n :: f\ (S\ n))\ 0$

# Indexed or coinductive (NLustre)

Indexed streams ( $\text{nat} \mapsto \text{value}$ )

Coinductive streams

```
CoFixpoint idx_to_coind (n: nat) (xs: nat → A) : Stream A :=  
  xs n ::: idx_to_coind (S n) xs.
```

`fun n => n`

`(cofix f n := n ::: f (S n)) 0`

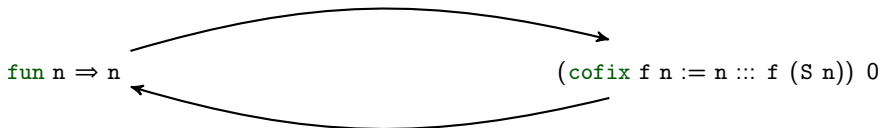


# Indexed or coinductive (NLustre)

Indexed streams ( $\text{nat} \mapsto \text{value}$ )

Coinductive streams

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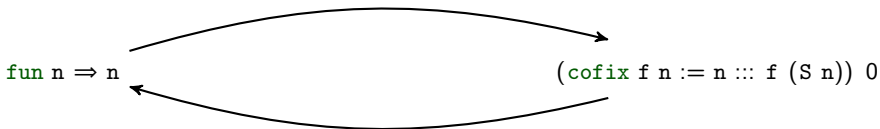
```
Definition coind_to_idx (xs: Stream A) : nat → A :=  
  fun n => hd (Str_nth_tl n xs).
```

# Indexed or coinductive (NLustre)

Indexed streams ( $\text{nat} \mapsto \text{value}$ )

Coinductive streams

```
CoFixpoint idx_to_coind (n: nat) (xs: nat → A) : Stream A :=  
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```
Definition coind_to_idx (xs: Stream A) : nat → A :=  
  fun n => hd (Str_nth_tl n xs).
```

```
idx_to_coind n (Idx.fby k xs)  
== CoInd.fby (Idx.hold k xs n) (idx_to_coind n xs).
```

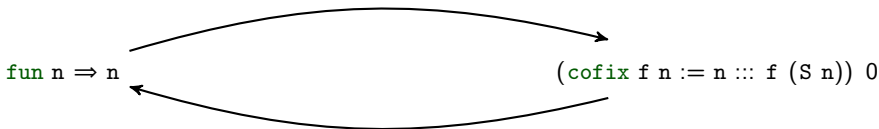
```
coind_to_idx (CoInd.fby k xs) == Idx.fby c (coind_to_idx xs).
```

# Indexed or coinductive (NLustre)

Indexed streams ( $\text{nat} \mapsto \text{value}$ )

Coinductive streams

```
CoFixpoint idx_to_coind (n: nat) (xs: nat → A) : Stream A :=  
  xs n ::: idx_to_coind (S n) xs.
```



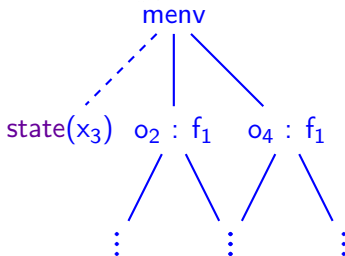
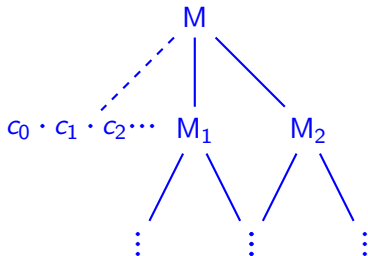
```
Definition coind_to_idx (xs: Stream A) : nat → A :=  
  fun n => hd (Str_nth_tl n xs).
```

```
idx_to_coind n (Idx.fby k xs)  
== CoInd.fby (Idx.hold k xs n) (idx_to_coind n xs).
```

```
coind_to_idx (CoInd.fby k xs) == Idx.fby c (coind_to_idx xs).
```

Extends to NLustre semantics (proof: L. Brun)

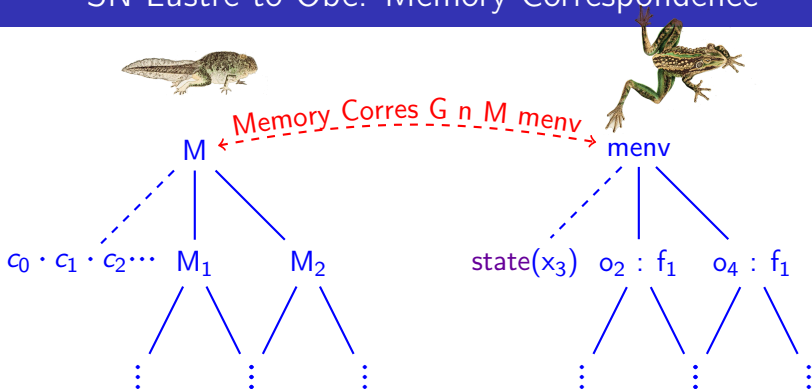
# SN-Lustre to Obc: Memory Correspondence



```

Inductive Memory_Corres (G: global) (n: nat) :
  ident → memory → heap → Prop :=
| MemC:
  find_node f G = Some(mk_node f i o eqs) →
  Forall (Memory_Corres_eq G n M menv) eqs →
  Memory_Corres G n f M menv
    
```

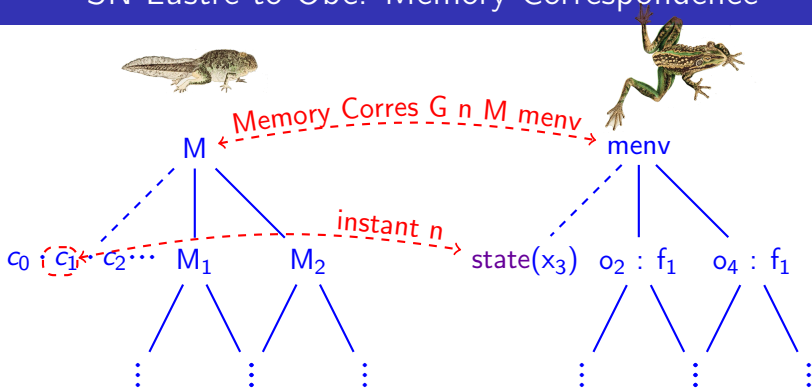
# SN-Lustre to Obc: Memory Correspondence



```

Inductive Memory_Corres (G: global) (n: nat) :
  ident → memory → heap → Prop :=
| MemC:
  find_node f G = Some(mk_node f i o eqs) →
  Forall (Memory_Corres_eq G n M menv) eqs →
  Memory_Corres G n f M menv
    
```

# SN-Lustre to Obc: Memory Correspondence



**Inductive** Memory\_Corres\_eq (G: global) (n: nat) :  
 memory → heap → equation → **Prop** :=

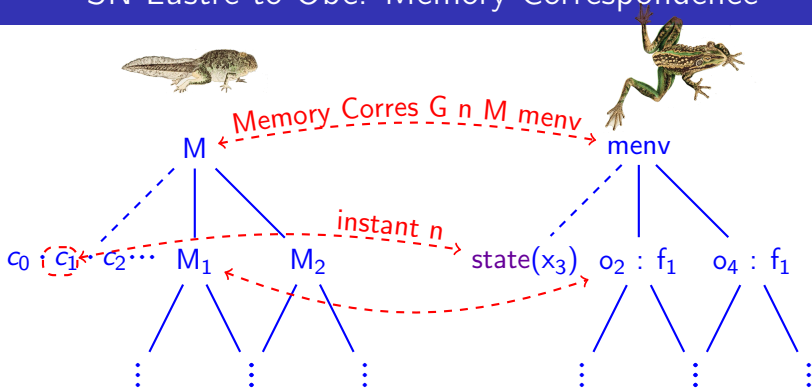
...

| MemC\_EqFby:

( $\forall$  ms, mfind\_mem x M = Some ms  
 → mfind\_mem x menv = Some (ms n))  
 → Memory\_Corres\_eq G n M menv (EqFby x v0 lae).



# SN-Lustre to Obc: Memory Correspondence



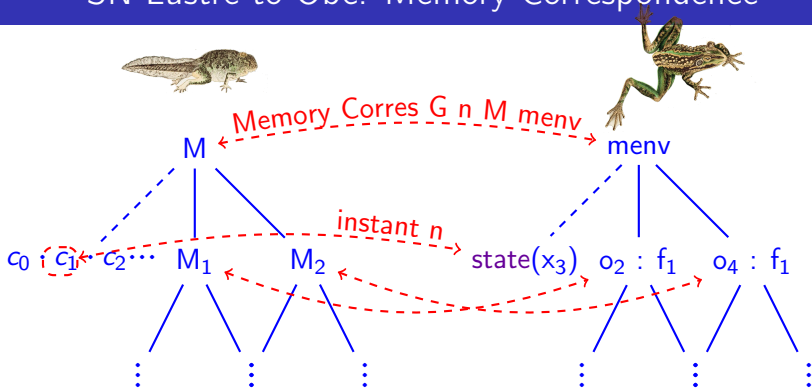
**Inductive** Memory\_Corres\_eq (G: global) (n: nat) :  
 memory  $\rightarrow$  heap  $\rightarrow$  equation  $\rightarrow$  Prop :=

...

| MemC\_EqApp:

( $\forall$  Mo, mfind\_inst x M = Some Mo  $\rightarrow$   
 ( $\exists$  omenv, mfind\_inst x menv = Some omenv  
 $\wedge$  Memory\_Corres G n f Mo omenv))  
 $\rightarrow$  Memory\_Corres\_eq G n M menv (EqApp x f lae)

# SN-Lustre to Obc: Memory Correspondence



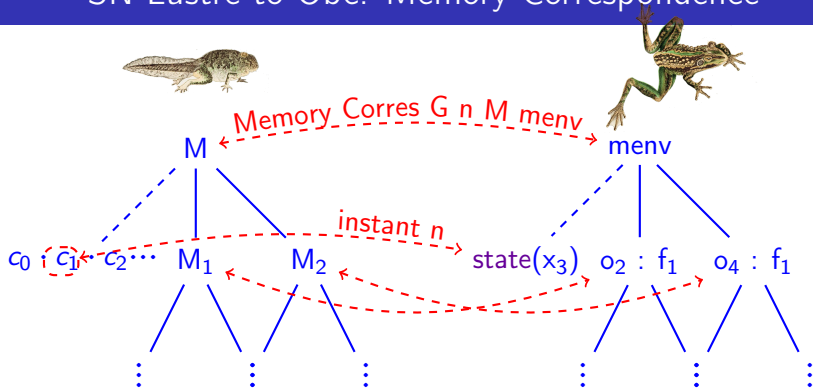
**Inductive** `Memory_Corres_eq` ( $G$ : global) ( $n$ : nat) :  
 memory  $\rightarrow$  heap  $\rightarrow$  equation  $\rightarrow$  **Prop** :=

...

| `MemC_EqApp`:

( $\forall$   $Mo$ ,  $mfind\_inst\ x\ M = Some\ Mo \rightarrow$   
 ( $\exists$   $omenv$ ,  $mfind\_inst\ x\ menv = Some\ omenv$   
 $\wedge\ Memory\_Corres\ G\ n\ f\ Mo\ omenv$ ))  
 $\rightarrow Memory\_Corres\_eq\ G\ n\ M\ menv\ (EqApp\ x\ f\ lae)$

# SN-Lustre to Obscure: Memory Correspondence



- Memory 'model' does not change between N-Lustre and Obscure.
  - » Corresponds at each 'snapshot'.
- The real challenge is in the change of semantic model:  
from **dataflow streams** to **sequenced assignments**

# Separation logic in CompCert

predicate

$$\text{massert} \triangleq \left\{ \begin{array}{l} \text{pred} : \text{memory} \rightarrow \mathbb{P} \\ \text{foot} : \text{block} \rightarrow \text{int} \rightarrow \mathbb{P} \\ \text{invar} : \forall m m', \text{pred } m \rightarrow \\ \qquad \qquad \qquad \text{unchanged\_on foot } m m' \rightarrow \\ \qquad \qquad \qquad \text{pred } m' \end{array} \right\}$$

notation:  $m \models P \triangleq P.\text{pred } m$

conjunction

$$P * Q \triangleq \left\{ \begin{array}{l} \text{pred} = \lambda m. (m \models P) \wedge (m \models Q) \\ \qquad \qquad \qquad \wedge \text{disjoint } P.\text{foot } Q.\text{foot} \\ \text{foot} = \lambda b \text{ ofs. } P.\text{foot } b \text{ ofs} \vee Q.\text{foot } b \text{ ofs} \end{array} \right\}$$

pure formula  $m \models \text{pure}(P) * Q \leftrightarrow P \wedge m \models Q$

```
(* Xavier's Separation.v *)
```

```
Record massert : Type := { m_pred : mem → Prop;  
    m_footprint : block → Z → Prop; ... }.
```

```
Notation "m |= p" := (m_pred p m) : sep_scope.
```

```
Definition disjoint_footprint (P Q: massert) : Prop :=  
  ∀ b ofs, m_footprint P b ofs → m_footprint Q b ofs → False.
```

```
Definition sepconj (P Q: massert) : massert := { |  
  m_pred := fun m ⇒ m_pred P m ∧ m_pred Q m ∧ disjoint_footprint P Q;  
  m_footprint := fun b ofs ⇒ m_footprint P b ofs ∨ m_footprint Q b ofs | }.
```

```
Infix "***" := sepconj : sep_scope.
```

```
(* Blockrep *)
```

```
Fixpoint sepall (p: A → massert) (xs: list A) : massert := match xs with  
  | nil ⇒ sepemp  
  | x::xs ⇒ p x *** sepall p xs  
end.
```

```
Definition match_value (e: PM.t val) (x: ident) (v': val) : Prop := match PM.find x e with  
  | None ⇒ True  
  | Some v ⇒ v' = v  
end.
```

```
Definition blockrep (ve: venv) (flds: members) (b: block) : massert :=  
  sepall (fun (x, ty) : ident * type ⇒  
    match field_offset ge x flds, access_mode ty with  
    | OK d, By_value chunk ⇒ contains chunk b d (match_value ve x)  
    | _, _ ⇒ sepfalse  
  end) flds.
```

# Invariant: staterep

```
Inductive memory (V: Type): Type := mk_memory {  
  mm_values : PM.t V;  
  mm_instances : PM.t (memory V) }.
```

```
Definition staterep_mems (cls: class) (me: memv) (b: block) (ofs: Z) ((x, ty) : ident * typ) :=  
  match field_offset ge x (make_members cls) with  
  | OK d => contains (chunk_of_type ty) b (ofs + d) (match_value me.(mm_values) x)  
  | Error _ => sepfalse  
  end.
```

```
Fixpoint staterep (p: program) (clsnm: ident) (me: memv) (b: block) (ofs: Z): massert :=  
  match p with  
  | nil => sepfalse  
  | cls :: p' => if ident_eqb clsnm cls.(c_name) then  
    sepall (staterep_mems cls me b ofs) cls.(c_mems)  
    ** sepall (fun ((i, c) : ident * ident) => match field_offset ge i (make_members cls) with  
      | OK d => staterep p' c (instance_match me i) b (ofs + d)  
      | Error _ => sepfalse  
    end) cls.(c_objs)  
  else staterep p' clsnm me b ofs  
  end.
```