

Long-Context Language Models

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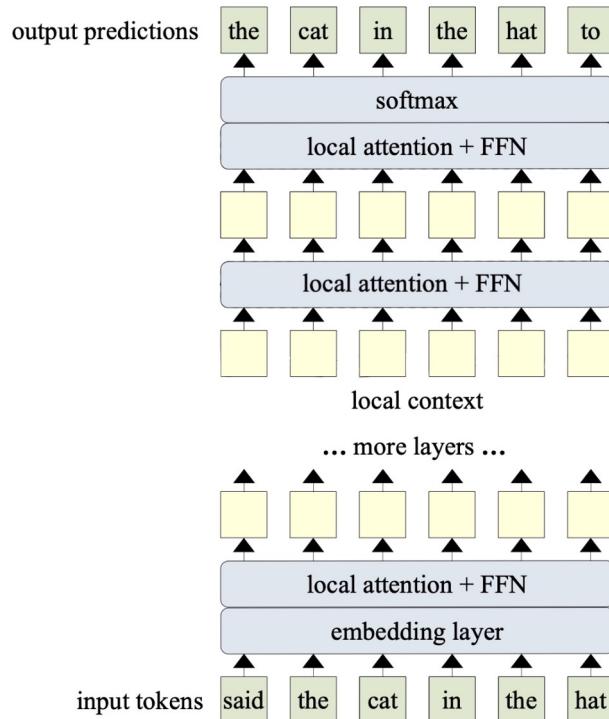


Outlines

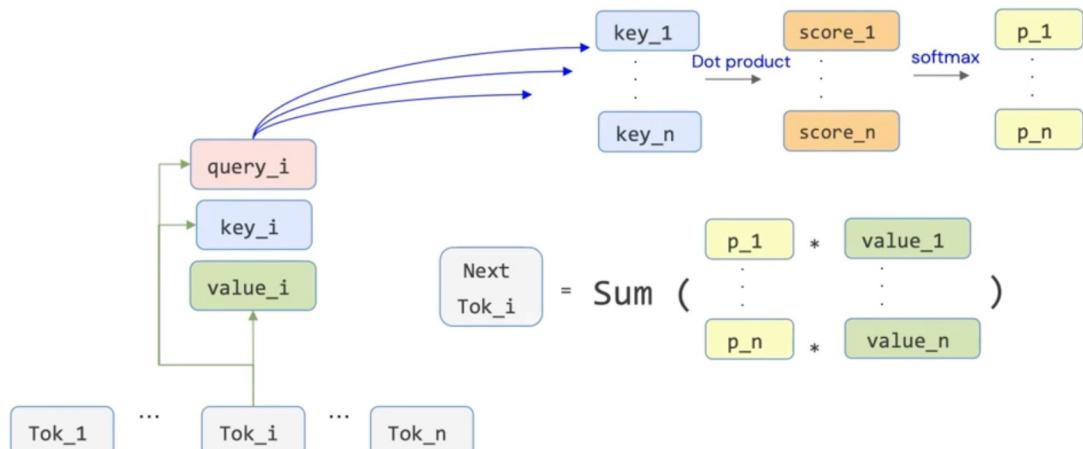
- Review: Transformer Architectures
- Papers
 - Memorizing Transformers (Mar, 2022)
 - LongNet: Scaling Transformers to 1,000,000,000 Token (Jul, 2023)
 - LongLoRA: Efficient Fine-tuning of Long-Context Large Language Models (Dec, 2023)
 - Lost in the Middle: How Language Models Use Long Contexts (Nov, 2023)
- Q&A



Transformer Architecture



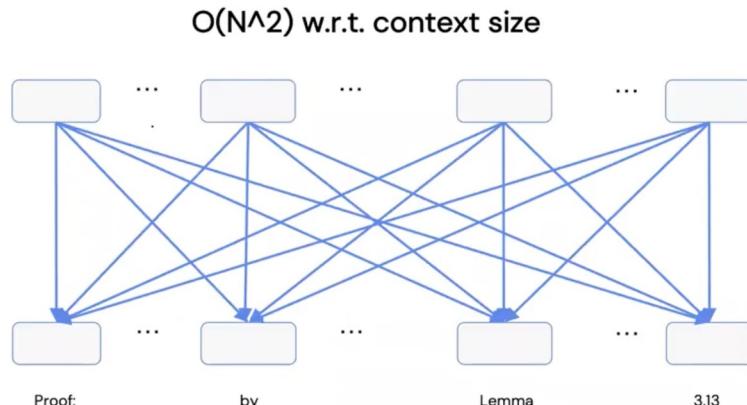
- Word Embedding
- Self-Attention Mechanism
 - Query, Key, Value
 - Dot product Query and Keys to find relevance between tokens: Attention score



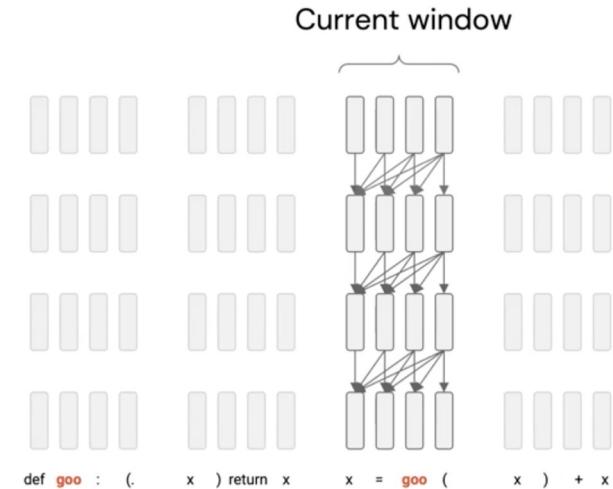


Limitation of Transformers

- Bottleneck
Attend from **each** of the token to **every other** token



- Fixed window size due to quadratic complexity



How to achieve a larger context window?



Memorizing Transformers

Yuhuai Wu, Markus N. Rabe, DeLesley Hutchins, Christian Szegedy

Reference: Wu, Y., Rabe, M. N., Hutchins, D., & Szegedy, C. (2022). Memorizing transformers.
arXiv (Cornell University). <https://doi.org/10.48550/arxiv.2203.08913>

Growing Knowledge Base



- Theorem database in mathematics
 - Codebase in program synthesis

- Codebase in program synthesis

```
def cast_tuple(val, length = 1):
    return val if isinstance(val, tuple) else ((val,),)
```

```
def l2norm(t):
    return F.normalize(t, dim = -1)
```

```
# helper classes
```

```
class PreNormResidual(nn.Module):
    def __init__(self, dim, fn):
        super().__init__()
        self.fn = fn
        self.norm = nn.LayerNorm(dim)
```

```
def forward(self, x, **kwargs):  
    out = self.fn(self.norm(x), **kwargs)
```

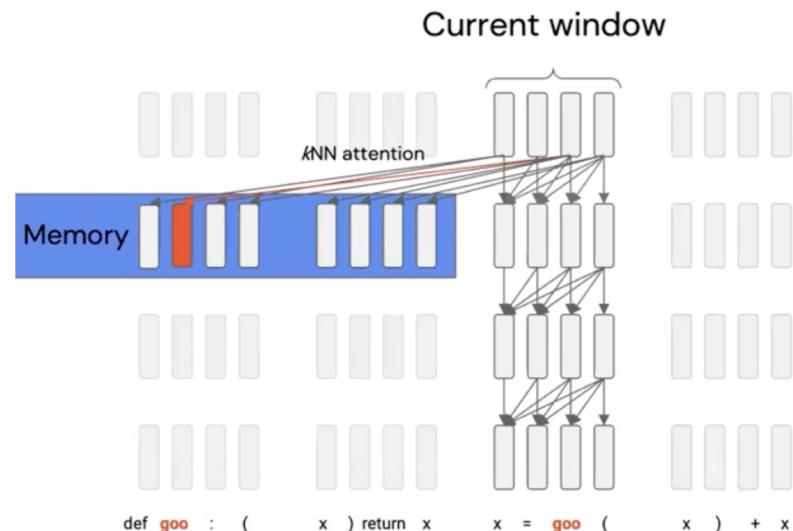
```
if not isinstance(out, tuple):
    return out + x
```

```
head, *tail = out  
return (head + x, *tail)
```



Memorizing Transformers

- Maintain an external memory
Memorize the previously generated keys and values
- kNN Attention
 - An approximate K-Nearest-Neighbor (kNN) lookup into the memory
 - Find top-k most relevant (key, value) pairs in the broad context





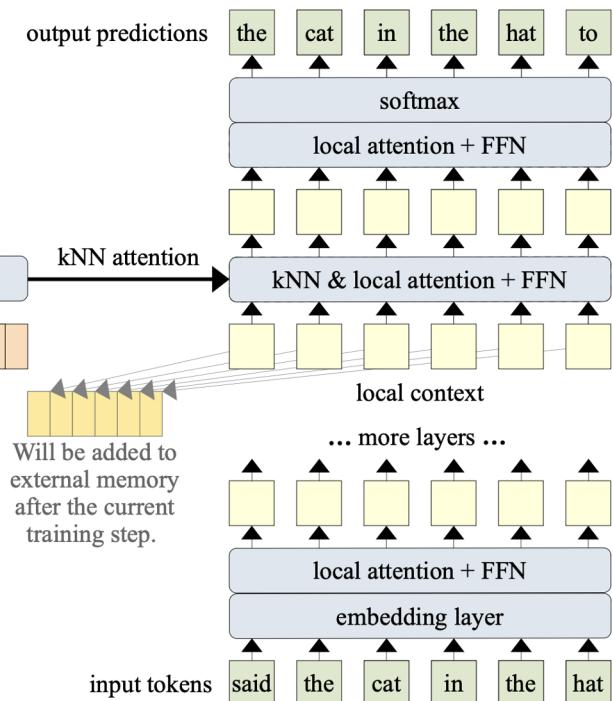
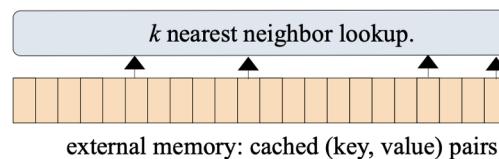
Innovations

- Precision
 - Other approaches average or summarize of tokens at long distances.
 - kNN lookup retrieves **exact values** even from the distant context.
- Scalability
 - In traditional transformer models, gradients are backpropagated through the entire model, updating weights of all the learned information .
 - In the non-differentiable external memory, key-value pairs **remain static** once they are stored and are not updated through the training process
 - The system focus **solely on retrieval** during inference without needing to re-learn or re-compute everything



Memorizing Transformers Architecture

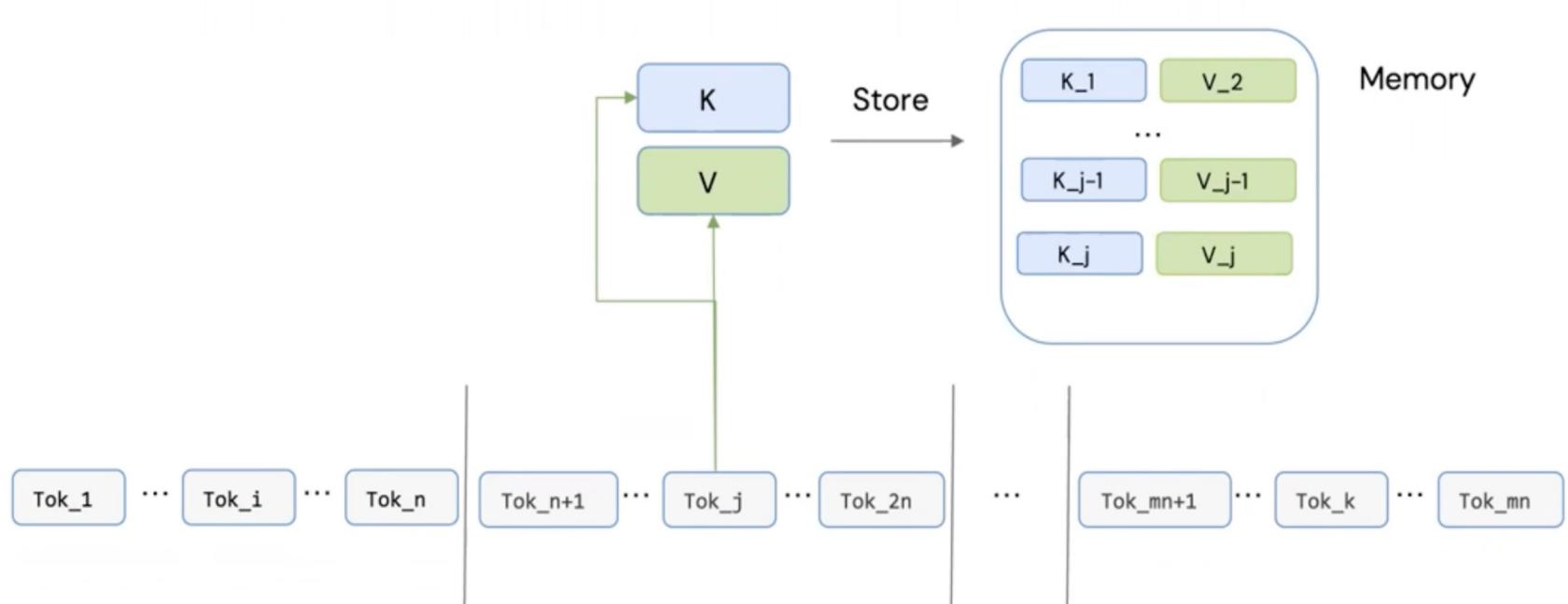
- Combines two forms of attention
 - Standard dense self-attention on the local context
 - Approximate KNN search into the external memory



- After each training step, the (key, value) pairs in the local context are appended to the end of the external memory

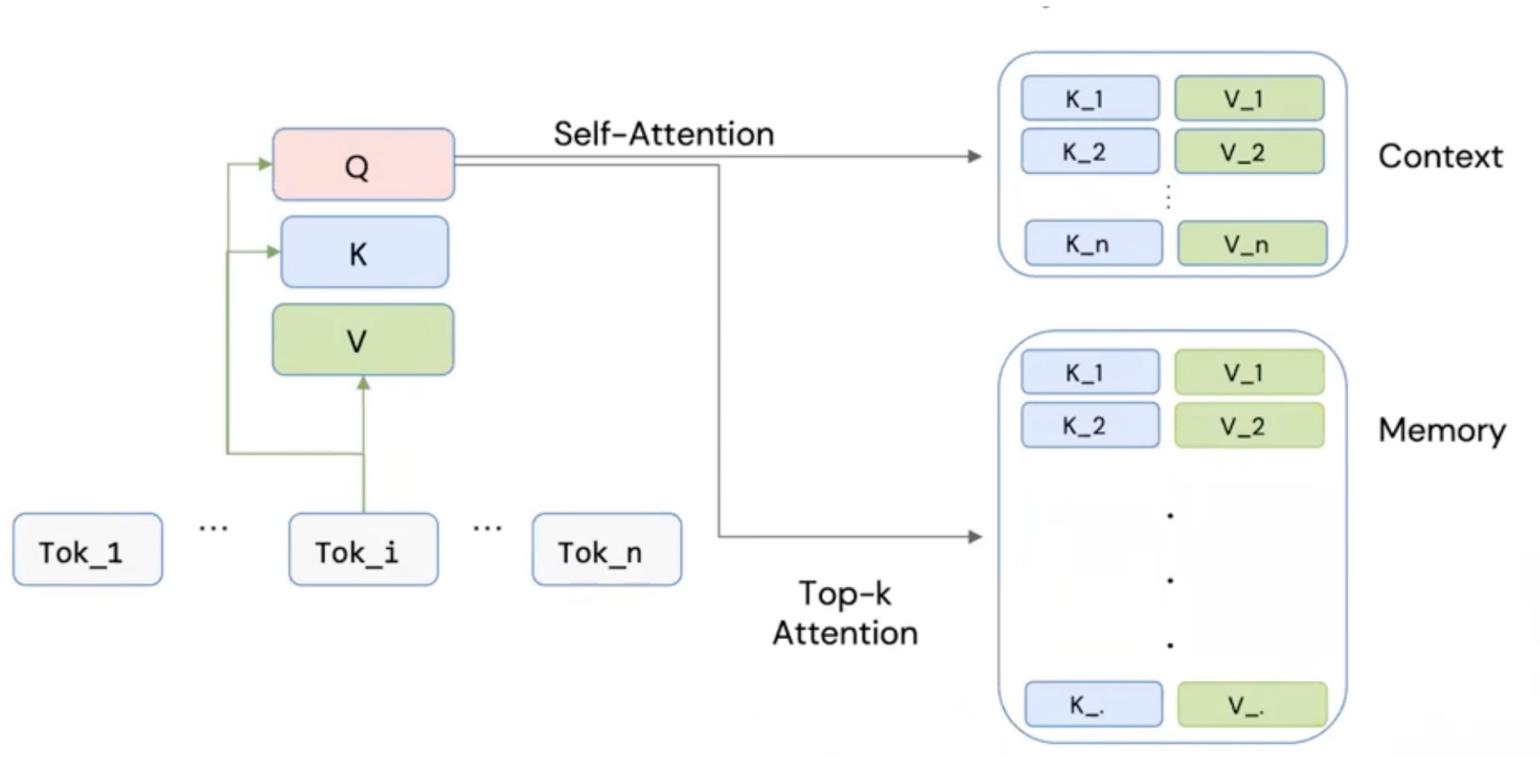


Memorizing Transformer Layers





Memorizing Transformer Layers





Memorizing Transformer Layers

$$\text{Next Tok}_i = \text{gate} * A(\text{Context}) + (1 - \text{gate}) * \text{TopkA}(\text{Memory})$$

Context

Memory

Diagram illustrating the computation of the next token Next Tok_i . The formula shows the weighted sum of the output from the current context layer and the output from the memory layer, scaled by learnable gates.

The Context part is represented by a box containing a grid of K key (K_1, K_2, \dots, K_n) and value (V_1, V_2, \dots, V_n) pairs.

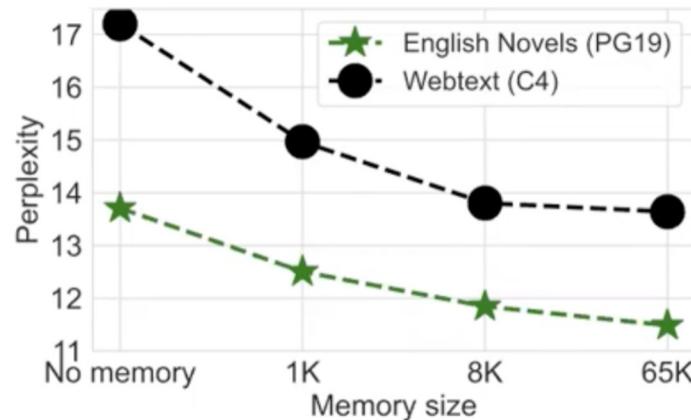
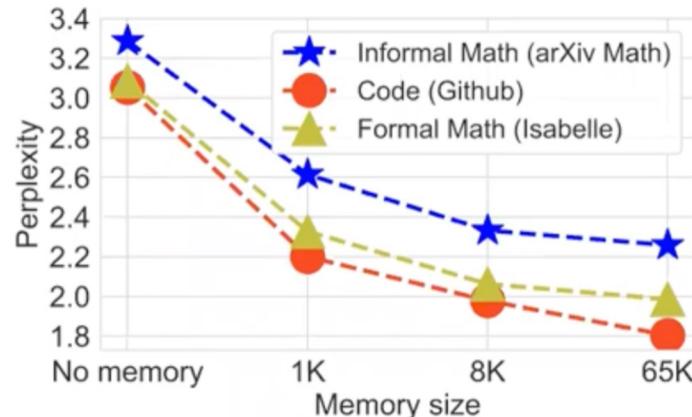
The Memory part is represented by a large rounded rectangle containing multiple pairs of keys ($K_1, K_2, \dots, K_{\dots}, K_{\dots}$) and values ($V_1, V_2, \dots, V_{\dots}$).

gate is a learnable scalar between 0 and 1.



Improvements with External Memory

- Test on a variety of language modelling tasks involving long-form text
- Evaluate perplexity: The uncertainty of a model to predict the next word
- Lower perplexity values = better (more confident) predictions by model

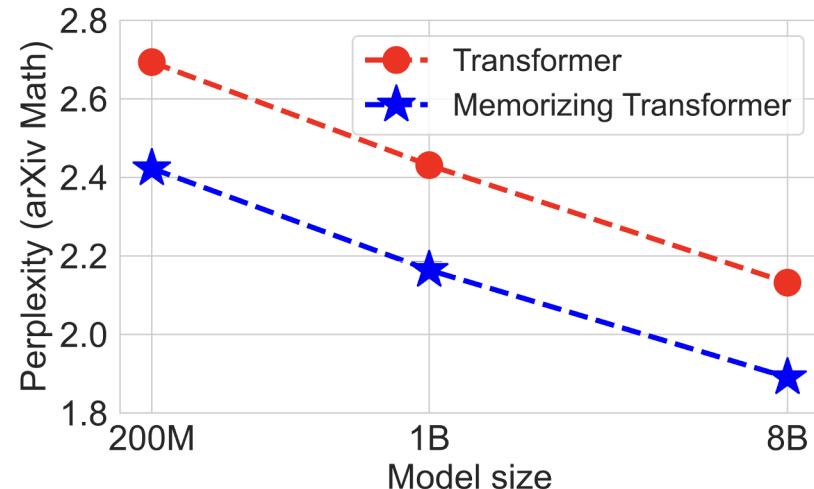


- Model perplexity steadily improves with the size of external memory
- Diminishing marginal decreasing from an increasing memory size



Improvements by Memory on Large Models

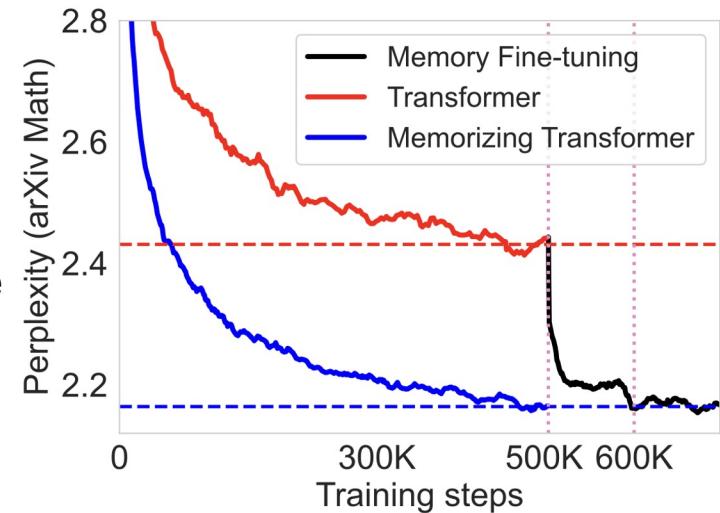
- Compare to normal transformers on arXiv math dataset
- Add a memory of size 8K to normal transformer models in different sizes
- The memory mechanism helps consistently when scaling model size up to 8B.
- 8K memory attained results comparable to the larger model which has 5-8X more trainable parameters





Fine-Tuning transformer to use memory

- Train memory from scratch v.s. Fine tunes the model to use memory
- Finetuning a 1B vanilla Transformer model to use external memory of size 65K.
- Within 20K steps (**4% of the pre-training time**), the fine-tuned model has already closed **85% of the gap** between it and the 1B Memorizing Transformer.
- After 100k steps it has closed the gap entirely.





Fine-Tuning for a Larger Memory

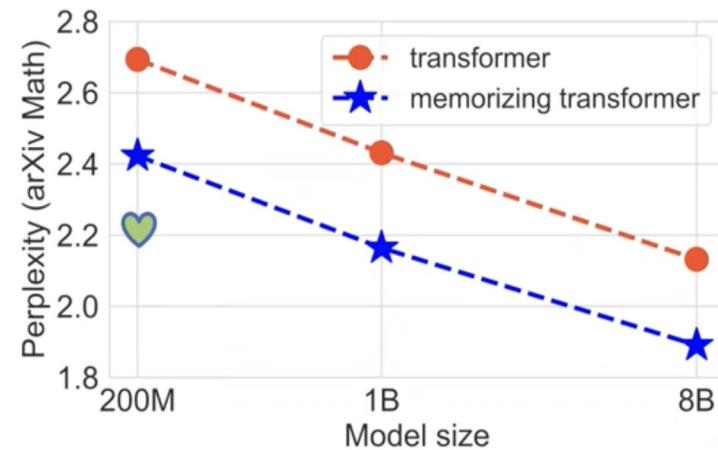
- Firstly pretrain the model with a small memory and fine tunes it to make use of a larger memory (on the arXiv dataset)
- Increasing the size of external memory provided consistent gains up to a size of **262K**, which achieved results comparable to a **40X** larger model

Perplexity: The lower the better.

Pretrain	Fine-tune	Perplexity
8192	None	2.33
65K	None	2.26
65K	131k	2.23
65K	262k	2.21

★ 8K memory

♡ 262K memory





Information Retrieval Patterns

- A qualitative study of what the model was actually retrieving from external memory
- Find tokens which showed the biggest improvements in cross-entropy loss when the size of the memory was increased, and then examining the **top-k retrieved memories** for those tokens.
- The model gained the most when looking up **rare words**: proper names, references, citations, and function names, where the first use of a name is too far away from subsequent uses to fit in the local context.



Information Retrieval Patterns

- Examples of memory retrieval
- The retrieved surrounding context (highlighted) is the definition body of the mathematical object highlighted in the querying context.

Predicting lemma name

```
Same structure  
also have "... ≤ ES.expectation ?Y / 1"  
  by (rule prob_space.markov_inequality)
```

Look up definitions -- 20K tokens apart.

```
lemma markov_inequality:  
  assumes "λa. 0 ≤ X a" and "integrable M X" "0 < t"  
  shows "prob {a ∈ space M. t ≤ X a} ≤ expectation X / t"  
proof -  
  --{* proof adapted from @{thm [source] edge_space.Markov_inequali-  
    @{term prob_space}s *}  
  have "(∫+ x. ennreal (X x) ∂M) = (∫x. X x ∂M)"  
  using assms by (intro nn_integral_eq_integral) auto
```



Takeaways

- K-Nearest-Neighbor lookup into a large external memory
- Dramatically increases the length of the context that a language model can attend to
- Genericness: A large improvement across variety of long-document tasks
- Scalability: Perplexity continues to improve with increasing memory size
- A Memorizing Transformer does not need to be pre-trained from scratch
- Immediate utilization of newly acquired knowledge



LONGNET: Scaling Transformers to 1,000,000,000 Tokens

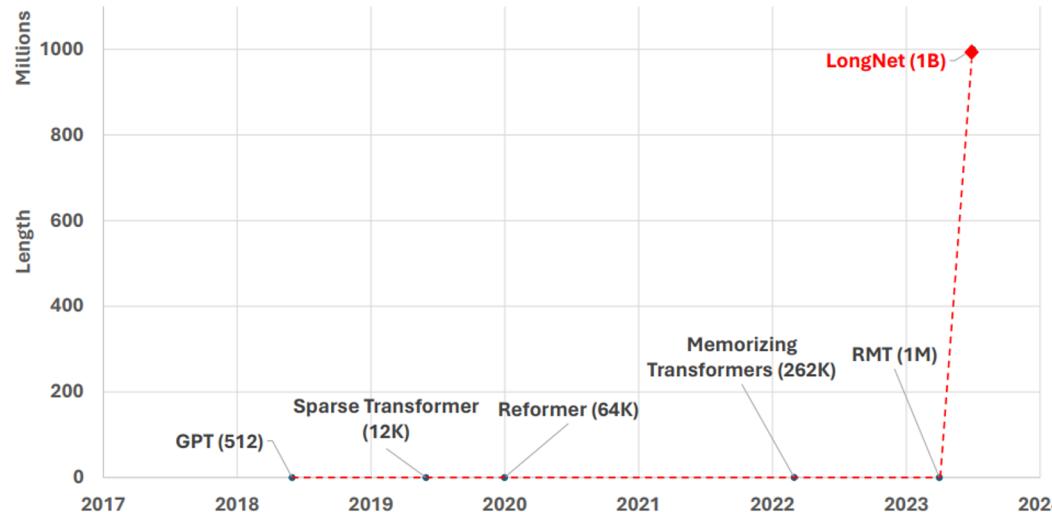
Jiayu Ding Shuming Ma Li Dong Xingxing Zhang
Shaohan Huang Wenhui Wang Nanning Zheng Furu Wei

<https://arxiv.org/pdf/2307.02486>



Background

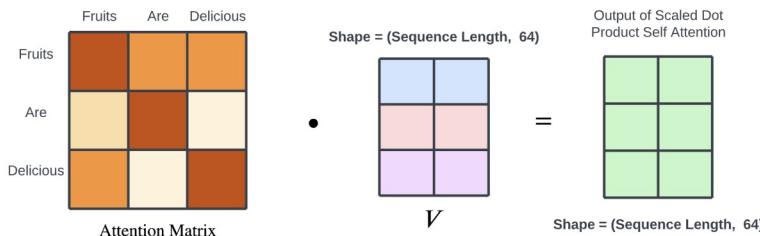
- Conflicts between the demanding need to scale up LLMs and degrades on performances.
- Degrades originate in the computational complexity, which is quadratic.





Attention Recap

- Why is it quadratic?
- Turn quadratic into linear or near linear

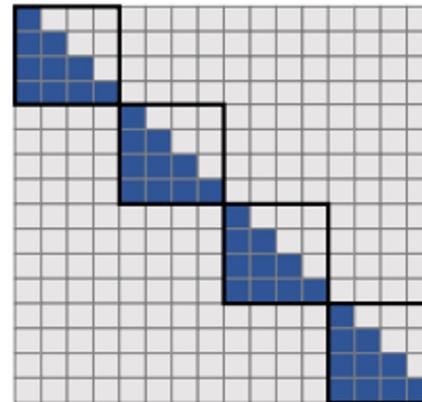


Method	Computation Complexity
Recurrent	$\mathcal{O}(Nd^2)$
Vanilla Attention	$\mathcal{O}(N^2d)$
Sparse Attention	$\mathcal{O}(N\sqrt{Nd})$
Dilated Attention (This Work)	$\mathcal{O}(Nd)$



Dilated Attention - Key innovation

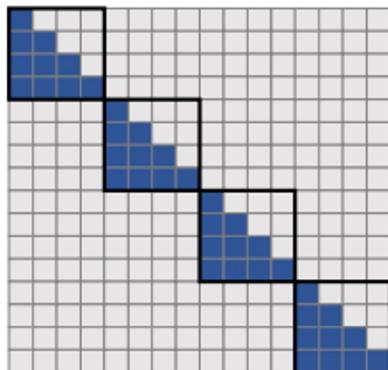
- Sparse attention did dramatically reduce the computation, but they are **LOCAL!!!**
- Dilated Attention with dilation rate = 1 is just the same as sparse attention.
- How to handle information flow



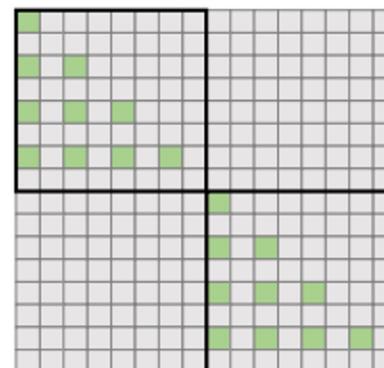


Dilated Attention

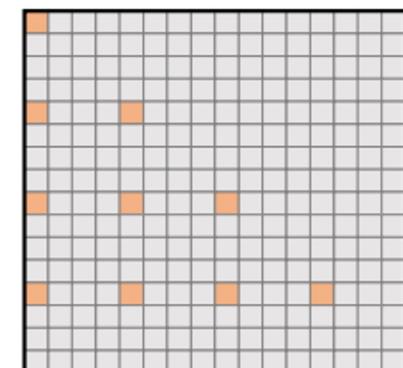
- Multiple dilation rates and stack the layers



Segment Length: 4
Dilated Rate: 1



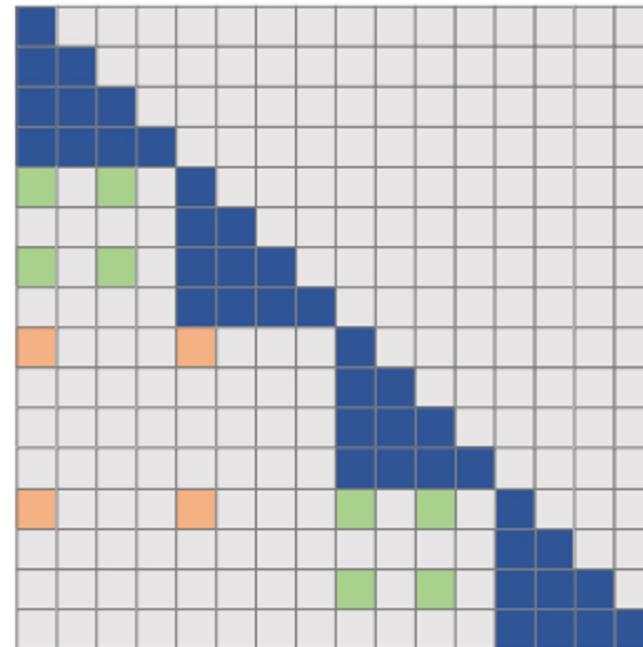
Segment Length: 8
Dilated Rate: 2



Segment Length: 16
Dilated Rate: 4



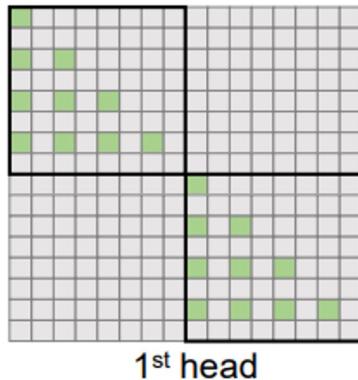
LongNet: Dilated Attention



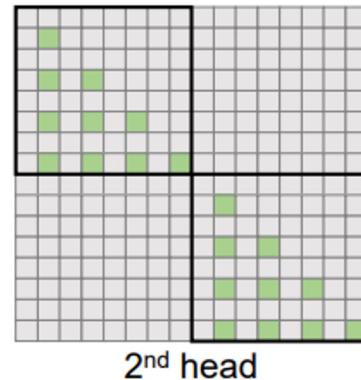


Multihead Dilated Attention

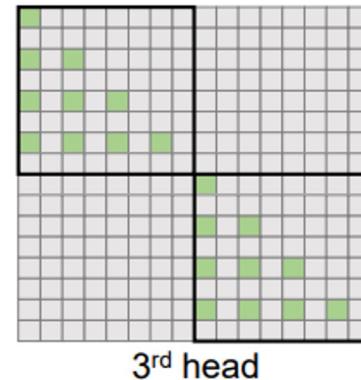
- To make it converge even faster, we can have different patterns under the same dilation rate for each head.



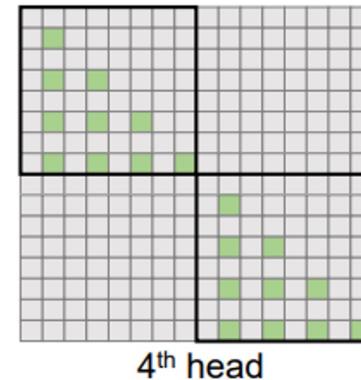
1st head



2nd head



3rd head



4th head

Segment Length: 8
Dilated Rate: 2
Heads: 4

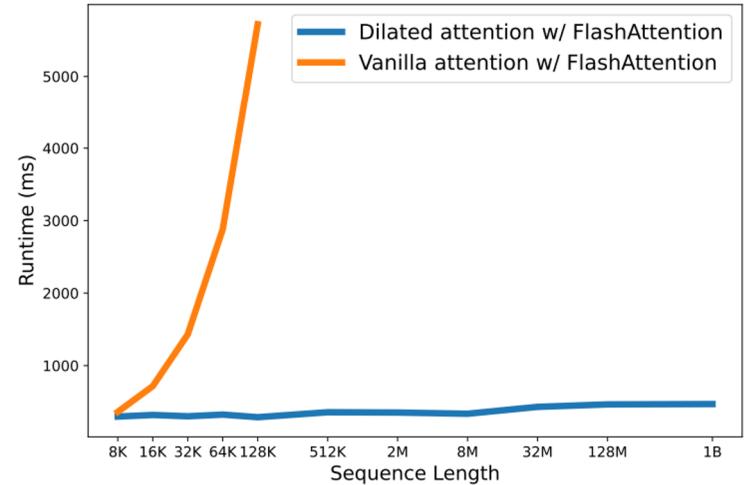


Computational Complexity

$$FLOPs = \frac{2N}{w} \left(\frac{w}{r}\right)^2 d = \frac{2Nwd}{r^2}$$

$$FLOPs = 2Nd \sum_{i=1}^k \frac{w_i}{r_i^2}$$

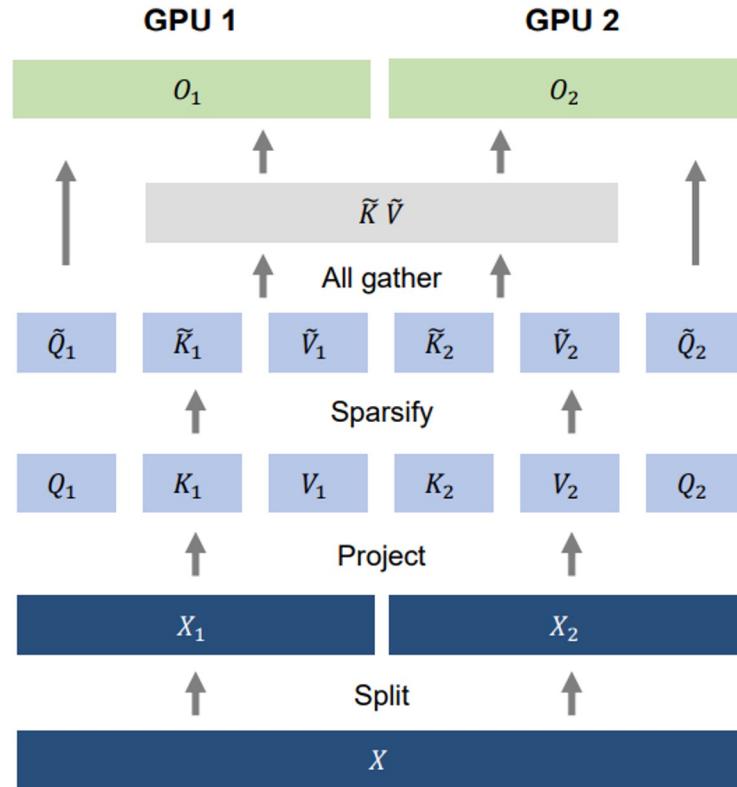
$$FLOPs = 2w_0Nd \sum_{i=0}^{k-1} \frac{1}{\alpha^i} \leq \frac{2\alpha}{\alpha - 1} w_0 Nd \quad (\alpha > 1)$$



The complexity is now $O(Nd)$. **LINEAR!**



Parallelizing computation on GPUs





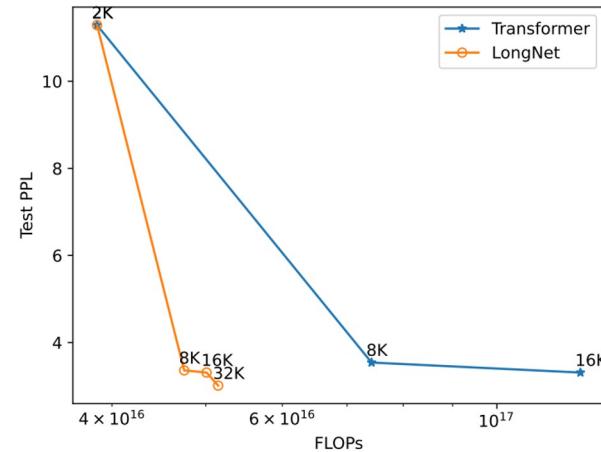
Results

Perplexity:

- LongNet consistently outperform the benchmark models with different context lengths.
- LongNet achieved similar performance level with significantly less computational cost.

Model	Length	Batch	Github		
			2K	8K	32K
Transformer [VSP ⁺ 17]	2K	256	4.24	5.07	11.29
Sparse Transformer [CGRS19] LONGNET (ours)	8K	64	4.39 4.23	3.35 3.24	8.79 3.36
Sparse Transformer [CGRS19] LONGNET (ours)	16K	32	4.85 4.27	3.73 3.26	19.77 3.31
Sparse Transformer [CGRS19] LONGNET (ours)	32K	16	5.15 4.37	4.00 3.33	3.64 3.01

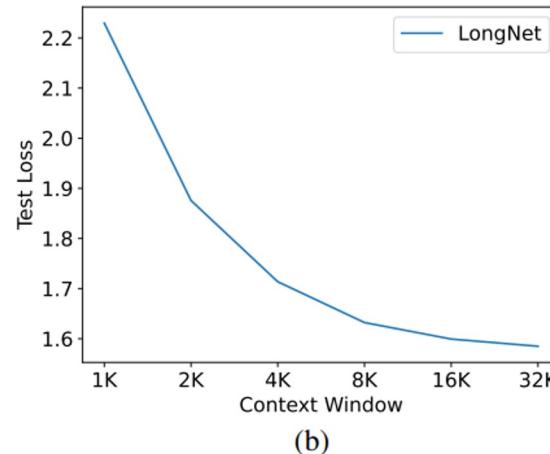
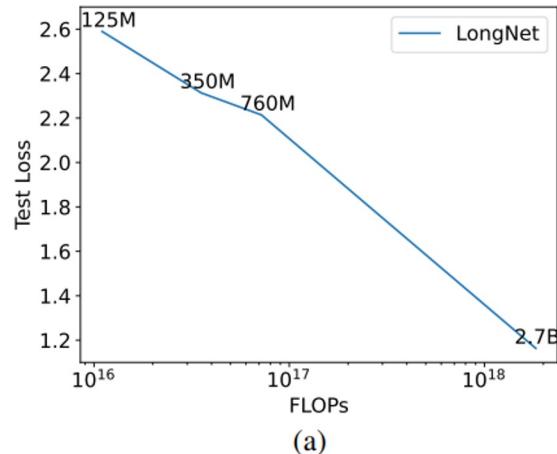
Table 2: Perplexity of language models for LONGNET and the baselines.





Results

- Larger model size → lower test loss
- Larger context window → lower test loss





LONGLORA: EFFICIENT FINE-TUNING OF LONGCONTEXT LARGE LANGUAGE MODELS

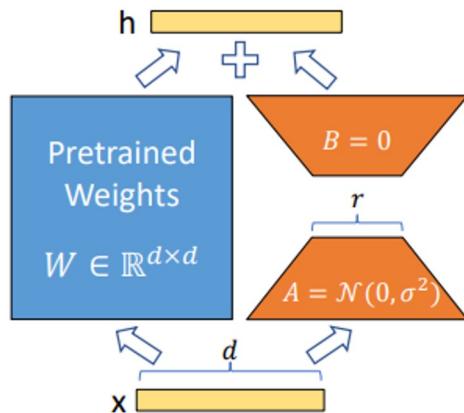
Yukang Chen Shengju Qian Haotian Tang Xin Lai Zhijian Liu Song Han Jiaya Jia

<https://arxiv.org/pdf/2309.12307>



LoRA Recap

- Observations: Weights learned after training contains redundancies.
- Using low-rank approximation instead of tuning the entire weights in the model.

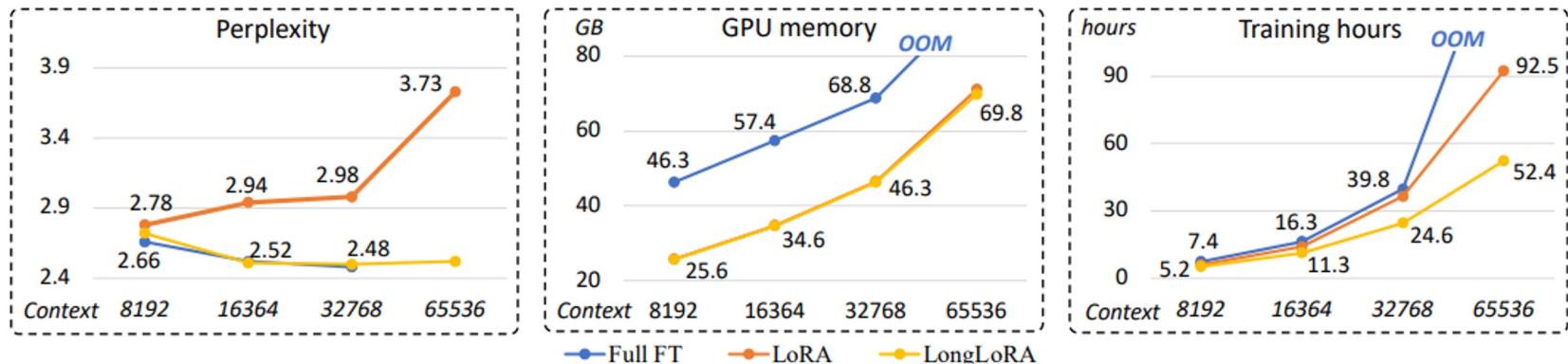


$$W_0 + \Delta W = W_0 + BA,$$



Problems with LoRA

- LoRA is neither sufficiently effective nor efficient when the context length increases to more than 8K tokens.

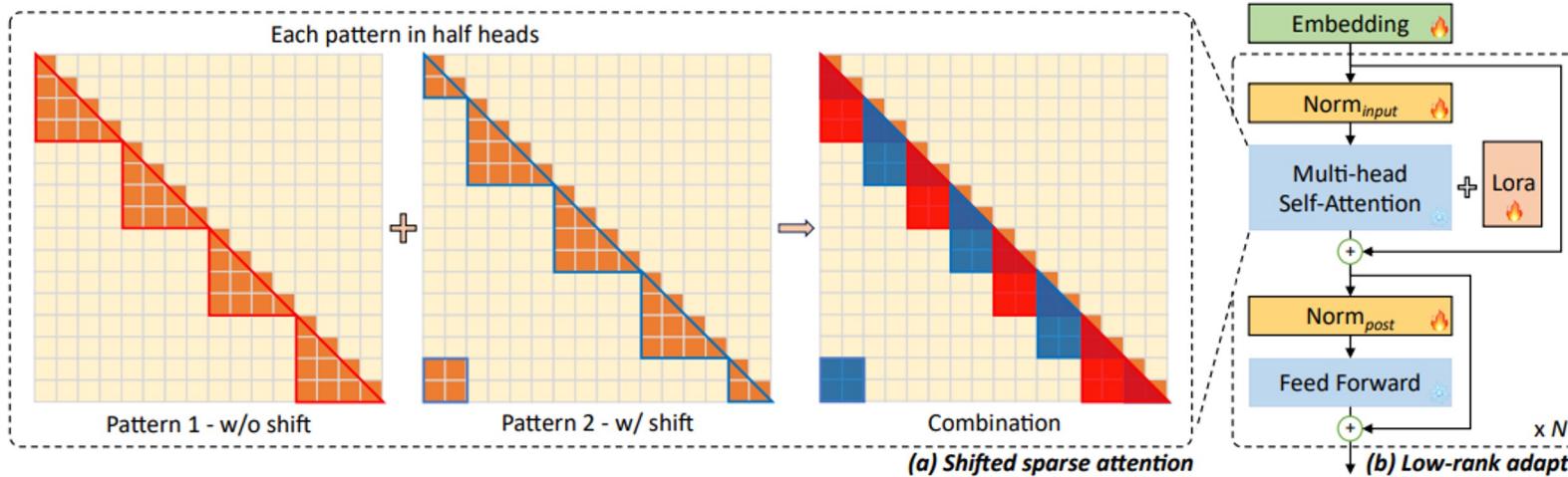


*A perplexity of N can be interpreted as the model being as confused as if it had to choose uniformly among N options for each word. The lower, the better.



What is LongLoRA

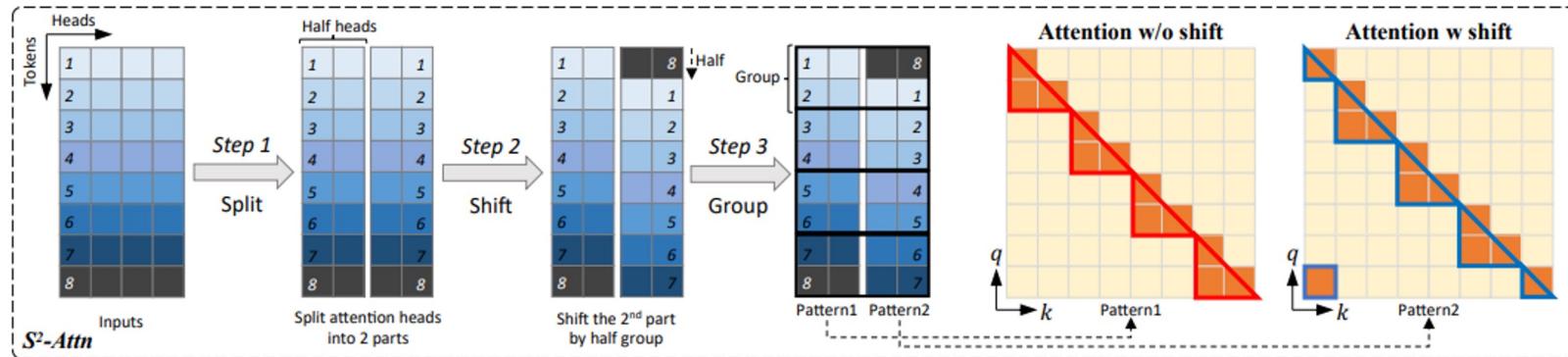
- Shifted Sparse Attention (S^2 attention)
- Parameter efficient tuning





S² Attention

- Split attention heads into two partitions, shift one of the partition half the group size.
- Reduce computation by local sparse attention.
- Ensure information flow by shifting.





S² Attention

Algorithm 1: Pseudocode of S²-Attn in PyTorch-like style.

```
# B: batch size; S: sequence length or number of tokens; G: group size;
# H: number of attention heads; D: dimension of each attention head

# qkv in shape (B, N, 3, H, D), projected queries, keys, and values
# Key line 1: split qkv on H into 2 chunks, and shift G/2 on N
qkv = cat((qkv.chunk(2, 3)[0], qkv.chunk(2, 3)[1].roll(-G/2, 1)), 3).view(B*N/G, G, 3, H, D)

# standard self-attention function
out = self_attn(qkv)

# out in shape (B, N, H, D)
# Key line 2: split out on H into 2 chunks, and then roll back G/2 on N
out = cat((out.chunk(2, 2)[0], out.chunk(2, 2)[1].roll(G/2, 1)), 2)
```

cat: concatenation; chunk: split into the specified number of chunks; roll: roll the tensor along the given dimension.



S² Attention

Design process:

- **Sparse attention** to reduce computational cost
- How to handle information flow → **Shifting**

Pros:

- Consistent to Full attention: same architecture & full attention while inferencing
- Easy implementation



Parameter Efficient Tuning

- Lora only works with attention layers → open normalization and embedding layers for training
- These layers only occupy **limited parameters** in the whole model and thus will not introduce new computational cost.

Table 2: **Finetuning normalization and embedding layers is crucial for low-rank long-context adaptation.** Llama2 7B (Touvron et al., 2023b) models with the proposed S²-Attn are trained on the RedPajama (Computer, 2023) dataset. The target context length is 32768. ‘+ Normal / Embed’ means normalization or embedding layers are trainable. Perplexity results are evaluated on PG19 (Rae et al., 2020) validation set. For long context adaptation, there is a large performance gap between standard LoRA (Hu et al., 2022) and full fine-tuning. Without trainable normalization or embeddings, larger ranks in LoRA can not close this gap.

Method	Full FT	LoRA (rank)						LoRA (rank = 8)		
		8	16	32	64	128	256	+ Norm	+ Embed	+ Norm & Embed
PPL	8.08	11.44	11.82	11.92	11.96	11.97	11.98	10.49	8.29	8.12



Evaluations

Experiment settings:

- 7B ,13B, 20B Llama2 pretrained;
- Position indices all rescaled based on *positional encoding*
- Trained on a single $8 \times$ A100 GPUs machine
- Fine tune objectives: **Next token prediction**
- Two tasks:
 - Long Sequence Language Modeling
 - Topic Retrieval



Evaluations - Long Sequence Language Modeling

Perplexity evaluation on PG19 dataset

Size	Training Context Length	LongLoRA		Evaluation Context Length				
		S ² -Attn	LoRA ⁺	2048	4096	8192	16384	32768
7B	8192	✓		3.14	2.85	2.66	-	-
		✓	✓	3.15	2.86	2.68	-	-
			✓	3.20	2.91	2.72	-	-
	16384	✓		3.17	2.87	2.68	2.55	-
		✓	✓	3.17	2.87	2.66	2.51	-
	32768	✓		3.20	2.90	2.69	2.54	2.49
		✓	✓	3.35	3.01	2.78	2.61	2.50
13B	8192	✓		2.96	2.69	2.53	-	-
		✓	✓	3.01	2.74	2.57	-	-
			✓	3.04	2.77	2.60	-	-
	16384	✓		2.99	2.72	2.53	2.40	-
		✓	✓	3.03	2.74	2.55	2.41	-
	32768	✓		3.04	2.75	2.56	2.42	2.33
		✓	✓	3.05	2.76	2.57	2.42	2.32



Evaluations

Maximum context length can be tuned

Size	Training Context Length	Evaluation Context Length						
		2048	4096	8192	16384	32768	65536	100,000
7B	100,000	3.36	3.01	2.78	2.60	2.58	2.57	2.52
13B	65536	3.20	2.88	2.66	2.50	2.39	2.38	-
70B	32768	2.84	2.57	2.39	2.26	2.17	-	-

Topic Retrieval

Evaluation Context	3k	6k	10k	13k	16k
ChatGLM2-6B (Du et al., 2022)	0.88	0.46	0.02	0.02	0.02
MPT-30B-chat (Team, 2023a)	0.96	1.0	0.76	-	-
MPT-7B-storywriter (Team, 2023b)	0.46	0.46	0.28	0.34	0.36
LongChat-13B (Li et al., 2023)	1.0	1.0	1.0	0.98	0.9
Ours-13B	1.0	0.98	0.98	0.98	0.94



Evaluations

Efficiency Evaluation

Substantially decreases FLOPs, particularly with longer context lengths.

Group size

Set group size as $\frac{1}{4}$ in experiments based on the results.

Context Length	S ² -Attn	FLOPs (T)				Total
		Attn	Proj	FFN	Others	
8192	✗	35.2	35.2	70.9	2.2	143.5
	✓	8.8				117.1
16384	✗	140.7	70.4	141.8	4.3	357.2
	✓	35.2				251.7
32768	✗	562.9	140.7	283.7	8.7	996.0
	✓	140.7				573.8
65536	✗	2251.8	281.5	567.4	17.3	3118.0
	✓	562.9				1429.1

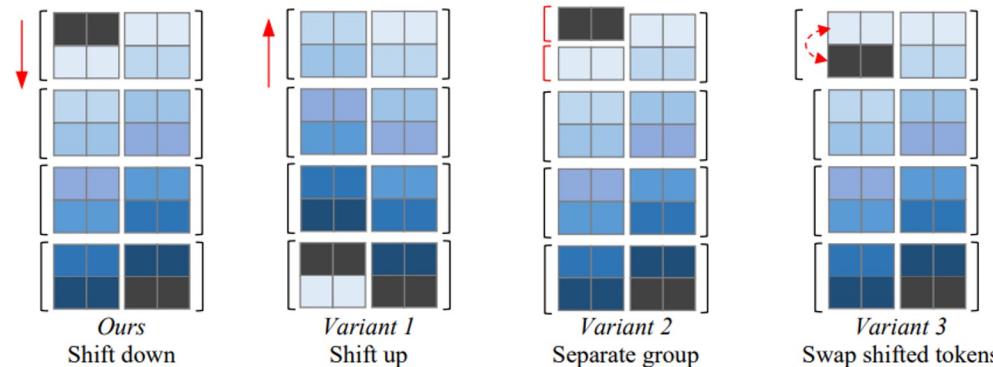
Context Length	Full	1/2	1/4	1/6	1/8
8192	8.02	8.04	8.04	8.10	8.16
16384	7.82	7.84	7.86	7.94	7.98



Ablation Studies

Variants of S² Attention

Shifting direction has no effect on the perplexity; performances are similar.



Attn	Full	Ours	Variant 1	Variant 2	Variant 3
PPL	8.02	8.04	8.04	8.03	8.05



Lost in the Middle: How Language Models Use Long Context

Nelson F. Liu, Kevin Lin, John Hewitt, Ashwin Paranjape,
Michele Bevilacqua, Fabio Petroni, Percy Liang

<https://arxiv.org/abs/2307.03172>

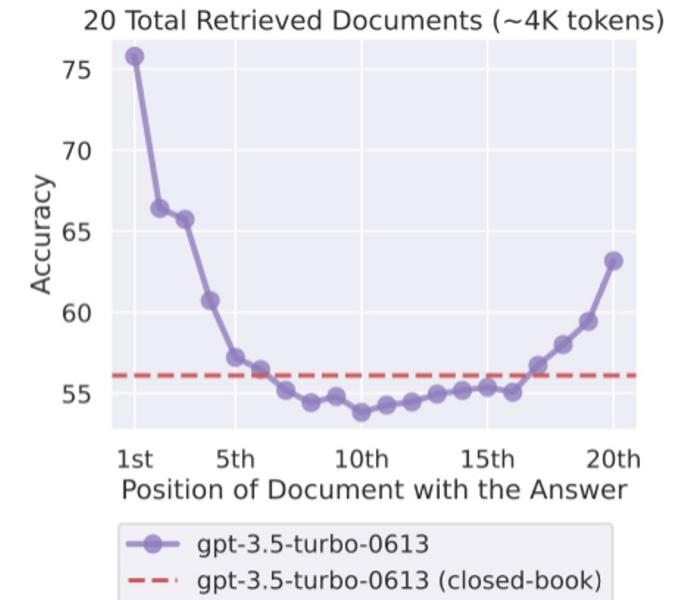


Background

Language models have significantly improved, enabling them to handle longer text inputs.

Despite these advancements, efficiently utilizing long text contexts remains a challenge.

How effectively do modern language models actually utilize long text contexts? Does the performance of these models significantly deteriorate when the relevant information is positioned **in the middle of the text**?





Multi-document question answering

Input: (1). A question to answer; (2). k documents

Dataset Utilization: NaturalQuestions-Open dataset featuring historical Google search queries and human-annotated answers from Wikipedia.

Open models: MPT-30B-Instruct, LongChat-13B

Closed models: GPT-3.5-Turbo, GPT-3.5-Turbo (16K), Claude-1.3, Claude-1.3 (100K)

Input Context

Write a high-quality answer for the given question using only the provided search results (some of which might be irrelevant).

Document [1] (Title: Asian Americans in science and technology) Prize in physics for discovery of the subatomic particle J/\psi. Subrahmanyan Chandrasekhar shared...

Document [2] (Title: List of Nobel laureates in Physics) The first Nobel Prize in Physics was awarded in 1901 to Wilhelm Conrad Röntgen, of Germany, who received...

Document [3] (Title: Scientist) and pursued through a unique method, was essentially in place. Ramón y Cajal won the Nobel Prize in 1906 for his remarkable...

Question: who got the first nobel prize in physics

Answer:

Desired Answer

Wilhelm Conrad Röntgen

Input Context

Write a high-quality answer for the given question using only the provided search results (some of which might be irrelevant).

Document [1] (Title: List of Nobel laureates in Physics) ...

Document [2] (Title: Asian Americans in science and technology) ...

Document [3] (Title: Scientist) ...

Question: who got the first nobel prize in physics

Answer:

Desired Answer

Wilhelm Conrad Röntgen

Input Context

Write a high-quality answer for the given question using only the provided search results (some of which might be irrelevant).

Document [1] (Title: Asian Americans in science and technology) ...

Document [2] (Title: List of Nobel laureates in Physics) ...

Document [3] (Title: Scientist) ...

Document [4] (Title: Norwegian Americans) ...

Document [5] (Title: Maria Goeppert Mayer) ...

Question: who got the first nobel prize in physics

Answer:

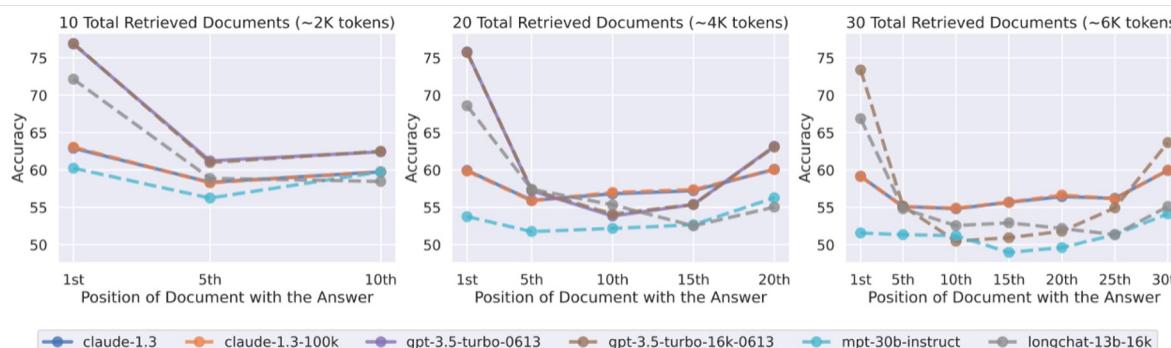
Desired Answer

Wilhelm Conrad Röntgen



Multi-document question answering

- Model performance is highest when relevant information occurs at the **beginning or end** of its input context.
- Extend-context models are not necessarily better at using input context.



Model	Closed-Book	Oracle
LongChat-13B (16K)	35.0%	83.4%
MPT-30B-Instruct	31.5%	81.9%
GPT-3.5-Turbo	56.1%	88.3%
GPT-3.5-Turbo (16K)	56.0%	88.6%
Claude-1.3	48.3%	76.1%
Claude-1.3 (100K)	48.2%	76.4%

Table 1: Closed-book and oracle accuracy of language models on the multi-document question answering task.



How well can language models retrieve from input context

- Objective: Assess model adaptability to input changes and complex scenarios.
- Input: Serialized JSON with key-value pairs.
- Task: Synthetic key-value retrieval to find specific values.
- Evaluation: Focuses on model performance amid input context and structural changes.

Input Context

Extract the value corresponding to the specified key in the JSON object below.

JSON data:

```
{"2a8d601d-1d69-4e64-9f90-8ad825a74195": "bb3ba2a5-7de8-434b-a86e-a88bb9fa7289",
 "a54e2eed-e625-4570-9f74-3624e77d6684": "d1ff29be-4e2a-4208-a182-0cea716be3d4",
 "9f4a92b9-5f69-4725-ba1e-403f08dea695
```

Key: **"9f4a92b9-5f69-4725-ba1e-403f08dea695"**

Corresponding value:

Desired Output

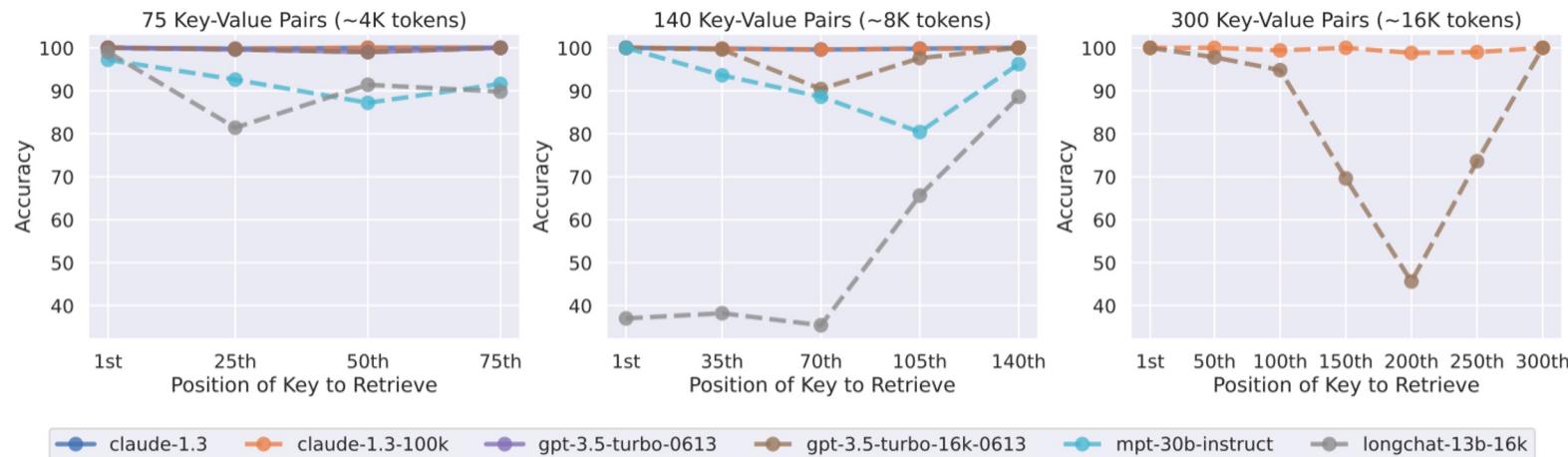
```
703a7ce5-f17f-4e6d-b895-5836ba5ec71c
```



How well can language models retrieve from input context

The models like [Claude-1.3](#) perform almost perfectly in retrieving values, regardless of the number of distractors.

Models such as [GPT-3.5-Turbo](#) and [LongChat-13B](#) exhibit difficulties when key-value pairs are positioned in the middle of the input, with LongChat-13B generating code to retrieve keys instead of directly outputting values.

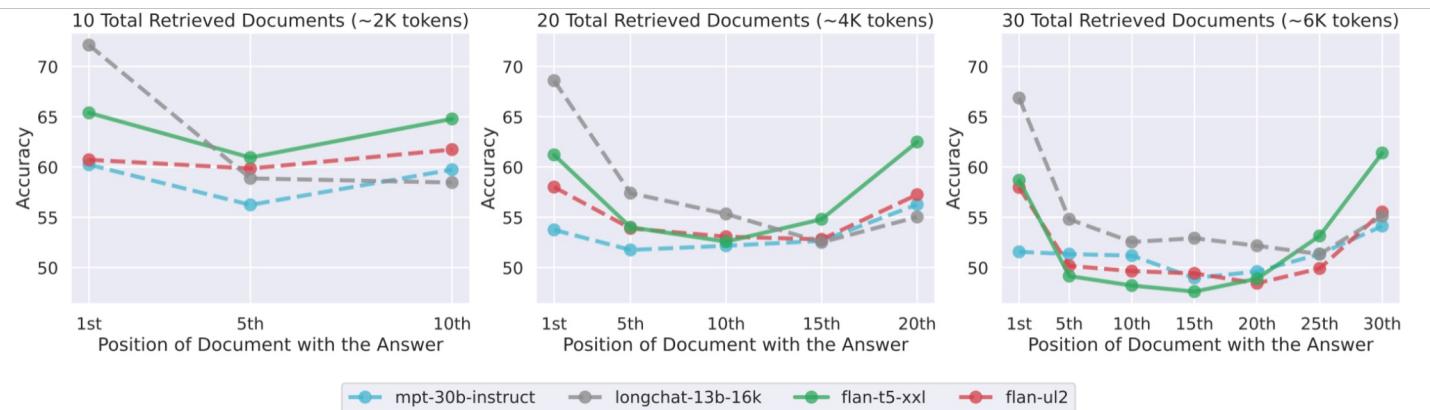




Why Are Language Models Not Robust to Changes in the Position of Relevant Information?

Effect of Model Architecture

- Decoder-only models struggle with long input contexts, especially when the relevant information shifts within the input.
- Encoder-decoder models like Flan-T5-XXL and Flan-UL2 show better resilience and performance due to their bi-directional context processing capabilities.





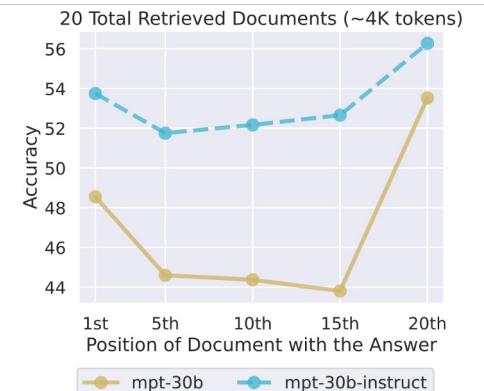
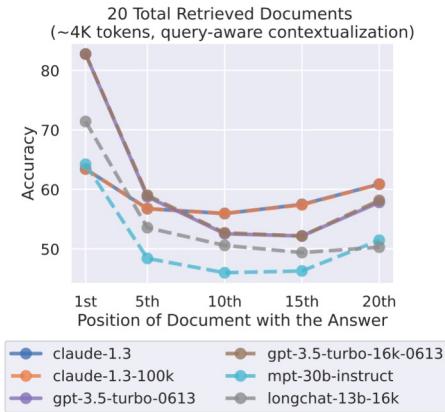
Why Are Language Models Not Robust to Changes in the Position of Relevant Information?

Effect of Query-Aware Contextualization

- Placing the query before and after documents
- **Minimal improvement** in question answering tasks; notable only when information is at the very beginning or end of the input.

Effect of Instruction Fine-Tuning

- Models are fine-tuned on instruction-specific datasets to enhance their response quality.
- **Fine-tuning** helps reduce performance disparity in models, especially in worst-case scenarios, but overall trends remain similar.



Is more context is always better? A case study with open-domain QA



Experiment Setup:

- Retriever-reader model with a retrieval system fine-tuned on MS-MARCO.
- Recall and accuracy based on retrieved documents containing correct answers.

Findings:

- Retrieval performance peaks with just **20 documents**.
- **Slight accuracy improvement** (~1-1.5%) with more context but at a high computational cost.
- Suggests better document **reranking** or **truncating** retrieved lists over simply increasing context.

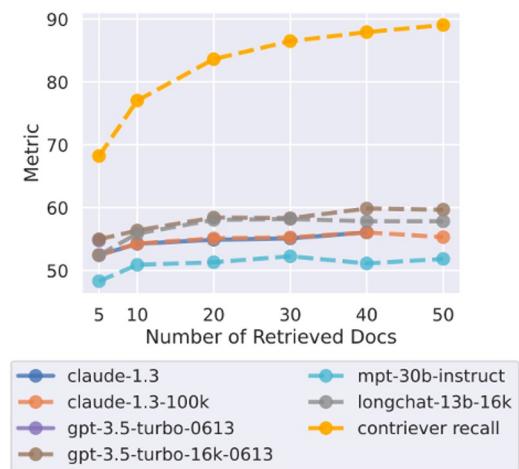


Figure 11: Retriever recall and model performance as a function of the number of retrieved documents. Model performance saturates long before retriever recall, indicating that the models have difficulty making use of the extra retrieved documents.



Conclusion

- Performance Degradation with Changing Information Position
 - Models struggle to robustly access and utilize information in long input contexts.
 - Performance is often **lowest** when the relevant information is located **in the middle of long input contexts**.
- Contributions and Future Directions
 - Provide a better understanding of how language models utilize their input context.
 - Propose new evaluation protocols for future long-context models and highlight areas for improvement.



Q&A