

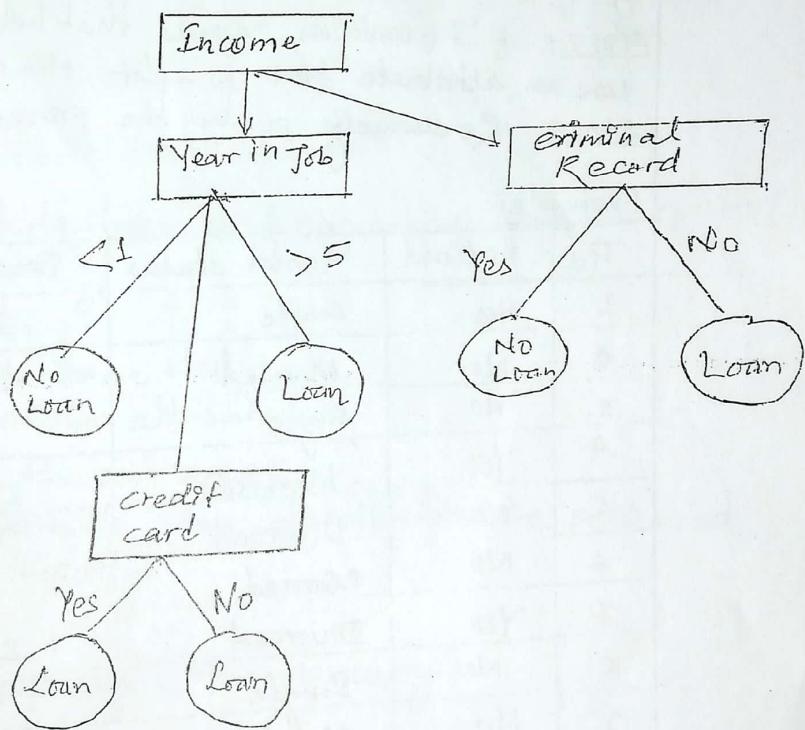
Classification

Grouping(1) Decision Tree:

→ A decision tree is a structure in which each branch represents a choice between a number of alternatives and each leaf node represents a classification or decision.

→ Decision tree is a classifier in the form of a tree structure where each node is either a leaf node, indicating a class instances or a decision node that represents some test to be carried out on a single attribute value with one branch a subtree for each possible outcome of tree.

→ It can be used to classify an instance by starting at root of the tree and moving through it until leaf node, which provides the classification of the instances.

Example :-Advantages:-

- Extremely fast for classifying unknown records
- Easy to interpret
- High accuracy for simple data.

Some Common Decision Tree Algorithms Are:

- Hunt's Algorithm
- CART
- ID3, J48, C45
- SID, SPRNT

Hunt's Algorithm:

Let D_t be the set of training records that reach at node T .

Algorithm:

Step 1: If D_t contains records that belong to the same class then the node T is a leaf node.

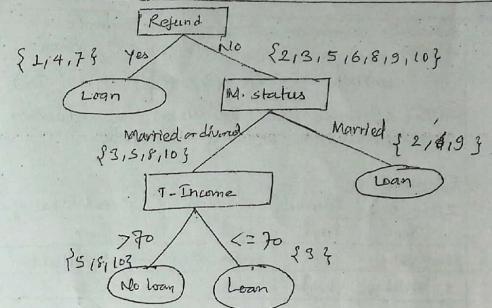
Step 2: If D_t is an empty set then T is a leaf node labelled by default class.

Step 3: If D_t contains records that belong to more than one class use an attribute test to split the data into smaller subsets.

Step 4: Recursively apply the procedure to each subset.

Example:

Tid	Refund	Marital status	Taxable income	Class
1	Yes	Single	125K	Loan
2	No	Married	100K	Loan
3	No	Single	70K	Loan
4	Yes	Married	120K	Loan
5	No	Divorced	95K	Loan
6	No	Married	60K	No loan
7	Yes	Divorced	220K	Loan
8	No	Single	85K	No loan
9	No	Married	75K	Loan
10	No	Single	90K	No loan



Tree Induction:-

Greedy Strategy:-

→ Split the record based on an attribute test that optimizes certain

Issues

- (i) How to split record?
- (ii) How to specify attribute test condition?

→ Depends on attribute type and number of ways to split (ie multiple way split.)

- (iii) When to stop splitting?

→ All records belong to same class.

→ All records have similar attributes.

- (iv) How to determine the best split?

→ Nodes with homogeneous class distribution are preferred

→ Measure of node Impurity

Measure of Node Impurity (Homogeneity)

• Gini Index

• Entropy calculation.

Gini Index:

The Gini Index measures the impurity of dataset (D) as,

$$Gini(D) = 1 - \sum_{i=1}^n p_i^2$$

where $p_i \rightarrow p_i$ is the probability that a tuple in D belongs to class c_i .

→ consider a binary split for each attribute

→ when D is partitioned into D_1 and D_2 , then,

$Gini(D) = \frac{D_1}{D} Gini(D_1) + \frac{D_2}{D} Gini(D_2)$

→ the attribute that maximizes the reduction in impurity is selected as the splitting attribute.

Example:

ID	Age	Income	Student	Credit Rating	Class (Buy-Computer)
1	Youth	High	No	Fair	No
2	Youth	High	No	Fair	No
3	Middle-Age	High	No	Excellent	No
4	Senior	Medium	No	Fair	Yes
5	Senior	Low	Yes	Fair	Yes
6	Senior	Low	Yes	Poor	Yes
7	Middle-Age	Low	Yes	Excellent	No
8	Youth	Medium	Yes	Excellent	Yes
9	Youth	Low	Yes	Fair	Yes
10	Senior	Medium	Yes	Fair	No
11	Youth	Medium	Yes	Fair	Yes
12	Middle-Age	Medium	No	Excellent	Yes
13	Middle-Age	High	Yes	Excellent	Yes
14	Senior	High	No	Poor	Yes
				Excellent	No

Solution:

$$\text{Gini}(\text{Income}) = \frac{10}{14} \left\{ 1 - \left(\frac{6}{10} \right)^2 - \left(\frac{4}{10} \right)^2 \right\} + \frac{4}{14} \left\{ 1 - \left(\frac{4}{4} \right)^2 - \left(\frac{2}{4} \right)^2 \right\}$$

$$= 0.4582$$

$$\text{Gini}(Age) = 1 - \left(\frac{9}{14} \right)^2 - \left(\frac{5}{14} \right)^2 = 0.459$$

Attribute: Income

Subset 1, $D_1 = \{ \text{low, medium} \}$, $D_2 = \{\text{high}\}$

$$\text{Gini}(Income) = \frac{10}{14} \text{Gini}(D_1) + \frac{4}{14} \text{Gini}(D_2)$$

$$= \frac{10}{14} \left\{ 1 - \left(\frac{6}{10} \right)^2 - \left(\frac{4}{10} \right)^2 \right\} + \frac{4}{14} \left\{ 1 - \left(\frac{2}{4} \right)^2 - \left(\frac{2}{4} \right)^2 \right\}$$

$$[\text{Here, } f_{high} \text{ computer from set } D_1 \text{ & 3 don't buy a computer}] \\ = 0.556$$

$$\text{Subset 2: } D_1 = \{ \text{low, high} \}, D_2 = \{\text{medium}\}$$

$$\text{Gini}(Income) = \frac{8}{14} \left\{ 1 - \left(\frac{6}{8} \right)^2 - \left(\frac{2}{8} \right)^2 \right\} + \frac{6}{14} \left\{ 1 - \left(\frac{4}{6} \right)^2 - \left(\frac{2}{6} \right)^2 \right\}$$

$$= 0.4550$$

Since, subset 2 has minimum value so selected as binary split for Income.

Attribute: Age

Subset 1: $D_1 = \{ \text{Youth, senior} \}$, $D_2 = \{\text{M-aged}\}$

$$\text{Gini}(Age) = \frac{10}{14} \left\{ 1 - \left(\frac{5}{10} \right)^2 - \left(\frac{5}{10} \right)^2 \right\} + \frac{4}{14} \left\{ 1 - \left(\frac{4}{4} \right)^2 \right\}$$

$$= 0.357$$

Subset 2: $D_1 = \{ \text{Youth, M-aged} \}$, $D_2 = \{\text{Senior}\}$

$$\text{Gini}(Age) = \frac{9}{14} \left\{ 1 - \left(\frac{3}{9} \right)^2 - \left(\frac{6}{9} \right)^2 \right\} + \frac{5}{14} \left\{ 1 - \left(\frac{3}{5} \right)^2 - \left(\frac{2}{5} \right)^2 \right\}$$

$$= 0.3678$$

Subset 3: $D_1 = \{ \text{Youth} \}$, $D_2 = \{\text{M-aged, Senior}\}$

$$\text{Gini}(Age) = \frac{5}{14} \left\{ 1 - \left(\frac{3}{5} \right)^2 - \left(\frac{2}{5} \right)^2 \right\} + \frac{9}{14} \left\{ 1 - \left(\frac{2}{9} \right)^2 - \left(\frac{7}{9} \right)^2 \right\}$$

$$= 0.3936$$

Attribute: Student

$D_1 = \{ \text{Yes} \}$, $D_2 = \{ \text{No} \}$

$$\text{Gini}(Student) = \frac{7}{14} \left\{ 1 - \left(\frac{6}{7} \right)^2 - \left(\frac{1}{7} \right)^2 \right\} + \frac{7}{14} \left\{ 1 - \left(\frac{4}{7} \right)^2 - \left(\frac{3}{7} \right)^2 \right\}$$

$$= 0.3775$$

Attribute: Credit Rating

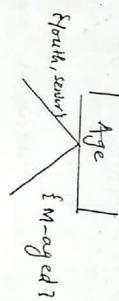
$D_1 = \{ \text{Fair} \}$, $D_2 = \{ \text{Excellent} \}$

$$\text{Gini}(Credit Rating) = \frac{8}{14} \left\{ 1 - \left(\frac{6}{8} \right)^2 - \left(\frac{2}{8} \right)^2 \right\} + \frac{6}{14} \left\{ 1 - \left(\frac{3}{6} \right)^2 - \left(\frac{3}{6} \right)^2 \right\}$$

$$= 0.4285$$

Impurity reduction for age = $0.459 - 0.357 = 0.102$
 Impurity reduction for income = $0.459 - 0.450 = 0.009$
 Impurity reduction for student = $0.459 - 0.3775 = 0.0815$
 Impurity reduction for credit-rating = $0.459 - 0.4285 = 0.0305$

Since, Age has maximum impurity reduction & it is selected as root node.



Nearest Neighbour Classifier:

→ It uses k -nearest points for performing classification. k nearest of record X are data points that have the k -nearest to X .

→ Classification based on learning by analogy i.e. by comparing given test tuple with training tuple that are similar.

→ When given an unknown tuple, a nearest neighbour classifier

searches the pattern space for k -training tuples which are closest to the unknown tuple.

(i) Nearest neighbour classifier requires:

(ii) Distance matrix to compute the distance between records.

(iii) The value of k i.e. the number of nearest neighbour

→ To classify an unknown record:

(i) Compute the distance to other training record.

(ii) Identify the k -nearest neighbour

(iii) Use class labels of nearest neighbour to determine class labels of unknown record by using majority vote.

-	-	-
-	-	*
+	+	+

-	-	-
-	-	*
+	+	+

-	-	-
-	-	*
+	+	+

$$K=1$$

$$\text{Class} = -$$

$$K=2$$

$$\text{Class} = -/+$$

$$K=3$$

$$\text{Class} = -$$

Classification Issues:

(a) choosing the value of K :

If K is too small it is sensitive to noise point. If K is too large neighbour may include points from other class.

(b) Scaling Issue:

Attributes may have to be scaled to prevent distance measure from being dominated by one or attributes like Height, weight.

(c) Distance computation for non-numeric data:

use distance as 0 (minimum) for same data & maximum for different data set.

(a) missing values:

use minimum possible distance.

Disadvantages:

- poor accuracy when data have noise and irrelevant attributes
- classifying unknown records are relatively expensive.
- slow when classifying test tuple.

Rule Based classifier:

If classify record by using a collection of 'if...then...' rules. i.e Rule based classifier uses a set of 'if...then...' rules of classification, the 'If' part or left hand side of rule is known as the rule antecedent where as the 'then' part or right hand side is known as rule consequent. In rule antecedent the condition consists of one or more attribute test.

e.g.

$$R_1 : (\text{Age} = \text{Youth}) \wedge (\text{Student} = \text{Yes}) \Rightarrow (\text{Lives_computer} = \text{Yes})$$

If the condition in the rule antecedent holds true for a given tuple the rule antecedent is satisfied and the rule covers the tuple i.e. covered by rule. If the rule fraction of record that satisfy the antecedent of rule,

$$\text{Coverage} = \frac{n \text{ covers}}{n \text{ total dataset}} \times 100\%$$

The accuracy of rule is the fraction of record that satisfy both the antecedent and consequent of rule. i.e.

$$\text{Accuracy} = \frac{n \text{ correct}}{n \text{ covers}} \times 100\%$$

How does rule based classifier work?

1. If a rule is satisfied by a tuple the rule is said to be triggered.
2. If only one rule is satisfied, then the rule fire by returning the class prediction for the tuple.
3. Triggering doesn't always mean firing because there may be more than one rule that can be satisfied.
4. If more than one rule is satisfied then the rule fire by returning the class by applying conflict resolution strategy to find which rule is fired.

Conflict Resolution Strategy:

- (1) when more than one rule is triggered rule ordering or ranking is applied. The rule ordering may be class based or rule based. When rule is used the rule set is given as a decision list.
- (2) when no rule is satisfied by tuple->(Unknown) then, a default rule can be setup to specify a default class.

Example:

Name	Blood type	Give birth	can fly	Lives in water	Class
Lemon	Warm	Yes	No	No	Mammal
Turtle	Cold	No	No	Sometimes	Reptile
Shark	Cold	Yes	No	Yes	Aquatic

Rules:

$$R_1 : (\text{Give birth} = \text{Yes}) \wedge (\text{Blood type} = \text{Warm}) \Rightarrow \text{Mammal}$$

$$R_2 : (\text{Give birth} = \text{No}) \wedge (\text{Can fly} = \text{No}) \Rightarrow \text{Reptile}$$

$$R_3 : (\text{Lives in water} = \text{Sometime}) \Rightarrow \text{Amphibian}$$

→ 4 lemon triggers R_{1,2,3}, it's a mammal

→ 4 turtle triggers R₂ and R₃ i.e. conflict

→ A shark triggers none of the rule, use default class

→ If conflict, apply rule ranking.

Characteristics of Rule based classifier.

1. Mutually exclusive rule: (covering)

Classifier contains mutually exclusive rule. If rules are independent

to each other.

(i) Every record is covered by almost one rule.

(ii) Rules are no longer mutually exclusive if record may trigger more than one rule.

(iii) To make mutually exclusive we apply ordering.

2. Exhaustive rule: (default)

→ Classifier has exhaustive coverage if it accounts for every possible combinations of attribute values.

→ Each record is covered by almost one rule

→ Rules are no longer exhaustive if a record may not trigger any rule.

→ To make exhaustive we apply default class.

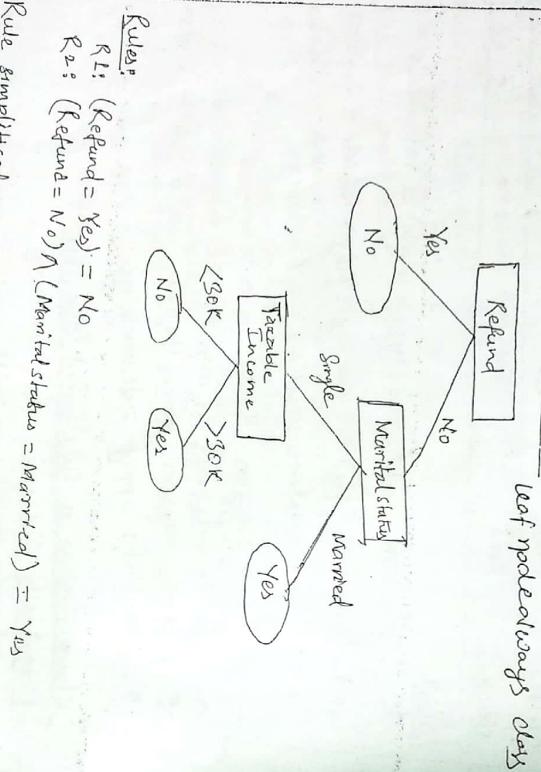
$$P(A|B) = \frac{P(B|A) * P(A)}{P(B)}$$

evidence

Building Classification Rules:

1. Direct Method: Sequential & Inductive Approach
→ Extract rule direct from data.
Eg: RIPPER, CN2
2. Indirect Method:
→ Extract rule from other classification.
Eg: Decision Tree, ANN.

Rule extraction from decision tree.



Rules:
 $R_1: (\text{Refund} = \text{Yes}) = \text{No}$
 $R_2: (\text{Refund} = \text{No}) \wedge (\text{Marital status} = \text{Married}) = \text{Yes}$

Rule Simplification:

R_2 can be simplified as

(Marital status = Married) = Yes.

Advantages of Rule-based classifier:

- Highly expressive
- easy to generate and interpret
- can classify new instances rapidly.
- High performance.

Rules Simplification

Bayesian classifier: Predicts class member

- It is statistical classifier which predicts class membership probabilities for a membership class.
- It has high accuracy and speed for large databases.
- It has minimum error rate in comparison to other classifiers.
- It has minimum error rate in comparison to other classifiers.

$$P(A|B) = \frac{P(A \cap B)}{P(B)}, \quad P(B|A) = \frac{P(A \cap B)}{P(A)}$$

Types:
 (1) Bayesian Belief Networks (Graphical Models)

- It assumes that the effect on an attribute value on a class is independent of the value of other attributes i.e. has conditional independence.
- Has simple computational complexity.

(2) Naive Bayesian classifier
 → It assumes that the effect on an attribute value on a class is independent of the value of other attributes i.e. has conditional independence.

→ It has simple computational complexity.

→ Let S be the training setup tuples and c_1, c_2, \dots, c_n their associated classes. The classifier will predict that x , given a tuple x , the classifier will predict that x belongs to the class having highest posterior probability condition i.e. the naive Bayesian classifier predicts that the tuple x belongs to the class c_i "only if" $P(c_i|x) > P(c_j|x)$ for $1 \leq i \leq m, j \neq i$

$$\begin{aligned} & P(c_i|x) = \frac{P(x|c_i) \cdot P(c_i)}{P(x)} \quad (\text{maximum}) \\ & \text{i.e. } P(c_i|x) = \frac{P(x|c_i) \cdot P(c_i)}{\sum_{j=1}^m P(x|c_j) \cdot P(c_j)} \end{aligned}$$

Here, $P(c_i) = \text{constant}$

$$P(c_i) = P(c_1) = P(c_2) = \dots = P(c_m)$$

So, we need to maximize $P(x|c_i)$ since, for naive assumption is class conditional independence.

$$\begin{aligned} P(x|c_i) &= \prod_{k=1}^n D(x_k|c_i) \\ &= D(x_1|c_i) * D(x_2|c_i) * \dots * D(x_n|c_i) \end{aligned}$$

These probability can be "calculated from training sample.

Example:

ID	Age	Income	Student	credit rating	elans	buy computer
1	Youth	High	No	Fair	No	No
2	Youth	High	No	Excellent	Fair	Yes
3	Male	High	No	Fair	Fair	Yes
4	Senior	Medium	No	Fair	Fair	Yes
5	Senior	Low	Yes	Excellent	No	No
6	Senior	Low	Yes	Excellent	Yes	No
7	Male	Low	No	Fair	Fair	No
8	Youth	Medium	No	Fair	Fair	Yes
9	Youth	Low	Yes	Fair	Fair	Yes
10	Senior	Medium	Yes	Fair	Fair	Yes
11	Youth	Medium	No	Excellent	Yes	Yes
12	Male	Medium	No	Excellent	Yes	Yes
13	Male	High	Yes	Fair	Yes	No
14	Senior	Medium	No	Excellent	Yes	No

Find class of x :

$X = (\text{age} = \text{Youth}, \text{income} = \text{medium}, \text{student} = \text{yes}, \text{credit_rating} = \text{fair})$

Solution :-

Let, C_1 (buys-computer = yes) = y
 C_2 (buys-computer = no) = 5

Prior probability of $C_1 = g_{1+4} = 0.642$

Prior probability of $c_2 = 5/14 = 0.357$

$$P(\text{Age} = \text{youth} \mid \text{buys_computer} = \text{yes}) = 2/9 = 0.222$$

$$P(Age = Youth \mid buys - computer = No) = 3/5 = 0.6$$

$$P(\text{income} = \text{medium} | c_1) = 4/9 = 0.44$$

(Student = medium) (C_2) = $2/5 = 0.4$

$$P(\text{student} = \text{yes} | E_3) = \frac{1}{9} = 0.666$$

$$P(\text{credit-risky} = \text{fair} | c) = 6/9 = 0.667$$

$$P_L \text{ credit-rating} = \text{fair}/(c_2) = 2/5 = 0.4$$

Since, $P(X|C_4) > P(X|C_2)$
 i.e., X is classified as buys - computer = yes.
 [Note: when count = 0 (Apply minimum probability rule place somewhere
 in such case, suppose count = 1)]

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Neutral Network Classifiers \rightarrow (ANN)

Artificial Network \rightarrow 510 units in which each connection

\rightarrow ANN is a set of connected units, the network learns by adjusting weights associated with it. the network learns by adjusting labels.

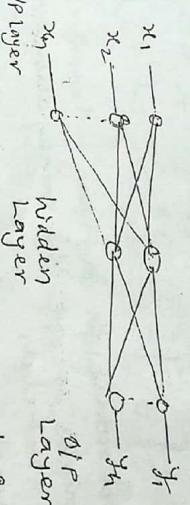
\rightarrow During the learning phase, predict the correct class label.

\rightarrow noisy, so as to be able to predict the correct class label.

\rightarrow ANN is also referred as connectionist learning due to connections between different units.

\rightarrow It has long training time and poor interpretability but has tolerance to noisy data.

\rightarrow It can classify pattern on which they have not been trained. It has parallel continuous value input.



The diagram shows a neural network structure with three layers: an input layer, a hidden layer, and an output layer. The input layer consists of nodes labeled x_1 , x_2 , ..., x_n . The hidden layer consists of nodes labeled z_1 , z_2 , ..., z_m . The output layer consists of nodes labeled y_1 , y_2 , ..., y_n . Every node in the input layer is connected to every node in the hidden layer, and every node in the hidden layer is connected to every node in the output layer. This fully connected architecture is used for classification tasks.

layer, number of output of
Back Propagation Algorithm:-

1. Initialization: set all the weights and threshold levels of the neurons uniformly distributed inside a small range

2. Activation: → Activate the networks by applying the inputs and desired output of the neurons(nodes) in the input layer and hence the output layers.

3. weight training!
→ update weight in the network by propagating the error associated with the output neurons by calculating error gradients and

hence to the hidden layers

4. Repeat step 2 and 3 until selected error gradient

Measure of Node Impurity:-

- Gini Index

T Entropy calculation
D ID3 Algorithm (Iterative Dichotomizer 3)

ID3 is an algorithm used in decision tree to generate no back tracking. ID3 builds the tree from the top down. \rightarrow Information gained is used to select the most useful attribute for classification.

\rightarrow Information gained is calculated from entropy calculation

$$\text{Entropy}(H) = - \sum_{i=1}^m P(x_i) \cdot \log_2 P(x_i)$$

where, m = no. of classes

$$P(x_i) = \text{Probability of 'x' in class 'i'}$$

Algorithm:

Step 1: Create a root node for a tree

Join with that class return a single

Step 3: If all examples are not of same class calculate entropy

and information gain to select root node and branch node

(nodes with highest information gain is selected as root node).

Step 4: Partition the examples into subsets.

Step 5: Repeat the process until all examples are classified.

Example:

Person	Hair Length	Weight	Age	Class
P ₁	0"	250	36	M
P ₂	10"	150	34	F
P ₃	2"	90	10	M
P ₄	6"	78	8	F
P ₅	4"	20	1	F
P ₆	1"	170	70	M
P ₇	8"	160	41	F
P ₈	10"	180	38	M
P ₉	6"	100	45	M

$$\text{Here entropy of data (H)} = - \sum_{i=1}^9 P(x_i) \log_2 (P(x_i)) \\ = - [4/9 \log_2 (4/9) + 5/9 \log_2 (5/9)] = 0.9911$$

Entropy for hair length;

$$(L \leq 5") = 4 \leftarrow S_M = -\left[\frac{1}{4} \log_2 (1/4) + \frac{3}{4} \log_2 (3/4)\right] = 0.8113 \\ (L > 5") = 5 \leftarrow S_F = -\left[\frac{2}{5} \log_2 (2/5) + \frac{3}{5} \log_2 (3/5)\right] = 0.9710$$

$$\text{Information gain} = 0.9911 - \text{mean} \\ = 0.9911 - (4 \times 0.8113 + 5 \times 0.9710) \\ = 0.09107$$

Entropy for weight;

$$(W > 160) = -\left[\frac{0}{4} \log_2 (0/4) + \frac{4}{4} \log_2 (4/4)\right] = 0 \\ (\leq 60) = -\left[\frac{1}{3} \log_2 (1/3) + \frac{2}{3} \log_2 (2/3)\right] = 0.7219$$

$$\text{Information gain} = 0.9911 - (0.7219 + 0.09107) = 0.59$$

Entropy for age;

$$(A \leq 40) = -\left[\frac{3}{6} \log_2 (3/6) + \frac{3}{6} \log_2 (3/6)\right] = 1 \\ (> 40) = -\left[\frac{1}{3} \log_2 (1/3) + \frac{2}{3} \log_2 (2/3)\right] = 0.9183$$

$$\text{Information gain} = 0.9911 - (0.9183 + 0.09107) = 0.0833$$

Since, weight has maximum information gain so selected as node.

Advantages of ID³:

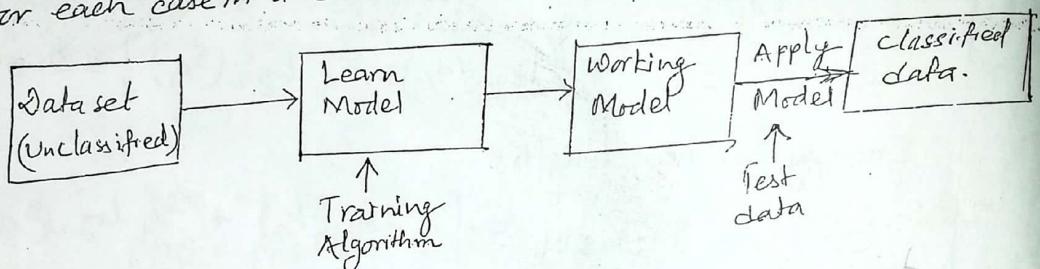
- Easy to construct and interpret for small sized data
- Higher accuracy for simple data
- fast for classifying unknown records

What is classification?

It is a data mining technique used to predict group-membership of data instances.

→ Classification assigns data in a collection of target category or class.

→ The goal of classification is to accurately predict the target class for each case in the data.



Model comparison:

✓ (1) Confusion Matrix (Contingency Table)

✗ (2) ROC