Lecture 2 - Image Fundamentals

This lecture will cover:

- Image acquisition
- Sampling and Quantization
- Pixels
- Image operation
- Color space



Color space

> Color fundamentals

- Primary colors
- Secondary colors
- Color gamut

> Color models

- RGB model
- CMY and CMYK model
- HSI model

Color transformation



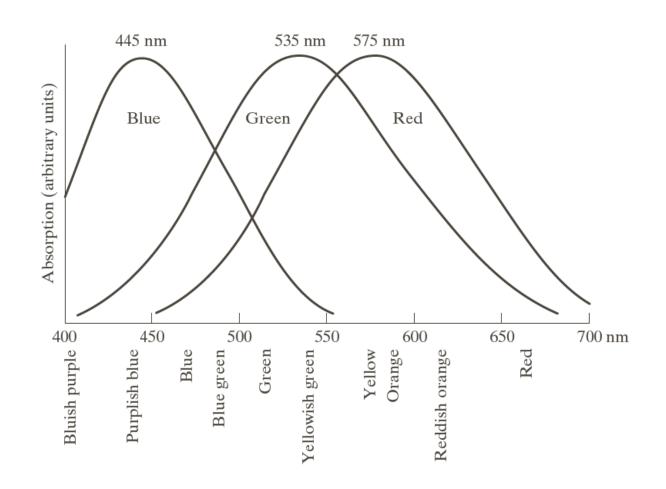
Primary colors

CIE RGB Standard

- Blue = 435.8 nm
- Green = 546.1 nm
- Red = 700 nm

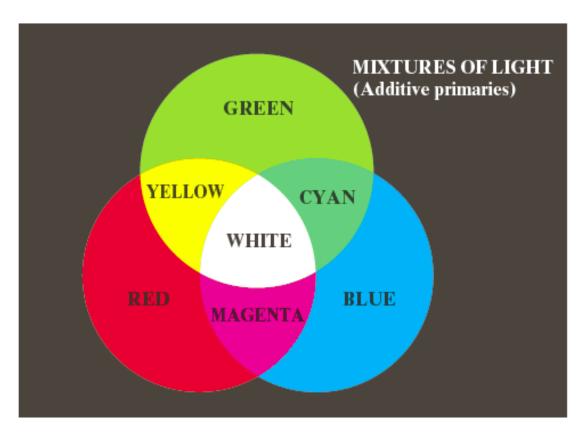
CMY and CMYK color

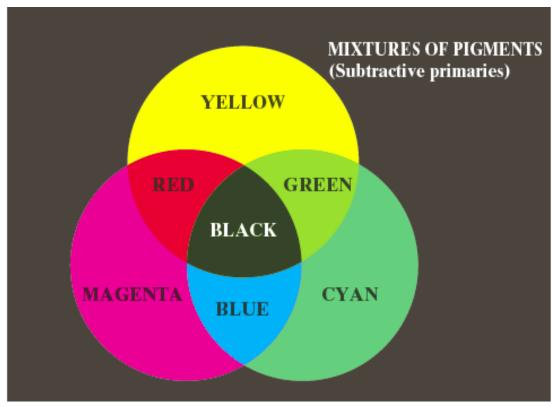
- Cyan = White Red
- Magenta = White Green
- Yellow = White Blue
- Black = White Red Green Blue





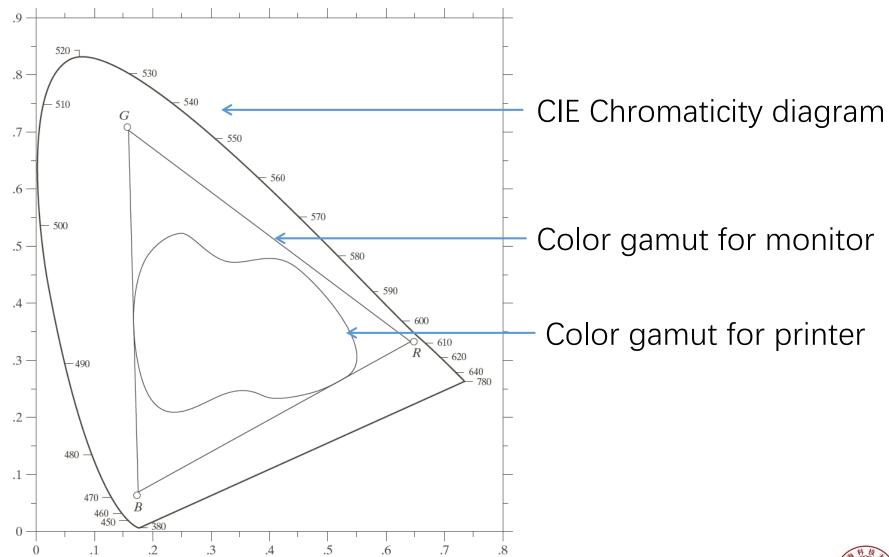
Secondary colors







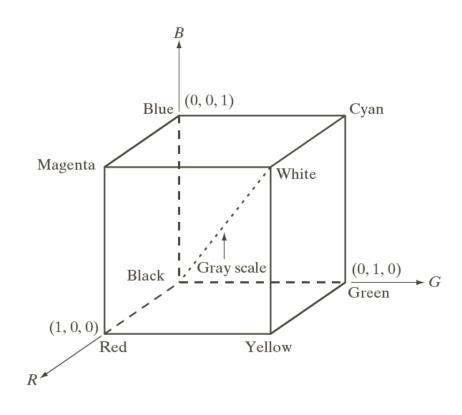
Color Gamut

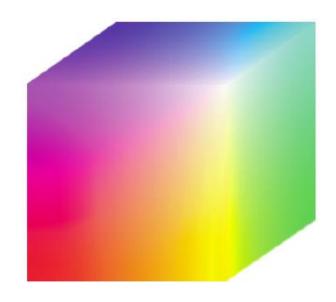


x-axis



RGB Color Model

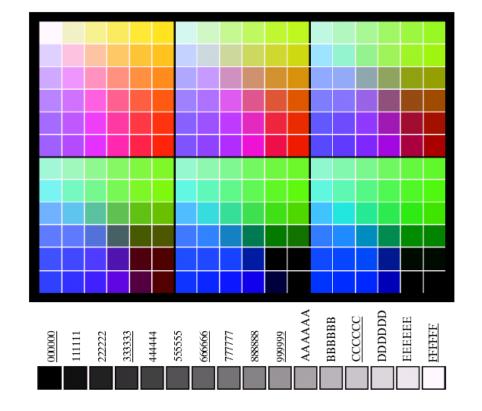


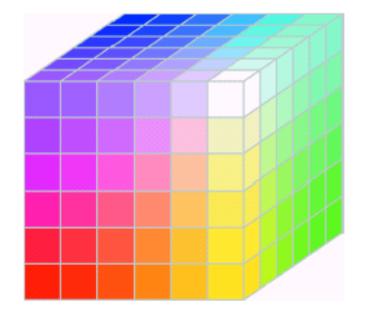




Safe RGB Color

Number System	n	Color Equivalents				
Hex	00	33	66	99	CC	FF
Decimal		51	102	153	204	255







CMY Color Model

> RGB to CMY conversion

$$\begin{bmatrix} C \\ M \\ Y \end{bmatrix} = \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} - \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

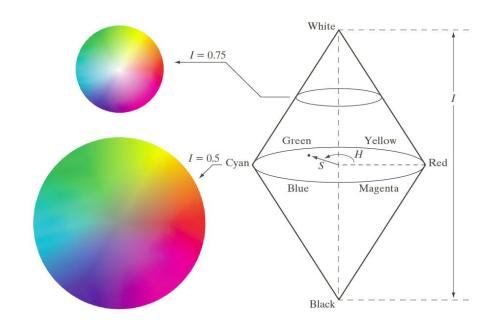
In order to produce true black in printing, a fourth color, black, is added into the CMYK color model

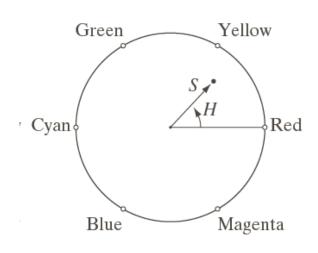


HSI Color Model

> HSI Color Model

- Hue: Dominant color associated with wavelength
- Saturation: relative purity, the amount of white light mixed with a hue
- Intensity







RGB to HSI

$$\theta = \arccos \left\{ \frac{\frac{1}{2}[(R-G) + (R-B)]}{[(R-G)^2 + (R-G)(G-B)]^{\frac{1}{2}}} \right\}$$

$$H = \begin{cases} \theta, & G \ge B \\ 360 - \theta, & G < B \end{cases}$$

$$S = 1 - \frac{3}{R + G + B} \left[\min(R, G, B) \right]$$

$$I = \frac{R + G + B}{3}$$

$$S=0 \rightarrow H=0$$
 , $I=0 \rightarrow S=0$, $H=0$



HSI to RGB

$$> 0^{\circ} \le H < 120^{\circ}$$

$$B = I(1-S),$$
 $R = I\left[1 + \frac{Scos(H)}{\cos(60^{\circ} - H)}\right],$ $G = 3I - (R+B)$

 $> 120^{\circ} \le H < 240^{\circ}$

$$R = I(1-S),$$
 $G = I\left[1 + \frac{Scos(H-120^{\circ})}{\cos(180^{\circ}-H)}\right],$ $B = 3I - (R+G)$

 $> 240^{\circ} \le H < 360^{\circ}$

$$G = I(1-S),$$
 $B = I\left[1 + \frac{Scos(H-240^{\circ})}{\cos(300^{\circ}-H)}\right],$ $R = 3I - (G+B)$



Inverse Color Transformation

$$\begin{bmatrix} g_R(x,y) \\ g_G(x,y) \\ g_B(x,y) \end{bmatrix} = \begin{bmatrix} 255 - f_R(x,y) \\ 255 - f_G(x,y) \\ 255 - f_B(x,y) \end{bmatrix}$$











RGB to Gray scale

➤ Maximum value:

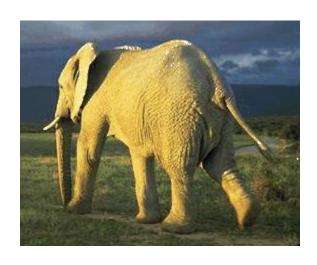
$$g_R(x,y) = g_G(x,y) = g_B(x,y) = \max[f_R(x,y), f_G(x,y), f_B(x,y)]$$

Average value

$$g_R(x,y) = g_G(x,y) = g_B(x,y) = [f_R(x,y) + f_G(x,y) + f_B(x,y)]/3$$

Weighted value

$$g_R(x,y) = g_G(x,y) = g_B(x,y) = 0.299 f_R(x,y) + 0.587 f_G(x,y) + 0.114 f_B(x,y)$$









Color Balance

White balance:

$$I(x,y) = 0.299 f_R(x,y) + 0.587 f_G(x,y) + 0.114 f_B(x,y)$$

$$k_R = \frac{\overline{I}}{\overline{R}} \qquad k_G = \frac{\overline{I}}{\overline{G}} \qquad k_B = \frac{\overline{I}}{\overline{B}}$$

$$\begin{bmatrix} g_R(x,y) \\ g_G(x,y) \\ g_B(x,y) \end{bmatrix} = \begin{bmatrix} k_R & & \\ & k_G & \\ & & k_B \end{bmatrix} \begin{bmatrix} f_R(x,y) \\ f_G(x,y) \\ f_B(x,y) \end{bmatrix}$$

Maximum value balance

$$S_{RGB} = \min[R_{max}, G_{max}, B_{max}]$$

$$k_R = \frac{S_{RGB}}{T_R}$$
 $k_G = \frac{S_{RGB}}{T_G}$ $k_B = \frac{S_{RGB}}{T_B}$

$$\begin{bmatrix} g_R(x,y) \\ g_G(x,y) \\ g_B(x,y) \end{bmatrix} = \begin{bmatrix} k_R \\ k_G \\ k_B \end{bmatrix} \begin{bmatrix} f_R(x,y) \\ f_G(x,y) \\ f_B(x,y) \end{bmatrix}$$





