

A

A'

$$d = (S, T, D) \iff d'(t_1-1, \dots, t_s-1, D)$$

d_1, \dots, d_n

\Leftarrow add a new vertex v adjacent to the S vertices (with degrees t_1-1, \dots, t_s-1)

\Rightarrow case 1) S is adjacent to T , remove S , $A \rightarrow A'$

case 2) " not adjacent " for $1 \leq i \leq s$

$d(S, T, D)$ is non-increasing order

S has at least degree of s so S must be adjacent to some $d_j \in D$ for $1 \leq j \leq n$.

We know $t_i \geq d_j$

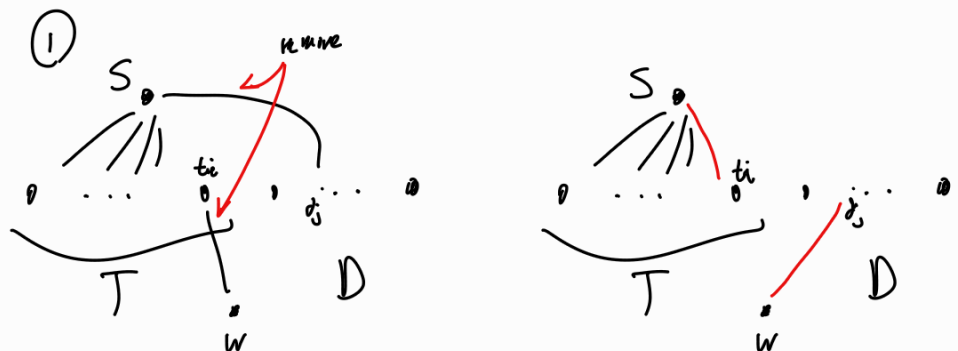
$$t_i = d_j$$

Then, switch t_i and d_j
& connect S to d_j instead of t_i

$$t_i > d_j$$

Let $w \in T_i$, but $w \notin D_j$

Then, remove $\{S, d_j\}$ and $\{T_i, w\}$
and add $\{S, T_i\}$ and $\{w, d_j\}$



Using this method,
any vertex not connected
to S can be adjusted
so that S is adjacent to
 T_i , while

effectively preserves degree sequence

\therefore we have the first trivial case

Reduction within reduction!!

$\therefore A$ is graphic IFF A' is graphic

□