(4) TBC-205/TBI-204

5. (a) Explain Karnaugh map method for 2 and 3 variables. (CO2)

OR

(b) Define the following: (CO2)

- (i) SOP and POS forms with example
- (ii) Logic gates

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TBC-205/TBI-204

B. C. A. (SECOND SEMESTER) MID SEMESTER EXAMINATION, 2021-22

DISCRETE MATHEMATICAL STRUCTURES
AND GRAPH THEORY

Time: 11/2 Hours

Maximum Marks: 50

- **Note:** (i) Answer all the questions by choosing any *one* of the sub-questions.
 - (ii) Each sub-question carries 10 marks.
- 1. (a) Define the following with examples:

(CO1)

Diagonal matrix, Signular matrix, Scalar matrix, Column matrix, Skew symmetric matrix

OR

(b) If: (CO1)

$$\mathbf{A} = \begin{bmatrix} -1 & 2 & 3 \\ 5 & 7 & 9 \\ -2 & 1 & 1 \end{bmatrix}$$

and $B = \begin{bmatrix} -4 & 1 & -2 \\ 1 & 2 & 0 \\ 1 & 3 & 1 \end{bmatrix}$

then show that:

(i)
$$(A+B)^T = A^T + B^T$$

(ii)
$$(A-B)^T = A^T - B^T$$

2. (a) Solve the system of linear equations by matrix method: (CO1)

$$x - y + z = 4$$

$$2x + y - 3z = 0$$

$$x + y + z = 0$$
OR

(b) Find the inverse of the matrix: (CO1)

$$A = \begin{bmatrix} 2 & 1 & 3 \\ 4 & -1 & 0 \\ -7 & 2 & 1 \end{bmatrix}$$

(3) TBC-205/TBI-204

3. (a) Find the eigen values and eigen vectors of the matrix: (CO1)

$$A = \begin{bmatrix} -2 & 2 & -3 \\ 2 & 1 & -6 \\ -1 & -2 & 0 \end{bmatrix}$$

OR

(b) Find the characteristic equation of the matrix: (CO1)

$$\mathbf{A} = \begin{bmatrix} 2 & -1 & 1 \\ -1 & 2 & -1 \\ 1 & -1 & 2 \end{bmatrix}$$

and verify that it is satisfied by A.

4. (a) (i) State and prove De-Morgan's law. (CO2)

(ii) Define Boolean algebra with properties.

OR

(b) Simplify the following Boolean expressions: (CO2)

(i)
$$(A+B)(A\overline{B}\overline{C}+A\overline{B}C+AB\overline{C}+ABC)$$

(ii)
$$\overline{\left(A\overline{B}+\overline{A}B\right)}$$