that in 2006, the number of passengers was 2,50,000 and in 2012, the number of passengers was 2,20,000. If 'n' represents the number of passengers using the airline per year, and 't' indicates the time in years. (CO2)

- (i) Model the number of passengers using the airline as a function of time.
- (ii) What is the number of riders expected in the year 2020?
- (iii) It is estimated that the airline will go out of business if the ridership falls below 20,000. According to your analysis, when will this happen?

OR

(b) Find maximum and minimum values of the function $f(x) = 2x^3 - 24x + 107$ in the interval [1, 3]. (CO2)

H Roll No.

BCH-106

B. COM. (HONS.) (FIRST SEMESTER) MID SEMESTER

EXAMINATION, Jan., 2023

BUSINESS MATHEMATICS

Time: 1½ Hours
Maximum Marks: 50

Note: (i) Answer all the questions by choosing any *one* of the sub-questions.

(ii) Each sub-question carries 10 marks.

1. (a) If
$$A = \begin{bmatrix} 1 & 3 & 1 \\ 3 & 2 & 4 \\ 5 & 8 & 2 \end{bmatrix}$$
 and $B = \begin{bmatrix} 3 & 1 & 5 \\ 3 & 2 & 7 \\ 5 & 8 & 0 \end{bmatrix}$

then show that
$$(AB)^T = B^T A^T$$
. (CO1)

(b) Find the inverse of matrix: (CO1)

2. (a) Two mobile service provides S_1 an S_2 currently enjoy the market share 53% and 47% respectively. Every month each of the service provider bring out new schemes and brand switching takes place as given in the following matrix. What is the share of S_1 and S_2 after one month? When is the equilibrium established? (CO1)

	S_1	S_2
S_1	0.42	0.58
S_2	0.28	0.72

OR

(b) By applying the properties of determinants show that: (CO1)

$$\begin{vmatrix} p + q & q + r & r + p \\ r & p & q \\ 1 & 1 & 1 \end{vmatrix} = 0$$

3. (a) Find the domain of the following function $x \in \mathbb{R}$. (CO2)

(i)
$$y = \frac{1}{(x-3)(x-5)}$$

(ii)
$$y = \sqrt{5 - 2x}$$

OR

- (b) If $f(x) = x^2 + 5x + 10$, for what values of 'x' 2f(x) = f(2x)? (CO2)
- 4. (a) If the total cost function:

$$TC = 11x - 2x^2 + \frac{x^3}{2},$$

identify the level of output at which average cost will be minimum. (CO2)

OR

(b) (i) Find the derivative of function:

$$f(x) = 2x^3 + e^{x^4} - \log_e x^5$$

- (ii) If the demand function D = 20 3Q. Find the marginal revenue when level of output produced Q is 3. (CO2)
- 5. (a) The ridership of Yatra airlines has been decreasing at a linear rate. Data reveals