## BCH-106

## B. COM. (HONS.) (FIRST SEMESTER) END SEMESTER EXAMINATION, Jan., 2023

**BUSINESS MATHEMATICS** 

Time: Three Hours

Maximum Marks: 100

- Note: (i) All questions are compulsory.
  - (ii) Answer any *two* sub-questions among (a), (b) and (c) in each main question.
  - (iii) Total marks in each main question are twenty.
  - (iv) Each sub-question carries 10 marks.
- 1. (a) Define the following with example:(CO1)
  - (i) Column matrix
  - (ii) Diagonal matrix
  - (iii) Null matrix
  - (iv) Symmetric matrix
  - (v) Identity matrix

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(b) If 
$$A = \begin{bmatrix} -1 & 2 & 3 \\ 5 & 7 & 9 \\ -2 & 1 & 1 \end{bmatrix}$$
 and  $B = \begin{bmatrix} -1 & 2 & 3 \\ 5 & 7 & 9 \\ -2 & 1 & 1 \end{bmatrix}$ 

$$\begin{bmatrix} -4 & 1 & -2 \\ 1 & 2 & 0 \\ 1 & 3 & 1 \end{bmatrix}$$
, then show that: (CO1)

(i) 
$$(A+B)^T = A^T + B^T$$

(ii) 
$$(A - B)^{T} = A^{T} - B^{T}$$

(c) Find the inverse of matrix defined by:

(CO1)

$$\mathbf{A} = \begin{bmatrix} 1 & -1 & 2 \\ 2 & 3 & 5 \\ -2 & 0 & 1 \end{bmatrix}$$

2. (a) Draw the following curves: (CO2)

- (i) y = 4x + 2
- (ii)  $y = x^2 + 2x$
- (iii) y = |x|

(b) Define the following with examples:

(CO2)

- (i) Mathematical function
- (ii) Exponential function
- (iii) Logarithmic function

- (c) Find the derivatives  $\frac{dy}{dx}$  of the following functions: (CO2)
  - (i)  $y = \frac{3x^4 + 4x^2 5x 1}{x}$
  - (ii)  $y = x^4 + e^x 4 \log x + 5 \cos x$
- 3. (a) Find the first and second partial derivatives of  $z = x^3 + y^3 3xy + 2x 5$ . (CO3)
  - (b) For what value of x the function  $y = x^3 2x^2 + x + 6$  have a maxima or minima. Find its maximum or minimum value. (CO3)
  - (c) Verify Euler's theorem: (CO3)

(i) 
$$z = \frac{x^3 + y^3}{x - y}$$

(ii) 
$$u = \log\left(\frac{x^2 + y^2}{x + y}\right)$$

4. (a) Solve the following Linear Programming

Problem graphically:

(CO4)

Maximize:

$$z = 4x + y$$

Subject to the constraints:

$$x + y \le 50$$

$$3x + y \le 90$$

$$x \ge 0, y \ge 0$$
.

(b) Define the following:

(CO4)

- (i) Basic feasible solution
- (ii) Unbounded solution
- (iii) Linear Programming Problem
- (c) Solve the following LPP by Graphical method: (CO4)

Minimize:

$$z = 200x + 500y$$

Subject to the constraints:

$$z + 2y \ge 10$$

$$3x + 4y \le 24$$

$$x \ge 0, y \ge 0$$
.

- 5. (a) Define the following with example:(CO5)
  - (i) Simple interest and Compound interest
  - (ii) Nominal and effective rate of interest
  - (b) If the difference between simple and compound interest on a sum for 3 years at 5 percent interest per annum is ₹ 76.25, then find the sum. (CO5)
  - (c) A moneylender charges 'interest' at the rate of 10 paise per rupee per month payable in advance. What effective rate of interest does he charge per annum? (CO5)