TCS-402

B. TECH. (FOURTH SEMESTER) MID SEMESTER EXAMINATION, April/May, 2022

FINITE AUTOMATA AND FORMAL LANGUAGE

Time: 11/2 Hours

Maximum Marks: 50

- Note: (i) Answer all the questions by choosing any *one* of the sub-questions.
 - (ii) Each question carries 10 marks.
- 1. (a) (i) Construct a DFA recognizing the following language (or strings): $\{a^n b^m | n \text{ is divisible by 3 and } m \text{ is divisible by 2 or } n-m \ge 1\}.$

10 Marks (CO1)

(ii) Find a DFA machine that accepts the language which has either odd

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OR

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number of 0's or even number of 1's but not both together over alphabet $\Sigma = \{0,1\}$.

OR

(b) Construct a minimum state automaton equivalent to the finite automaton given in the following table:

| State | Input $[\Sigma] \rightarrow$ | |
|-------|------------------------------|----|
| | a | b |
| → q0 | q0 | q3 |
| q1 | q2 | q5 |
| q2 ; | q3 | q4 |
| q3 | q0 | q5 |
| q4 | q0 | q6 |
| q5 | q1 | q4 |
| (q6) | q1 | q3 |

10 Marks (CO1)

2. (a) Write short notes on the following:

10 Marks (CO1)

- (i) Kleene Closures
- (ii) Generalized Transition Graph
- (iii) Applications and Limitations of FA

(b) Discuss the finite state machine with the help of an appropriate example.

(3)

10 Marks (CO1)

- 3. (a) Explain CHOMSKY classification of languages with example. 10 Marks (CO1)

 OR
 - (b) Design DFA for a Language of string 0 and 1 that: 10 Marks (CO1)
 - (i) ending with 10
 - (ii) ending with 11
 - (iii) ending with 1
- 4. (a) State Arden's theorem. Consider a DFA machine, $M = (\{q1, q2, q3\}, \{0, 1\} \delta, q1, \{q1\})$, where the transition function is defined as following:

$$\delta$$
 (q1, 0) = q1, δ (q1, 1) = q2,

$$\delta$$
 (q2, 0) = q3, δ (q2, 1) = q2,

$$\delta$$
 (q3, 0) = q1, δ (q3, 1) = q2

Find a regular expression 'r' such that

$$L(r) = L(M)$$
.

10 Marks (CO2)

OR

(b) Write the statement of Pumping Lemma for regular languages. Show that $L = \{ a^n : n > = 2, \text{ is a prime number} \}$ is not a regular language over $\Sigma = \{a\}$.

10 Marks (CO2)

5. (a) Consider the Mealy machine described by the trasition table given in table. Construct a Moore machine which is equivalent to the Mealy machine. 10 Marks (CO2)

| P. State | Input $a = 0$ | | Input a = 1 |
|----------|---------------|--------|-------------|
| | State | Output | State |
| q1 | q3 | 0 | q2 |
| q2 | q1 | 1 | q4 |
| q3 | q2 | 1 | q1 |
| q4 | q4 | 1 | q3 |

OR

(b) Draw the NFA for the regular expression
 (a|b)* a b b with € move. Convert this
 NFA to DFA using € closure method.

10 Marks (CO2)