

# Computer Vision

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universidade de aveiro





- Morphological operations
  - Dilation, erosion
  - Opening, closing
- Segmentation
  - Thresholding
  - Region growing

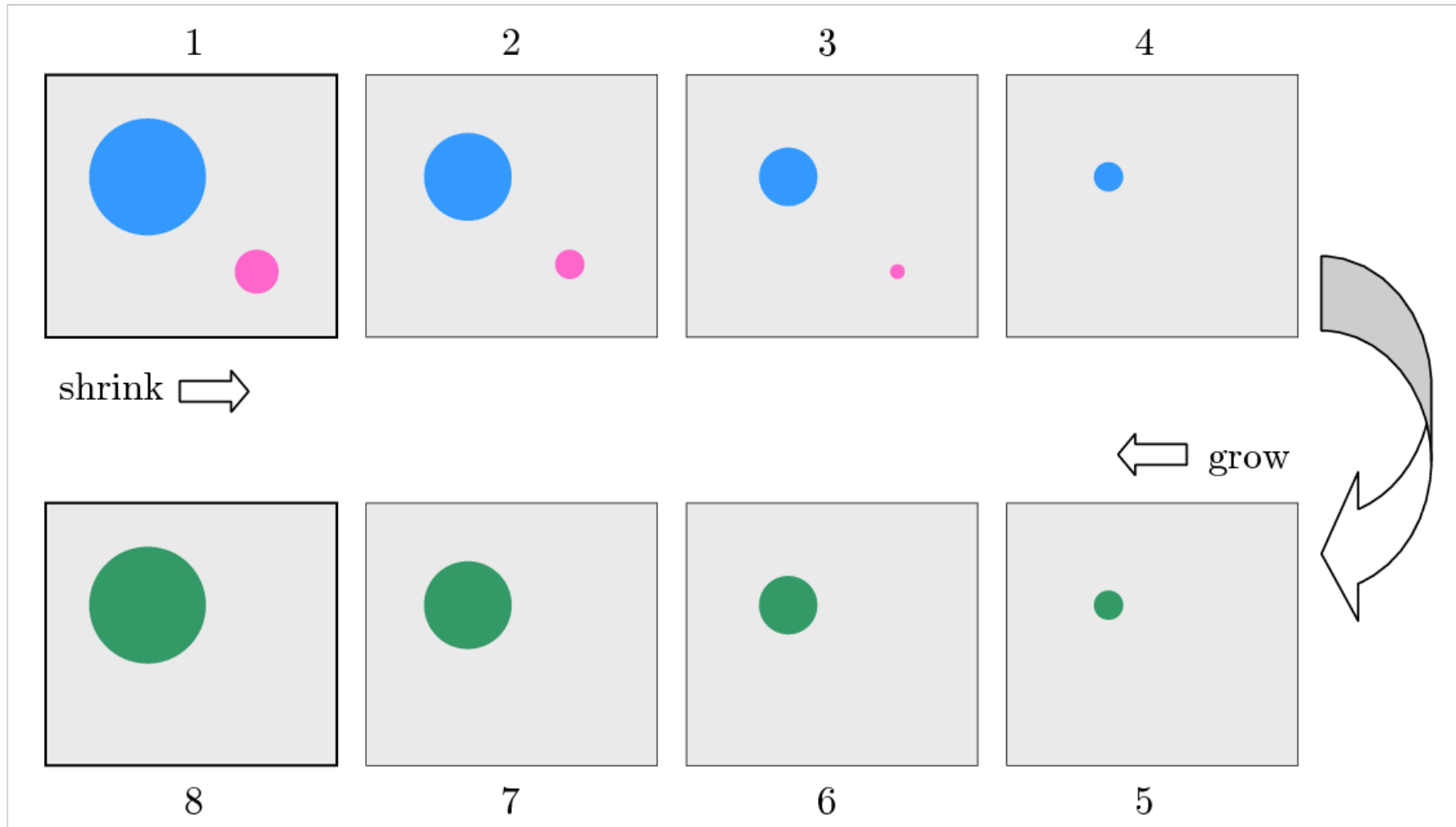


- Morphological operations
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  - Region growing



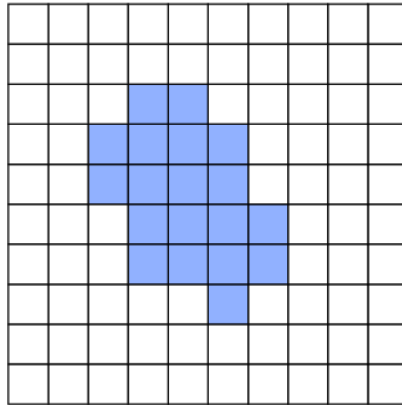
- Morphological mathematics operates on images as a **set of points**
- **Modify in a control way** the structure/morphology of an image
- Typically used in **binary images**
- Can be used in graylevel or colour image as well
- Used in Image Processing for
  - Filtering
  - Segmentation
  - Object description

- Main idea

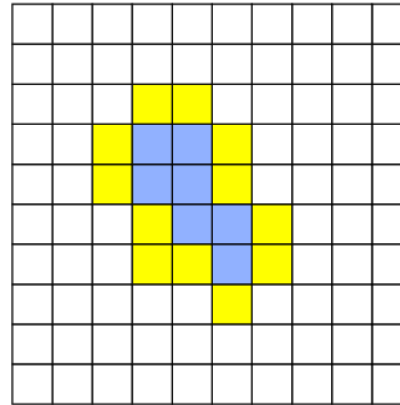


- Main idea

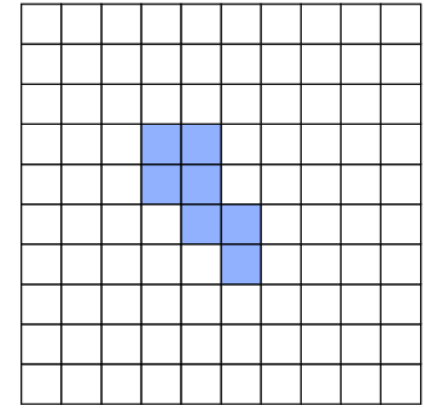
Erosion



(a)

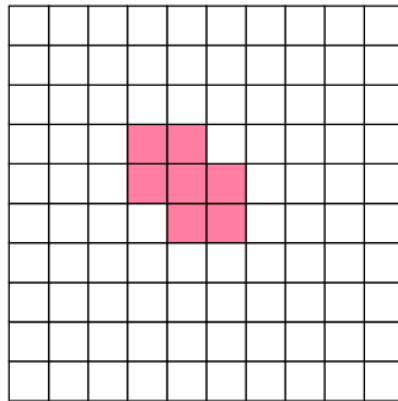


(b)

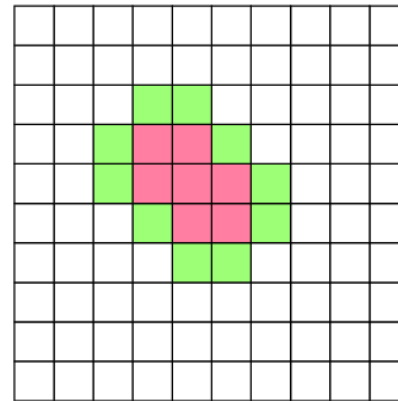


(c)

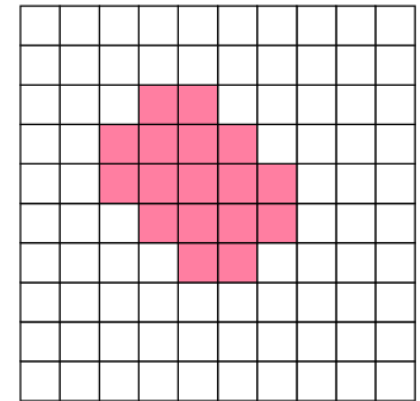
Dilation



(a)



(b)




(c)



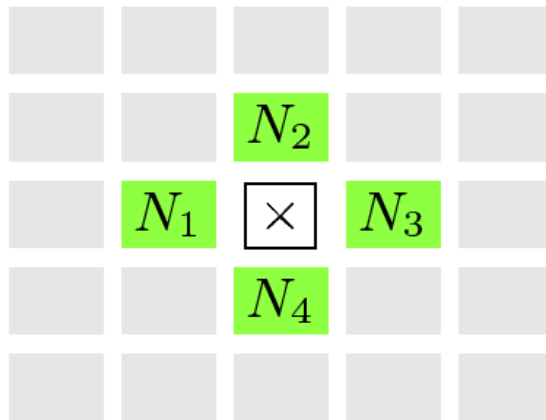
- Structuring element

$$H = \begin{array}{|c|c|c|} \hline \square & \bullet & \square \\ \hline \bullet & \blacksquare & \bullet \\ \hline \square & \bullet & \square \\ \hline \end{array}$$

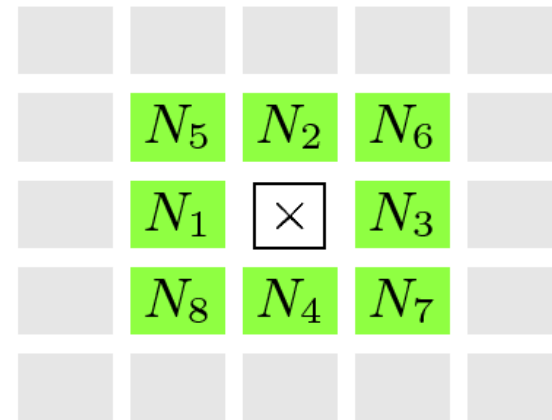
 origin (hot spot)

- Neighbourhood

$\mathcal{N}_4$



$\mathcal{N}_8$



- Main Morphological operations

- Dilation
  - Erosion

} Basic Operations

- Opening
  - Closing

} Composed Operations

Dilation



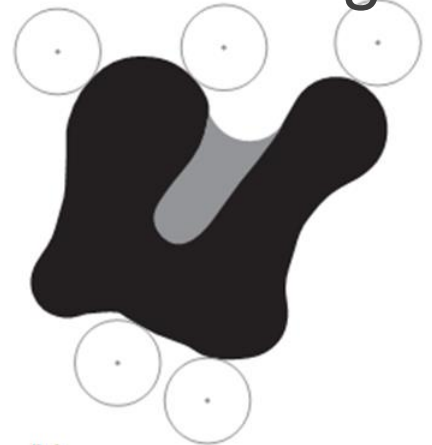
Erosion



Opening




Closing




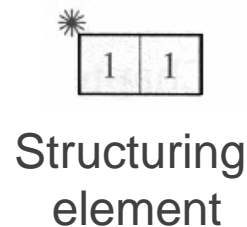


- Dilation
  - gradually enlarge the boundaries of regions
  - small holes and gaps are filled




0	1	0	0	0
0	1	0	0	0
0	1	0	0	0
0	1	1	1	0
0	0	0	0	0

Original image



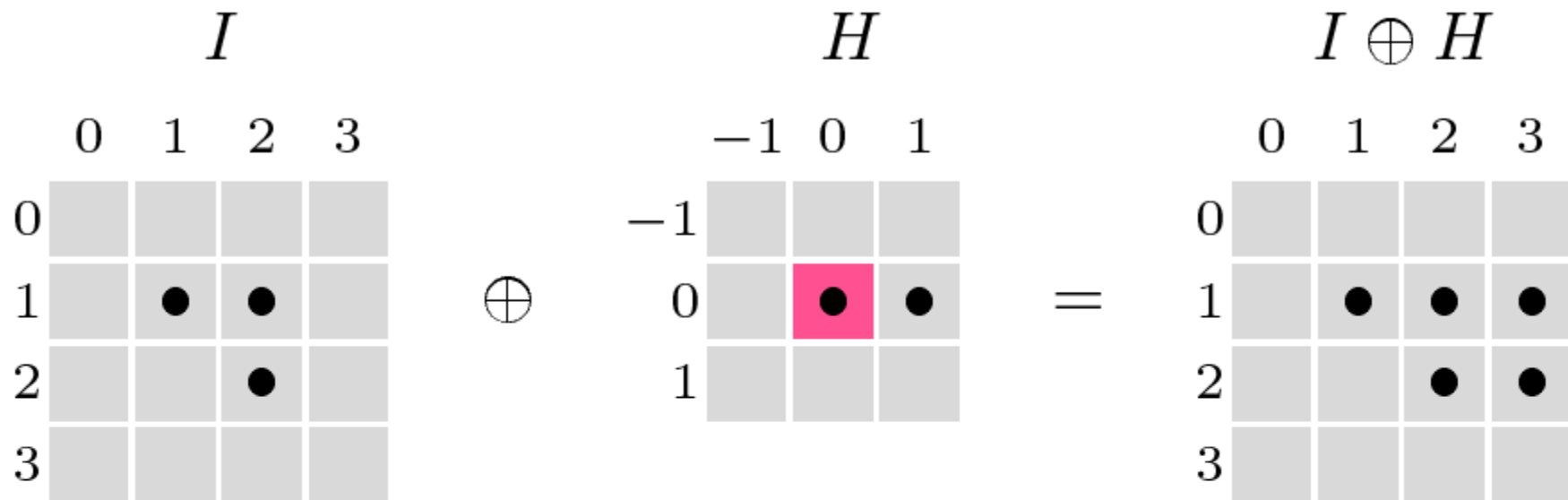
0	1	1	0	0
0	1	1	0	0
0	1	1	0	0
0	1	1	1	1
0	0	0	0	0

Dilation



0	1	1	0	0
0	1	1	0	0
0	1	1	0	0
0	1	1	1	1
0	0	0	0	0

$I \oplus X$



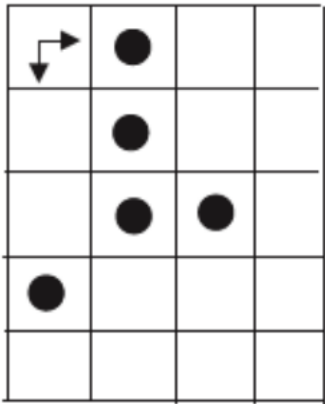
$$I \equiv \{(1, 1), (2, 1), (2, 2)\}, \quad H \equiv \{(\mathbf{0}, \mathbf{0}), (\mathbf{1}, \mathbf{0})\}$$

$$I \oplus H \equiv \{ (1, 1) + (\mathbf{0}, \mathbf{0}), (1, 1) + (\mathbf{1}, \mathbf{0}), \\ (2, 1) + (\mathbf{0}, \mathbf{0}), (2, 1) + (\mathbf{1}, \mathbf{0}), \\ (2, 2) + (\mathbf{0}, \mathbf{0}), (2, 2) + (\mathbf{1}, \mathbf{0}) \}$$

# Morphological operations - Dilation



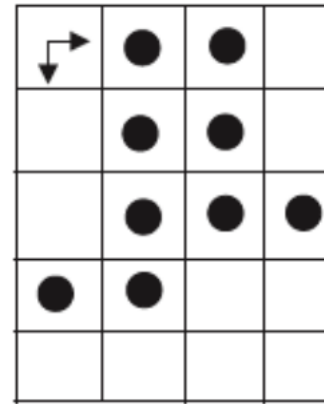
**05:00**



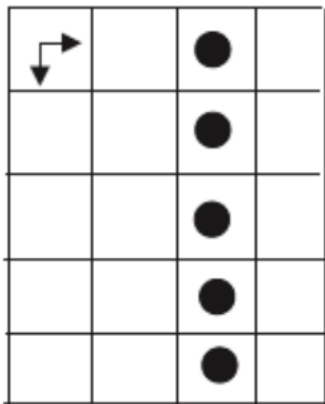
A



B



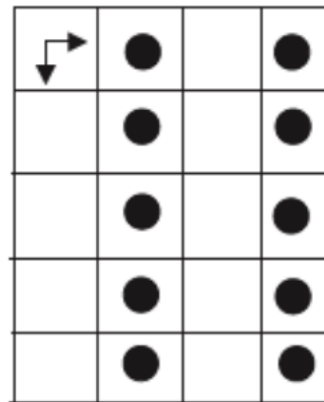
$A \oplus B$



A




B




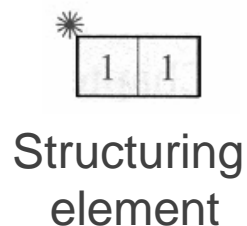
$A \oplus B$

- Erosion
  - Dual of the dilation operation
  - Erode away the boundaries of regions of foreground
  - holes and gaps are increased




0	1	0	0	0
0	1	0	0	0
0	1	0	0	0
0	1	1	1	0
0	0	0	0	0

Original image



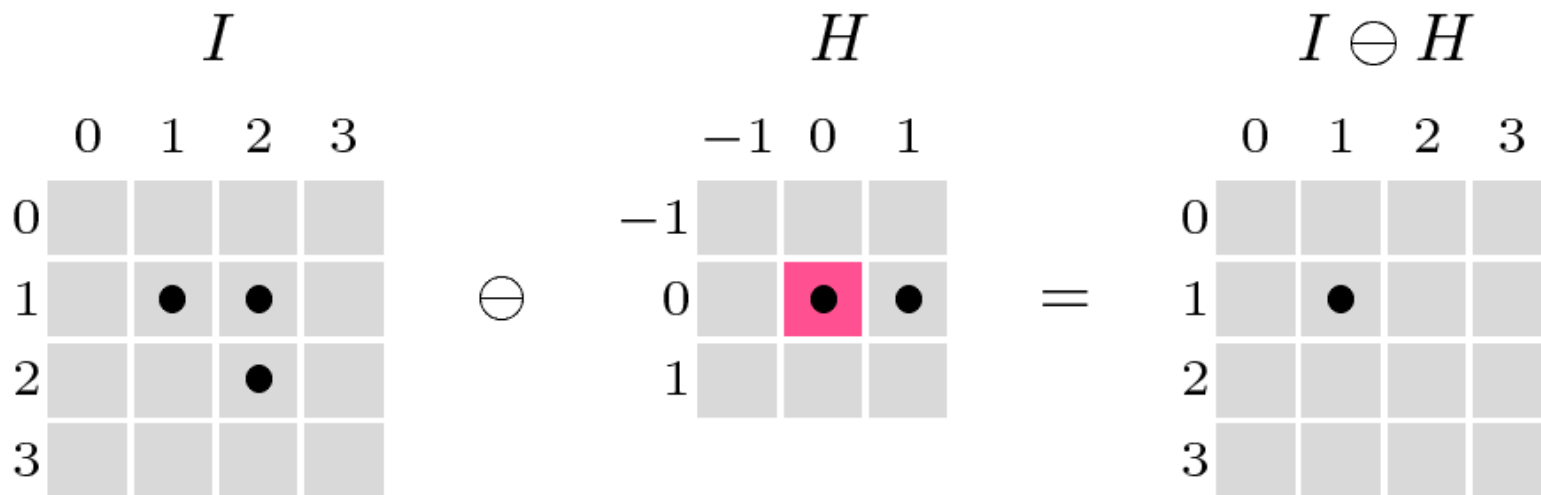
0	1	0	0	0
0	1	0	0	0
0	1	0	0	0
0	1	1	1	0
0	0	0	0	0

Erosion



0	0	0	0	0
0	0	0	0	0
0	0	0	0	0
0	1	1	0	0
0	0	0	0	0

$I \ominus X$



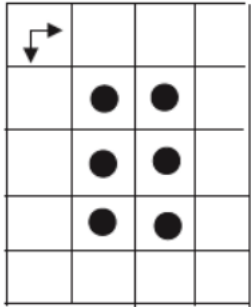
$$I \equiv \{(1, 1), (2, 1), (2, 2)\}, \quad H \equiv \{(\mathbf{0}, \mathbf{0}), (\mathbf{1}, \mathbf{0})\}$$

$$I \ominus H \equiv \{(1, 1)\} \text{ because}$$

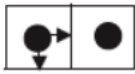
$$(1, 1) + (\mathbf{0}, \mathbf{0}) = (1, 1) \in I \quad \text{and} \quad (1, 1) + (\mathbf{1}, \mathbf{0}) = (2, 1) \in I$$



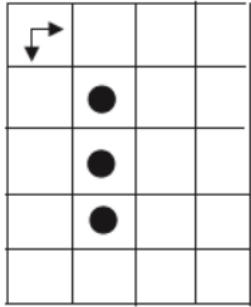
05:00



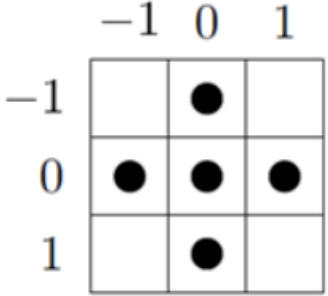
A



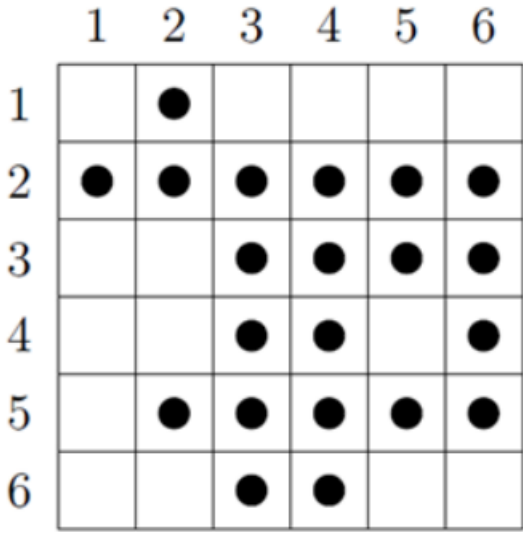
B



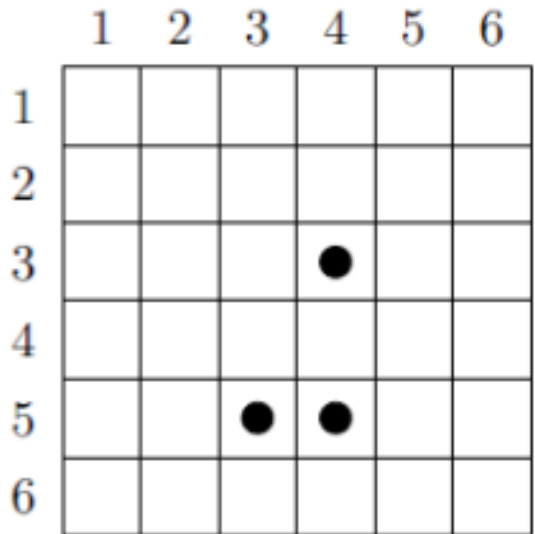
$A \ominus B$



B

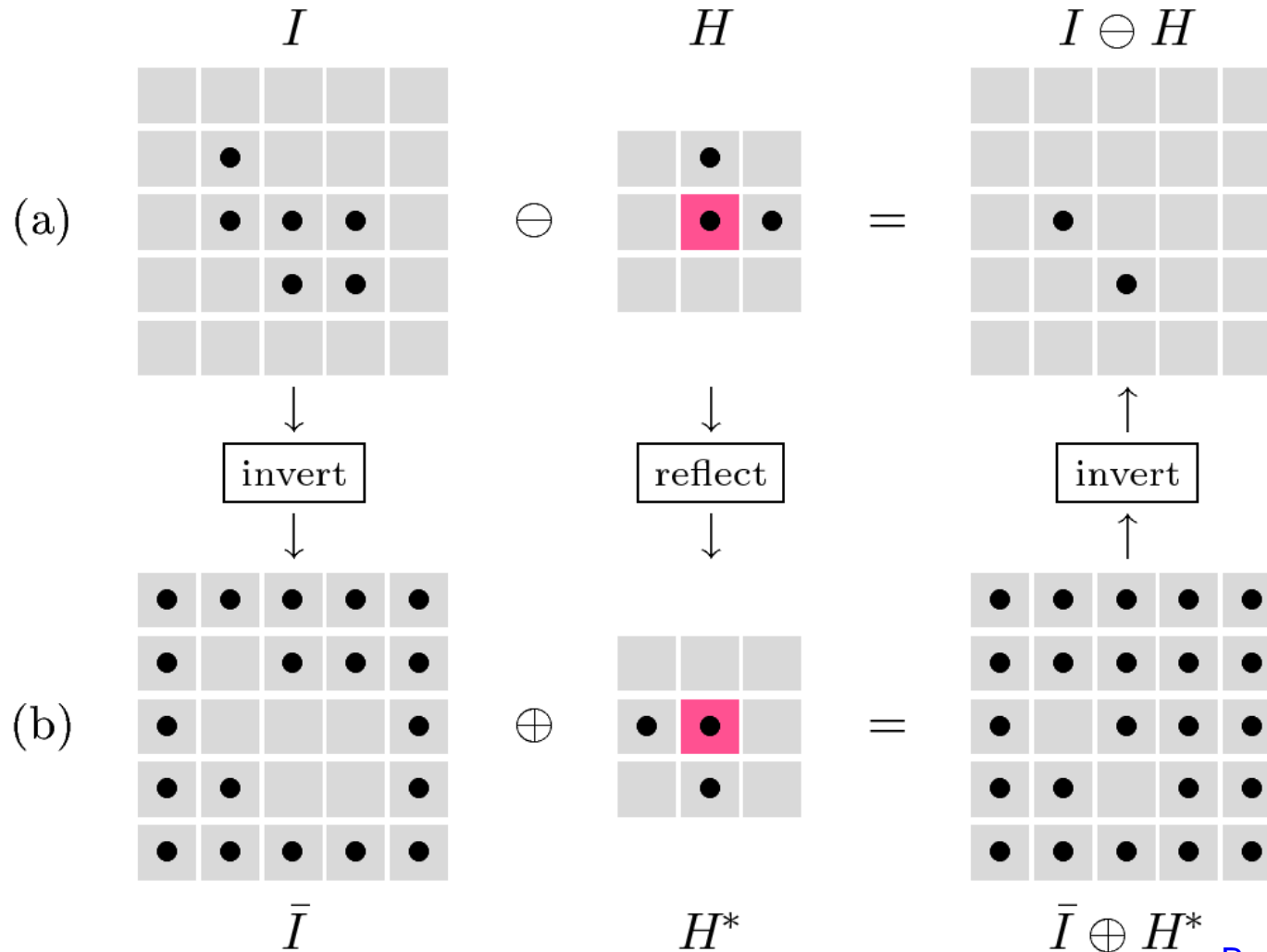


A



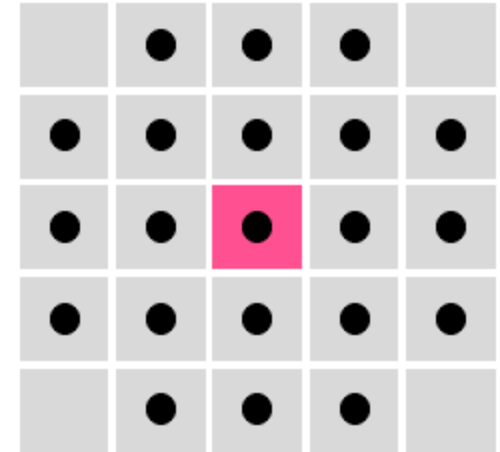
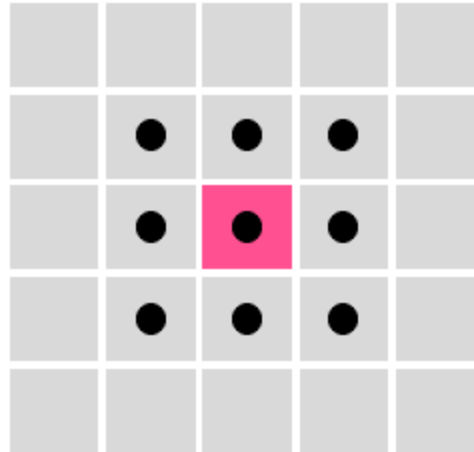
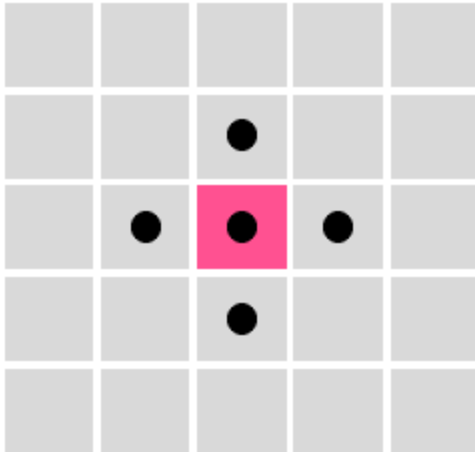
$A \ominus B$

- Dilation and Erosion are dual operations





- Typical structuring elements








- Morphological operations
  - Dilation, erosion
  - Opening, closing
- Segmentation
  - Thresholding
  - Region growing



- Opening
  - Erosion followed by dilation
  - Idempotent operation
    - Results will not change applied multiple time
  - Union of all objects that fit in Structuring Element
  - Circular kernel:
    - Smooth edges of object
    - Broke thin connections




$$I \circ X = (I \ominus X) \oplus X$$




0	1	1	0	0
0	1	1	0	0
0	1	0	0	0
0	1	1	1	0
0	0	1	1	0

Original image




1	1
---	---

Structuring element



0	1	1	0	0
0	1	1	0	0
0	1	0	0	0
0	1	1	1	0
0	0	1	1	0

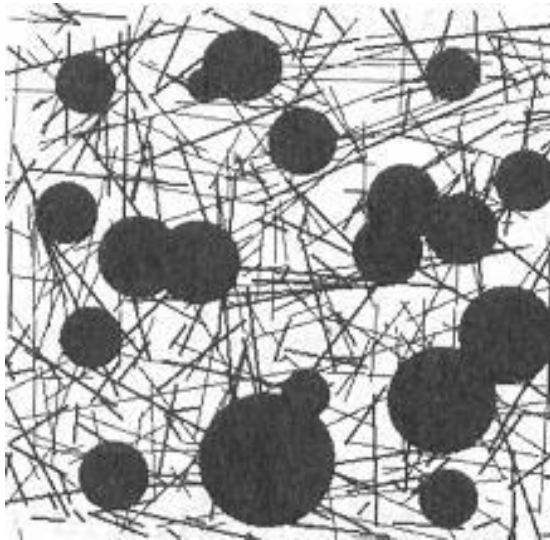
Opening



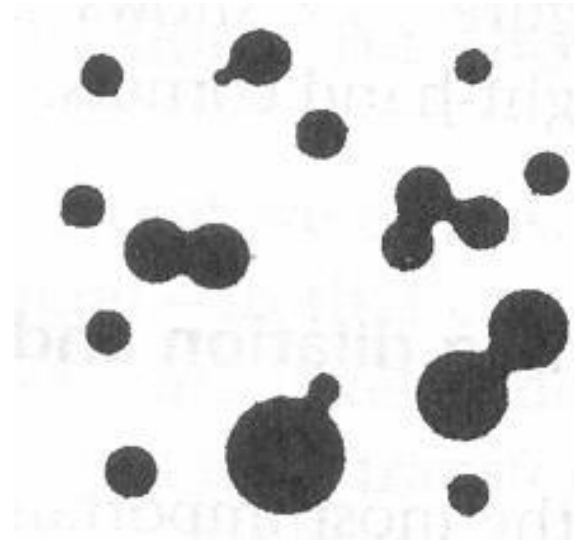
0	1	1	0	0
0	1	1	0	0
0	0	0	0	0
0	1	1	1	0
0	0	1	1	0

$I \circ X$

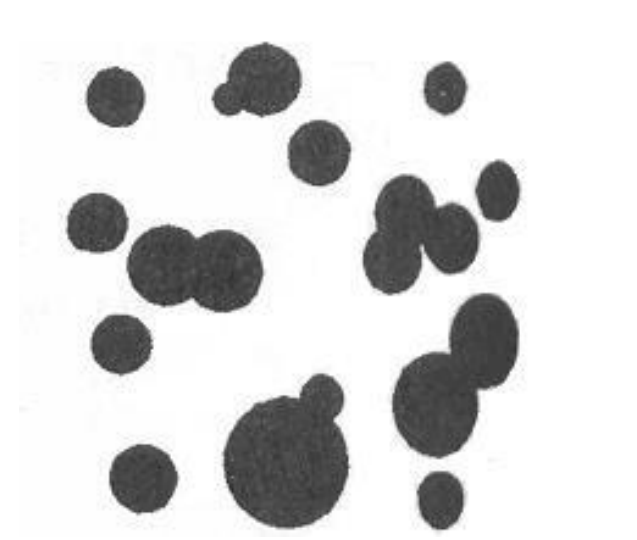
- Opening example
  - Circular structuring element
  - Radius of structuring element must be larger than subsets to remove



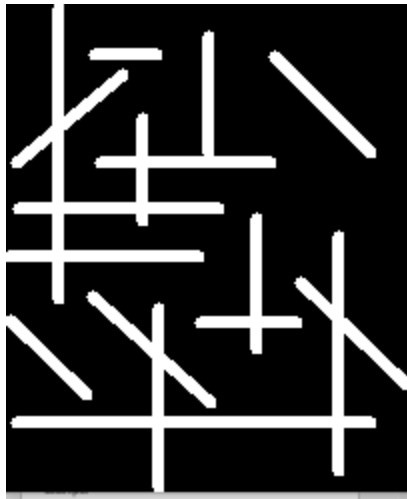
Original image

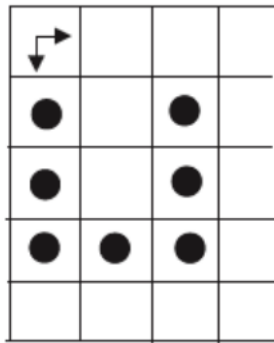


After erosion

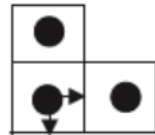


After dilation

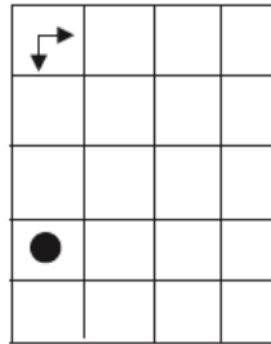




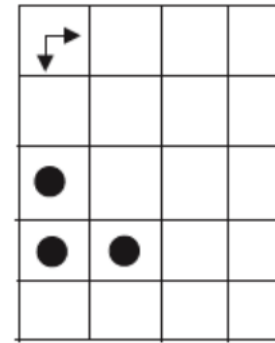
A



B

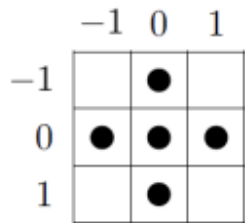


$A \ominus B$

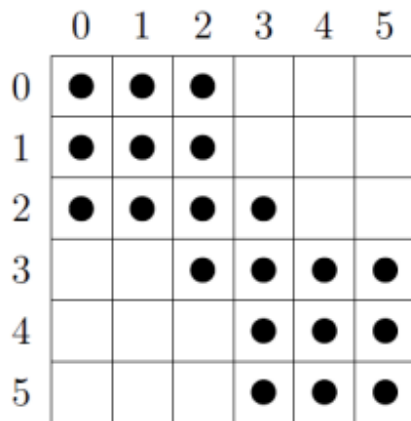


$(A \ominus B) \oplus B$

**05:00**

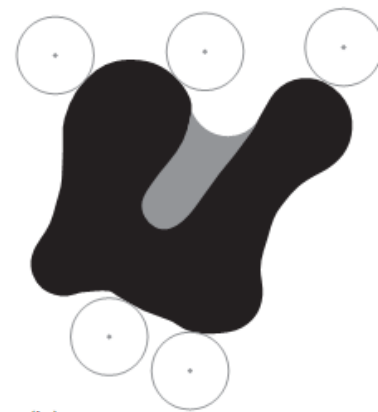


B



A

- Closing
  - Dilation followed by erosion
  - Dual to opening
  - Idempotent operation
    - Results will not change applied multiple time



$$I \bullet X = (I \oplus X) \ominus X$$

0	1	1	0	0
0	1	1	0	0
0	1	0	0	0
0	1	1	1	0
0	0	1	1	0

Original image

1	1
---	---

Structuring element

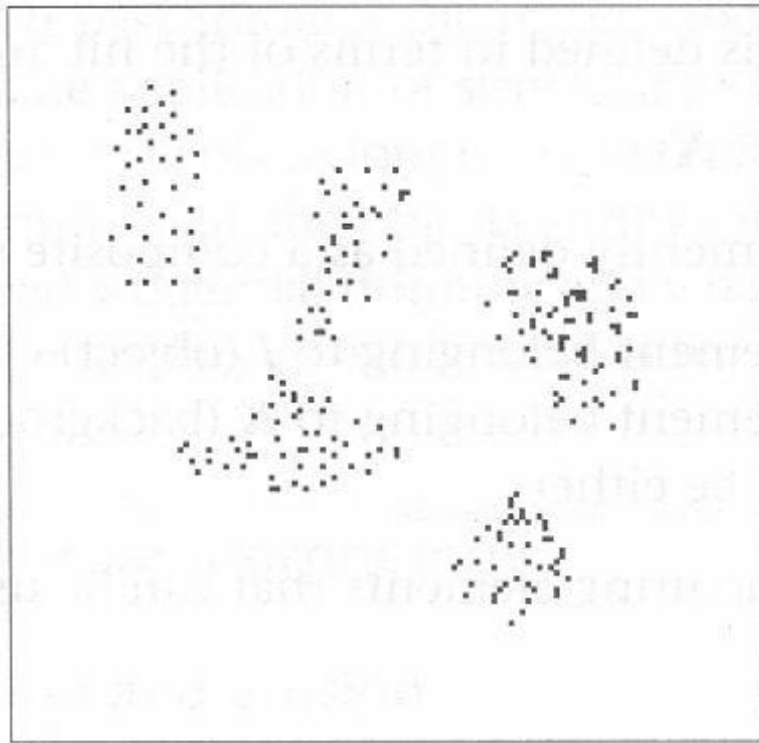
0	1	1	1	0
0	1	1	1	0
0	1	1	0	0
0	1	1	1	1
0	0	1	1	1

Closing

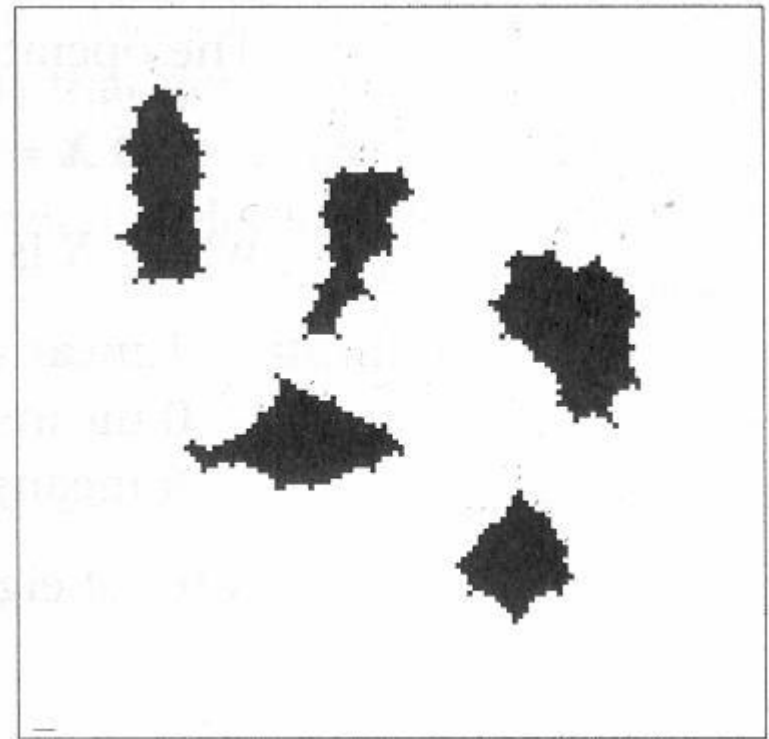
?

$I \bullet X$

- Closing example



Original image



After closing



	-1	0	1
-1		●	
0	●	●	●
1		●	

*B*

	0	1	2	3	4	5	6
0							
1		●	●	●		●	
2		●		●			
3		●	●	●		●	
4							
5		●	●	●	●		
6							

*A*

**05:00**



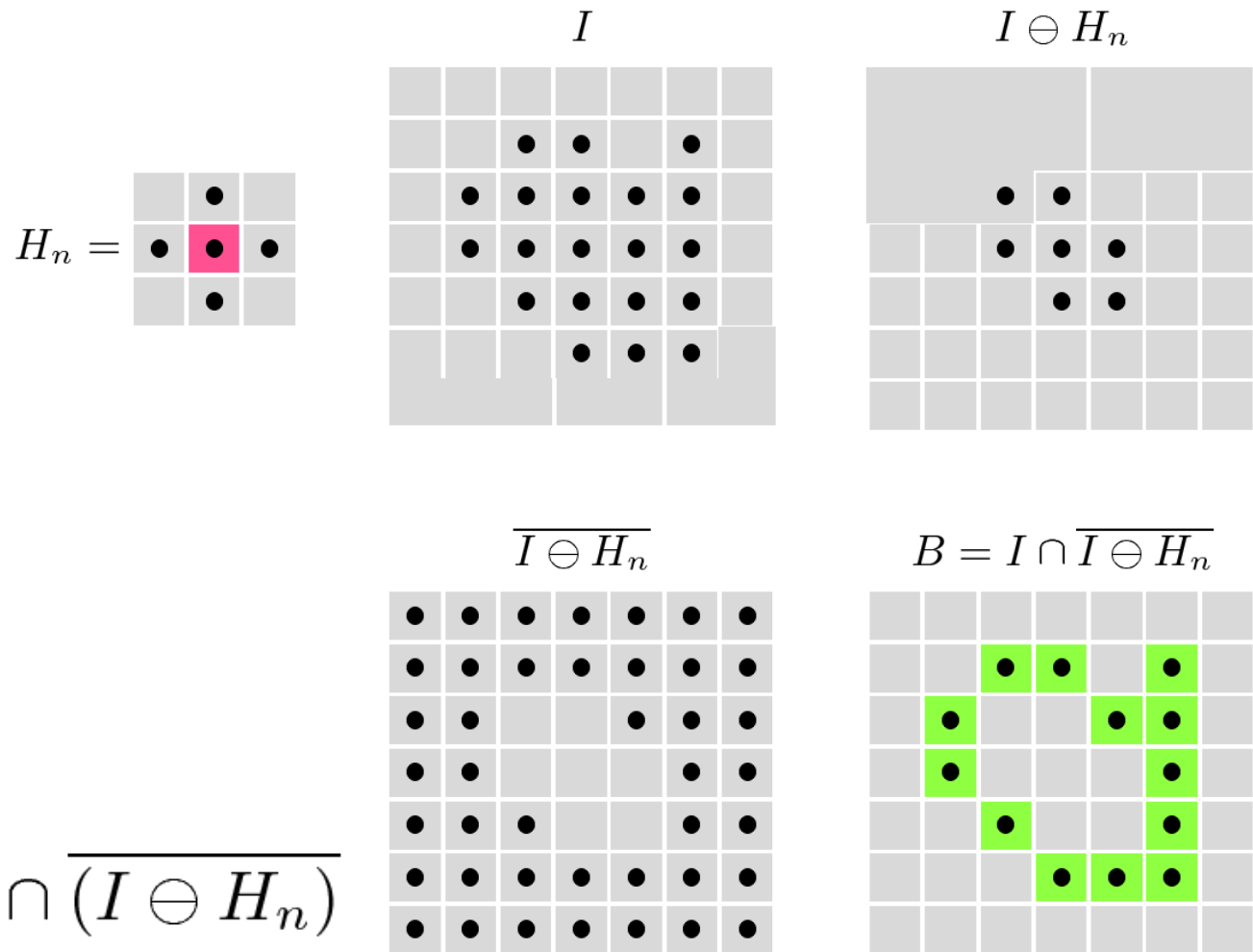
- Edge detection with morphology (outlining)
  - Since erosion results in an isotropic contraction of images, can be used for edge detection:

$$Edge = I - (I \ominus X)$$

- Erosion of objects and then subtraction from original (using 3x3 or 5x5 structuring element)
- Size of structuring element will have impact of contour thickness



- Edge detection with morphology (outlining)



$$I' = I \ominus H_n$$

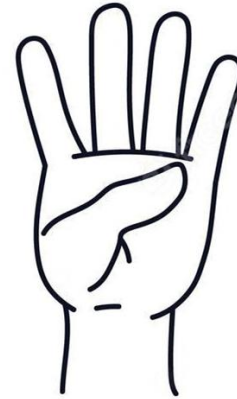
$$B = I \cap \overline{I'} = I \cap \overline{(I \ominus H_n)}$$



**Which method is more adequate to ensure you do not loose any pixel in a binary region you wish to segment?**

1. Open
2. Close
3. Dilation
4. Erosion

**When timer ends...**





**Which method is more adequate to ensure you do not loose any pixel in a binary region you wish to segment?**

**03:00**

1. Open

2. Close

3. Dilation

4. Erosion



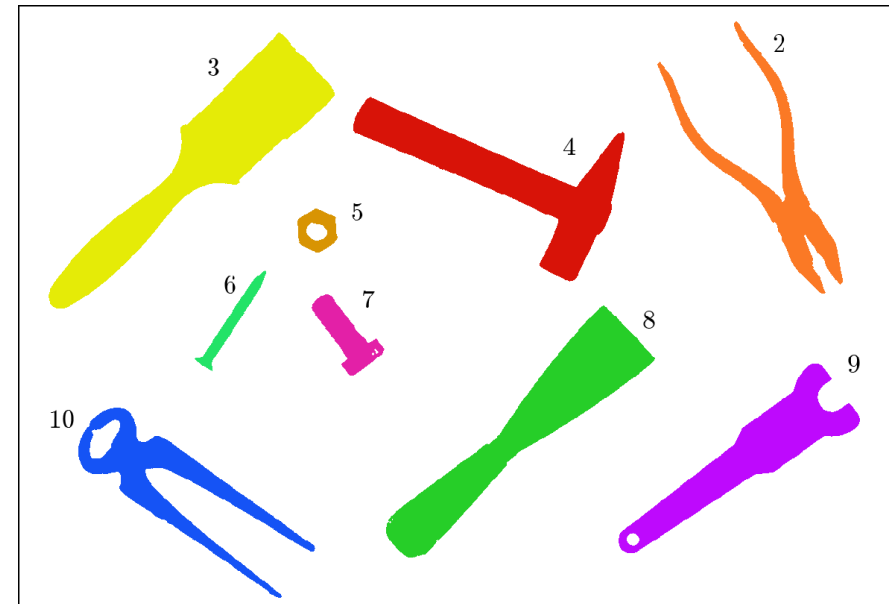
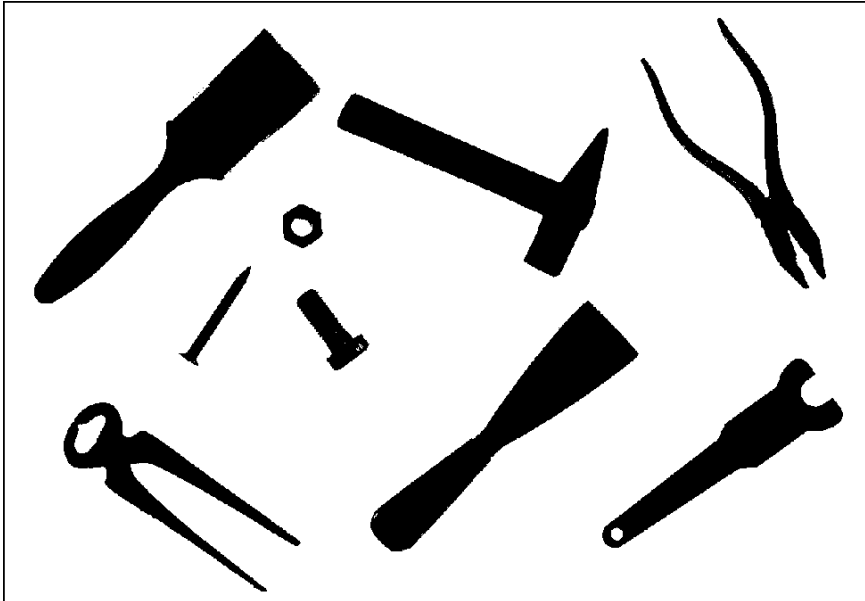


- Morphological operations
  - Dilation, erosion
  - Opening, closing
- **Segmentation**
  - Thresholding
  - Region growing



- Segmentation means **dividing image in regions**
- Often applied before image analysis
- Typical approach is to group pixels with similar properties

- Examples



Burger and Burge



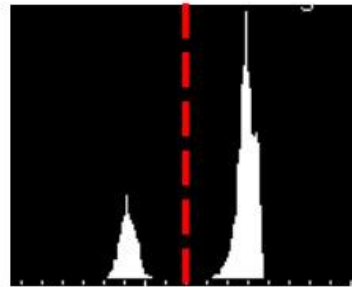
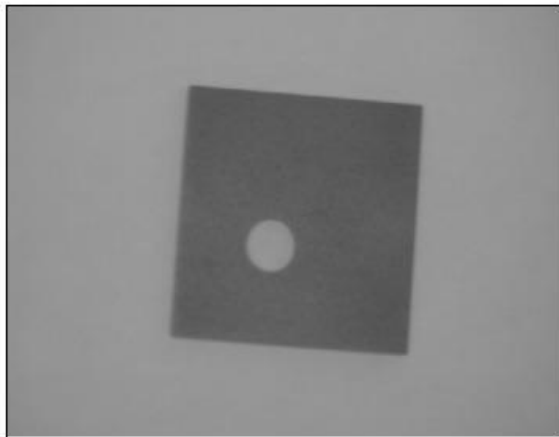


- No segmentation methods that can be used in every case
- No “perfect” segmentation method
- Typical segmentation are based in:
  - pixel intensity
  - regions
  - edges

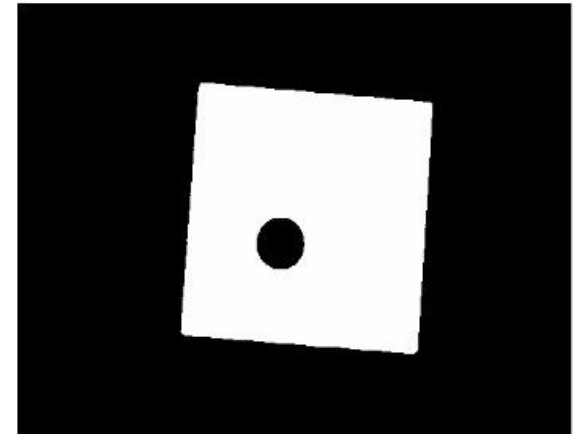


- Morphological operations
  - Dilation, erosion
  - Opening, closing
- Segmentation
  - **Thresholding**
  - Region growing

- Thresholding
  - Oldest segmentation method
  - Appropriate when object of interest have **homogeneous** intensity different from background
  - Not **easy** to find the **adequate** value



Adequate  
threshold

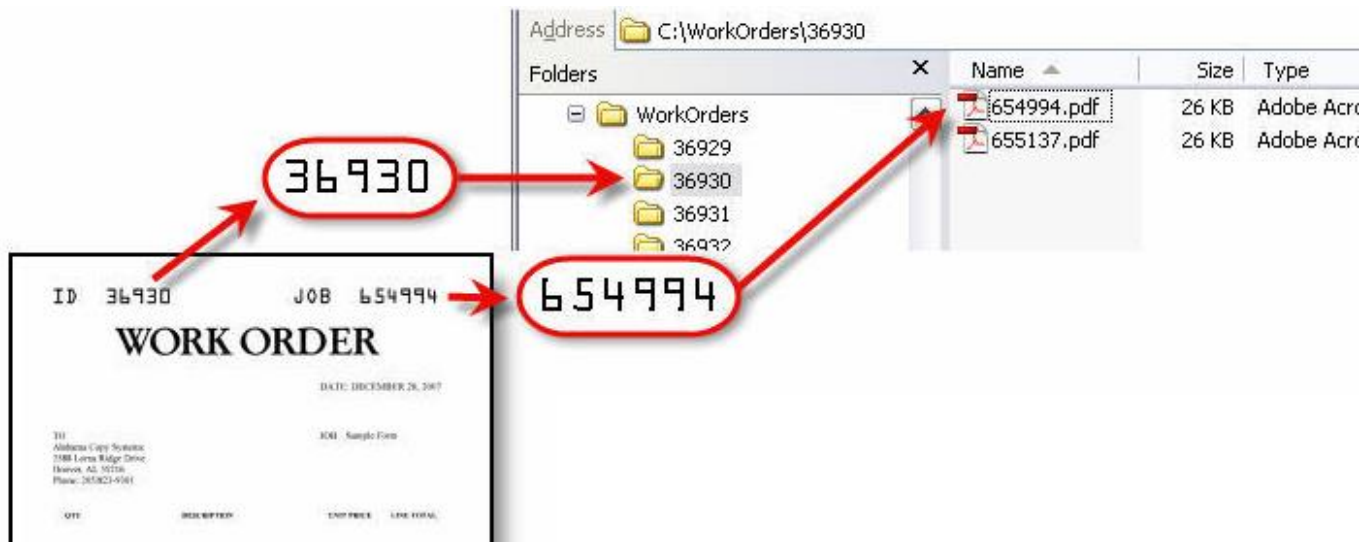
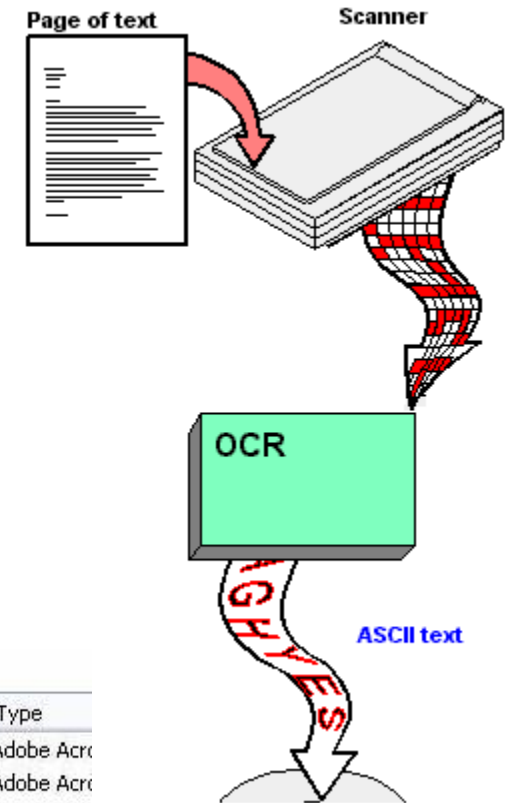


# Segmentation - Thresholding

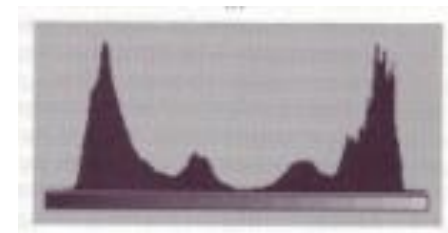
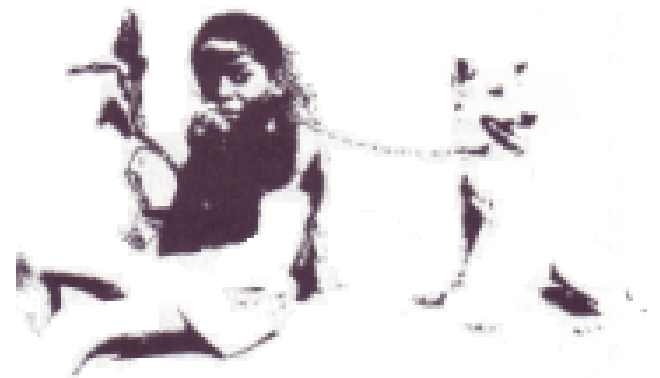
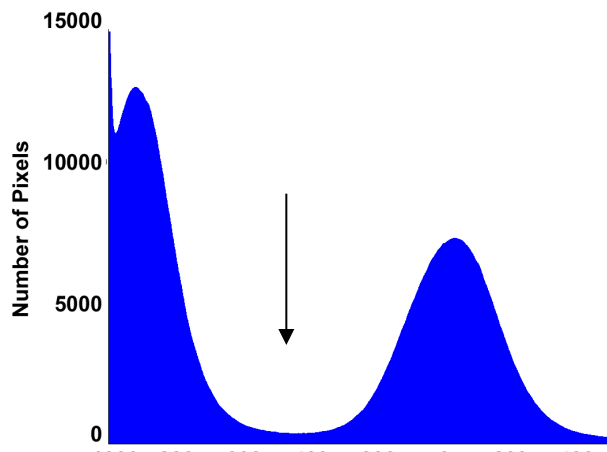


- Oldest segmentation approach
- Appropriate whenever the intensity of the objects of interest is homogeneous and they are different from the background

Example: *OCR (Optical Character Recognition)*



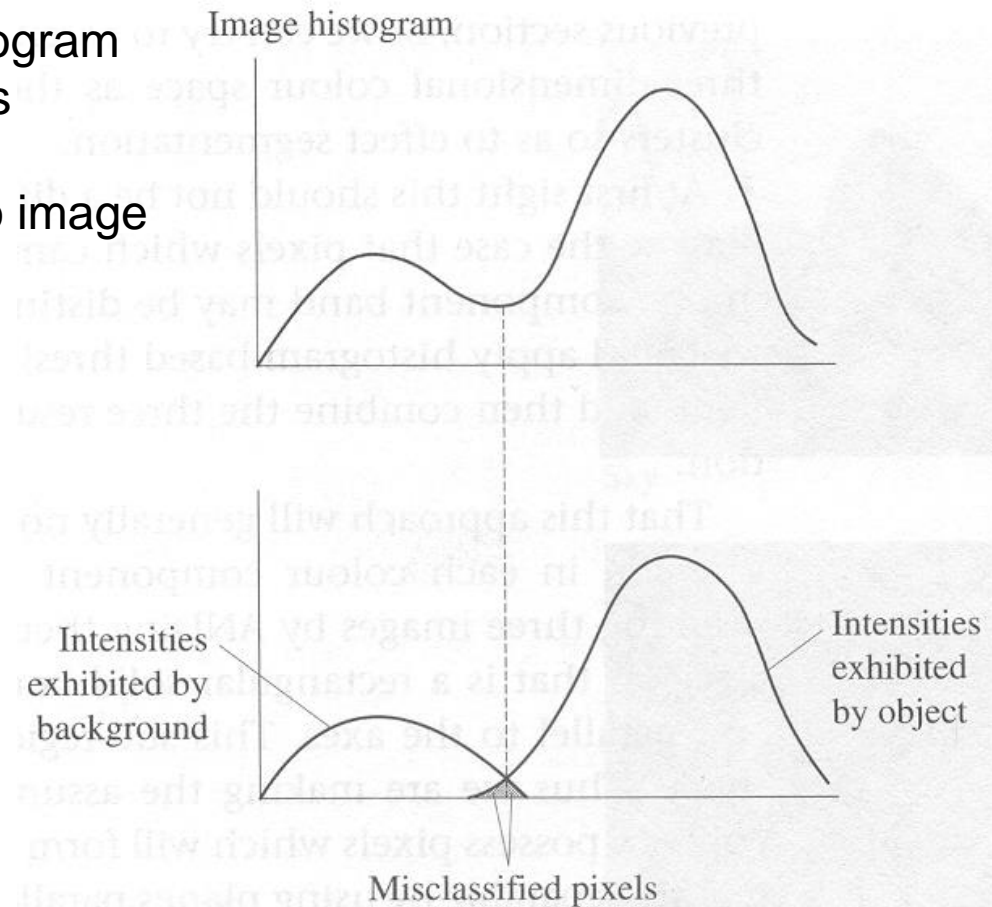
- If the **threshold** value is unknown, analyze the histogram to choose an adequate threshold value
- For a bimodal histogram, the threshold value corresponds to the **valley** between the **peaks**



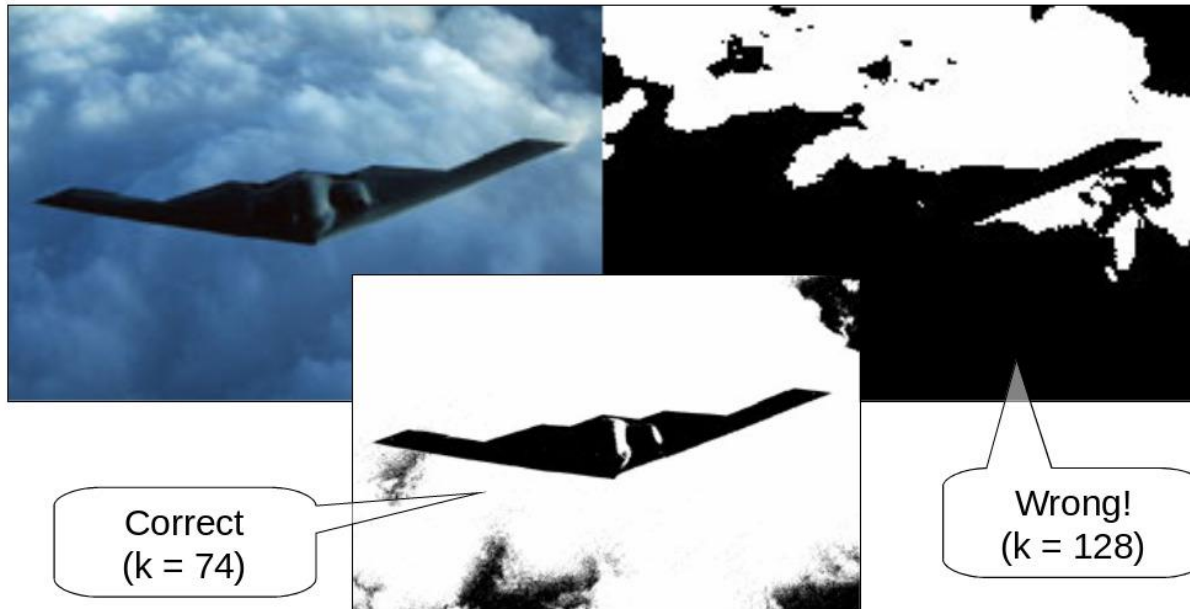
# Segmentation - Thresholding



- This approach can produce “**classification errors**”, depending on the image histogram and the intensity values of the objects
- The **thresholding** can be applied to image sub-regions



- Several approaches for threshold selection
  - Global
  - Variable
    - **Local** - depends on properties of neighbouring pixels
    - **Adaptive** – depends on spatial coordinates
    - **Otsu's** method – based on probabilistic analysis obtained from histogram





- Morphological operations
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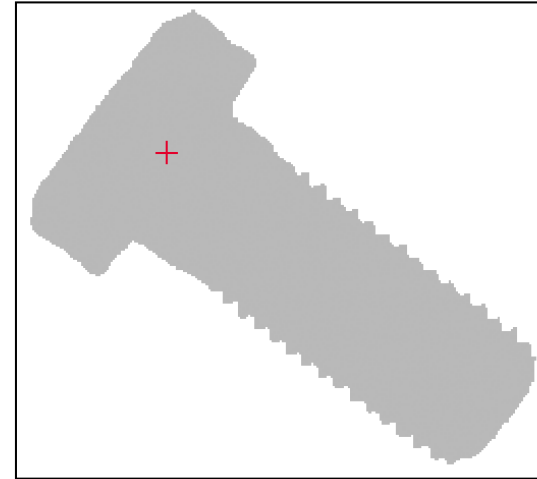




- Grow region by **aggregation of pixels** starting at a **seed point**
- All neighbouring pixels that **comply the rule** are labelled as belonging to the region
- A problem is to obtain “good” seed pixels
- Seed can be obtained using
  - Histograms
  - Interactively
  - ...

- Flood-Filling

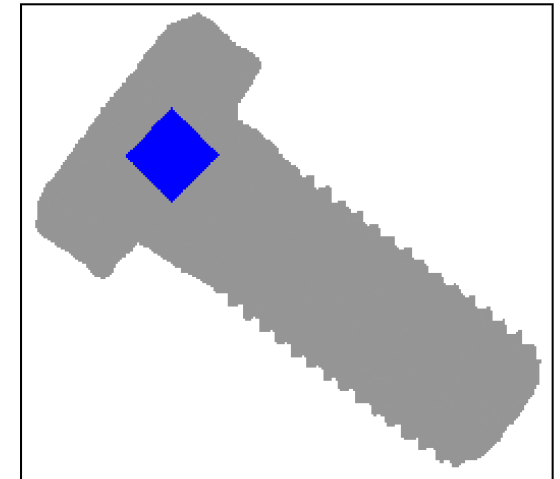
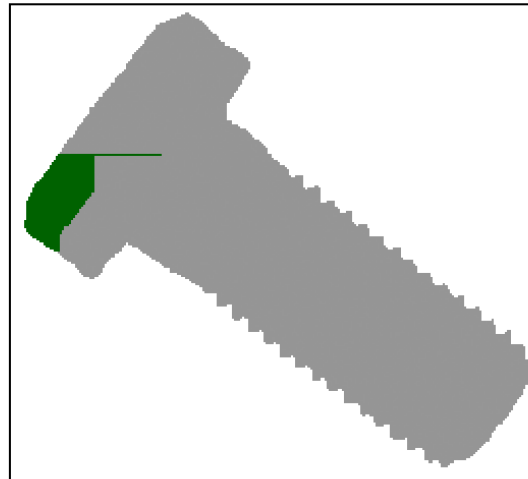
(a)  
Original



depth-first

breadth-first

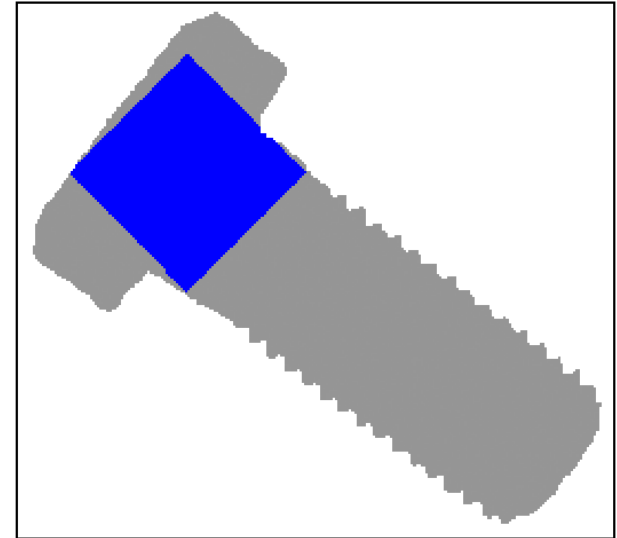
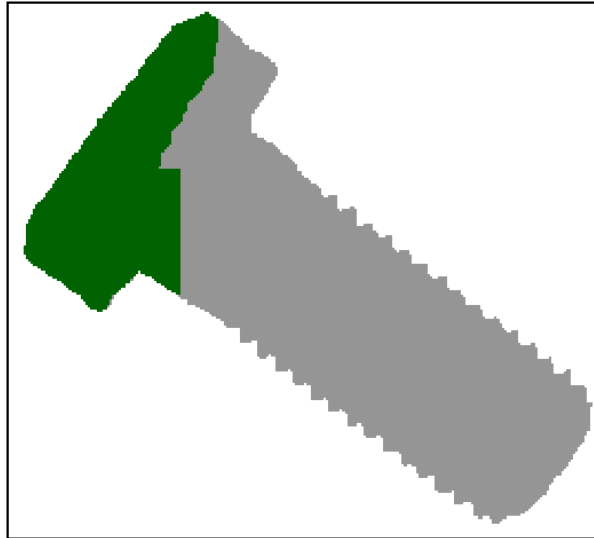
(b)  
 $K = 1.000$



- Flood-Filling

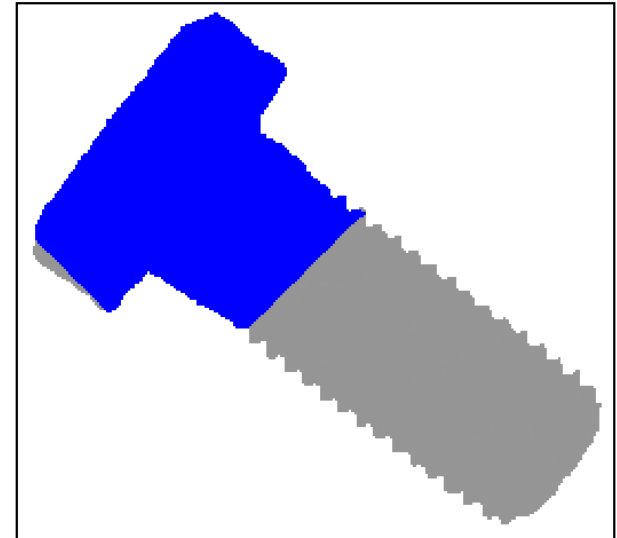
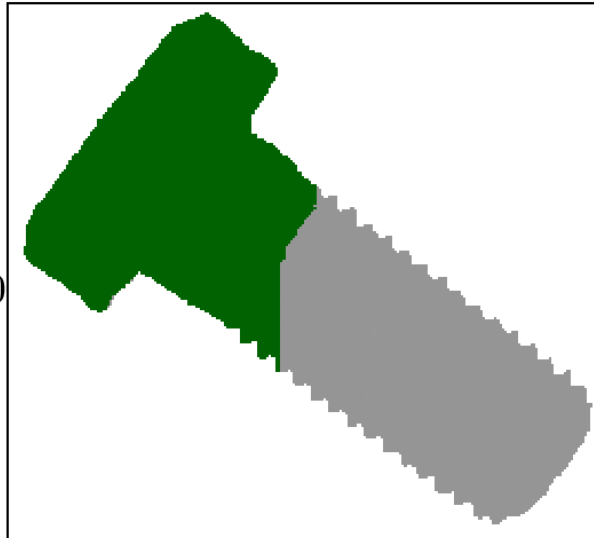
(c)

$K = 5.000$



(d)

$K = 10.000$

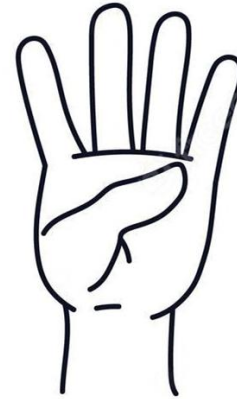
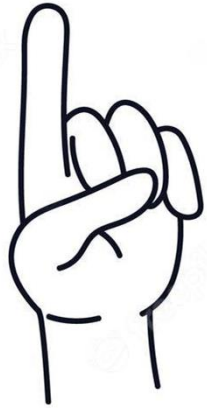




**Which method is more adequate to ensure you do not loose any pixel in a binary region you wish to segment?**

1. Open
2. Close
3. Dilation
4. Erosion

**When timer ends...**





**Which method is more adequate to ensure you do not loose any pixel in a binary region you wish to segment?**

**03:00**

1. Open

2. Close

3. Dilation

4. Erosion

