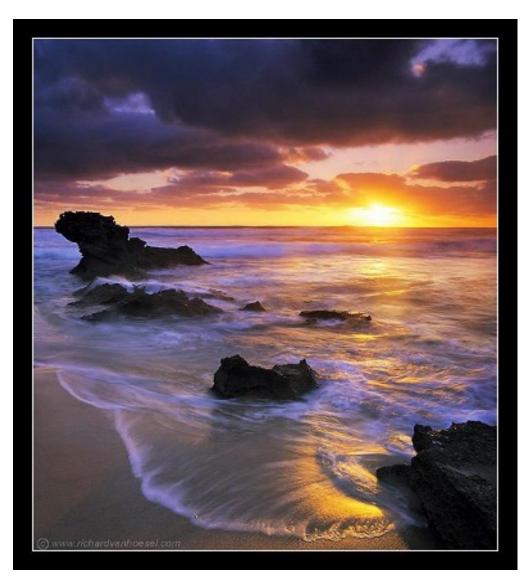
## Light and shading

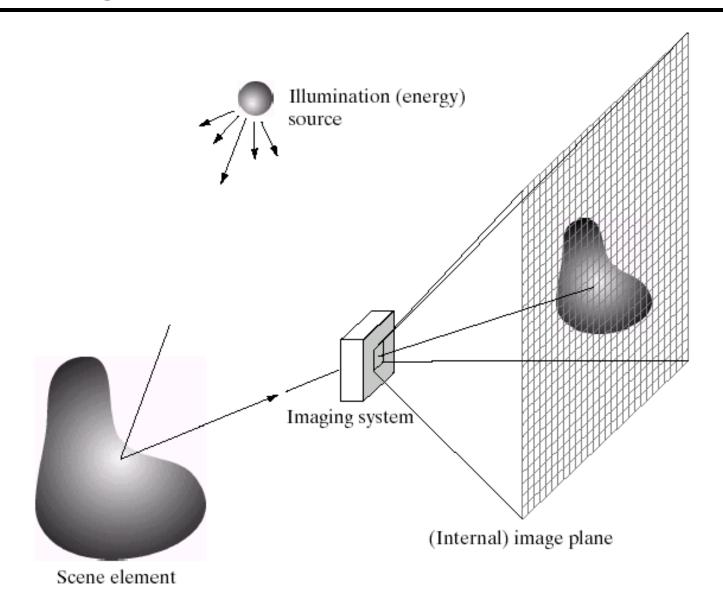


What determines a pixel's intensity?

What can we infer about the scene from pixel intensities?

Image Source: A. Efros

# How light is recorded



## Digital camera

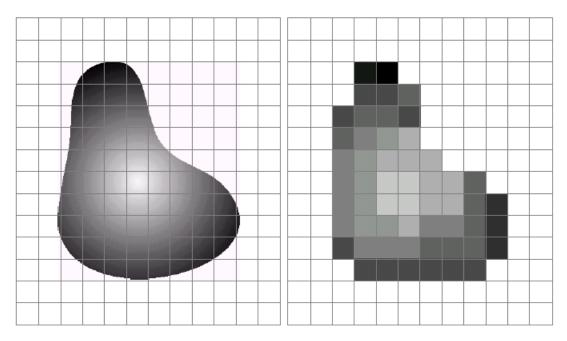


### A digital camera replaces film with a sensor array

Each cell in the array is light-sensitive diode that converts photons to electrons

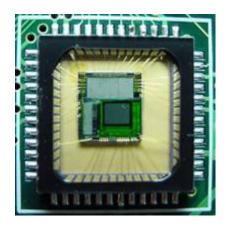
Two common types: Charge Coupled Device (CCD) and CMOS <a href="http://electronics.howstuffworks.com/digital-camera.htm">http://electronics.howstuffworks.com/digital-camera.htm</a>

## Sensor Array

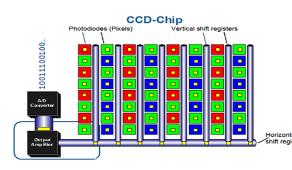




**FIGURE 2.17** (a) Continuos image projected onto a sensor array. (b) Result of image sampling and quantization.



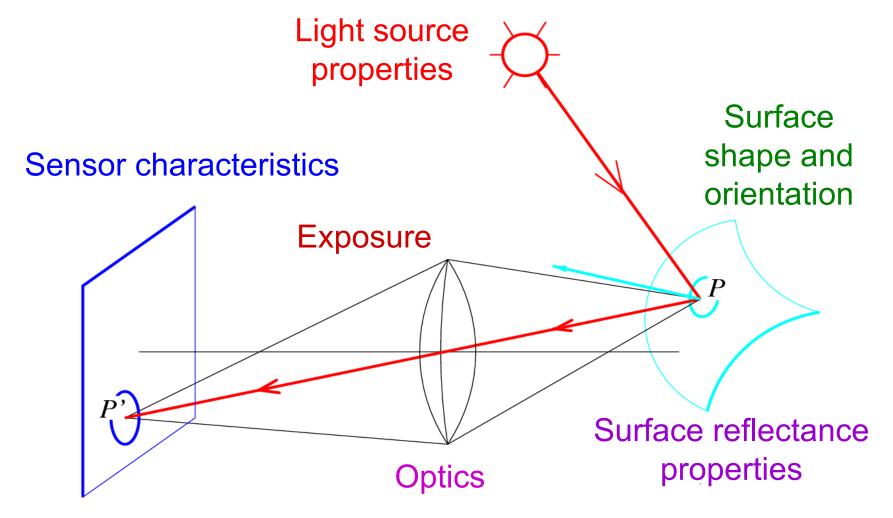
CMOS sensor



Each sensor cell record a small range of orientations amount of light coming in

## Image formation

What determines the brightness of an image pixel?



## Intensity and Surface Orientation

Intensity depends on illumination angle because less light comes in at oblique angles.

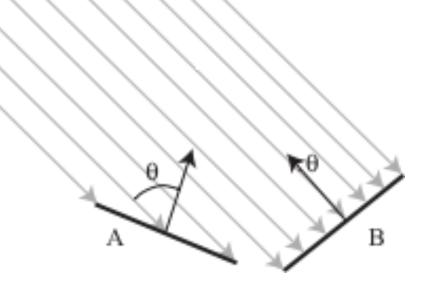
 $\rho$  = albedo

S =directional source

N =surface normal

I = reflected intensity

$$I(x) = \rho(x)(S \cdot N(x))$$



Slide: Forsyth

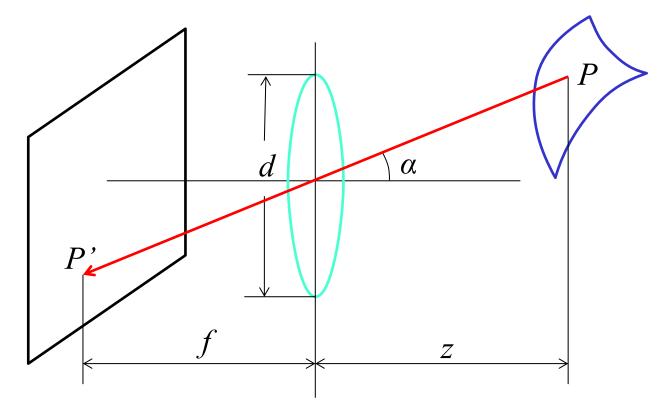
### Fundamental radiometric relation

L: Radiance emitted from P toward P' (辐射度)

Energy carried by a ray (Watts per sq. meter per steradian)

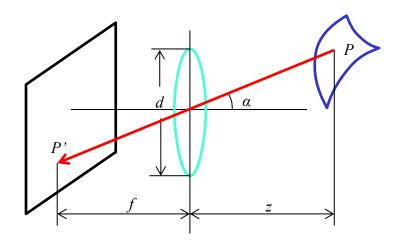
E: Irradiance falling on P' from the lens (辐照度)

Energy arriving at a surface (Watts per sq. meter)



What is the relationship between *E* and *L*?

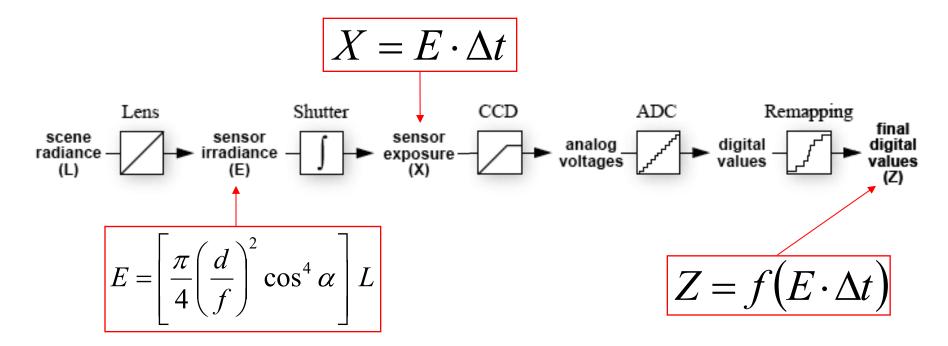
### Fundamental radiometric relation



$$E = \left[\frac{\pi}{4} \left(\frac{d}{f}\right)^2 \cos^4 \alpha\right] L$$

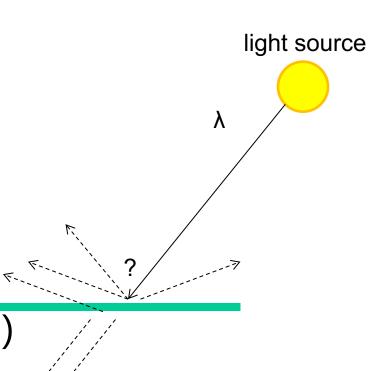
- Image irradiance is linearly related to scene radiance
- Irradiance is proportional to the area of the lens and inversely proportional to the squared distance between the lens and the image plane
- The irradiance falls off as the angle between the viewing ray and the optical axis increases ( natural vignetting )

## From light rays to pixel values



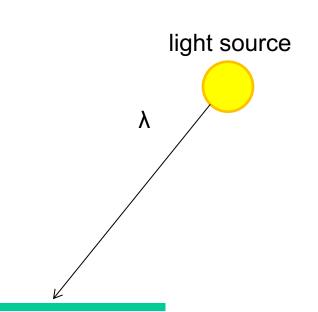
- Camera response function: the mapping f from irradiance to pixel values
  - Useful if we want to estimate material properties
  - Enables us to create high dynamic range images
  - For more info: P. E. Debevec and J. Malik, <u>Recovering High</u>
     <u>Dynamic Range Radiance Maps from Photographs</u>, SIGGRAPH 97

- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence ( 荧光 )
- Subsurface scattering
- Phosphorescence (磷光)
- Interreflection

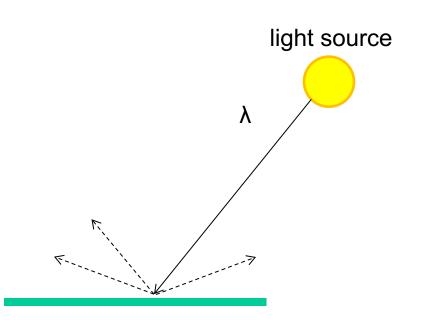


### Absorption

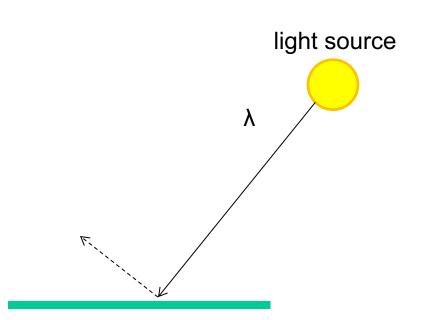
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



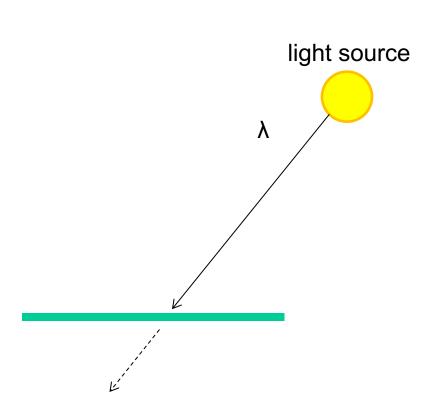
- Absorption
- Diffuse Reflection
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



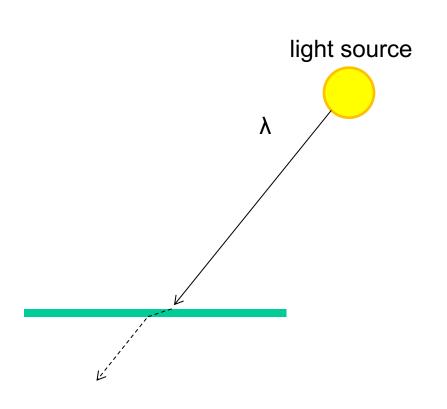
- Absorption
- Diffusion
- Specular Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



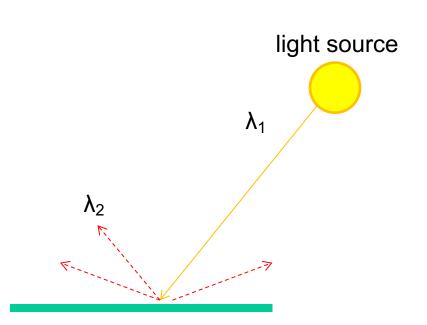
- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



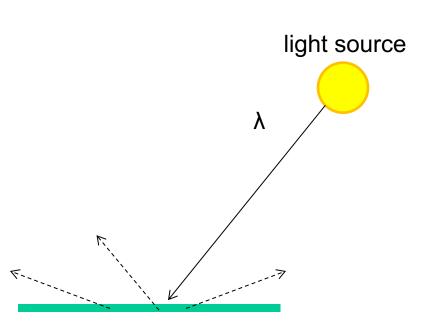
- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



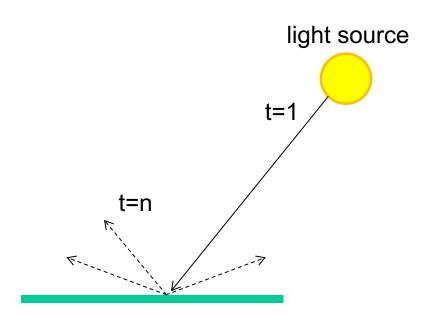
- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



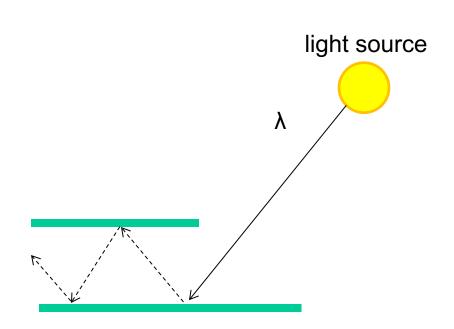
- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection



- Absorption
- Diffusion
- Reflection
- Transparency
- Refraction
- Fluorescence
- Subsurface scattering
- Phosphorescence
- Interreflection

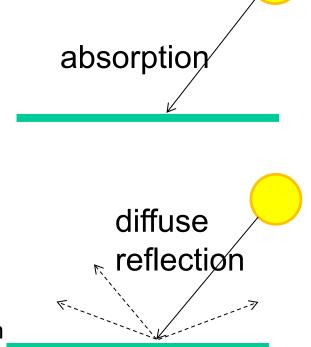


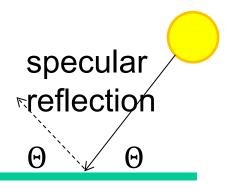
(Specular Interreflection)

### Some common effects

### When light hits a typical surface

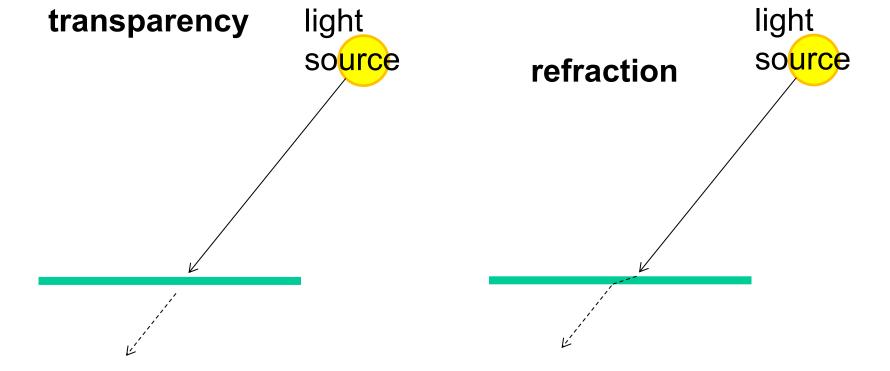
- Some light is absorbed  $(1-\rho)$ 
  - More absorbed for low albedos
- Some light is reflected diffusely
  - Independent of viewing direction
- Some light is reflected specularly
  - Light bounces off (like a mirror), depends on viewing direction





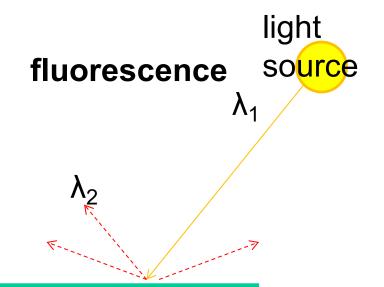
# Other possible effects

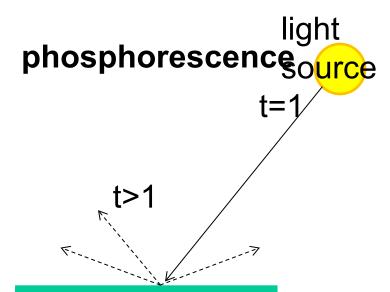




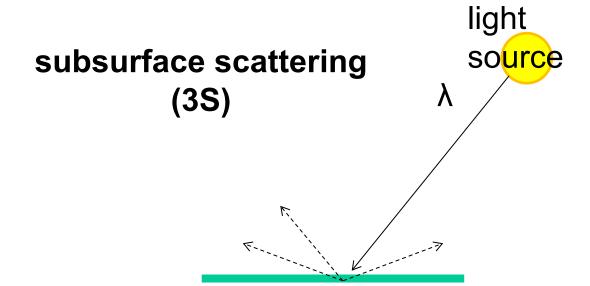






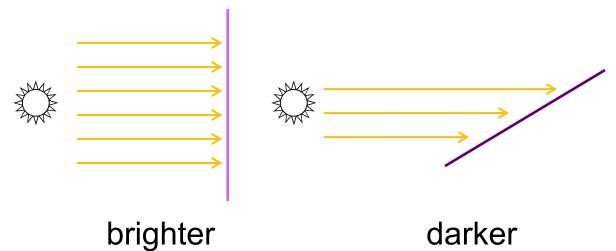


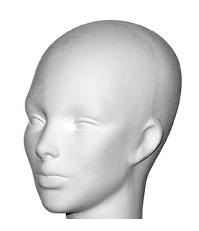


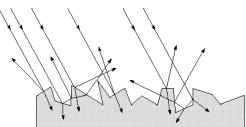


### Diffuse reflection

- Light is reflected equally in all directions
  - Dull, matte surfaces like chalk or latex paint
  - Microfacets scatter incoming light randomly
  - Effect is that light is reflected equally in all directions
- Brightness of the surface depends on the incidence of illumination







## Photometric stereo (shape from shading)

 Can we reconstruct the shape of an object based on shading cues?



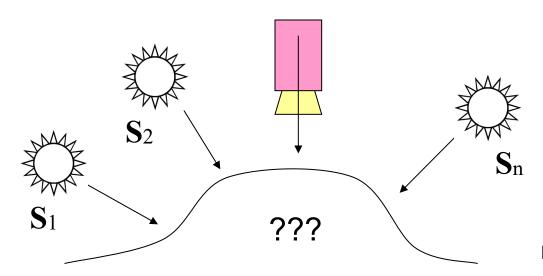
Luca della Robbia, Cantoria, 1438

#### Photometric stereo

#### Assume:

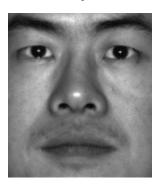
- A Lambertian object
- A local shading model (each point on a surface receives light only from sources visible at that point)
- A set of known light source directions
- A set of pictures of an object, obtained in exactly the same camera/object configuration but using different sources

### Goal: reconstruct object shape and albedo



# Example

Input





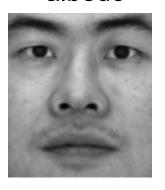


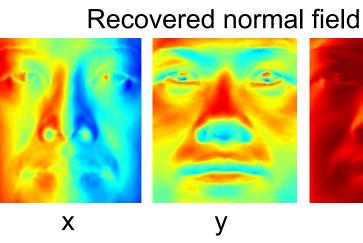


0.5

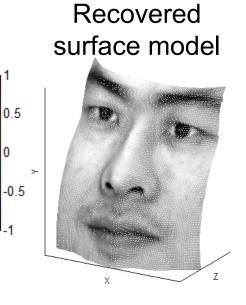


Recovered albedo



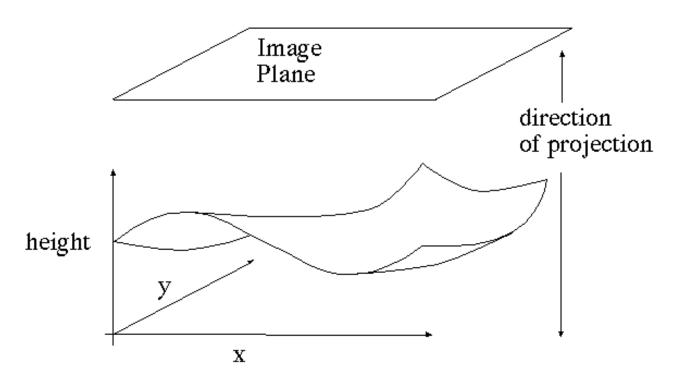






## Image model

- **Known:** source vectors  $S_j$  and pixel values  $I_j(x,y)$
- Unknown: surface normal N(x,y) and albedo 反照 p(x,y)



## Image model

- **Known:** source vectors  $S_j$  and pixel values  $I_j(x,y)$
- Unknown: surface normal N(x,y) and albedo 反照 率  $\rho(x,y)$
- Assume that the response function of the camera is a linear scaling by a factor of k
- Lambert's law:

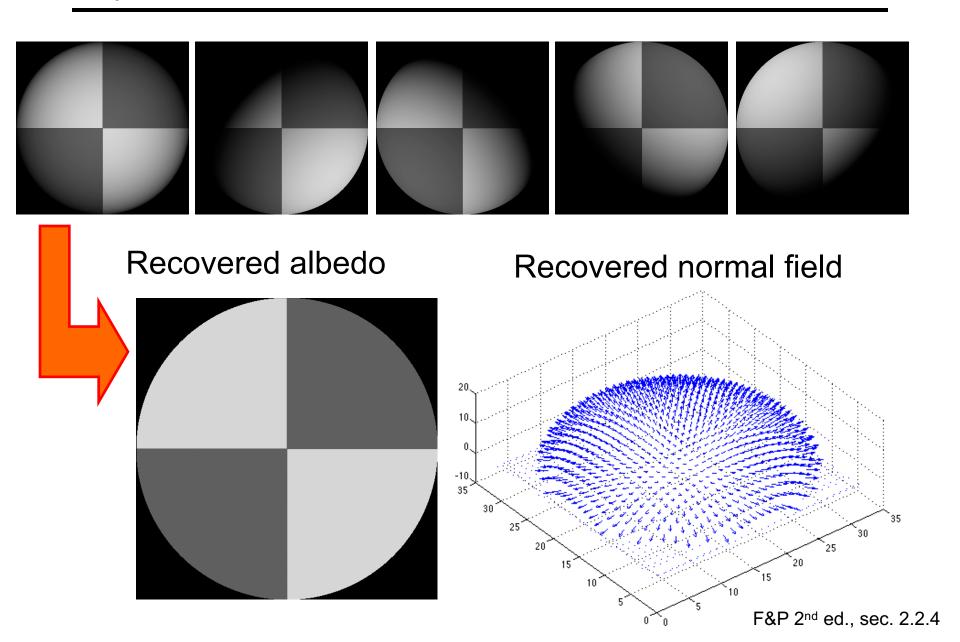
$$I_{j}(x,y) = k \rho(x,y) (\mathbf{N}(x,y) \cdot \mathbf{S}_{j})$$
$$= (\rho(x,y) \mathbf{N}(x,y)) \cdot (k\mathbf{S}_{j})$$
$$= \mathbf{g}(x,y) \cdot \mathbf{V}_{j}$$

## Least squares problem

For each pixel, set up a linear system:

- Obtain least-squares solution for g(x,y) (which we defined as  $N(x,y) \rho(x,y)$ )
- Since N(x,y) is the unit normal,  $\rho(x,y)$  is given by the magnitude of g(x,y)
- Finally,  $N(x,y) = g(x,y) / \rho(x,y)$

## Synthetic example



## Recovering a surface from normals

Recall the surface is written as

This means the normal has the form:

$$\mathbf{N}(x,y) = \frac{1}{\sqrt{f_x^2 + f_y^2 + 1}} \begin{pmatrix} f_x \\ f_y \\ 1 \end{pmatrix}$$
 the surface:  

$$f_x(x,y) = g_1(x,y) / g_3(x,y)$$

If we write the estimated vector g as

$$\mathbf{g}(x,y) = \begin{pmatrix} g_1(x,y) \\ g_2(x,y) \\ g_3(x,y) \end{pmatrix}$$

Then we obtain values for the partial derivatives of

$$f_x(x, y) = g_1(x, y) / g_3(x, y)$$
  
 $f_y(x, y) = g_2(x, y) / g_3(x, y)$ 

## Recovering a surface from normals

We can now recover the surface height at any point by integration along some path, e.g.

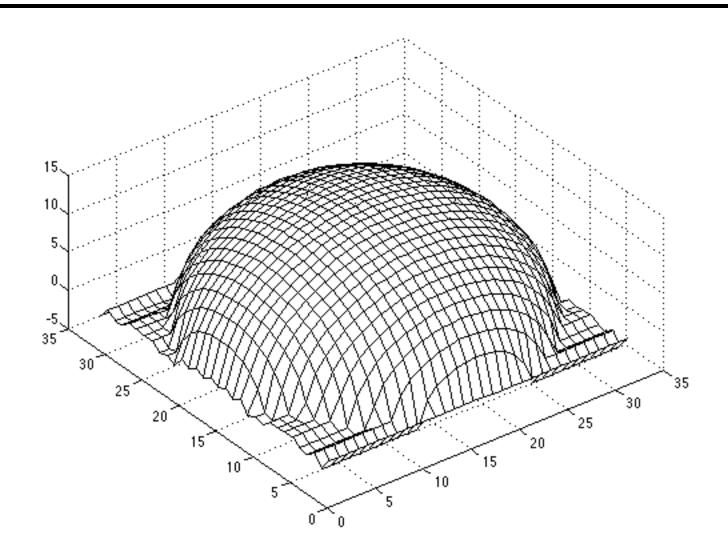
$$f(x,y) = \int_0^x f_x(s,0) ds + \int_0^y f_y(x,t) dt + C$$

(for robustness, should take integrals over many different paths and average the results) Integrability: for the surface f to exist, the mixed second partial derivatives must be equal:

$$\frac{\partial}{\partial y}(g_1(x,y)/g_3(x,y)) = \frac{\partial}{\partial x}(g_2(x,y)/g_3(x,y))$$

(in practice, they should at least be similar)

# Surface recovered by integration



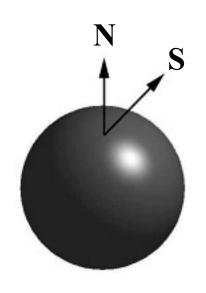
### Limitations

- Simplistic reflectance and lighting model
- No shadows
- No interreflections
- No missing data
- Integration is tricky

## Finding the direction of the light source

$$I(x,y) = \mathbf{N}(x,y) \cdot \mathbf{S}(x,y)$$

#### Full 3D case:



N
$$S = \begin{pmatrix} N_x(x_1, y_1) & N_y(x_1, y_1) & N_z(x_1, y_1) \\ N_x(x_2, y_2) & N_y(x_2, y_2) & N_z(x_2, y_2) \\ \vdots & \vdots & \vdots \\ N_x(x_n, y_n) & N_y(x_n, y_n) & N_z(x_n, y_n) \end{pmatrix} \begin{pmatrix} S_x \\ S_y \\ S_z \end{pmatrix} = \begin{pmatrix} I(x_1, y_1) \\ I(x_2, y_2) \\ \vdots \\ I(x_n, y_n) \end{pmatrix}$$

For points on the occluding contour:

$$\begin{pmatrix} N_{x}(x_{1}, y_{1}) & N_{y}(x_{1}, y_{1}) \\ N_{x}(x_{2}, y_{2}) & N_{y}(x_{2}, y_{2}) \\ \vdots & \vdots & \\ N_{x}(x_{n}, y_{n}) & N_{y}(x_{n}, y_{n}) \end{pmatrix} \begin{pmatrix} S_{x} \\ S_{y} \end{pmatrix} = \begin{pmatrix} I(x_{1}, y_{1}) \\ I(x_{2}, y_{2}) \\ \vdots \\ I(x_{n}, y_{n}) \end{pmatrix}$$

P. Nillius and J.-O. Eklundh, "Automatic estimation of the projected light source direction," CVPR 2001

## Finding the direction of the light source



P. Nillius and J.-O. Eklundh, "Automatic estimation of the projected light source direction," CVPR 2001

## Application: Detecting composite photos

#### Real photo

Fake photo





M. K. Johnson and H. Farid, <u>Exposing Digital Forgeries by Detecting Inconsistencies in Lighting</u>, ACM Multimedia and Security Workshop, 2005.