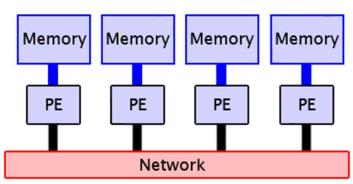
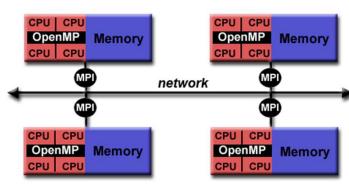
# Distributed memory programming using MPI

CS121 Parallel Computing Fall 2023

#### Distributed memory programming

- Processes have local memory, and communicate by sending messages over network.
- Use standard C / C++ / Fortran. Call library for communication functions.
- Message Passing Interface (MPI)
  - □ Library developed by academics and industry in early 1990's.
    - Standardized clutter of existing HPC languages and tools.
  - ☐ Goals are portability, efficiency and flexibility.
  - Four versions
    - MPI 1.1-1.3, Jun 1995 May 2008
    - MPI 2.1-2.2, Sep 2008 Sep 2009
    - MPI 3.1, Jun 2015
    - MPI 4.0, June 2021
  - □ Defines an interface of message passing routines, but not implementation.
  - □ Vendors create own implementations optimized for their hardware.
  - ☐ MPICH (Argonne National Lab) and OpenMPI are most widely used implementations.
  - ☐ Also commercial implementations from Intel, Microsoft, etc.







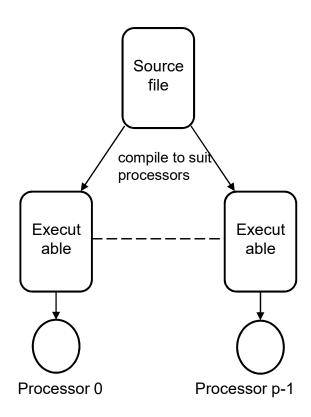
#### Structure of MPI

- MPI contains four main types of functions.
- Process creation
  - Divide the program into separate processes that can be executed on different processors.
- Sending and receiving messages
  - □ Point to point vs collective communication.
  - In contrast to shared memory programming where processes interact by reading and writing shared data in memory.
  - □ Newer versions of MPI also support shared memory style (one way) remote memory access.
- Defining new derived data types.
- Defining and structuring communication groups.
  - Communicators organize processes performing common task.
  - Define topologies for efficient communication.



#### Process model

- MPI based on SPMD (single program multiple data).
- Same program runs on different processors.
  - Processes do different things based on their ID.
  - □ Different from Single Instruction Multiple Data (SIMD)!
    - Processes aren't synchronized, and can execute different instructions or different branches of code.
- Process mapping
  - Typically map one process to each processor / core.
    - More processes can cause thrashing, though may also help reduce idling.
  - Programmer can't control the mapping.



### Process creation example

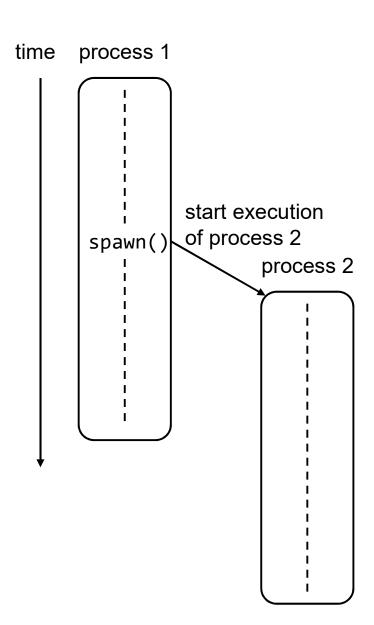
- Include mpi.h
- Must call MPI\_Init and MPI\_Finalize before and after using MPI functions.

- Start program with mpirun -hostfile hosts -np n myprog
- Output appears on host starting myprog.
- Messages may get printed in arbitrary order, because processes run asynchronously.



#### MPMD model

- Separate programs for each processor.
  - Multi program multi data.
- Usually takes master-slave approach.
  - One processor executes master process, other processes started from within master process.
  - □ Dynamic process creation.
  - Higher overhead from starting processes, but sometimes easier to understand and program.
  - Used e.g. in Parallel Virtual Machine (PVM) programming system.



#### MPI in a nutshell

- Many functions, but most programs require only a few functions.
- Initialization.
- Point-to-point communication.
  - □ Send, receive.
- Collective communication.
  - Broadcast, scatter / gather, all to all, reduce, scan, barrier.
- Derived data types.
  - □ Contiguous, indexed, struct.
- Communicators, virtual topologies.
- More info at http://www.mpi-forum.org/docs/

### Communicators

- Communication domain, aka communicator, is a set of processes that can communicate with each other.
  - ☐ A program can define multiple communicators.
  - □ Processes can belong to multiple communication domains.
  - Used to isolate and organize communication.
- Communicators have type MPI\_Comm.
- All communication must specify a communicator.
- MPI\_COMM\_WORLD default communicator created automatically.
- Communicator has a size (number of processes in communicator).
  - □ int MPI\_Comm\_size(MPI\_Comm comm, int \*size)
- Each process in communicator has a rank (ID).
  - □ int MPI\_Comm\_rank(MPI\_Comm comm, int \*rank)
  - □ Used to allow different processors to do different things.

### b/A

### Sending messages

```
int MPI_Send(void *buf, int count, MPI_Datatype type, int dest,
int tag, MPI_Comm comm)
```

- buf is the data to send, i.e. a program variable.
- There are count items in buf, e.g. the size of the array.
- Buffer items must have type MPI Datatype.
  - □ MPI\_CHAR, MPI\_SHORT, MPI\_INT, MPI\_FLOAT, MPI\_BYTE, MPI\_PACKED
  - □ Can also send user defined (derived) types.
- Message sent to process in communicator comm with rank dest.
- tag used to differentiate multiple messages between source and destination.
- Messages between pair of processes sent / received in FIFO order.

### re.

#### Receiving messages

```
int MPI_Recv(void *buf, int count, MPI_Datatype type, int source,
int tag, MPI_Comm comm, MPI_Status *status)
```

- buf gives location to store received messge.
- count must be at least number of items to receive.
  - ☐ If message too large, MPI\_ERROR\_TRUNCATE will occur.
- Message received from process with rank source in communicator comm.
  - Source can also be set to MPI\_ANY\_SOURCE to receive from any process.
- Will only receive message with tag tag.
  - ☐ Tag can also be set to MPI\_ANY\_TAG.
- status useful when receiving using wildcards.
  - MPI\_Status is a struct with fields MPI\_SOURCE, MPI\_TAG, MPI\_ERROR to get info on wildcard message.
- Fairness not guaranteed. If two sends match a receive, only one send completes.

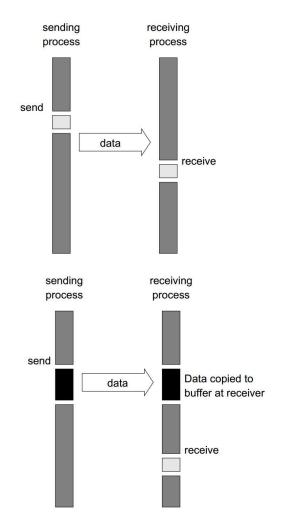
```
#include "mpi.h"
#include <stdio.h>
main(int argc, char *argv[]) {
int numtasks, rank, dest, source, rc, count, tag=1;
char inmsg, outmsg='x';
MPI Status Stat; // required variable for receive routines
MPI Init(&argc, &argv);
MPI Comm size(MPI COMM WORLD, &numtasks);
MPI Comm rank (MPI COMM WORLD, &rank);
// task 0 sends to task 1 and waits to receive a return message
if (rank == 0) {
  dest = 1;
  source = 1;
 MPI Send(&outmsg, 1, MPI CHAR, dest, tag, MPI COMM WORLD);
 MPI Recv (&inmsg, 1, MPI CHAR, source, tag, MPI COMM WORLD, &Stat);
// task 1 waits for task 0 message then returns a message
else if (rank == 1) {
  dest = 0;
  source = 0;
 MPI Recv (&inmsg, 1, MPI CHAR, source, tag, MPI COMM WORLD, &Stat);
  MPI Send(&outmsg, 1, MPI CHAR, dest, tag, MPI COMM WORLD);
// query recieve Stat variable and print message details
MPI Get count(&Stat, MPI CHAR, &count);
printf("Task %d: Received %d char(s) from task %d with tag %d \n",
       rank, count, Stat.MPI SOURCE, Stat.MPI TAG);
MPI Finalize();
```

Source: https://computing.llnl.gov/tutorials/mpi/



#### Blocking communication

- MPI\_Send is blocking: the function won't return immediately after being called.
- Blocking ensures the data is correctly sent.
  - Sender and receiver aren't synchronized, so sender must wait until receiver is ready.
- Waiting time depends on if an MPI implementation uses a hardware send buffer.
  - If there's a buffer, MPI\_Send returns after data copied from application buffer to hardware buffer.
    - Data is later transferred to HW buffer of receiver.
  - With no buffer, sender waits until matching receive occurred.
    - At this point, the data is either in the receiver's hardware or application buffer.
- MPI\_Recv always causes process to block until data is received into its store buffer.

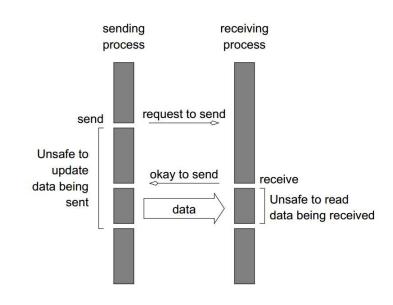


Source: Introduction to Parallel Computing.
Grama et al.



### Nonblocking communication

- Would be more efficient if process can immediately resume execution after calling send or receive.
- Data to be transferred is stored in memory buffer.
  - Process continues with computation while data is being transferred.
  - □ But must not modify buffer until transfer complete.
- Need functions to detect when transfer complete.



Source: Introduction to Parallel Computing.
Grama et al.

### 10

### Nonblocking communication

```
int MPI_Isend(void *buf, int count, MPI_Datatype type, int
dest, int tag, MPI_Comm comm, MPI_Request *req);
int MPI_Irecv(void *buf, int count, MPI_Datatype type, int
source, int tag, MPI_Comm comm, MPI_Request *req);
int MPI_Test(MPI_Request *req, int *flag, MPI_Status *status);
int MPI_Wait(MPI_Request *req, MPI_Status *status);
```

- MPI\_Isend and MPI\_Irecv return immediately after being called.
- But must still know when operations complete.
- Use a request object to identify the operation.
  - □ This object used later to test completion.
  - Can also use to make process wait (block) until operation completes.

### Deadlock example 1

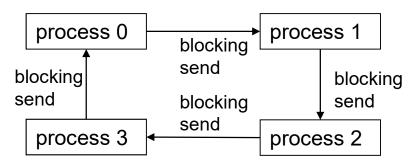
Must be careful about ordering of sends or receives. Otherwise processes can deadlock, i.e. wait forever.

- ☐ If buffering, then probably no deadlock.
- ☐ If no buffering, processes will deadlock waiting to receive from each other.
- ☐ Cause is that tags are sent and received in different orders

Resolve the deadlock by using same tag order for send and recv.

#### Deadlock example 2

- □ Here, npes processes in a ring. Process i sends to i+1, receives from i-1.
- No deadlock with buffering, since MPI\_Send returns and MPI\_Recv can occur.
- Without buffering, processes deadlock blocking for matching receive.



- □ Solution is to first let even numbered processes send and odd processes recv, then let odd processes send and even processes recv.
- ☐ This is cumbersome. It would be nice to have built-in way to avoid deadlock.

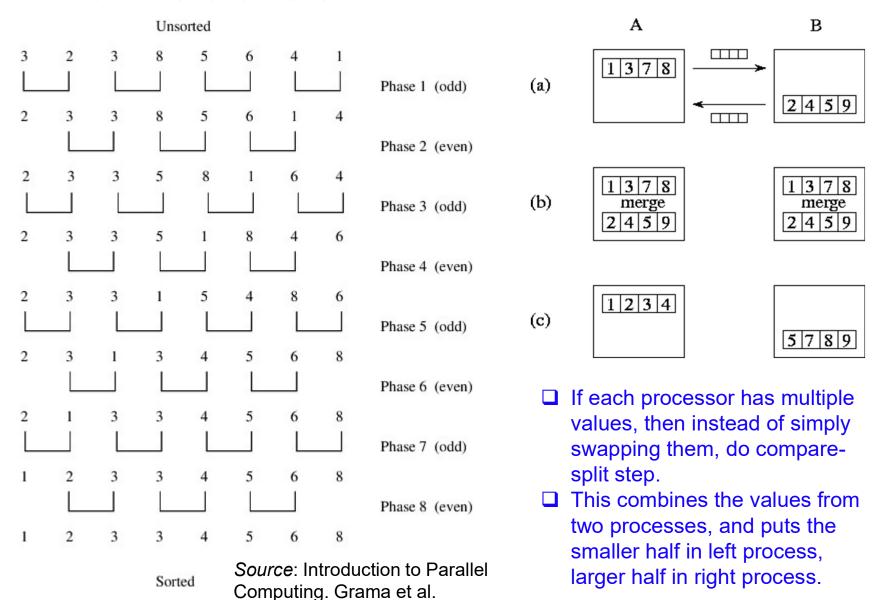
### r,e

#### Send and receive simultaneously

```
int a[10], b[10], npes, myrank;
MPI_Status status;
...
MPI_Comm_size(MPI_COMM_WORLD, &npes);
MPI_Comm_rank(MPI_COMM_WORLD, &myrank);
MPI_Sendrecv(a, 10, MPI_INT, (myrank+1)%npes, 1, b, 10, MPI_INT, (myrank-1)%npes, 1, MPI_COMM_WORLD, &status);
```

- MPI\_Sendrecv sends a message and starts a receive before blocking.
- Will block until send completes and receiving application buffer receives message.
  - No deadlock on ring.

#### Even-odd sort



#### Even-odd sort in MPI

```
#include <stdlib.h>
#include <mpi.h> /* Include MPI's header file */
main(int argc, char *argv[])
int n; /* The total number of elements to be sorted */
int npes; /* The total number of processes */
int myrank; /* The rank of the calling process */
int nlocal; /* The local number of elements, and the
            array that stores them */
int *elmnts; /* The array that stores the local
            elements */
int *relmnts; /* The array that stores the received
            elements */
int oddrank; /* The rank of the process during odd-
            phase communication */
int evenrank; /* The rank of the process during even-
            phase communication */
int *wspace; /* Working space during the compare-split
            operation */
int i;
MPI_Status status;
/* Initialize MPI and get system information */
MPI Init(&argc, &argv);
MPI Comm size(MPI COMM WORLD, &npes);
MPI Comm rank(MPI COMM WORLD, &myrank);
n = atoi(argv[1]);
nlocal = n/npes; /* Compute the number of elements to
            be stored locally. */
```

```
/* Allocate memory for the various arrays */
elmnts = (int *)malloc(nlocal*sizeof(int));
relmnts = (int *)malloc(nlocal*sizeof(int));
wspace = (int *)malloc(nlocal*sizeof(int));
/* Fill-in the elmnts array with random elements */
srandom(myrank);
for (i=0; i<nlocal; i++)</pre>
      elmnts[i] = random();
/* Sort the local elements using the built-in
auicksort routine */
gsort(elmnts, nlocal, sizeof(int), IncOrder);
/* Determine the rank of the processors that myrank
needs to communicate with during the */
/* odd and even phases of the algorithm */
if (myrank%2 == 1) {
      oddrank = mvrank-1:
      evenrank = mvrank+1:
else {
      oddrank = myrank+1;
      evenrank = myrank-1;
}
```

Source: Introduction to Parallel Computing. Grama et al.

#### Even-odd sort in MPI

```
/* Set first processor's communication ranks */
if (oddrank == -1 || oddrank == npes)
      oddrank = MPI PROC NULL;
if (evenrank == -1 || evenrank == npes)
      evenrank = MPI PROC NULL;
/* Main loop of the odd-even sorting algorithm */
for (i=0; i<npes-1; i++) {</pre>
      if (i%2 == 1) /* Odd phase */
            MPI Sendrecv(elmnts, nlocal, MPI INT,
            oddrank, 1, relmnts, nlocal, MPI INT,
            oddrank, 1, MPI_COMM_WORLD, &status);
      else /* Even phase */
            MPI Sendrecv(elmnts, nlocal, MPI INT,
            evenrank, 1, relmnts, nlocal, MPI INT,
            evenrank, 1, MPI COMM WORLD, &status);
      CompareSplit(nlocal, elmnts, relmnts, wspace,
            myrank < status.MPI SOURCE);</pre>
      }
free(elmnts); free(relmnts); free(wspace);
MPI Finalize();
```

```
CompareSplit(int nlocal, int *elmnts, int *relmnts,
int *wspace, int keepsmall) {
   int i, j, k;
   for (i=0; i<nlocal; i++)</pre>
      wspace[i] = elmnts[i];
/* Copy the elmnts array into the wspace array */
   if (keepsmall) { /* Keep nlocal smaller elts */
      for (i=j=k=0; k<nlocal; k++) {</pre>
         if (j == nlocal || (i < nlocal &&</pre>
            wspace[i] < relmnts[j]))</pre>
            elmnts[k] = wspace[i++];
         else
            elmnts[k] = relmnts[j++];
      }}
   else { /* Keep the nlocal larger elements */
      for (i=k=nlocal-1, j=nlocal-1; k>=0; k--) {
         if (j == 0 || (i >= 0 && wspace[i] >=
            relmnts[i]))
            elmnts[k] = wspace[i--];
         else
            elmnts[k] = relmnts[j--];
}}}
int IncOrder(const void *e1, const void *e2) {
   return (*((int *)e1) - *((int *)e2));
}
```

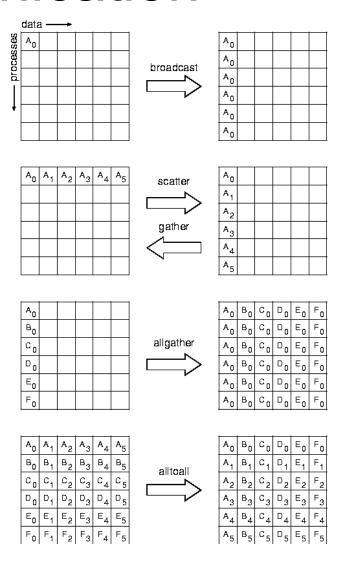


#### Collective communication

- Collective communication are routines that provide message passing between a group of processes.
  - □ One-to-many, e.g. broadcast, scatter
  - Many-to-one, e.g. gather, reduce
  - Many-to-many, e.g. All-to-all
- Collective communication may be implemented using point-to-point routines.
- Specialized implementation of collective communication is likely to be more efficient.
- Collectives are blocking in MPI 1 and 2, but MPI 3 includes nonblocking collectives.

#### Collective communication

- As with point to point communication, need to specify the communicator.
- o MPI\_Bcast()
- o MPI\_Reduce()
  - o MPI Allreduce()
- o MPI\_Scan()
- o MPI\_Gather()
- o MPI\_Scatter()
  - o MPI\_Scatterv()
- MPI\_Alltoall()
  - o MPI\_Alltoallv()
- o MPI\_Barrier()

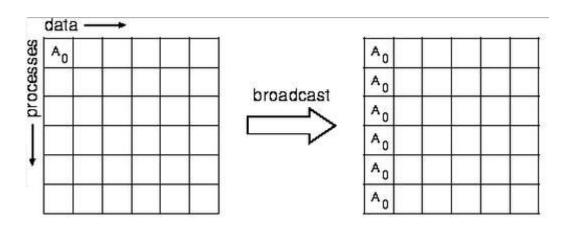


Source: http://www.mpi-forum.org/docs/mpi-1.1/mpi-11-html/coll-fig1.gif

#### **Broadcast**

int MPI\_Bcast(void \*buf, int count, MPI\_Datatype type, int
source, MPI\_Comm comm)

- Send the data in buf at the source process to all processes (including source) in comm.
  - □ Non-source nodes store the incoming data in their buf.
- Note that even though the message is coming from source, all processes, including the receiving ones, call MPI\_Bcast().
  - □ See the example on the next slide.





```
#include <mpi.h>
int main(int argc, char** argv) {
  int myrank;
  int buf;
  const int root=0;
  MPI Init(&argc, &argv);
  MPI Comm rank(MPI COMM WORLD, &myrank);
  if (myrank == root) {
    buf = 1; }
  /* All procs call bcast. buf is sent from
  root to all procs */
  MPI_Bcast(&buf, 1, MPI_INT, root,
    MPI COMM WORLD);
  MPI Finalize();
  return 0;
```

- ☐ This code causes process root to send buf (i.e. the value 1) to all the processes.
- ☐ Since MPI uses an SPMD model, all processes run the same code.
- ☐ So even the non-root processes do MPI\_Bcast(&buf, 1, MPI\_INT, root, MPI COMM WORLD)
- □ However, since their myrank != root, then instead of sending, the MPI\_Bcast() will cause them to receive.
- ☐ Think of MPI\_Bcast() as saying "participate in a broadcast", with the type of participation depending on the process's rank.
- ☐ The other collective operations work similarly, i.e. all procs run the same code, but do different things depending on their rank.

#### Reduce

int MPI\_Reduce(void \*sendbuf, void \*recvbuf, int count,
MPI\_Datatype type, MPI\_Op op, int target, MPI\_Comm comm)

- Combine the elements stored in the buffer sendbuf of each process in comm using the operation op, and store the combined values in recybuf of process target.
- Ex Add the values from all the processes.

MPI\_Reduce

- Operations include MPI\_MAX, MPI\_MIN, MPI\_SUM, MPI\_PROD, MPI\_LAND, MPI\_MAXLOC.
  - □ MPI\_MAXLOC p returns a pair of values (v,l) in recvbuf, where v is the max value, and l is the smallest ranked process with the value.

0 5 1 1 2 3 2 7 8 3 4 2

MPI\_SUM

Source: http://mpitutorial.com/tutorials/mpi-reduce-and-allreduce/



#### Allreduce

int MPI\_Allreduce(void \*sendbuf, void \*recvbuf, int count,
MPI\_Datatype type, MPI\_Op op, MPI\_Comm comm)

Same as reduce, but store the result at all the processes.

MPI\_Allreduce

0 5 1 1 2 3 2 7 8 3 4 2

MPI\_SUM

0 18 14 1 18 14 2 18 14 3 18 14

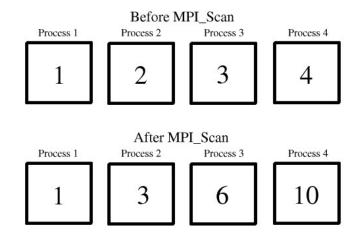
Source: http://mpitutorial.com/tutorials/mpi-reduce-and-allreduce/



#### Scan

int MPI\_Scan(void \*sendbuf, void \*recvbuf, int count,
MPI\_Datatype type, MPI\_Op op, MPI\_Comm comm)

- List the data in the sendbuf's of all the processes by process rank.
- Process i applies op (elementwise) to the first i sendbuf's and stores the result in its recybuf.
- Ex Add values from the processes.
- This operation is also called prefix sum.
  - □ Can apply other operators besides sum, as in reduce.



Source: http://www.rc.usf.edu/tutorials/classes/tutorial/mpi/images/scan\_ex.jpg

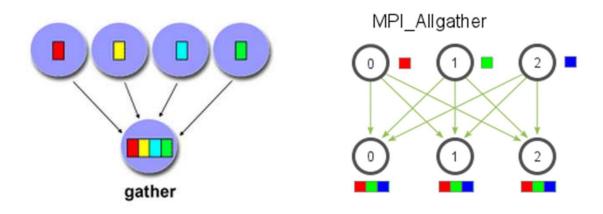
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#### Gather

int MPI\_Gather(void \*sendbuf, int sendcount, MPI\_Datatype sendtype, void
\*recvbuf, int recvcount, MPI\_Datatype recvtype, int target, MPI\_Comm comm)

int MPI\_Allgather(void \*sendbuf, int sendcount, MPI\_Datatype sendtype, void
\*recvbuf, int recvcount, MPI\_Datatype recvtype, MPI\_Comm comm)

- Gather collects the sendbuf's from all the processes in comm into the recybuf of process target.
  - □ If k processes in comm each with sendbuf of size t, then target will receive k\*t items.
  - Allgather collects this data at all the processes.

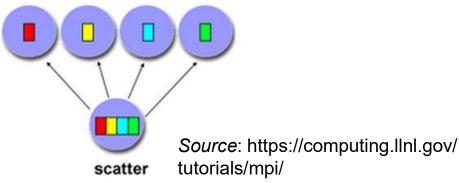


#### Scatter

int MPI\_Scatter(void \*sendbuf, int sendcount, MPI\_Datatype sendtype, void \*recvbuf,
int recvcount, MPI\_Datatype recvtype, int source, MPI\_Comm comm)

int MPI\_Scatterv(void \*sendbuf, int \*sendcounts, int \*displs, MPI\_Datatype sendtype, void \*recvbuf, int recvcount, MPI\_Datatype recvtype, int source, MPI\_Comm comm)

- Scatter sends the data at location i\*recvcount in sendbuf to the recvbuf of i'th process in comm.
  - All scattered data have the same size.
- Scattery sends data of different sizes to different processes.
  - ☐ Sizes of data specified in sendcounts.
  - □ Data to send to process i starts at location displs[i] in sendbuf.
  - ☐ For the receiving processes (i.e. all processes other than source), the first 4 arguments don't matter.
  - □ Each receiving process sets recvcount to the number of items it expects to get.



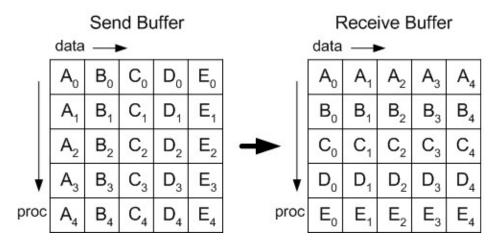


#### Alltoall

int MPI\_Alltoall(void \*sendbuf, int sendcount, MPI\_Datatype sendtype, void
\*recvbuf, int recvcount, MPI\_Datatype recvtype, MPI\_Comm comm)
int MDI\_Alltoally(void \*sendbuf int \*sendcounts int \*sedianle

int MPI\_Alltoallv(void \*sendbuf, int \*sendcounts, int \*sdispls,
MPI\_Datatype sendtype, void \*recvbuf, int \*recvcounts, int \*rdispls,
MPI\_Datatype recvtype, MPI\_Comm comm)

- Alltoall sends to process i sendcount elements from sendbuf starting from location i\*sendcount of sendbuf.
- Alltoally is similar, but allows sending different size data to each process.



Source: https://cvw.cac.cornell.edu/

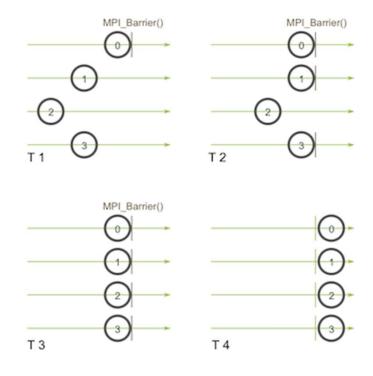
MPIcc/alltoall



#### Barrier

int MPI\_Barrier(MPI\_Comm comm)

- Used to synchronize all the processes in comm at a certain point in the code before any of them can proceed.
  - All processes in comm must reach the barrier. Otherwise, all processes will block forever.
- Can use multiple barriers.
  - □ All processes must reach the b'th barrier before proceeding to barrier b+1.

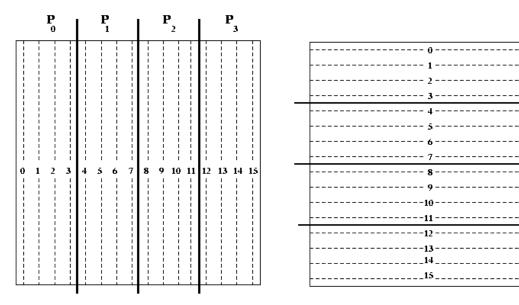


Source: http://mpitutorial.com/tutorials/mpibroadcast-and-collectivecommunication/barrier.png



### Storing a matrix

- Linear algebra one of the main applications for parallel computing.
- A large matrix can be stored in a distributed fashion on the parallel processors using row or column striping.
- Even with columnwise block stripping, we store columns in row-major format.



(a) Columnwise block stripping

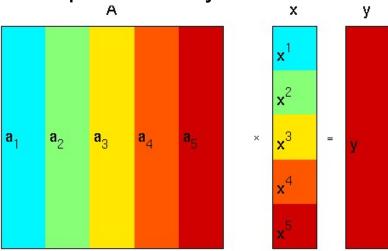
(b) Rowwise block stripping

Source: http://www.cse.iitd.ernet.in/~dheerajb/MPI/Document/onedblk.gif



#### Column-wise matrix vector mult

- Compute y = A\*x using p processes.
  - $\square$  A is an  $n \times n$  matrix, x and y are  $n \times 1$  vectors.
  - □ Each process holds n/p columns from A and n/p values from x.
- Each process does dot product on its columns with its portions of x.
  - □ Process ends up with n (partial) dot products.
- y[i] = sum of the p partial dot products for the i'th row held at the different processes.
  - □ Do a sum reduce for each row of y.
- Finally, distribute n/p values of y to each of the processes.



Source: https://www.informatik.uni-konstanz.de/fileadmin/informatik/ag-saupe/Webpages/lehre/na\_08/Lab1/1\_Preliminaries/html/matrixVectorProduct.html



#### Column-wise matrix vector mult

```
ColMatrixVectorMultiply(int n, double *a,
    double *x, double *y, MPI Comm comm)
{
    int i, j;
    int nlocal;
    double *py;
    double *fv;
    int npes, myrank;
    MPI Status status;
/* Get communicator information */
    MPI_Comm_size(comm, &npes);
    MPI Comm rank(comm, &myrank);
    nlocal = n/npes;
                                             vector x */
/* Allocate memory for arrays storing
intermediate results. */
    py = (double *)
         malloc(n*sizeof(double));
    fy = (double *)
                                             }
         malloc(n*sizeof(double));
```

```
/* Compute partial-dot products that
correspond to local columns of A*/
     for (i=0; i<n; i++) {
         py[i] = 0.0;
         for (j=0; j<nlocal; j++)</pre>
              py[i] += a[i*nlocal+j]*x[j];
/* Sum-up results by performing an
element-wise reduction operation */
    MPI_Reduce(py, fy, n, MPI_DOUBLE,
         MPI SUM, 0, comm);
/* Redistribute fy in a fashion similar to
    MPI Scatter(fy, nlocal, MPI DOUBLE,
         y, nlocal, MPI DOUBLE, 0, comm);
    free(py); free(fy);
Source: Introduction to Parallel
Computing. Grama et al.
```

### re.

#### Derived data types

- MPI comes with a number of standard built in types.
- To send more complicated data structures, programmer defines derived types.
- Four main types, contiguous, vector, indexed and struct.
- MPI\_Type\_commit(&datatype) commits defined datatype.
- MPI\_Type\_extent(&datatype) returns size in bytes of the datatype.
- MPI\_Type\_free(&datatype) Deallocates a datatype, prevent memory exhaustion.

### ra.

### Defining new datatypes

- MPI\_Type\_contiguous(count, oldtype, &newtype)
  - □ Place count copies of oldtype contiguously.
- MPI\_Type\_vector(count, blocklength, stride, oldtype, &newtype)
  - □ Similar to contiguous, use count copies of oldtype each of blocklength, with stride bytes in between.
- MPI\_Type\_indexed (count, blocklens[], offsets[], old\_type, &newtype)
  - Similar to vector, except blocklens and offsets vectors (of size count) specify size and offset of each element in the datatype.
- MPI\_Type\_struct (count,blocklens[], offsets[], old\_types, &newtype)
  - Form a datatype according to a completely defined map of the component data types.

```
1
       #include "mpi.h"
 2
       #include <stdio.h>
                                                                                           MPI Type vector
 3
       #define SIZE 4
 4
                                                                                           count = 4; blocklength = 1; stride = 4;
 5
      main(int argc, char *argv[]) {
                                                                                      MPI Type vector(count, blocklength, stride, MPI FLOAT,
 6
       int numtasks, rank, source=0, dest, tag=1, i;
                                                                                                 &columntype);
 7
       float a[SIZE][SIZE] =
 8
         {1.0, 2.0, 3.0, 4.0,
                                                                                             1.0
                                                                                                  20
                                                                                                       3.0
                                                                                                             4.0
 9
          5.0, 6.0, 7.0, 8.0,
10
          9.0, 10.0, 11.0, 12.0,
                                                                                             5.0
                                                                                                  6.0
                                                                                                            8.0
11
         13.0, 14.0, 15.0, 16.0};
                                                                                                                    a[4][4]
12
       float b[SIZE];
13
                                                                                             9.0
                                                                                                  10.0
                                                                                                      11.0
                                                                                                            12.0
14
      MPI Status stat:
15
      MPI Datatype columntype; // required variable
                                                                                            13.0
                                                                                                  14.0
                                                                                                       15.0
                                                                                                            16.0
16
17
18
      MPI Init(&argc, &argv);
19
      MPI Comm rank (MPI COMM WORLD, &rank);
                                                                                       MPI Send(&a[0][1], 1, columntype, dest, tag, comm);
20
      MPI Comm size (MPI COMM WORLD, &numtasks);
21
                                                                                                           14.0
                                                                                             2.0
                                                                                                      10.0
                                                                                                                    1 element of
22
       // create vector derived data type
                                                                                                                    columntype
23
      MPI Type vector (SIZE, 1, SIZE, MPI FLOAT, &columntype);
24
      MPI Type commit(&columntype);
25
26
       if (numtasks == SIZE) {
27
          // task 0 sends one element of columntype to all tasks
                                                                                   rank= 0 b= 1.0 5.0 9.0 13.0
28
          if (rank == 0) {
                                                                                   rank= 1 b= 2.0 6.0 10.0 14.0
29
             for (i=0; i<numtasks; i++)
                                                                                   rank= 2 b= 3.0 7.0 11.0 15.0
30
                MPI Send(&a[0][i], 1, columntype, i, tag, MPI COMM WORLD);
31
             }
                                                                                   rank= 3 b= 4.0 8.0 12.0 16.0
32
33
          // all tasks receive columntype data from task 0
          MPI Recv(b, SIZE, MPI FLOAT, source, tag, MPI COMM WORLD, &stat);
34
          printf("rank= %d b= \frac{1}{3}.1f %3.1f %3.1f %3.1f\n",
35
36
                 rank,b[0],b[1],b[2],b[3]);
37
          }
38
       else
39
          printf("Must specify %d processors. Terminating.\n",SIZE);
40
41
       // free datatype when done using it
42
      MPI Type free (&columntype);
      MPI Finalize();
43
44
       }
                                                                  Source: https://computing.llnl.gov/tutorials/mpi
```

```
#include "mpi.h"
      #include <stdio.h>
 3
      #define NELEM 25
 4
 5
      main(int argc, char *argv[]) {
      int numtasks, rank, source=0, dest, tag=1, i;
 7
 8
      typedef struct {
 9
        float x, y, z;
10
        float velocity;
11
        int n, type;
12
                   Particle;
       }
                   p[NELEM], particles[NELEM];
13
      Particle
      MPI Datatype particletype, oldtypes[2]; // required variables
14
15
                   blockcounts[2];
16
17
      // MPI Aint type used to be consistent with syntax of
18
      // MPI Type extent routine
19
      MPI Aint offsets[2], extent;
20
21
      MPI Status stat;
22
23
      MPI Init(&argc, &argv);
24
      MPI Comm rank (MPI COMM WORLD, &rank);
25
      MPI Comm size(MPI_COMM_WORLD, &numtasks);
26
27
      // setup description of the 4 MPI FLOAT fields x, y, z, velocity
      offsets[0] = 0;
28
29
      oldtypes[0] = MPI FLOAT;
30
      blockcounts[0] = \overline{4};
31
32
      // setup description of the 2 MPI INT fields n, type
33
      // need to first figure offset by getting size of MPI FLOAT
34
      MPI Type extent(MPI FLOAT, &extent);
      offsets[1] = 4 * extent;
35
      oldtypes[1] = MPI_INT;
36
37
      blockcounts[1] = \overline{2};
38
39
      // define structured type and commit it
40
      MPI Type struct(2, blockcounts, offsets, oldtypes, &particletype);
41
      MPI Type commit(&particletype);
42
43
      // task 0 initializes the particle array and then sends it to each task
44
      if (rank == 0) {
45
        for (i=0; i<NELEM; i++) {
46
           particles[i].x = i * 1.0;
47
           particles[i].y = i * -1.0;
48
           particles[i].z = i * 1.0;
49
           particles[i].velocity = 0.25;
50
           particles[i].n = i;
51
           particles[i].type = i % 2;
52
53
        for (i=0; i<numtasks; i++)
54
           MPI Send (particles, NELEM, particletype, i, tag, MPI COMM WORLD);
55
56
57
      // all tasks receive particletype data
58
      MPI Recv(p, NELEM, particletype, source, tag, MPI COMM WORLD, &stat);
59
60
      printf("rank= %d %3.2f %3.2f %3.2f %d %d\n", rank,p[3].x,
61
           p[3].y,p[3].z,p[3].velocity,p[3].n,p[3].type);
62
63
      // free datatype when done using it
64
      MPI Type free (&particletype);
65
      MPI Finalize();
66
      }
```

#### MPI\_ Type\_struct

typedef struct { float x, y, z, velocity; int n, type; } Particle;
Particle particles[NELEM];

MPI\_Type\_extent(MPI\_FLOAT, &extent);

count = 2; oldtypes[0] = MPI\_FLOAT; oldtypes[1] = MPI\_INT offsets[0] = 0; offsets[1] = 4 \* extent; blockcounts[1] = 2;

particles[NELEM]

MPI\_Type\_struct(count, blockcounts, offsets, oldtypes, &particletype);
MPI Send(particles, NELEM, particletype, dest, tag, comm);

Sends entire (NELEM) array of particles, each particle being comprised four floats and two integers.

```
rank= 0 3.00 -3.00 3.00 0.25 3 1
rank= 2 3.00 -3.00 3.00 0.25 3 1
rank= 1 3.00 -3.00 3.00 0.25 3 1
rank= 3 3.00 -3.00 3.00 0.25 3 1
```

#### 1 #include "mpi.h" 2 #include <stdio.h> 3 #define NPROCS 8 4 5 main(int argc, char \*argv[]) { rank, new rank, sendbuf, recvbuf, numtasks, 6 7 ranks1[4]= $\{0,1,2,3\}$ , ranks2[4]= $\{4,5,6,7\}$ ; 8 orig group, new group; // required variables MPI Group new comm; // required variable 9 MPI Comm 10 11 MPI Init(&argc, &argv); MPI Comm rank (MPI COMM WORLD, &rank); 12 MPI Comm size (MPI COMM WORLD, &numtasks); 13 14 15 if (numtasks != NPROCS) { printf("Must specify MP PROCS= %d. Terminating.\n", NPROCS); 16 17 MPI Finalize(); exit(0); 18 19 20 21 sendbuf = rank; 22 23 // extract the original group handle MPI Comm group (MPI COMM WORLD, &orig group); 24 25 26 // divide tasks into two distinct groups based upon rank 27 if (rank < NPROCS/2) { MPI Group incl(orig group, NPROCS/2, ranks1, &new group); 28 29 30 else { MPI Group incl (orig group, NPROCS/2, ranks2, &new group); 31 32 33 34 // create new new communicator and then perform collective communicat 35 MPI Comm create (MPI COMM WORLD, new group, &new comm); MPI Allreduce (&sendbuf, &recvbuf, 1, MPI INT, MPI SUM, new comm); 36 37 38 // get rank in new group MPI Group rank (new group, &new rank); 39 printf("rank= %d newrank= %d recvbuf= %d\n",rank,new rank,recvbuf); 40 41 42 MPI Finalize(); 43

#### More on communicators

- Communicators are a programming aid to group processes that perform a common task.
- Collective computations are done within a communicator.
  - MPI 2 allows collectives between communicators.
- Processes have a unique rank in each communicator they belong to.

```
rank= 7 newrank= 3 recvbuf= 22
rank= 0 newrank= 0 recvbuf= 6
rank= 1 newrank= 1 recvbuf= 6
rank= 2 newrank= 2 recvbuf= 6
rank= 6 newrank= 2 recvbuf= 22
rank= 3 newrank= 3 recvbuf= 6
rank= 4 newrank= 0 recvbuf= 22
rank= 5 newrank= 1 recvbuf= 22
```

### Virtual topologies

- Map a communicator of processes to a virtual topology.
- Virtual topology may not correspond to the physical topology of underlying hardware.
- Nevertheless, allows MPI implementation to try to optimize mapping of virtual to physical topology, e.g. mapping a virtual mesh to a physical hypercube.
- Also a programming convenience, to match topology of application communications to virtual topology.
  - □ A 3D physics code can use a virtual 3D mesh topology.
- Main topologies are regular torus and graph.
  - MPI\_Cart\_create(MPI\_Comm oldcomm, int ndim, int dims[], int qperiodic[], int qreorder, MPI\_Comm \*newcomm)
  - MPI\_Dist\_graph\_create\_adjacent(MPI\_Comm oldcomm, int indegree, int sources[], int sourceweights[], int outdegree, int dests[], int destweights[], MPI\_Info info, int greorder, MPI\_Comm \*newcomm)

```
#include <stdio.h>
#define SIZE 16
#define UP
#define DOWN 1
#define LEFT 2
#define RIGHT 3
main(int argc, char *argv[]) {
int numtasks, rank, source, dest, outbuf, i, tag=1,
   inbuf[4]={MPI PROC NULL,MPI PROC NULL,MPI PROC_NULL,MPI_PROC_NULL,},
  nbrs[4], dims[2] = \{4,4\},
  periods[2]={0,0}, reorder=0, coords[2];
MPI Request regs[8];
MPI Status stats[8];
MPI Comm cartcomm; // required variable
MPI Init (&argc, &argv);
MPI Comm size (MPI COMM WORLD, &numtasks);
if (numtasks == SIZE) {
  // create cartesian virtual topology, get rank, coordinates, neighbor ranks
  MPI Cart create (MPI COMM WORLD, 2, dims, periods, reorder, &cartcomm);
  MPI Comm rank (cartcomm, &rank);
  MPI Cart coords (cartcomm, rank, 2, coords);
  MPI Cart shift(cartcomm, 0, 1, &nbrs[UP], &nbrs[DOWN]);
  MPI Cart shift(cartcomm, 1, 1, &nbrs[LEFT], &nbrs[RIGHT]);
  printf("rank= %d coords= %d %d neighbors(u,d,l,r)= %d %d %d %d\n'
          rank, coords[0], coords[1], nbrs[UP], nbrs[DOWN], nbrs[LEFT],
          nbrs[RIGHT]):
   outbuf = rank;
  // exchange data (rank) with 4 neighbors
   for (i=0; i<4; i++) {
      dest = nbrs[i];
      source = nbrs[i];
      MPI Isend (&outbuf, 1, MPI INT, dest, tag,
                MPI COMM WORLD, &reqs[i]);
      MPI Irecv(&inbuf[i], 1, MPI INT, source, tag,
                MPI COMM WORLD, &reqs[i+4]);
      }
  MPI Waitall(8, reqs, stats);
  printf("rank= %d
                                     inbuf(u,d,1,r) = %d %d %d %d\n",
          rank,inbuf[UP],inbuf[DOWN],inbuf[LEFT],inbuf[RIGHT]); }
else
  printf("Must specify %d processors. Terminating.\n",SIZE);
MPI Finalize();
}
```

1

2

3

4

5

6

7

8

10

11

12

13

14 15

16

17

18

19

20

21 22

23

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26

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31

32

33

34

35

36

37

38

39

40

41

42

43

44

45

46

47 48

49 50

51

52 53

54

#include "mpi.h"

```
0
(0,0)
          (0,1)
                     (0,2)
                               (0,3)
 4
            5
                       6
(1,0)
          (1,1)
                    (1,2)
                               (1,3)
 8
                     10
            9
                               11
(2,0)
          (2,1)
                    (2,2)
                               (2,3)
                               15
 12
           13
                     14
(3,0)
          (3,1)
                               (3,3)
                    (3,2)
```

```
rank=
       0 coords= 0 0 neighbors(u,d,l,r)= -1 4 -1 1
                          inbuf(u,d,l,r) = -1 \ 4 \ -1 \ 1
rank=
rank=
       8 coords= 2 0 neighbors(u,d,l,r)= 4 12 -1 9
rank=
                          inbuf(u,d,l,r)=
                                         4 12 -1 9
rank=
       1 coords= 0 1 neighbors(u,d,l,r)= -1 5 0
                          inbuf(u,d,l,r) = -1 5 0 2
rank=
       1
rank=
      13 coords= 3 1 neighbors(u,d,l,r)= 9 -1 12 14
rank= 13
                          inbuf(u,d,l,r) = 9 -1 12 14
. . .
. . .
rank=
       3 coords= 0 3 neighbors(u,d,l,r)= -1 7 2 -1
                          inbuf(u,d,l,r) = -1 7 2 -1
rank=
      11 coords= 2 3 neighbors(u,d,l,r)=
                                         7 15 10 -1
rank=
rank=
      11
                          inbuf(u,d,l,r) = 7 15 10 -1
rank=
      10 coords= 2 2 neighbors(u,d,l,r)=
                                          6 14 9 11
rank= 10
                          inbuf(u,d,l,r)=
                                          6 14 9 11
rank=
       9 coords= 2 1 neighbors(u,d,l,r)=
                                          5 13 8 10
rank=
                          inbuf(u,d,l,r)=
                                           5 13 8 10
```

#### MPI 2, 3 and 4

- MPI 2 added
  - Dynamic process creation.
  - □ Improved collectives.
  - □ Thread-safe.
  - □ Parallel I/O.
  - One sided communication.
    - Access memory on a remote process without it "expecting it".
- MPI 3 added
  - □ Nonblocking collectives.
  - □ Better support for multi-threading.
  - □ Improved shared memory parallelism.
  - □ User-defined collectives.
  - Large counts for large datasets.
- MPI 4 added
  - More fault tolerance.
  - □ Hybrid programming (MPI + OpenMP / CUDA)