

Deep Learning

1 Artificial Neuron

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The Neuron

- About 100 billion neurons in human brain

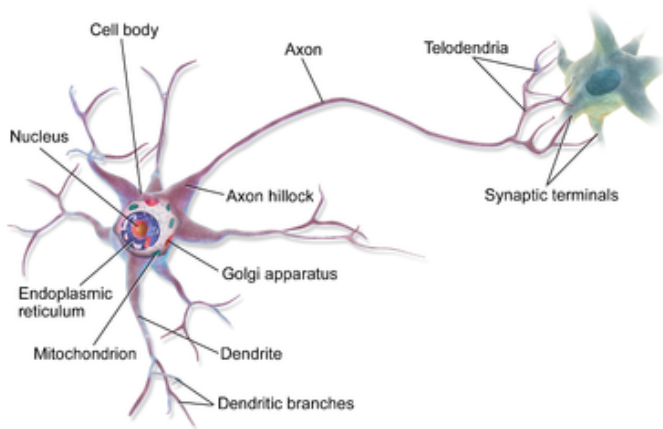
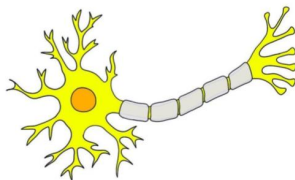


Figure credits: Wikipedia

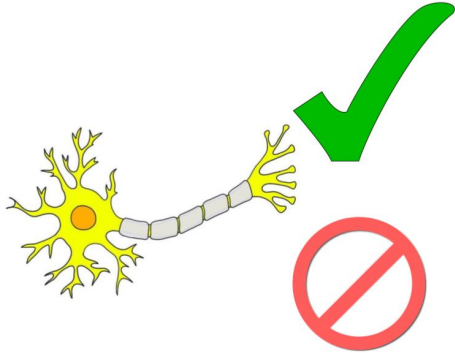
Neuron in action



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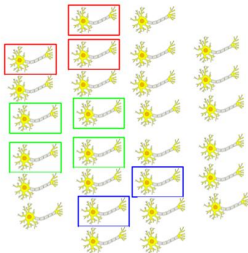


Neuron in action



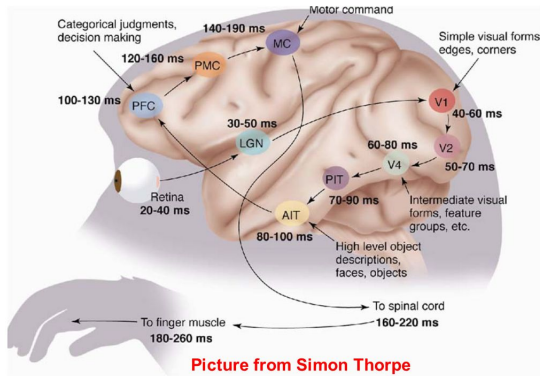
Neuron in action

Favorite genre



Favorite actors

Neurons in the brain have a hierarchy



Threshold Logic Unit

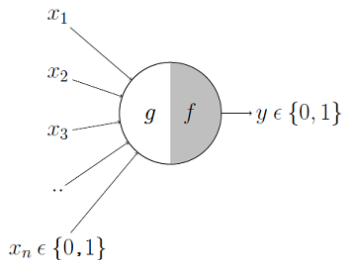
① First Mathematical Model for a neuron

Threshold Logic Unit

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- ② McCulloch and Pitts, 1943 \rightarrow MP neuron

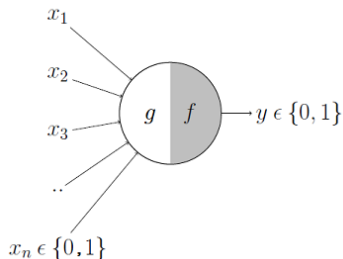
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④

$$f(x) = \mathbb{1}(\sum_i x_i \geq \theta)$$

Threshold Logic Unit

- ① Inputs can be of excitatory or inhibitory nature

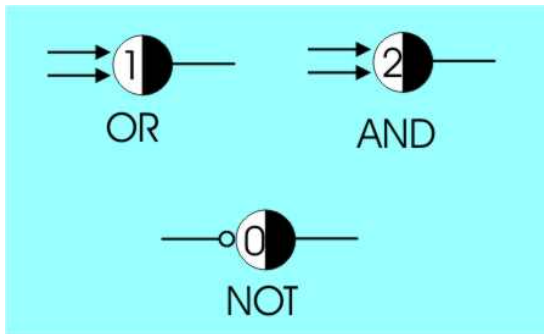
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- ② When an inhibitory input is set ($=1$) output $\rightarrow 0$
- ③ Counts the number of 'ON' signals on the excitatory inputs versus the inhibitory

Threshold Logic Unit



Example Boolean functions

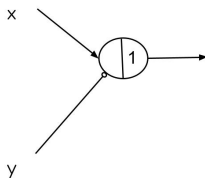
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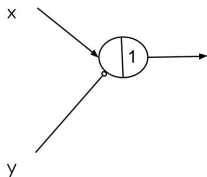
② xy'



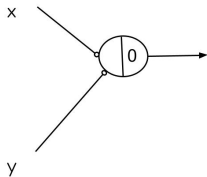
Threshold Logic Unit

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③ NOR



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Threshold Logic Unit

- ① What one unit does? - Learn linear separation
 - line in 2D, plane in 3D, hyperplane in higher dimensions
- ② No learning; heuristic approach

Perceptron

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⑤

$$f(x) = \begin{cases} 1 & \text{when } \sum_i w_i x_i + b \geq 0 \\ 0 & \text{else} \end{cases}$$

Perceptron

① For simplicity we consider +1 and -1 responses

$$\sigma(x) = \begin{cases} 1 & \text{when } x \geq 0 \\ -1 & \text{else} \end{cases}$$



$$f(\mathbf{x}) = \sigma(\mathbf{w}^T \cdot \mathbf{x} + \mathbf{b})$$

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- ③ \mathbf{w} are referred to as weights and b as the bias

Perceptron vs. MP neuron

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- ② Inputs can be real
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- ④ Mechanism for learning weights

Weights and Bias

① Why are the weights important?

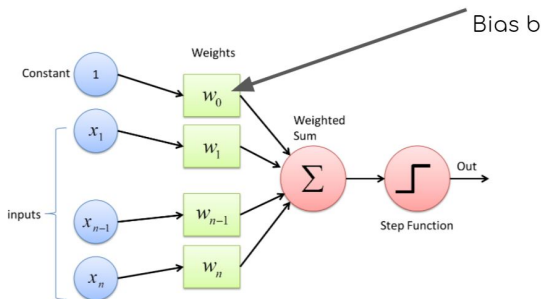


Figure credits: DeepAI

Weights and Bias

- ① Why are the weights important?
- ② Why is it called 'bias'? What does it capture?

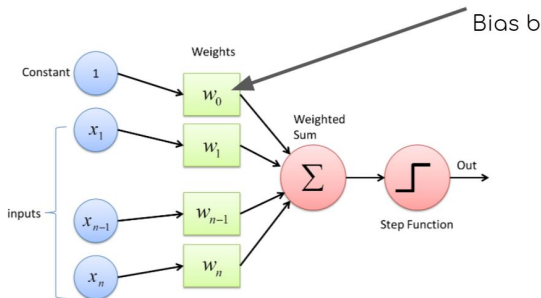


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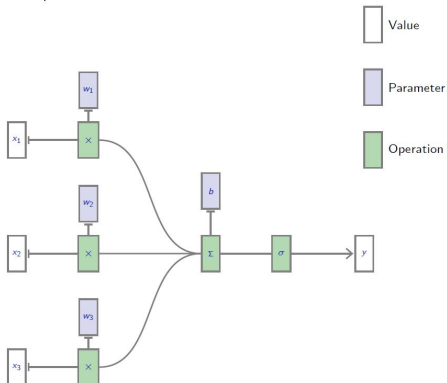


Figure credits: François Fleuret

Perceptron

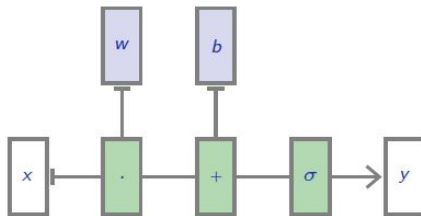


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- ④ Note that the bias b is absorbed as a component of \mathbf{w} and \mathbf{x} is appended with 1 suitably

Perceptron Learning Algorithm

► Colab Notebook: Perceptron

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- ② Stops as soon as it finds a separating boundary
- ③ Other algorithms maximize the margin from boundary to the samples