

# Modern C++ Programming

## 12. TEMPLATES AND META-PROGRAMMING II

CLASS TEMPLATES , SFINAE, AND CONCEPTS

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# Class Template

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## Class Template

Similarly to function templates, **class templates** are used to build a family of classes

```
template<typename T>
struct A { // class template (typename template)
    T x = 0;
};

template<int N1>
struct B { // class template (numeric template)
    int N = N1;
};

A<int>    a1; // a1.x is int    x = 0
A<float>   a2; // a2.x is float x = 0.0f
B<1>       b1; // b1.N is 1
B<2>       b2; // b2.N is 2
```

The *main difference* with template functions is that classes can be partially specialized

*Note:* Every class specialization (both partial and full) is a completely new class, and it does not share anything with the generic class

```
template<typename T, typename R>
struct A {};
```

*// generic class template*

```
template<typename T>
struct A<T, int> {};
```

*// partial specialization*

```
template<>
struct A<float, int> {};
```

*// full specialization*

# Class Template Specialization

2/2

```
template<typename T, typename R>
struct A {           // GENERIC class template
    T x;
};

template<typename T>
struct A<T, int> { // PARTIAL specialization
    T y;
};

A<float, float> a1;
a1.x;    // ok, generic template
// a1.y; // compile error

A<float, int> a2;
a2.y;    // ok, partial specialization
// a2.x; // compile error
```

## Example 1: Implement a Simple Type Trait

```
template<typename T, typename R> // GENERIC template declaration
struct is_same {
    static constexpr bool value = false;
};

template<typename T>
struct is_same<T, T> {           // PARTIAL template specialization
    static constexpr bool value = true;
};

cout << is_same< int, char>::value; // print false, generic template
cout << is_same<float, float>::value; // print true, partial template
```

## Example 2: Check if a Pointer is const

```
#include <type_traits>

// std::true_type and std::false_type contain a field "value"
// set to true or false respectively

template<typename T>
struct is_pointer_to_const : std::false_type {}; // GENERIC template declaration

template<typename R> // PARTIAL specialization
struct is_pointer_to_const<const R*> : std::true_type {};

cout << is_pointer_to_const<int*>::value; // print false, generic template
cout << is_pointer_to_const<const int*>::value; // print true, partial template
cout << is_pointer_to_const<int* const>::value; // print false, generic template
```

## Example 3: Compare Class Templates

```
#include <type_traits>

template<typename T>
struct A {};

template<typename T, typename R>
struct Compare : std::false_type {};           // GENERIC template declaration

template<typename T, typename R>
struct Compare<A<T>, A<R>> : std::true_type {}; // PARTIAL specialization

cout << Compare<int, float>::value;           // false, generic template
cout << Compare<A<int>, A<int>>::value;      // true, partial template
cout << Compare<A<int>, A<float>>::value;     // true, partial template
```

## Class Template Constructor

Class template arguments don't need to be repeated if they are the default ones

```
template<typename T>
struct A {
    A(const A& x); // A(const A<T>& x);

    A f();          // A<T> f();
};
```

# Constructor Template Automatic Deduction (CTAD)

---

# Constructor Template Automatic Deduction (CTAD)

C++17 introduces *automatic* deduction of class template arguments in constructor calls

```
template<typename T, typename R>
struct A {
    A(T x, R y) {}
};

A<int, float> a1(3, 4.0f); // < C++17
A           a2(3, 4.0f); // C++17

// A<int> a{3, 5}; compile error, "partial" specialization
```

# CTAD - User-Defined Deduction Guides

**Template deduction guide** is a mechanism to instruct the compiler how to map constructor parameter types into class template parameters

```
template<typename T>
struct MyString {
    MyString(T) {}
};

// constructor           class instantiation
MyString(char const*) -> MyString<std::string>; // deduction guide

MyString s{"abc"}; // construct 'MyString<std::string>'
```

## CTAD - User-Defined Deduction Guides - Aggregate Example

```
template<typename T>
struct A {
    T x, y;
};

template<typename T>
A(T, T) -> A<T>; // deduction guide
                    // not required in C++20+ for aggregates

A a{1, 3};          // construct 'A<int, int>'
```

## CTAD - User-Defined Deduction Guides - Independent Argument Example

```
template<int I>
struct A {
    template<typename T>
    A(T) {}
};

template<typename T>
A(T) -> A<sizeof(T)>; // deduction guide

A a{1}; // construct 'A<4>', 4 == sizeof(int)
```

## CTAD - User-Defined Deduction Guides - Universal Reference Example

```
#include <type_traits> // std::remove_reference_t

template<typename T>
struct A {
    template<typename R>
    A(R&&) {}
};

template<typename R>
A(R&&) -> A<std::remove_reference_t<R>>; // deduction guide

int x;
A a{x}; // construct 'A<int>' instead of 'A<int&>'
```

## CTAD - User-Defined Deduction Guides - Iterator Example

```
#include <type_traits> // std::remove_reference_t
#include <vector>      // std::vector

template<typename T>
struct Container {
    template<typename Iter>
    Container(Iter beg, Iter end) {}
};

template<typename Iter>
Container(Iter b, Iter e) ->          // deduction guide
    Container<typename std::iterator_traits<Iter>::value_type>;

std::vector v{1, 2, 3};
Container c{v.begin(), v.end()}; // construct 'Container<int>'
```

## CTAD - User-Defined Deduction Guides - Alias Template

*Alias template deduction requires C++20*

```
template<typename T>
struct A {
    A(T) {}
};

template<typename T>
A(T) -> A<int>;           // deduction guide

template<typename T>
using B = A<T>;           // alias template

B c{3.0};                  // alias template deduction
                           // construct 'A<int>'
```

## CTAD User-Defined Deduction Guides - Limitation

*Template deduction guide* doesn't work within the class scope

```
template<typename T>
struct MyString {
    MyString(T) {}
    auto f() { return MyString("abc"); }           // create 'MyString<const char*>'
};                                              // NOT 'MyString<std::string>'

MyString(const char*) -> MyString<std::string>; // deduction guide

MyString<const char*> s{"abc"}; // construct 'MyString<const char*>'
```

The problem can be avoided by using fully-qualifying the class type

```
auto f() { return ::MyString("abc"); }
```

# Class Template - Advanced Concepts

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Given a class template and a template member function

```
template<typename T, typename R>
struct A {
    template<typename X, typename Y>
    void f();
};
```

There are two ways to specialize the class/function:

- **Generic class + generic function**
- **Full class specialization + generic/full specialization function**

```
template<typename T, typename R>
template<typename X, typename Y>
void A<T, R>::f() {}
// ok, A<T, R> and f<X, Y> are not specialized
```

```
template<>
template<typename X, typename Y>
void A<int, int>::f() {}
// ok, A<int, int> is full specialized
// ok, f<X, Y> is not specialized
```

```
template<>
template<>
void A<int, int>::f<int, int>() {}
// ok, A<int, int> and f<int, int> are full specialized
```

```
template<typename T>
template<typename X, typename Y>
void A<T, int>::f() {}

// error A<T, int> is partially specialized
//      (A<T, int> class must be defined before)

template<typename T, typename R>
template<typename X>
void A<T, R>::f<int, X>() {}

// error function members cannot be partially specialized

template<typename T, typename R>
template<>
void A<T, R>::f<int, int>() {}

// error function members of a non-specialized class cannot be specialized
//      (requires a binding to a specific template instantiation at compile-time)
```

*Structure templates* can have different data members for each specialization.

The compiler needs to know in advance if a symbol within a structure is a type or a static member when the structure template *depends on* another template parameter

The keyword `typename` placed before a *structure template* solves this ambiguous

```
template<typename T>
struct A {
    using type = int;
};

template<typename R>
void g() {
    using X = typename A<R>::type; // "type" is a typename or
}                                // a data member depending on R
```

The `using` keyword can be used to simplify the expression to get the structure type

```
template<typename T>
struct A {
    using type = int;
};

template<typename T>
using ATYPE = typename A<T>::type;

template<typename R>
void g() {
    using X = ATYPE<R>;
}
```

## Template Dependent Names - template Keyword

The `template` keyword tells the compiler that what follows is a *template name (function or class)*

*note:* recent compilers don't strictly require this keyword in simple cases

```
template<typename T>
struct A {
    template<typename R>
    void g() {}
};

template<typename T> // A<T> is a dependent name (from T)
void f(A<T> a) {
// a.g<int>(); // compile error A<T> is dependent on T
// interpreted as: "a.g < int > () ;"
// namely:           "(a.g < int) > () ;"
    a.template g<int>(); // ok
}
```

## Class Template Hierarchy and using

Member of class templates can be used *internally* in derived class templates by specifying the particular type of the base class with the keyword **using**

```
template<typename T>
struct A {
    T      x;
    void f() {}
};

template<typename T>
struct B : A<T> {
    using A<T>::x;   // needed (otherwise it could be another specialization)
    using A<T>::f;   // needed

    void g() {
        x;    // without 'using': this->x
        f();
    }
};
```

# virtual Function and Template

## Virtual functions cannot have template arguments

- **Templates** are a compile-time feature
- **Virtual functions** are a run-time feature

Full story:

*The reason for the language disallowing the particular construct is that there are potentially infinite different types that could be instantiating your template member function, and that in turn means that the compiler would have to generate code to dynamically dispatch those many types, which is infeasible*

[stackoverflow.com/a/79682130](http://stackoverflow.com/a/79682130)

## friend Keyword

```
template<typename T> struct A {};
template<typename T, typename R> struct B {};
template<typename T> void f() {}

//-----
class C {
    friend void f<int>(); // match only f<int>

    template<typename T> friend void f(); // match all templates

    friend struct A<int>; // match only A<int>

    template<typename> friend struct A; // match all A templates

// template<typename T> friend struct B<int, T>;
//     partial specialization cannot be declared as a friend
};
```

## Template Template Arguments

**Template template parameters** match *templates* instead of concrete types

```
template<typename T> struct A {};  
  
template< template<typename> class R >  
struct B {  
    R<int>    x;  
    R<float>  y;  
};  
template< template<typename> class R, typename S >  
void f(R<S> x) {} // works with every class with exactly one template parameter  
  
B<A> y;  
f( A<int>() );
```

class and typename keyword are interchangeably in C++17

# Template Meta-Programming

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## Template Meta-Programming

*“Metaprogramming is the writing of computer programs with the ability to **treat programs as their data**. It means that a program could be designed to read, generate, analyze or transform other programs, and even modify itself while running”*

*“Template meta-programming refers to uses of the C++ template system to **perform computation at compile-time** within the code. Templates meta-programming include compile-time constants, data structures, and complete functions”*

# Template Meta-Programming

- **Template Meta-Programming is fast** (runtime)

Template Metaprogramming is computed at compile-time (nothing is computed at run-time)

- **Template Meta-Programming is Turing Complete**

Template Metaprogramming is capable of expressing all tasks that standard programming language can accomplish

- **Template Meta-Programming requires longer compile time**

Template recursion heavily slows down the compile time, and requires much more memory than compiling standard code

- **Template Meta-Programming is complex**

Everything is expressed recursively. Hard to read, hard to write, and also very hard to debug

## Example 1: Factorial

```
template<int N>
struct Factorial {      // GENERIC template: Recursive step
    static constexpr int value = N * Factorial<N - 1>::value;
};

template<>
struct Factorial<0> {  // FULL SPECIALIZATION: Base case
    static constexpr int value = 1;
};

constexpr int x = Factorial<5>::value; // 120
// int y = Factorial<-1>::value;      // Infinite recursion :)
```

## Example 1: Factorial (Notes)

The previous example can be easily written as a `constexpr` in C++14

```
template<typename T>
constexpr int factorial(T value) {
    T tmp = 1;
    for (int i = 2; i <= value; i++)
        tmp *= i;
    return tmp;
};
```

### Advantages:

- Easy to read and write (easy to debug)
- Faster compile time (no recursion)
- Works with different types (typename T)
- Works at run-time *and* compile-time

## Example 2: Log2

```
template<int N>
struct Log2 {    // GENERIC template: Recursive step
    static_assert(N > 0, "N must be greater than zero");

    static constexpr int value = 1 + Log2<N / 2>::value;
};

template<>
struct Log2<1> { // FULL SPECIALIZATION: Base case
    static constexpr int value = 0;
};

constexpr int x = Log2<20>::value; // 4
```

## Example 3: Log

```
template<int A, int B>
struct Max { // utility
    static constexpr int value = A > B ? A : B;
};

template<int N, int BASE>
struct Log {      // GENERIC template: Recursive step
    static_assert(N > 0, "N must be greater than zero");
    static_assert(BASE > 0, "BASE must be greater than zero");
                           // Max is used to avoid Log<0, BASE>
    static constexpr int TMP = Max<1, N / BASE>::value;
    static constexpr int value = 1 + Log<TMP, BASE>::value;
};
template<int BASE>
struct Log<1, BASE> { // PARTIAL SPECIALIZATION: Base case
    static constexpr int value = 0;
};
```

## Example 4: Unroll (Compile-time/Run-time Mix) ★

```
template<int NUM_UNROLL, int STEP = 0>
struct Unroll {           // GENERIC template: Recursive step
    template<typename Op>
    static void run(Op op) {
        op(STEP);
        Unroll<NUM_UNROLL, STEP + 1>::run(op);
    }
};

template<int NUM_UNROLL>
struct Unroll<NUM_UNROLL, NUM_UNROLL> { // PARTIAL SPECIALIZATION: Base case
    template<typename Op>
    static void run(Op) {}
};

auto lambda = [](int step) { cout << step << ", "; };
Unroll<5>::run(lambda); // print "0, 1, 2, 3, 4"
```

# SFINAE: Substitution Failure Is Not An Error

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## SFINAE

**Substitution Failure Is Not An Error (SFINAE)** applies during overload resolution of function templates. When substituting the deduced type for the template parameter fails, the specialization is discarded from the overload set *instead* of causing a compile error

## The Problem

```
template<typename T>
T ceil_div(T value, T div);

template<>
unsigned ceil_div<unsigned>(unsigned value, unsigned div) {
    return (value + div - 1) / div;
}

template<>
int ceil_div<int>(int value, int div) { // handle negative values
    return (value > 0) ^ (div > 0) ?
        (value / div) : (value + div - 1) / div;
}
```

What about long long int, long long unsigned, short, unsigned short, etc.?

## std::enable\_if Type Trait

The common way to adopt SFINAE is using the

`std::enable_if/std::enable_if_t` type traits

`std::enable_if` allows a function template or a class template specialization to include or exclude itself from a set of matching functions/classes

```
template<bool Condition, typename T = void>
struct enable_if {
    // "type" is not defined if "Condition == false"
};

template<typename T>
struct enable_if<true, T> {
    using type = T;
};
```

**helper alias:** `std::enable_if_t<T>` instead of `typename std::enable_if<T>::type`

## Function SFINAE - Return type

1/5

```
#include <type_traits> // std::is_signed_v, std::enable_if_t

template<typename T>
std::enable_if_t<std::is_signed_v<T>>
f(T) {
    cout << "signed";
}

template<typename T>
std::enable_if_t<!std::is_signed_v<T>>
f(T) {
    cout << "unsigned";
}

f(1); // print "signed"
f(1u); // print "unsigned"
```

```
#include <type_traits> compiler-explorer ↗

template<typename T>
void f(std::enable_if_t<std::is_signed_v<T>, T>) {
    cout << "signed";
}

template<typename T>
void f(std::enable_if_t<!std::is_signed_v<T>, T>) {
    cout << "unsigned";
}

// NOTE: explicit SFINAE on parameter prevents argument deduction
f<int>(1);          // print "signed"
f<unsigned>(1u);     // print "unsigned"
// f(1);              // compile error
// f(1u);             // compile error
```

```
#include <type_traits>

template<typename T>
void f(T,
       std::enable_if_t<std::is_signed_v<T>, int> = 0) {
    cout << "signed";
}

template<typename T>
void f(T,
       std::enable_if_t<!std::is_signed_v<T>, int> = 0) {
    cout << "unsigned";
}

f(1); // print "signed"
f(1u); // print "unsigned"
```

```
#include <type_traits>

template<typename T,
          std::enable_if_t<std::is_signed_v<T>, int> = 0>
void f(T) {}

template<typename T,
          std::enable_if_t<!std::is_signed_v<T>, int> = 0>
void f(T) {}

f(4);
f(4u);
```

```
#include <type_traits>
template<typename T, typename R>          // (1)
decltype(T{} + R{}) add(T a, R b) {        // T{} + R{} is not possible with 'A'
    return a + b;
}

template<typename T, typename R>          // (2)
std::enable_if_t<std::is_class_v<T>, T> // 'int' is not a class
add(T a, R b) {
    return a;
}

struct A {};

add(1, 2u);    // call (1)
add(A{}, A{}); // call (2)
// if 'A' supports operator+, then we have a conflict
```

## Function SFINAE Example - Array vs. Pointer

```
#include <type_traits> compiler-explorer
template<typename T, int Size>
void f(T (&array) [Size]) {} // (1)

// template<typename T>
// void f(T array) {} // (2)

template<typename T>
std::enable_if_t<std::is_pointer_v<T>>
f(T ptr) {} // (3)

// void f(int* pointer) {} // (4) has the highest priority among (1), (2), and (3)

int array[3];
f(array); // It is not possible to call (1) if (2) is present
           // The reason is that 'array' decays to a pointer
           // Now with (3), the code calls (1)
```

# Function SFINAE Notes

The wrong way to achieve SFINAE

```
template<typename T, typename = std::enable_if_t<std::is_signed_v<T>>>
void f(T) {}

// template<typename T, typename = std::enable_if_t<!std::is_signed_v<T>>>
// void f(T) {}
// compile error redefinition of the second template parameter
```

Using `std::enable_if_t` for the *return type* prevents `auto` deduction

```
// template<typename T>
// std::enable_if_t<std::is_signed_v<T>, auto> f(T) {}
// compile error auto is not allowed here
```

## Class SFINAE

```
#include <type_traits>

template<typename T, typename Enable = void>
struct A;

template<typename T>
struct A<T, std::enable_if_t<std::is_signed_v<T>>> {
};

template<typename T>
struct A<T, std::enable_if_t<!std::is_signed_v<T>>> {
};

A<int>      a1;
A<unsigned> a2;
```

SFINAE can be also used to check if a structure has a specific data member or type

Let consider the following structures:

```
struct A {  
    static int x;  
    int y;  
    using type = int;  
};  
  
struct B {};
```

```
#include <type_traits>
template<typename T, typename = void>
struct has_x : std::false_type {};

template<typename T>
struct has_x<T, decltype((void) T::x)> : std::true_type {};

template<typename T, typename = void>
struct has_y : std::false_type {};

template<typename T>
struct has_y<T, decltype((void) std::declval<T>().y)> : std::true_type {};

has_x< A >::value; // returns true
has_x< B >::value; // returns false
has_y< A >::value; // returns true
has_y< B >::value; // returns false
```

```
template<typename...>
using void_t = void; // included in C++17 <utility>

template<typename T, typename = void>
struct has_type : std::false_type {};

template<typename T>
struct has_type<T,
                std::void_t<typename T::type> > : std::true_type {};
```

has\_type< A >::value; // returns true  
has\_type< B >::value; // returns false

## Support Trait for Stream Operator ★

```
template<typename T>
using EnableP = decltype( std::declval<std::ostream&>() <<
                         std::declval<T>() );

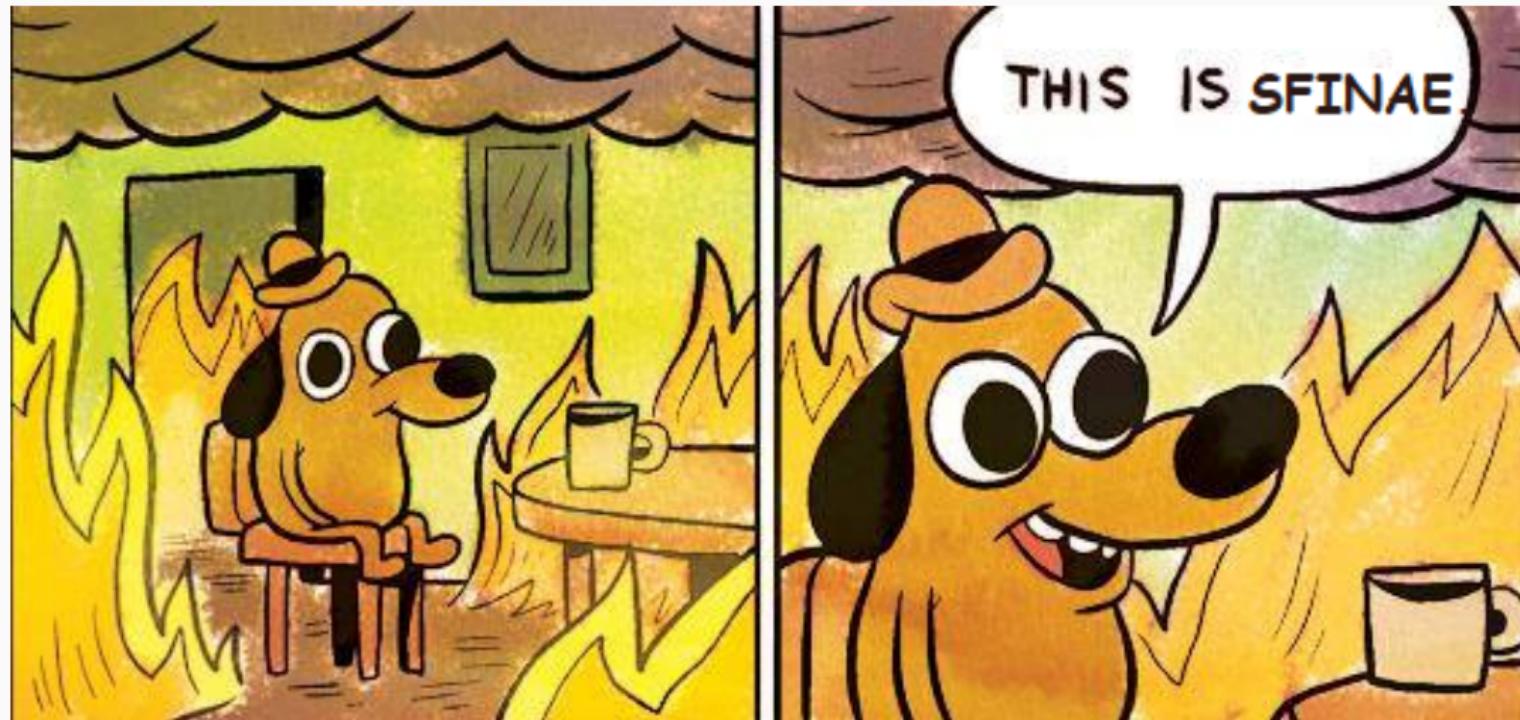
template<typename T, typename = void>
struct is_stream_supported : std::false_type {};

template<typename T>
struct is_stream_supported<T, EnableP<T>> : std::true_type {};

struct A {};

is_stream_supported<int>::value; // returns true
is_stream_supported<A>::value;   // returns false
```

SFINAE



# Variadic Templates

---

## Variadic template (C++11)

A **variadic template** captures a *parameter pack* of arguments, which hold an arbitrary number of values or types

```
template<typename... TArgs> // Variadic typename -> parameter pack: ... TArgs
void f(TArgs... args) {}    // pack expansion      -> pattern:       TArgs
```

A **parameter pack** is introduced by an identifier `TArgs` prefixed by an **ellipsis** `...` `TArgs`. Once captured, a *parameter pack* can later be used in a *pattern* expanded by an *ellipsis* `...`

A **pack expansion** is equivalent to a comma-separated list of instances of the *pattern*

A **pattern** is a *set of tokens* containing the identifiers of one or more *parameter packs*.

When a *pattern* contains more than one *parameter pack*, all packs must have the same length

```
template<typename... TArgs>
void f(TArgs... args) {           // Typename expansion
    int values[] = {args...}; // Arguments expansion
}
f(1, 2, 3);
```

The pack `TArgs` expands in a *template-argument-list*, i.e. list of template arguments

The pack `args` expands in an *initializer-list*, i.e. list of values

The number of variadic arguments can be retrieved with the `sizeof...` operator

```
sizeof...(args) // e.g. 3
```

*Note:* variadic arguments must be the last one in the declaration

## Example 1

```
// BASE CASE
template<typename T, typename R>
auto add(T a, R b) {
    return a + b;
}

// RECURSIVE CASE
template<typename T, typename... TArgs> // Variadic typename
auto add(T a, TArgs... args) {           // Typename expansion
    return a + add(args...);            // Arguments expansion
}

add(2, 3.0); // 5
add(2, 3.0, 4); // 9
add(2, 3.0, 4, 5); // 14
// add(2); // compile error the base case accepts only two arguments
```

## Example 2 - Function Unpack

```
template<typename T, typename... TArgs>
auto add(T a, TArgs... args); // see previous slides

struct A {
    int v;
    int f() { return v; }
};

template<typename... TArgs>
int f(TArgs... args) {
    return add(args.f()...); // equivalent to: 'A{1}.f(), A{2}.f(), A{3}.f()'
}

f(A{1}, A{2}, A{3}); // return 6
```

## Example 3 - Function Application

```
template<typename T, typename... TArgs>
auto add(T a, TArgs... args); // see previous slides

template<typename T>
T square(T value) { return value * value; }

//-----

template<typename... TArgs>
auto add_square(TArgs... args) {
    return add(square(args)...); // square() is applied to each
}                                // variadic argument

add_square(2, 2, 3.0f); // returns 17.0f
```

## Example 4 - Type Expansion

```
template<typename... TArgs>
int g(TArgs... args) {}

template<typename... TArgs>
int f(TArgs... args) {
    g<std::make_unsigned_t<TArgs>...>(args...);
}

f(1, 2, 3);
```

## Function Initializer List Types

```
template<typename... TArgs>
void f(TArgs... args)           // pass by-value

template<typename... TArgs>
void g(const TArgs&... args)    // pass by-const reference

template<typename... TArgs>
void h(TArgs*... args)          // pass by-pointer

template<int... Sizes>
void l(int (&...arrays)[Sizes]) {} // pass a list of array references

int a[] = {1, 2};
int b[] = {1, 2, 3};
f(1, 2.0);
h(a, b);
l(a, b); // same as g()
```

## Homogeneous Variadic Template Parameters

Parameter pack can be also used to create a **homogeneous variadic template parameters**

```
template<int... IntSeq> // sequence of integers
void f() {}

f<1, 2, 3>();
```

```
template<int... IntSeq> // sequence of integers
class A {};

A<1, 2, 3> a{};
```

## Other Usages

Variadic templates can be also applied to lambdas with *generic parameters* (C++14) and *concepts* (C++20)

```
auto lambda = [](auto... args) {};
```

```
lambda(1, 2u, 3.0f, 1ull);
```

```
void f(std::floating_point auto... args) {}
```

```
f(1.0, 2.0f); // ok
```

```
// f(1u, 2.0f); // compile error
```

## Advanced Usages ★

Besides *initializer-lists*, *template-argument-list*, parameter pack can be used in:  
*capture list*, *constructor initializer-list*, *using declaration*

```
template<typename... BaseClasses>
struct A : BaseClasses... {           // : BaseClass_1, BaseClass_2, ...
    A(int v) : BaseClasses...{v} {} // BaseClass_1{v},  BaseClass_2{v}, ...

    using BaseClasses::f;
// equivalent to:
//     using BaseClass_1::f;
//     using BaseClass_2::f;
// ...
};

void f(auto... args) {
    auto lambda = [arg&...](){}; // capture by-reference
}
```

C++17 **Folding expressions** perform a *fold* of a template parameter pack over any binary operator in C++ (+, \*, , , +=, &&, <= etc.)

## Unary/Binary folding

```
template<typename... Args>
auto add_unary(Args... args) { // Unary folding
    return (... + args);      // unfold: 1 + 2.0f + 3ull
}

template<typename... Args>
auto add_binary(Args... args) { // Binary folding
    return (1 + ... + args);   // unfold: 1 + 1 + 2.0f + 3ull
} // the value on the left of the ellipsis is typically the identity

add_unary(1, 2.0f, 3ll); // returns 6.0f (float)
add_binary(1, 2.0f, 3ll); // returns 7.0f (float)
```

## Example 1 - Extract The Last Argument

```
template<typename... TArgs>
int f(TArgs... args) {
    return (args, ...); // the comma operator discards left values
}                      // same as (... , args)

f(1, 2, 3); // return 3
```

## Example 2 - Function Application

Same example of “Variadic Template - Function Application” ... but shorter

```
template<typename T>
T square(T value) { return value * value; }

template<typename... TArgs>
auto add_square(TArgs... args) {
    return (square(args) + ...); // square() is applied to each
}                                // variadic argument

add_square(2, 2, 3.0f); // returns 17.0f
```

Note: binary unfolding  $(1 + \dots + \text{args})$  cannot be combined with functions

## Example 3 - Homogeneous Variadic Parameter Type

Parameter pack can be constrained to obtain a **homogeneous variadic parameter type**

```
template <typename ... TArgs>
std::enable_if_t<(std::is_same_v<TArgs, int> && ... && true)>
f(const TArgs ... args) {}

f(1, 2, 3);      // ok
// f(1u, 2, 3); // compile error
```

## Variadic Template and Classes

```
template<int... NArgs>
struct Add; // data structure declaration

template<int N1, int N2>
struct Add<N1, N2> { // BASE case
    static constexpr int value = N1 + N2;
};

template<int N1, int... NArgs>
struct Add<N1, NArgs...> { // RECURSIVE case
    static constexpr int value = N1 + Add<NArgs...>::value;
};

Add<2, 3, 4>::value; // returns 9
// Add<>; // compile error no match
// Add<2>::value; // compile error
// call Add<N1, NArgs...>, then Add<>
```

# Variadic Class Template ★

Variadic Template can be used to build recursive data structures

```
template<typename... TArgs>
struct Tuple;          // data structure declaration

template<typename T>
struct Tuple<T> {    // base case
    T value;        // specialization with one parameter
};

template<typename T, typename... TArgs>
struct Tuple<T, TArgs...> { // recursive case
    T             value;    // specialization with more
    Tuple<TArgs...> tail;   // than one parameter
};

Tuple<int, float, char> t1 { 2, 2.0, 'a' };
t1.value;           // 2
t1.tail.value;     // 2.0
t1.tail.tail.value; // 'a'
```

Get function arity at compile-time:

```
template <typename T>
struct GetArity;

// generic function pointer
template<typename R, typename... Args>
struct GetArity<R(*)(Args...)> {
    static constexpr int value = sizeof...(Args);
};

// generic function reference
template<typename R, typename... Args>
struct GetArity<R(&)(Args...)> {
    static constexpr int value = sizeof...(Args);
};

// generic function object
template<typename R, typename... Args>
struct GetArity<R(Args...)> {
    static constexpr int value = sizeof...(Args);
};
```

```
void f(int, char, double) {}

int main() {
    // function object
    GetArity<decltype(f)>::value;

    auto& g = f;
    // function reference
    GetArity<decltype(g)>::value;

    // function reference
    GetArity<decltype((f))>::value;

    auto* h = f;
    // function pointer
    GetArity<decltype(h)>::value;
}
```

Get operator() (and lambda) arity at compile-time:

```
template <typename T>
struct GetArity;

template<typename R, typename C, typename... Args>
struct GetArity<R(C::*)(Args...)> {           // class member
    static constexpr int value = sizeof...(Args);
};

template<typename R, typename C, typename... Args>
struct GetArity<R(C::*)(Args...) const> { // "const" class member
    static constexpr int value = sizeof...(Args);
};

struct A {
    void operator()(char, char) {}
    void operator()(char, char) const {}
};

GetArity<A>::value;           // call GetArity<R(C::*)(Args...)>
GetArity<const A>::value; // call GetArity<R(C::*)(Args...) const>
```

# C++20 Concepts

---

C++20 introduces **concepts** as an extension for *templates* to enforce *constraints*, which specifies the *requirements* on template arguments

**Concepts** allows performing compile-time validation of template arguments

Advantages compared to SFINAE (`std::enable_if_t`):

- Better express the intention
- Concepts are easier to read and write
- Clear compile-time messages for debugging
- Faster compile time

- 
- The concept behind C++ concepts
  - Concepts vs type traits
  - Constraints and concepts
  - What are C++20 concepts and constraints? How to use them?

## Keyword introduced:

`concept` Constrain

`requires` Constrain list/Requirements, *clause* and *expression*

# The Problem

*Goal:* define a function to sum only arithmetic types

```
template<typename T>
T add(T valueA, T valueB) {
    return valueA + valueB;
}

struct A {};
```

```
add(3, 4);          // ok
// add(A{}, A{}); // not supported
```

SFINAE solution (ugly, verbose):

```
template<typename T>
std::enable_if_t<std::is_arithmetic_v<T>, T>
add(T valueA, T valueB) {
    return valueA + valueB;
}
```

## concept Keyword

```
[template arguments]  
concept [name] = [compile-time boolean expression];
```

Example: arithmetic type concept

```
template<typename T>  
concept Arithmetic = std::is_arithmetic_v<T>;
```

- *Template argument constrain*

```
template<Arithmetic T>  
T add(T valueA, T valueB) {  
    return valueA + valueB;  
}
```

- *auto deduction constrain (constrained auto)*

```
auto add(Arithmetic auto valueA, Arithmetic auto valueB) {  
    return valueA + valueB;  
}
```

## requires Clause

```
requires [compile-time boolean expression or Concept]
```

it acts like SFINAE

- After *template parameter list*

```
template<typename T>
requires Arithmetic<T>
T add(T valueA, T valueB) {
    return valueA + valueB;
}
```

- After *function declaration*

```
template<typename T>
T add(T valueA, T valueB) requires (sizeof(T) == 4) {
    return valueA + valueB;
}
```

## requires Clause and concept Notes

*Concepts* and *requirements* can have *multiple* statements. It must be a *primary expression*, e.g. `constexpr` value (not a `constexpr` function) or a sequence of *primary expressions* joined with the operator `&&` or `||`

```
template<typename T>
concept Arithmetic2 = std::is_arithmetic_v<T> && sizeof(T) >= 4;
```

*Concepts* and *requirements* can be used together

```
template<Arithmetic T>
requires (sizeof(T) >= 4)
T add(T valueA, T valueB) {
```

A **requires expression** is a *compile-time* expression of type `bool` that defines the **constraints** on template arguments

```
requires [(arguments)] {
    [SFINAE constrain];      // or
    requires [predicate];
} -> bool
```

```
template<typename T>
concept MyConcept = requires (T a, T b) { // First case: SFINAE constrains
    a + b;                  // Req. 1 - support add operator
    a[0];                   // Req. 2 - support subscript operator
    a.x;                     // Req. 3 - has "x" data member
    a.f();                  // Req. 4 - has "f" function member
    typename T::type; // Req. 5 - has "type" field
};
```

## Concept library

```
#include <concepts>

template<typename T>
concept MyConcept2 = requires (T a, T b) {
    {*a + 1} -> std::convertible_to<float>; // Req. 6 - can be deferred and the sum
                                                // with an integer is convertible
                                                // to float
    {a * a} -> std::same_as<int>;           // Req. 7 - "a * a" must be valid and
                                                // the result type is "int"
};
```

## requires Expression + Clause

requires expression can be combined with requires clause

(see requires definition, second case) to compute a boolean value starting from SFINAE expressions

```
template<typename T>
concept Arithmetic = requires {           // expression -> bool (zero args)
    T::value;                          // clause      -> direct SFINAE
    requires std::is_arithmetic_v<T>; // clause      -> SFINAE from boolean

template<typename T>
concept MyConcept = requires (T value) { // expression -> bool (one arg)
    requires sizeof(value) >= 4;        // clause      -> SFINAE from boolean
    requires std::is_floating_point_v<T>; // clause      -> SFINAE from boolean
};
```

## requires Clause + Expression

`requires clause` can be combined with `requires expression` to apply SFINAE (functions, structures) starting from a compile-time *boolean expressions*

```
template<typename T>
void f(T a) requires requires { T::value; }
//           clause -> SFINAE followed by
//                           expression -> bool (zero args)

template<typename T>
T increment(T a) requires requires (T x) { x + 1; }
//           clause -> SFINAE followed by
//                           expression -> bool (one arg)
{
    return a + 1;
}
```

## requires and constexpr

Some examples:

- `constexpr bool has_member_x = requires(T v){ v.x; };`
- `if constexpr (MyConcept<T>)`
- `static_assert(requires(T v){ ++v; }, "no increment");`
- `template<typename Iter>  
constexpr bool is_iterator() {  
 return requires(Iter it) { *it++; };  
}`

## Nested requires

Nested requires example:

```
requires(Iter v) { // expression -> bool (one arg)
    Iter it;
    requires requires(typename Iter::value_type v) {
        // clause -> SFINAE followed by
        //           expression -> bool (one arg)
        v     = *it; // read
        *it = v;    // write
    };
}
```

# Template Debugging

---

## Template Debugging

- **-ftemplate-backtrace-limit=<N>** Maximum number of template instantiation notes for a single *warning/error* to `N`, default 10  
`N=1` is useful when looking only at the last instantiation (much less verbose output). `N=100` (or higher) if you are looking at all template instantiations (rare)
- **-ftemplate-depth=<N>** Set the maximum instantiation depth for template classes to `N`, default 900
- **-Wfatal-errors** Abort compilation on the first error occurred rather than trying to keep going and printing further error messages

# Template Debugging

- `-fdiagnostics-show-template-tree` Display the templates as an indented text tree

```
map<
  [...],
  map<
    [float != double],
    [...]>>
```